This page shows how you can derive the simple form of the LSLR slope using only algebra:

$$b = \frac{s_y}{s_x} r$$

from its original definition.

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$

Denominator looks a bit like variance:

$$s_{x} = \sqrt{\frac{\sum (x - \bar{x})^{2}}{(n - 1)}}$$

$$s_{x}^{2} = \frac{\sum (x - \bar{x})^{2}}{(n - 1)}$$

$$s_{x}^{2}(n - 1) = \sum (x - \bar{x})^{2}$$

So we can rewrite b as:

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{s_x^2(n-1)}$$

And the factors of the numerator look a bit like z-scores...

$$z_{\chi} = \frac{(\chi - \bar{\chi})}{S_{\chi}}$$

$$z_{x}s_{x}=(x-\bar{x})$$

$$z_y = \frac{(y - \bar{y})}{s_y}$$

$$z_{y}s_{y} = (y - \bar{y})$$

So we can rewrite the numerator:

$$\sum (x - \bar{x})(y - \bar{y}) = \sum z_x s_x z_y s_y$$

And now we can rewrite b, using our simplified b from above:

$$b = \frac{\sum (x - \bar{x})(y - \bar{y})}{s_x^2(n-1)}$$

$$b = \frac{\sum z_x s_x z_y s_y}{s_x^2 (n-1)}$$

But since standard deviation is a scalar (just a number, not a list of numbers), we can take it outside the summation:

$$b = \frac{s_x s_y \sum z_x z_y}{s_x^2 (n-1)}$$

$$b = \frac{s_y \sum z_x z_y}{s_x (n-1)}$$

But this summation above should remind you of the simple form of Pearson's correlation formula!

$$r = \frac{\sum z_x z_y}{(n-1)}$$

So we can finally rewrite the slope of the LSLR line as:

$$b = \frac{s_y}{s_x} r$$

Note that if x has zero standard deviation, then b is undefined! But that's ok, because that means x is a constant, and therefore has no predictive power for y anyway.

In R code, b is given by:

$$lslr\_slope = (sd(y)/sd(x))*cor(x, y)$$