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Kelas: B

Tugas Pengganti Liburan Praktikum Analgo

Heap Sort

Pseudocode

procedure heapsort(a, count) **is**

input: an unordered array a of length count

(Build the heap in array a so that largest value is at the root)

 heapify(a, count)

(The following loop maintains the invariants that a[0:end] is a heap and every element

beyond end is greater than everything before it (so a[end:count] is in sorted order))

 end ← count - 1

while end > 0 **do**

(a[0] is the root and largest value. The swap moves it in front of the sorted elements.)

 swap(a[end], a[0])

(the heap size is reduced by one)

 end ← end - 1

(the swap ruined the heap property, so restore it)

 siftDown(a, 0, end)

(Put elements of 'a' in heap order, in-place)

procedure heapify(a, count) **is**

(start is assigned the index in 'a' of the last parent node)

(the last element in a 0-based array is at index count-1; find the parent of that element)

 start ← iParent(count-1)

while start ≥ 0 **do**

(sift down the node at index 'start' to the proper place such that all nodes below

the start index are in heap order)

 siftDown(a, start, count - 1)

(go to the next parent node)

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    start ← start - 1
    (after sifting down the root all nodes/elements are in heap order)

    (Repair the heap whose root element is at index 'start', assuming the
    heaps rooted at its children are valid)

procedure siftDown(a, start, end) is
    root ← start

    while iLeftChild(root) ≤ end do      (While the root has at least one
    child)
        child ← iLeftChild(root)      (Left child of root)
        swap ← root                    (Keeps track of child to swap with)

        if a[swap] < a[child]
            swap ← child
            (If there is a right child and that child is greater)
        if child+1 ≤ end and a[swap] < a[child+1]
            swap ← child + 1
        if swap = root
            (The root holds the largest element. Since we assume the heaps
            rooted at the
            children are valid, this means that we are done.)
        return
    else
        swap(a[root], a[swap])
        root ← swap                    (repeat to continue sifting down the
        child now)

```

Hitung Manual

Terdapat 6 angka : 1 4 3 2 6 5

1 4 5 2 6 3

1 6 5 2 4 3

6 4 5 2 1 3

3 4 5 2 1 6

1 4 3 2 5 6

1 2 3 4 5 6

1 2 3 4 5 6

1 2 3 4 5 6

1 2 3 4 5 6

Hasil : 1 2 3 4 5 6

Analisa Big-O:

Langkah-langkah heapsort:

1. Mengerjakan fungsi `heapfy()`, yang membutuhkan waktu operasi $O(n)$
2. Menukar elemen pertama dalam list dengan elemen terakhir, dan mengurangi range operasi sebanyak: 1
3. Memanggil fungsi `siftDown()` ke list yang untuk menggeser elemen awal yang baru ke index list heap yang sebenarnya
4. Kembali ke step 2 hingga range operasinya tinggal 1

`heapfy()` membutuhkan waktu operasi sebanyak $O(n)$ dan hanya dipanggil sekali

`siftDown()` membutuhkan waktu operasi sebanyak $O(\log n)$ dan dipanggil sebanyak n -kali

Sehingga big-O: $O(n + n \log n) = O(n \log n)$