

INTRO TO DATA SCIENCE HW 2

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Question 1

1a.

The probability of a bit in the array remaining 0 is:

$$e^{\frac{-20}{99}} \quad (1)$$

which comes out to .819. So, $1 - .819 = .181$ is the expected fraction of 1's.

1b.

The expected fraction of 0's is $1 - .181 = .819$

Question 2

The false positive rate is:

$$(1 - e^{\frac{-3*2}{11}}) = (1 - e^{\frac{-6}{11}}) \quad (2)$$

Question 3

a	b	c	a	d	e	a	c	b	b
1									
.9	1								
.81	.9	1							
	.81	.9	1.81						
	.729	.81	1.1629	1					
	.6561	.729	1.4661	.9	1				
	.5905	.6561		.81	.9	2.4661			
	.5314			.729	.81	2.219	1.6561		
				.6561	.729	1.997	1.4904	1.5314	
				.5905	.6561	1.797	1.3413		2.5314

3a.

D is dropped, as its popularity score is .5905 at the end of the stream.

3b.

The most popular element is B, with a score of 2.5314.

Question 4

$(3x + 7) \bmod 11$

$X=1, 10 \bmod 11 = 10, 1010$

$x=2, 13 \bmod 11 = 2, 0010$

$X=3, 16 \bmod 11 = 5, 0101$

$X=4, 19 \bmod 11 = 8, 1000$

$X=5, 22 \bmod 11 = 0, 0000$

$X=6, 25 \bmod 11 = 3, 0011$

$X=7, 28 \bmod 11 = 6, 0110$

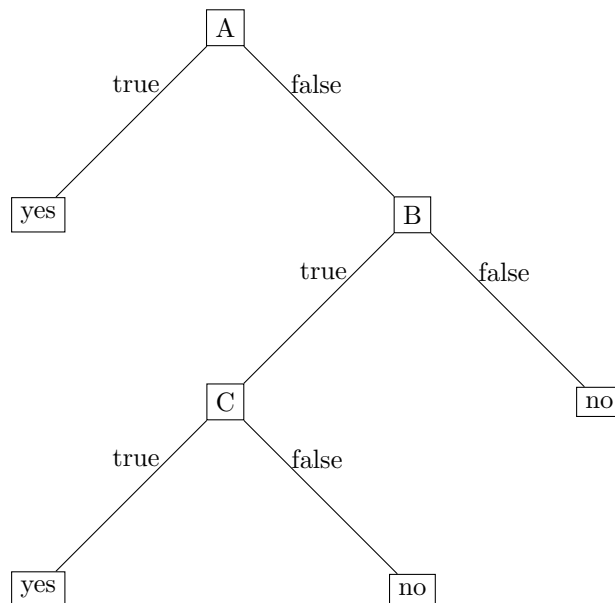
$X=8, 31 \bmod 11 = 9, 1001$

$X=9, 34 \bmod 11 = 1, 0001$

$X=10, 37 \bmod 11 = 4, 0100$

With set $\{10\ 9\ 1\ 7\}$, 10 would have to be in the set since the estimate of the number of distinct elements is 2^r where r is the max tail length in the set.

Question 5



Question 6

6a.

$$H[12+, 9-] = -\frac{12}{21} \log_2 \frac{12}{21} - \frac{9}{21} \log_2 \frac{9}{21} = -.5714 * -.8074 - .4286 * -1.2223 = .9852 \quad (3)$$

6b.

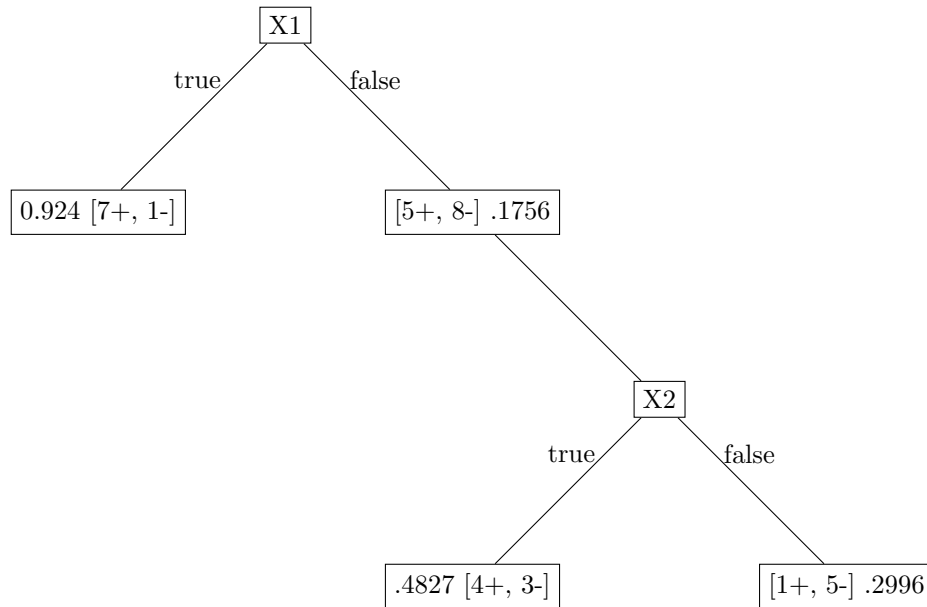
$$IG(X1) = T[7+, 1-]F[5+, 8-] \quad (4)$$

$$.9582 - \frac{8}{21} * 1.3925 - \frac{13}{21} * .6920 = .0265 \quad (5)$$

$$IG(X2) = T[7+, 3-]F[5+, 6-] \quad (6)$$

$$.9852 - \frac{10}{21} * 1.0704 - \frac{11}{21} * .9329 = .013 \quad (7)$$

6c.



6d.

$$\frac{4}{7} = .5714 \quad (8)$$

Question 7

Assuming that you've picked door number 1, there are three (equally likely) possible scenarios:

1. You pick the door with the prize, and the other two doors are empty.
2. Both your door and door number 2 are empty.
3. Both your door and door number 3 are empty.

Overall, there are two groups of possibilities - that you've picked a winning door ($1/3$) or you've picked an empty door ($2/3$).

If an empty door is revealed, it must either be door 2 or 3, because you picked door number 1. Now you are presented with the same two groups - but the second group's doors now have probabilities 0 and $2/3$ of containing the prize, when originally they were $1/3$ each.

Since your door (door number 1) has a probability of $1/3$ and the other closed door has a probability of $2/3$, you should switch doors.