

First Name \_\_\_\_\_ Last Name \_\_\_\_\_ Date \_\_\_\_ - \_\_\_\_ - \_\_\_\_ Period \_\_\_\_ Score \_\_\_\_

### Learning Objectives.

- Verify a pair of inverse functions via composition

**Skill Builder.** *Work on the Skill Builder problems on the screen while the teacher is taking attendance and returning work.*

---



---



---



---



---



---

### Discussion.

Find the operation that undoes the given operation.

1. Adding 2.

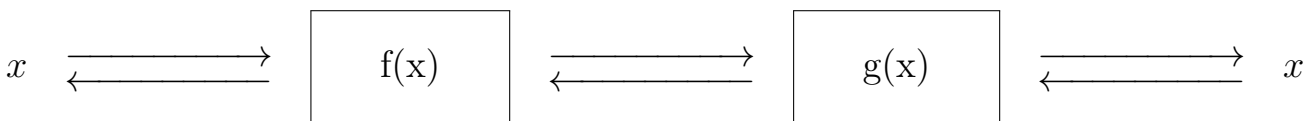
2. Multiplying by 10.

3. Squaring a negative number.

**Concepts.** The *inverse function* undoes the original function. Formally,  $g(x)$  is called the **inverse function** of  $f(x)$  if both of the following are true:

1.  $(f \circ g)(x) = x$
2.  $(g \circ f)(x) = x$

See the diagram below.



The inverse function of  $f(x)$  is denoted by  $f^{-1}(x)$ . It is worthwhile to note that

- $\text{domain}(f(x)) = \text{range}(f^{-1}(x))$
- $\text{domain}(f^{-1}(x)) = \text{range}(f(x))$

Moreover, the graph of  $f(x)$  and the graph of  $f^{-1}(x)$  are symmetric about the line  $y = x$ .

**Examples.**

Verify the pair of functions below are the inverse functions of each other.

1.  $f(x) = x + 2$ ,  $g(x) = x - 2$ .

2.  $f(x) = x \times 10$ ,  $g(x) = x \div 10$ .

**Challenge.** Is  $g(x) = \sqrt{x}$  the inverse function of  $f(x) = x$ ? Why or why not?