

# Eigenvalues and Eigenvectors

MAT215 Intro to Linear Algebra

Instructor: Ben Huang

**DUTCHESS**  

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**COMMUNITY COLLEGE**

# The Hierarchy of Matrices

B.H.

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The second to the best - diagonal matrix:

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

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More generally,

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}^k = \begin{bmatrix} 1^k & 0 & 0 \\ 0 & 2^k & 0 \\ 0 & 0 & 3^k \end{bmatrix}$$