

Problem. Let $f(x, y) = \frac{x - y}{(x + y)^3}$.

1. Does $\lim_{(x,y) \rightarrow (0,0)} f(x, y)$ exist? Is $f(x, y)$ continuous at $(0, 0)$?

2. Evaluate the following two integrals.¹

$$\int_0^1 \int_0^1 \frac{x - y}{(x + y)^3} dx dy \quad \text{and} \quad \int_0^1 \int_0^1 \frac{x - y}{(x + y)^3} dy dx$$

3. Does the result of Part 2 contradict Fubini's Theorem (Theorem 14.2)? Why or why not? Type your response. (**Hint:** A theorem should never be contradicted. **Remark:** Handwritten response receives NO credit for this part.)

¹It would be a fun exercise to work them out by hand, but it's okay to use a CAS if you get stuck.