

Section 13.8

B.H.

Section 13.8 Extrema of Functions of Two Variables

MATH211 Calculus III

Instructor: Ben Huang

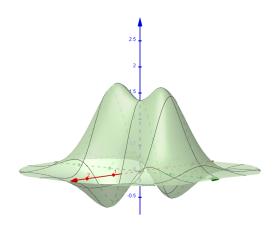


DEPARTMENT OF COMPUTING, MATHEMATICS AND PHYSICS



Relative Extrema

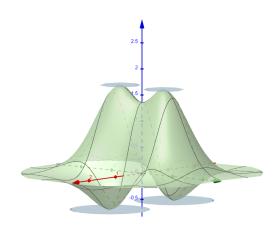
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Relative Extrema

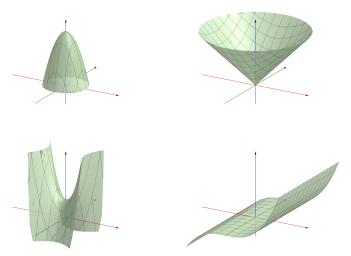
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Critical points

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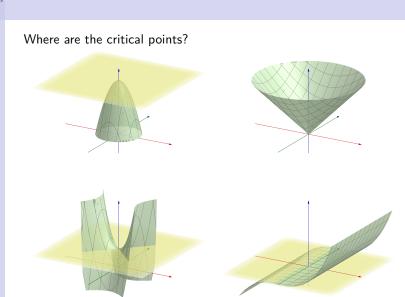
Where are the critical points?





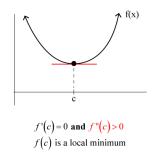
Critical points

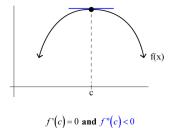
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Second Derivative Test From Calculus I

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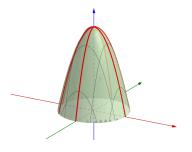




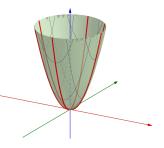
f(c) is a local maximum

Classification of Critical Points

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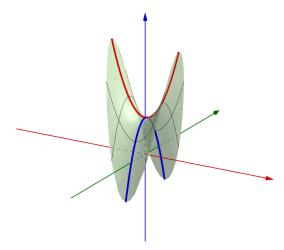
 $f_{xx} < 0 \ \& \ f_{yy} < 0$ at the critical point local maximum



 $f_{xx} > 0 \& f_{yy} > 0$ at the critical point local minimum

Classification of Critical Points

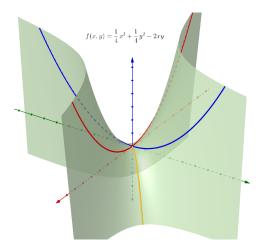
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 $f_{\rm xx} > 0$ & $f_{\rm yy} < 0$ at the critical point saddle point

Classification of Critical Points

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 $f_{xx} > 0$ & $f_{yy} > 0$ at the critical point saddle point



The Second Partials Test

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The tool to systematically classify critical points: The Second Partials Test

Failure of the Second Partials Test

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When $d(x,y) = f_{xx}f_{yy} - f_{xy}^2 = 0$ at the critical point in question, the Second Partials Test is **inconclusive**.



Figure 1:
$$z = y^2$$



Figure 2: $z = -x^2$

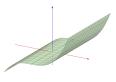


Figure 3: $z = \frac{1}{50}x^3$