

First Name _____ Last Name _____ Date ___ - ___ - ___ Period ___ Score ___

Learning Objectives.

- Verify a pair of inverse functions via composition

Skill Builder. *Work on the Skill Builder problems on the screen while the teacher is taking attendance and returning work.*

Discussion.

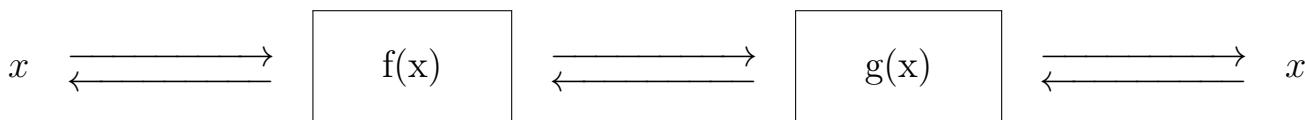
Find the operation that undoes the given operation.

1. Adding 2.
2. Multiplying by 10.
3. Squaring a negative number.

Concepts. The *inverse function* undoes the original function. Formally, $g(x)$ is called the **inverse function** of $f(x)$ if both of the following are true:

1. $(f \circ g)(x) = x$
2. $(g \circ f)(x) = x$

See the diagram below.



The inverse function of $f(x)$ is denoted by $f^{-1}(x)$. It is worthwhile to note that

- $\text{domain}(f(x)) = \text{range}(f^{-1}(x))$
- $\text{domain}(f^{-1}(x)) = \text{range}(f(x))$

Moreover, the graph of $f(x)$ and the graph of $f^{-1}(x)$ are symmetric about the line $y = x$.

Examples.

Verify the pair of functions below are the inverse functions of each other.

1. $f(x) = x + 2, g(x) = x - 2.$

2. $f(x) = x \times 10, g(x) = x \div 10.$

Challenge. Is $g(x) = \sqrt{x}$ the inverse function of $f(x) = x$? Why or why not?