Typeclass-driven Polymorphism in Scala

"Classic" map

Collection method map(f) transforms a collection by applying f to each element
 List(1, 2, 3).map(toString) == List("1", "2", "3")

 Scala 2.7 collections included a map method with the "classic" signature

```
trait scala.lterable[A] { ..
    def map [B](f : (A) => B) : Iterable[B]
}
```

2.7 Collections API problems

 Subclasses had to repeatedly override map to return a more specific collection type

```
trait scala.Seq[A] { ..
override def map [B](f : (A) => B) : Seq[B] = {...}}
```

- Not just map
 - Approx 30 other generic methods had to be repeatedly overridden in each sub-trait

```
trait scala.Seq[A] { ..
override def filter (p : (A) => Boolean) : Seq[A] = {...}}
```

A solution?

 The repetition of methods can be solved by passing a higher-kinded Collection type to a common super definition

```
trait TraversableLike[+Elem, +Coll[+X]] {
    def map[NewElem](f: Elem => NewElem): Coll[NewElem]
    def filter(p: Elem => Boolean): Coll[Elem]
}
trait scala.Seq[A] extends TraversableLike[A, Seq]
```

New requirements...

The designers of the Collections redesign also wished to tackle tricky use cases like:

Map("a" -> 1, "b" -> 2) map {case
$$(x, y) => (y, x)$$
}
== Map(1 -> "a", 2 -> "b")

New requirements

- Another example: Bitsets
 - "Bitsets are sets of non-negative integers which are represented as variable-size arrays of bits packed into 64-bit words. The memory footprint of a bitset is determined by the largest number stored in it."

$$BitSet(1, 2, 3).map(_ * 2) == BitSet(2, 4, 6)$$

$$BitSet(1, 2, 3).map(_.toFloat) == Set(2.0, 4.0, 6.0)$$

2.8 Collections re-design (2010)

- Code-duplication greatly reduced
- New requirements met
- Great paper title



Leibniz International Proceedings in Informatics

Fighting Bit Rot with Types (Experience Report: Scala Collections)

M. Odersky¹, A. Moors²*

1 EPFL, Switzerland martin.odersky@epfl.ch

² K.U.Leuven, Belgium adriaan.moors@cs.kuleuven.be

ABSTRACT. We report on our experiences in redesigning Scala's collection libraries, focussing on the role that type systems play in keeping software architectures coherent over time. Type systems can make software architecture more explicit but, if they are too weak, can also cause code duplication. We show that code duplication can be avoided using two of Scala's type constructions: higher-kinded types and implicit parameters and conversions.

1 Introduction

Bit rot is a persistent problem in most long-running software projects. As software systems evolve, they gain in bulk but lose in coherence and clarity of design. Consequently, maintenance costs increase and adaptations and fixes become more complicated. At some point, it's better to redesign the system from scratch (often this is not done and software systems are left to be limping along because the risk of a redesign is deemed to high).

At first glance it seems paradoxical that bits should rot. After all, computer programs differ from other engineering artefacts in that they do not deteriorate in a physical sense.

```
trait TraversableLike[+A, +Repr] {
  def map[B, That](f: (A) ⇒ B)(implicit bf: CanBuildFrom[Repr, B, That]): That
  def filter(p: (A) ⇒ Boolean): Repr
}
trait Seq[+A] extends TraversableLike[A, Seq[A]]
```

- Separate implementation traits (ending in -Like) where method implementations defined
 - parameterized on the representation type Repr

```
trait TraversableLike[+A, +Repr] { def map[B, That](f: (A) \Rightarrow B)(implicit bf: CanBuildFrom[Repr, B, That]): That def filter(p: (A) \Rightarrow Boolean): Repr } trait Seq[+A] extends TraversableLike[A, Seq[A]]
```

- map is passed a 3-parameter CanBuildFrom typeclass
 - Source type Repr
 - New element type B
 - Result type That

```
trait TraversableLike[+A, +Repr] {
  def map[B, That](f: (A) ⇒ B)(implicit bf: CanBuildFrom[Repr, B, That]): That
  def filter(p: (A) ⇒ Boolean): Repr
}
trait Seq[+A] extends TraversableLike[A, Seq[A]]
```

- Paraphrasing of what CanBuildFrom[Repr, B, That] means:
 - "when mapping from a Repr to a new element type B, the new collection shall have type That"
- Type-inference guided by the result of implicit parameter lookup!

```
trait TraversableLike[+A, +Repr] { def map[B, That](f: (A) \Rightarrow B)(implicit bf: CanBuildFrom[Repr, B, That]): That def filter(p: (A) \Rightarrow Boolean): Repr } trait Seq[+A] extends TraversableLike[A, Seq[A]]
```

- Note filter() does not accept a CanBuildFrom typeclass
 - Never changes the element type, only the number of elements

CanBuildFrom

```
trait CanBuildFrom[-From, -Elem, +To] {
def apply(from: From): Builder[Elem, To]
def apply(): Builder[Elem, To]
   A factory for Builders, mutable object that accumulates
   elements, then builds a new collection with them
object Seq {
implicit def canBuildFrom[A]: CanBuildFrom[Seq[_], A, Seq[A]] = {..}
```

CanBuildFrom instances

- Default typeclass instances are defined for each collection type
 - Live in companion objects (global provider scope)

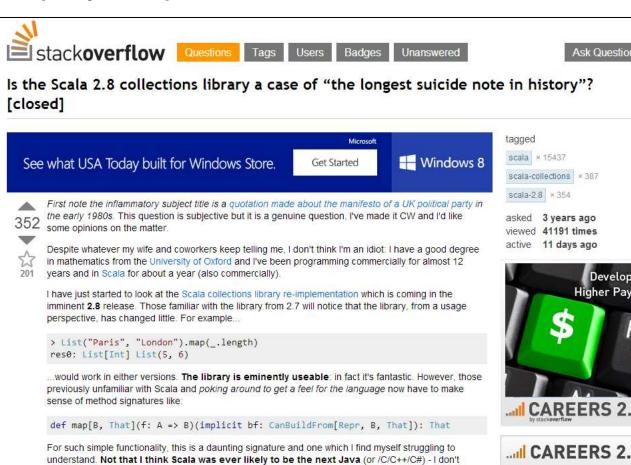
```
object Set {
  implicit def canBuildFrom[A]: CanBuildFrom[Set[_], A, Set[A]] = {..}
}
```

- Defaults can be overridden by more specific typeclasses
 - Definition of specificity partial ordering is 2 dense pages in Scala spec (Section 6.26.3 Overload Resolution)
 - Basically follows intuition

```
object BitSet {
  implicit def canBuildFrom: CanBuildFrom[BitSet, Int, BitSet]= {..}
}
```

After Scala 2.8

- Scala 2.8 Collections API was the first time typeclass-driven polymorphism used in Scala
- Mechanism
 "worked" but
 was unfamiliar
 to Scala devs
- Extra
 complexity in
 type signatures
 unwelcome



After Scala 2.8

 To my knowledge, Stanford's Daniel Ramage was the first person to apply the technique outside Collections

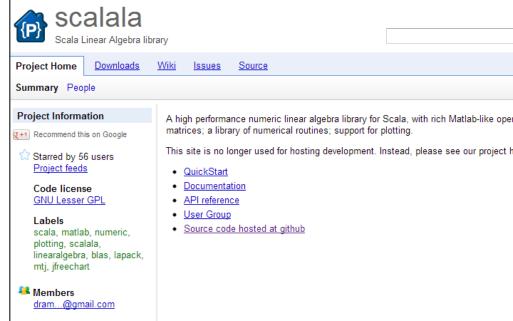
def :*[B,That](b : B)(implicit op : BinaryOp[This,B,OpMul,That]) : That = op(repr,b)

scala> SparseArray(1,0,2) :* Array(2.0,2.0,2.0)

res3: SparseArray[Double](2.0,0.0,4.0) **

scala> SparseArray(1,0,2) :+ Array(2,2,2)

res4: Array[Int](3,2,4) **



After Scala 2.8

- "Functional Dependencies in Scala"
 - July 2011 blog by Scala researcher/engineer Miles Sabin
 - Recognized that typeclass-driven polymorphism technique was equivalent to Functional Dependencies in Haskell



What is "Functionally Dependent"?

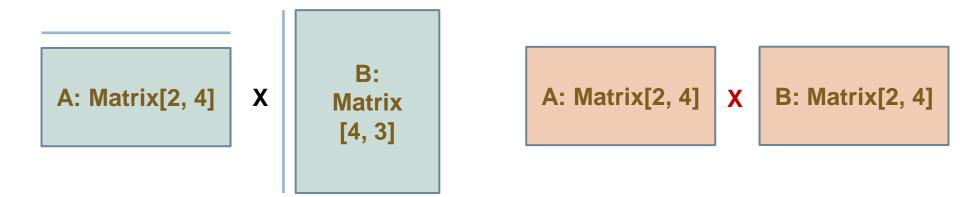
- The technique relies on a 3+ parameter typeclass where the last parameter is uniquely determined by the first two
 - I.e. it is "functionally dependent" upon them

def map[B, That](f: (A) \Rightarrow B)(implicit bf: CanBuildFrom[Repr, B, That]): That

- Working in tandem with type-inference, this creates a type-level function
 - **CanBuildFrom[A, B, C]** is $A \otimes B => C$
- The static type of map() is computed by a type level function that runs during compilation

An Example: Shaped Matrices

 Matrix multiplication is only defined when the columns in the matrix left match the rows in the right matrix



- 1. Encode a matrix's shape into it's type
- 2. Typeclass-based polymorphic product operator
- 3. Type-safe, shaped matrix multiplication!

Thank you