- 1). Find the derivative of the function $f(x) = 5(x + 47)^2$
- 2). Determine the minimum and maximum of the function $f(x) = 3x^3 + 15x^2$. Then sketch it.

Find the partial derivatives $\frac{\partial f}{\partial x}$ and $\frac{\partial f}{\partial y}$ for the following functions:

3).
$$f(x, y) = 3x + 4y$$

4).
$$f(x, y) = xy^3 + x^2y^2$$

5).
$$f(x, y) = x^3y + e^x$$

6).
$$f(x, y) = xe^{2x+3y}$$

7). Given the function $J(\mathbf{w})$:

$$J(w_0, w_1) = \frac{1}{2m} \sum_{i=1}^{m} (w_0 + w_1 \mathbf{x}^{(i)} - y_i)^2$$

Determine
$$\frac{\partial J(\mathbf{w})}{\partial w_0}$$
 and $\frac{\partial J(\mathbf{w})}{\partial w_1}$

8). Find the derivative of the function $f(x) = \frac{1}{1 + e^{-x}}$