

Course: COEN279/AMTH377

Lecturer: Yuan Wang

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Data/Time: 2021/04/28 7:10am - 8am

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1. If c_2 and n_0 exist such that $6n^3 \leq c_2$ for all $n \geq n_0$.

Then $n \leq c_2/6$, is a contradiction.

Since c_2 is constant, it cannot possibly hold for arbitrary large n

Hence, it is proved that, $6n^3$ is not equal to $\Theta(n^2)$

2. MyFunction(n) {	running time
i, j, k, count = 0	1
for i = n/2; i <= n; i = i+1	n/2
for j = 1; j <= n; j = 2*j	(n/2-1)log n
for k = 1; k <= n; k = k*2	(n/2-1)(log n-1)log n
count = count + 1	(n/2-1)(log n-1)(log n-1)
}	

Time complexity = $1 + (n/2) + (n/2-1)\log n + (n/2-1)(\log n)\log n + (n/2-1)(\log n)(\log n) = (n/2)(\log_2 n)^2$

$$= n/2(n)$$

$$= O(n^2 \log n)$$

3. $T(n) = 9T(n/3) + T(n^2)$

We have $a = 9$, $b = 3$, $f(n) = \Theta(n^2)$

$$n^{\log_b a} = n^{\log_3 9} = n^2$$

, so $f(n) = \Theta(n^{\log_b a})$.

This is Case 2 of the Master Theorem. Thus,

$T(n) = \Theta(n^2 \log n)$.

4.

```
// Function to find the winner present in a given array
public static int findwinner (int[] A)
{
    // `w` stores the winner
    int w = -1;                                C1

    // initialize counter `i` with 0
    int i = 0;                                C2

    // do for each element `A[j]` in the array
    for (int j = 0; j < A.length; j++)          n+1
    {
        // if counter `i` becomes 0
        if (i == 0)                            C3
        {
            // set the current candidate to `A[j]`
            w = A[j];                          C4*(n)

            // reset counter to 1
            i = 1;                              C5
        }

        // increments the counter if `A[j]` is a current candidate
        else if (w == A[j]) {
            i++;                                C6
        }

        // decrements the counter if `A[j]` is a current candidate
        else {
            i--;                                C7
        }
    }

    return w;                                  C8
}
```

```

}

public static void main (String[] args)
{
    // If Winning person is present
    //here, b represents array of candidates
    int[] b= { //array of candidates}           C9

    System.out.println("The winning person is " + findwinner(b)); C10
}

```

Time complexity= $c_1 + c_2 + n + 1 + c_3 + c_4 * (n) + c_5 + c_6 + c_7 + c_8 + c_9 + c_{10}$

So, the time complexity $T(n) = O(n)$.

Here, the algorithm is a linear algorithm so the time complexity will be $O(n)$.