

Given: $\hat{y} = [0.5 \quad -4.5 \quad -9.5]^T$ $y = [0 \quad -4 \quad -9]^T$

• Find RMSE and MAE of (y, \hat{y})

$$\begin{aligned} \text{RMSE} &= \sqrt{\frac{\sum (\hat{y} - y)^2}{n}} = \sqrt{\frac{(0.5 - 0)^2 + (-4.5 + 4)^2 + (-9.5 + 9)^2}{3}} \\ &= \sqrt{\frac{(0.5)^2 + (-0.5)^2 + (-0.5)^2}{3}} = \sqrt{\frac{0.25 + 0.25 + 0.25}{3}} \\ &= \sqrt{\frac{0.75}{3}} = \sqrt{\frac{75}{100 \times 3}} = \sqrt{\frac{1}{4}} = \frac{1}{2} = 0.5 // \end{aligned}$$

$$\begin{aligned} \text{MAE} &= \left(\frac{1}{n}\right) * \sum |\hat{y} - y| = \left(\frac{1}{3}\right) * [0 - 0.5| + |-4 + 4.5| + |-9 + 9.5|] \\ &= \frac{1}{3} * [0.5 + 0.5 + 0.5] = \frac{1}{3} * 1.5 = \frac{1}{3} * \frac{15}{10} \\ &= \frac{1}{2} = 0.5 // \end{aligned}$$

• Find $\|y\|_0$, $\|y\|_1$, $\|y\|_2$ and $\|y\|_\infty$

$$\rightarrow \|y\|_0 = 2 //$$

$$\|y\|_1 = |0| + |-4| + |-9| = 0 + 4 + 9 = 13 //$$

$$\|y\|_2 = \sqrt{(0)^2 + (-4)^2 + (-9)^2} = \sqrt{0 + 16 + 81} = \sqrt{97} //$$

$$\|y\|_\infty = 9 //$$