

HOMEWORK 2**Assigned 09/04/25****Due 09/11/25 on ELC before class.**

Combine the gauss function from the lecture notes with the shape functions from Homework 1.

Using gauss quadrature, evaluate the integral below to produce a stiffness matrix. **Use linear shape functions**, assuming that the single element extends from $x=0$ to $x=3$ in the global domain. Remember that the shape functions from the previous homework are written with respect to ξ (parent domain), not x (global domain).

$$\begin{aligned} [K]^e &= \int_0^3 [B]^{eT} AE [B]^e dx \\ A &= 1 + 0.05x^2 \\ E &= 10^5 \end{aligned}$$

Based on the shape functions selected, the form of the polynomial you are integrating is $\alpha_0 + \alpha_1 x + \alpha_2 x^2$. This should only require two gauss points for exact evaluation.

Remember the following conversions. We can calculate the corresponding value of x for each gauss point ξ_{gp} using shape functions:

$$x(\xi_{gp}) = [N(\xi_{gp})][x]^e$$

This is a necessary step when evaluating the area A as a function of x .

This approach allows us to calculate the Jacobian by taking the derivative of the shape functions with respect to ξ :

$$J = \frac{dx}{d\xi} = \frac{d}{d\xi} ([N(\xi_{gp})][x]^e) = [GN(\xi_{gp})][x]^e$$

Which then allows us to take the derivatives of our shape functions with respect to x :

$$[B(\xi_{gp})]^e = \frac{d}{dx} [N(\xi_{gp})]^e = \frac{d\xi}{dx} \frac{d}{d\xi} [N]^e = \frac{1}{J} [GN(\xi_{gp})]$$