

Mini-Project 2: Logistic Regression & Disaster Survival

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In this mini-project you will use logistic regression to determine whether you would have survived the Titanic sinking. To find out, we will use the titanic dataset (`titanic_data.csv`), containing the following information of 887 passengers: 1) whether they survived or not (1 = survived, 0 = deceased), 2) passenger class, 3) gender (0 = male, 1 = female), 4) age, 5) number of siblings/spouses aboard, 6) number of parents/children aboard, and 7) fare:

	Passenger 1	Passenger 2	Passenger 3	...	Passenger 887
Survived	0	1	1	...	0
Passenger Class	3	1	3	...	3
Gender	0	1	1	...	0
Age	22	38	26	...	32
Siblings/Spouses	1	1	0	...	0
Parents/Children	0	0	0	...	0
Fare	7.25	71.2833	7.925	...	7.75

Our goal is to construct a classifier that determines/predicts whether an individual would survive or not. Let $y_i \in \{0, 1\}$ be the *label* indicating whether the i^{th} individual survived, and let $\mathbf{x}_i \in \mathbb{R}^6$ denote the feature vector of the i^{th} individual (containing all remaining variables). For example, $y_1 = 0$ and $\mathbf{x}_1 = [3 \ 0 \ 22 \ 1 \ 0 \ 7.25]^\top$. Our goal is to construct a classifier that given \mathbf{x} determines y .

In this mini-project we will use logistic regression, whose classifier has the form:

$$\underbrace{\frac{1}{1 + e^{-\boldsymbol{\beta}^\top \mathbf{x}}}}_{P(y=1|\mathbf{x})} \stackrel{\hat{y}=1}{\underset{\hat{y}=0}{\gtrless}} \underbrace{1 - \frac{1}{1 + e^{-\boldsymbol{\beta}^\top \mathbf{x}}}}_{P(y=0|\mathbf{x})}, \quad (2.1)$$

and is parametrized by the coefficient vector $\boldsymbol{\beta} \in \mathbb{R}^6$, which we aim to find by maximizing:

$$\ell(\boldsymbol{\beta}) := \sum_{i=1}^N \log \left[\left(\frac{1}{1 + e^{-\boldsymbol{\beta}^\top \mathbf{x}_i}} \right)^{y_i} \left(1 - \frac{1}{1 + e^{-\boldsymbol{\beta}^\top \mathbf{x}_i}} \right)^{1-y_i} \right], \quad (2.2)$$

which is simply another way to write (2.1) for N training samples.

- (a) Create a function that implements (2.2).
- (b) The gradient of $\ell(\boldsymbol{\beta})$, which is also a vector in \mathbb{R}^6 , is given by:

$$\nabla \ell(\boldsymbol{\beta}) = \sum_{i=1}^N \left(y_i - \frac{1}{1 + e^{-\boldsymbol{\beta}^\top \mathbf{x}_i}} \right) \mathbf{x}_i \quad (2.3)$$

Create a function that implements (2.3).

- (c) Since we cannot simply set (2.3) to zero and solve for β , we have to use optimization techniques like gradient ascent, whose update is given by:

$$\beta_{t+1} = \beta_t + \eta \nabla \ell(\beta_t), \quad (2.4)$$

where $\eta \in \mathbb{R}$ is the *step size* (often called *learning parameter*). Gradient ascent simply iterates (2.4) until $\ell(\beta_t)$ converges. Create a function that implements gradient ascent.

- (d) Randomly split your data into training (80%) and testing (20%).
- (e) Run gradient ascent on your training data for different values of η . If η is too big, you may run into numerical errors or loose accuracy. If η is too small, it may take too long to converge. What value of η seems best to maximize $\ell(\beta)$? What is the best (largest) $\ell(\beta)$ you can achieve?
- (f) What coefficient vector β do you obtain using your choice of η from (e)? How accurately does this predict survival on the test data?
- (g) What would be *your* feature vector. According to your classifier, would *you* have survived? Under which circumstances (passenger class, family aboard, and fare), would your prediction be different?
- (h) According to your answer from (f), which seem to be the 3 features that most affect survival? Visualize survivals as a function of these variables.

I have created the following code to help you get started:

```

1  % © Daniel L. Pimentel-Alarcón, 2018, http://danielpimentel.github.io
2  close all; clear all; clc;
3
4  % ===== LOAD DATA =====
5  data = csvread('titanic_data.csv',1,0);
6  Y = data(:,1)'; % labels
7  X = data(:,2:end)'; % feature vectors
8
9  % ===== SPLIT DATA =====
10 Y_train = % COMPLETE HERE: 80% of labels
11 X_train = % COMPLETE HERE: 80% of features
12 Y_test = % COMPLETE HERE: 20% of labels
13 X_test = % COMPLETE HERE: 20% of features
14
15 % ===== GRADIENT ASCENT =====
16 eta = % COMPLETE HERE: Choose step size
17 tol = % COMPLETE HERE: Choose tolerance for convergence
18 beta = gradientAscent(Y_train,X_train,eta,tol); %COMPLETE HERE: Code this function
19
20 % ===== TEST =====
21 Y_hat = classify_logReg(X_test,beta); %COMPLETE HERE: Code this function
22 error = sum(abs(Y_hat - Y_test)) / length(Y_test)
23
24 % ===== WOULD I HAVE SURVIVED? =====
25 my_class = %COMPLETE HERE: What class would you have bought?
26 my_gender = %COMPLETE HERE: 0=male, 1=female
27 my_age = %COMPLETE HERE: Your age
28 my_ss = %COMPLETE HERE: How many spouse/siblings would you have traveled with?
29 my_pc = %COMPLETE HERE: How many parents/children would you have traveled with?
30 idx = find(X(1,:)==my_class); % people in the same class as me
31 my_fare = mean(X(6,idx)); % average fare in my class
32
33 % Construct my feature vector
34 my_x = %COMPLETE HERE: Put together your feature vector
35
36 % Classify
37 my_y = classify_logReg(my_x,beta) %COMPLETE HERE: (You already coded this function above)
38
39 % ===== VISUALIZE 3 MOST IMPORTANT VARIABLES =====
40 %COMPLETE HERE: Hint: you may use bar/pie plots.
```

References

- [1] Xiaoli Fern, *Xiaoli Fern*, available at <http://web.engr.oregonstate.edu/~xfern/classes/cs534/notes/logistic-regression-note.pdf>