

Utiliser le gradient boosting pour prédire une variable continue

↳ Gradient boost for regression

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Gradient boost for regression ≠ Linear regression

1<sup>er</sup> étape: | Moyenne des valeurs |

→ Création d'un premier arbre

→ Amélioration de l'arbre

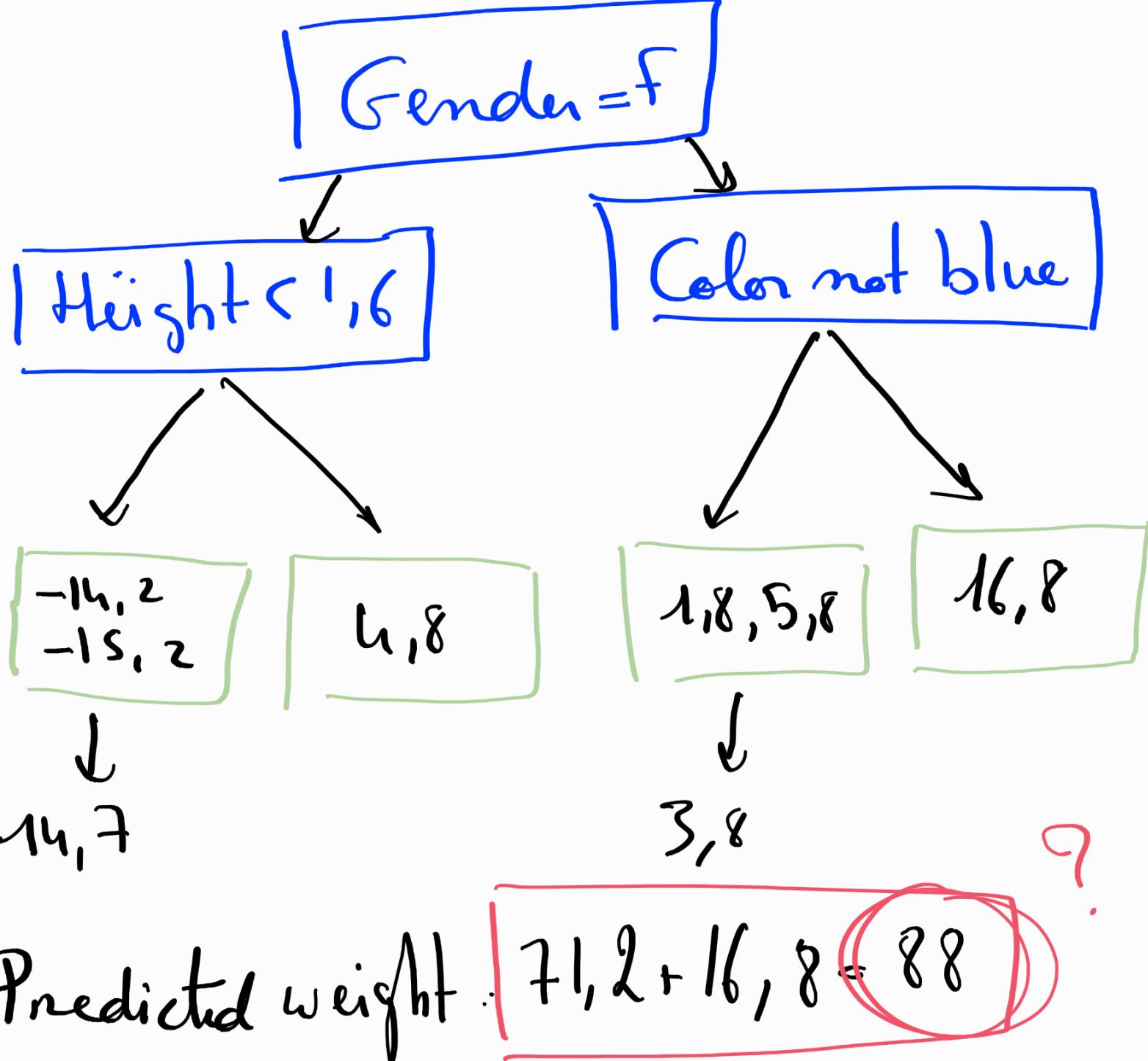
- 1) Nombre d'arbre demandé
- 2) Meilleur modèle trouvé

Height	Favorite color	Gender	Weight
1,6	Blue	n	88
1,6	Green	F	76
1,5	Blue	f	56
1,8	Red	n	73
1,5	Green	n	77
1,6	Blue	f	57

→  $\bar{w} = 71,2$

## Residual

-6,8	4,8	-15,2	1,8	5,8	-14,2
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Predicted weight:  $71,2 + 16,8 = 88$  ?

No! The model fits the training data too well

→ low Bias  
high Variance

$\Rightarrow$  learning rate

↳ average weight

$$\boxed{71,2}$$

+ Learning rate.



$$0 < < 1$$

fix it st : 0, 1

Predicted weight :  $71,2 + (0,1 \times 16,8) = 72,9$

$$\Rightarrow 72,9 \neq 88$$

↳ Let's built one other tree

↳ Recalcul the residual  
with the learning rate  
superposition.

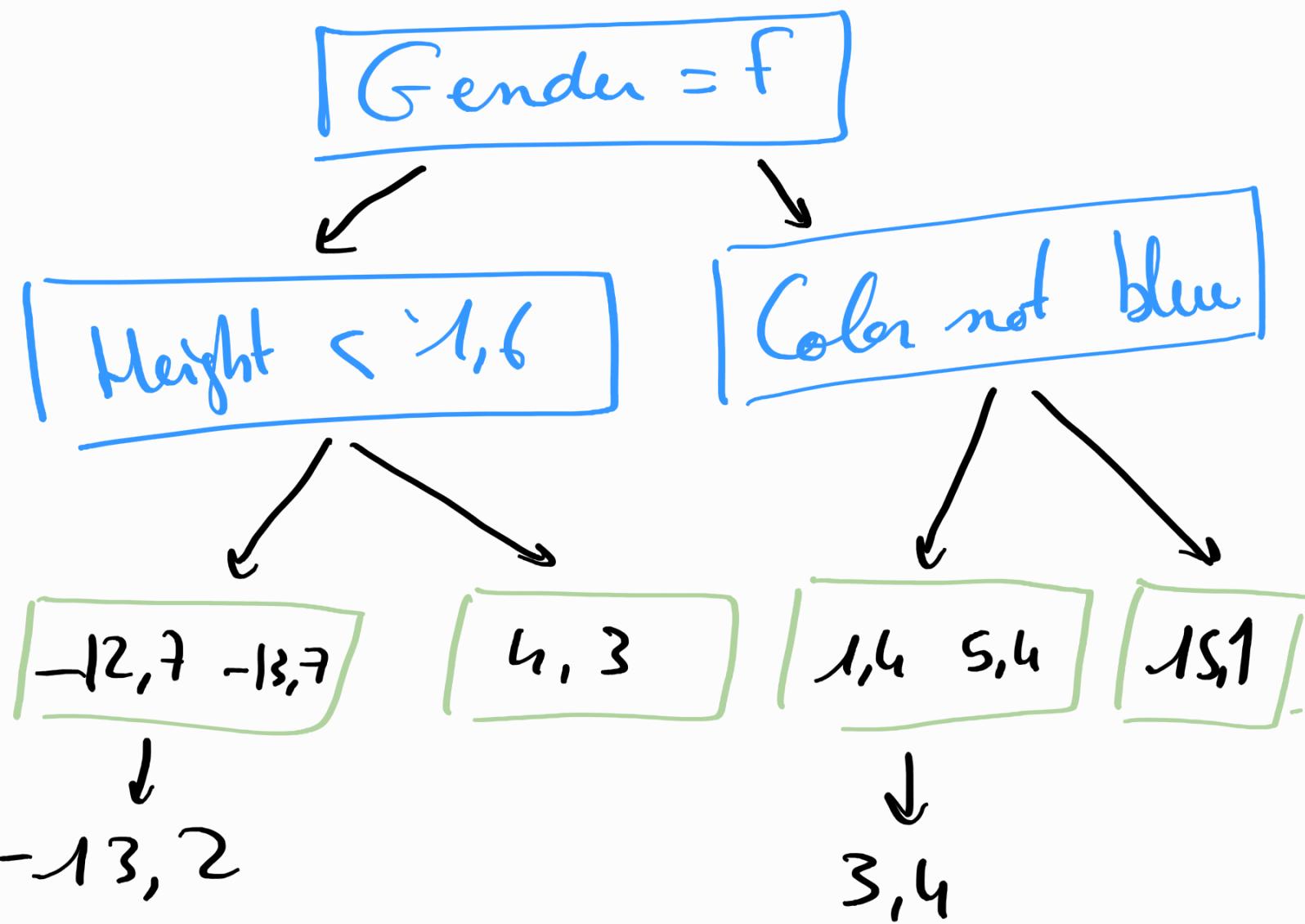
## New Residual

-15,1	4,3	-13,7	-1,4	5,4	-12,7
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$$\hookrightarrow 88 - (71,2 + 0,1 \times 16,8) = 15,1$$

→ The new residuals are a bit smaller than before. We are getting closer and closer from the right prediction

→ Let's build the tree with the new residual



Now we use the average weight plus the 1<sup>st</sup> tree plus the 2<sup>nd</sup> tree

$$\Rightarrow 71,2 + 0,1 \times 16,8 + 0,1 \times 15,1$$

$$= 71,4$$

The new prediction

## New residual

13,6	3,9	-12,4	-1,1	5,1	-11,4
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Another small step through the  
good prediction

The a third tree  
↳ skip the details

→ Prediction of the first  
weight is  $\underline{\underline{70}}$

## Conclusion:

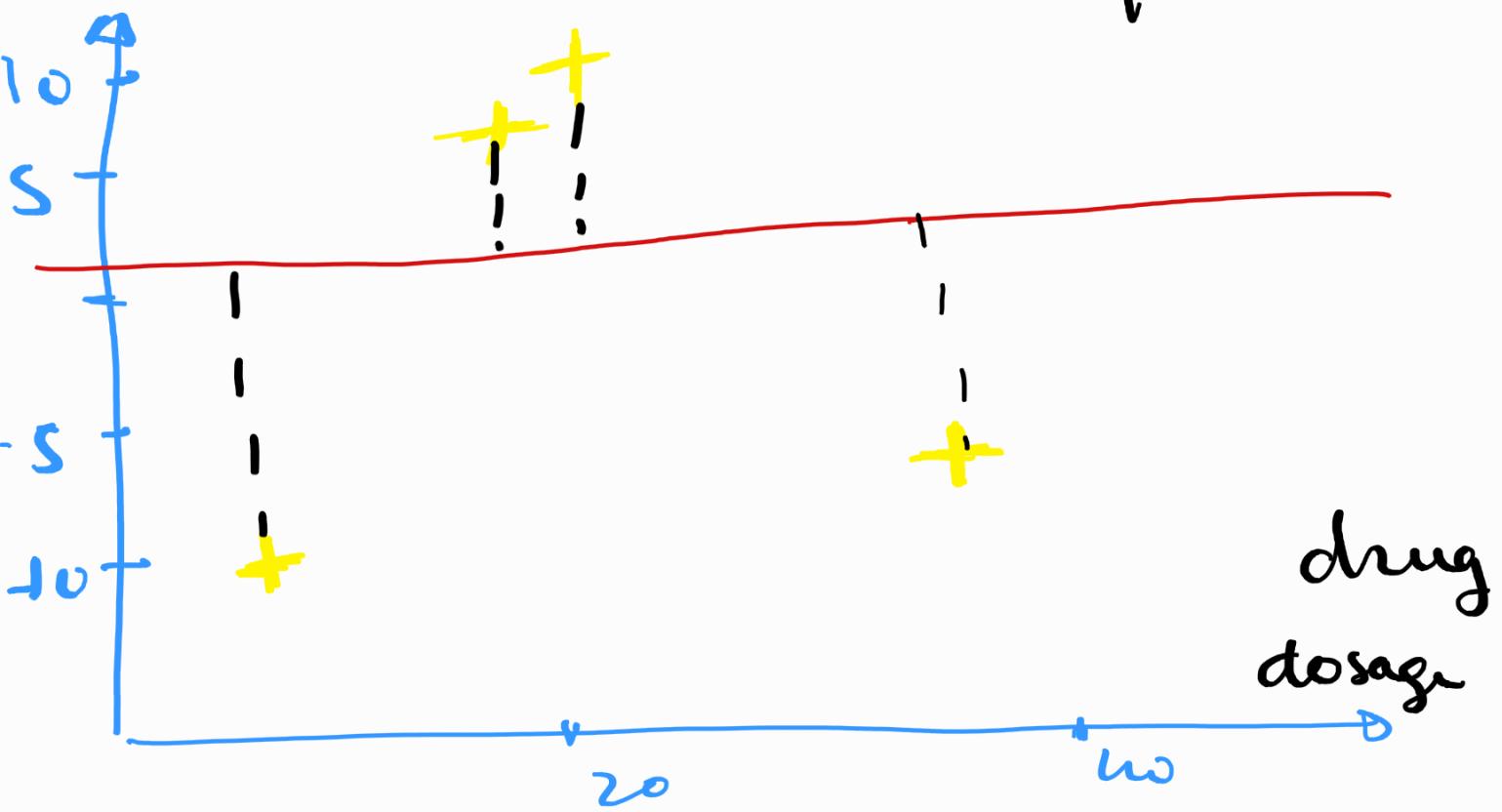
$$f_{1,2} + \underline{0,1} \times \text{Tree}_1$$

$$+ \underline{0,1} \times \text{Tree}_2$$

depth

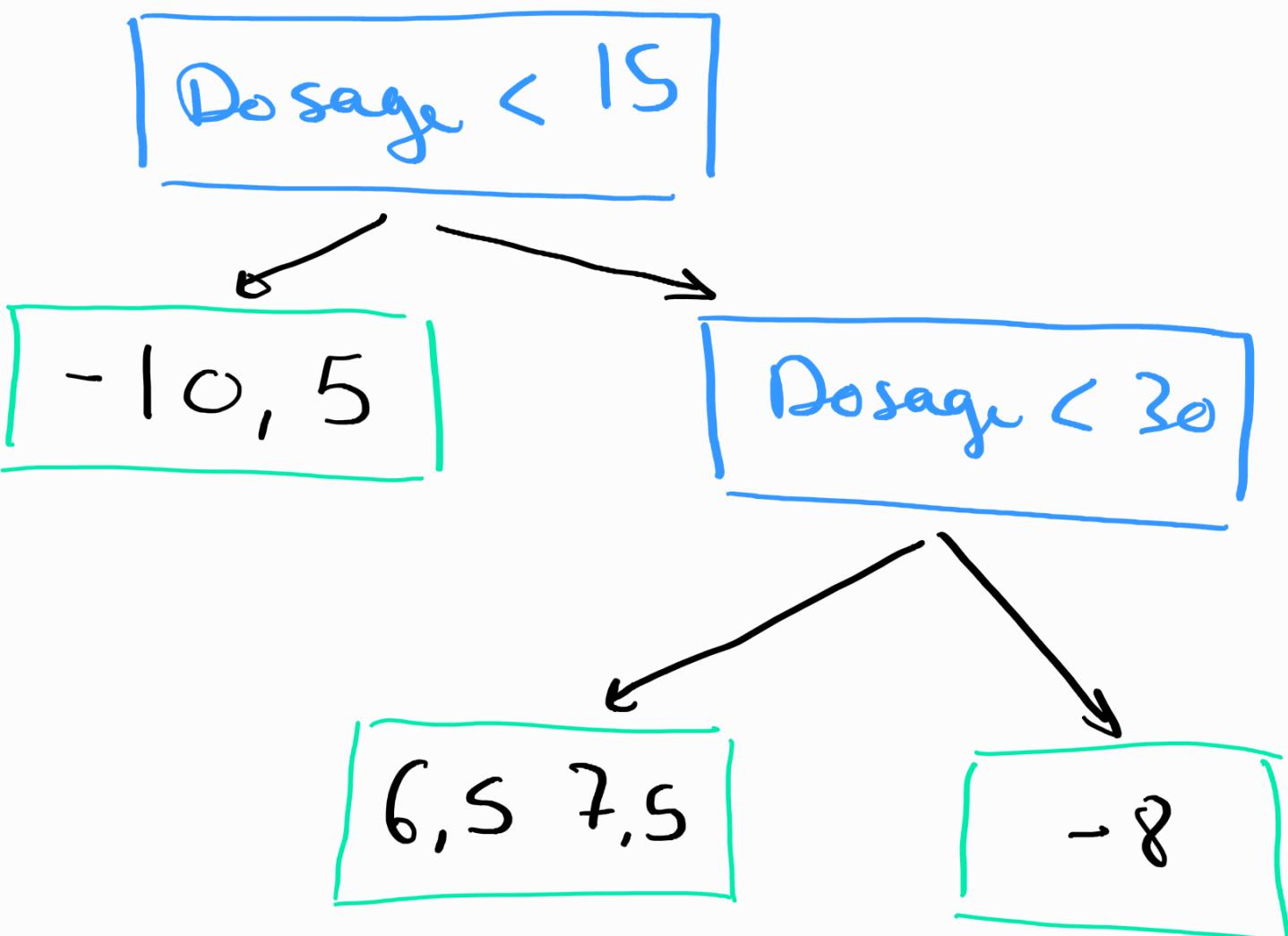
$$+ \underline{0,1} \times \text{Tree}_3$$

XG boost → Regression  
→ Classification



# Predicted drug Effectiveness

→ 0,5



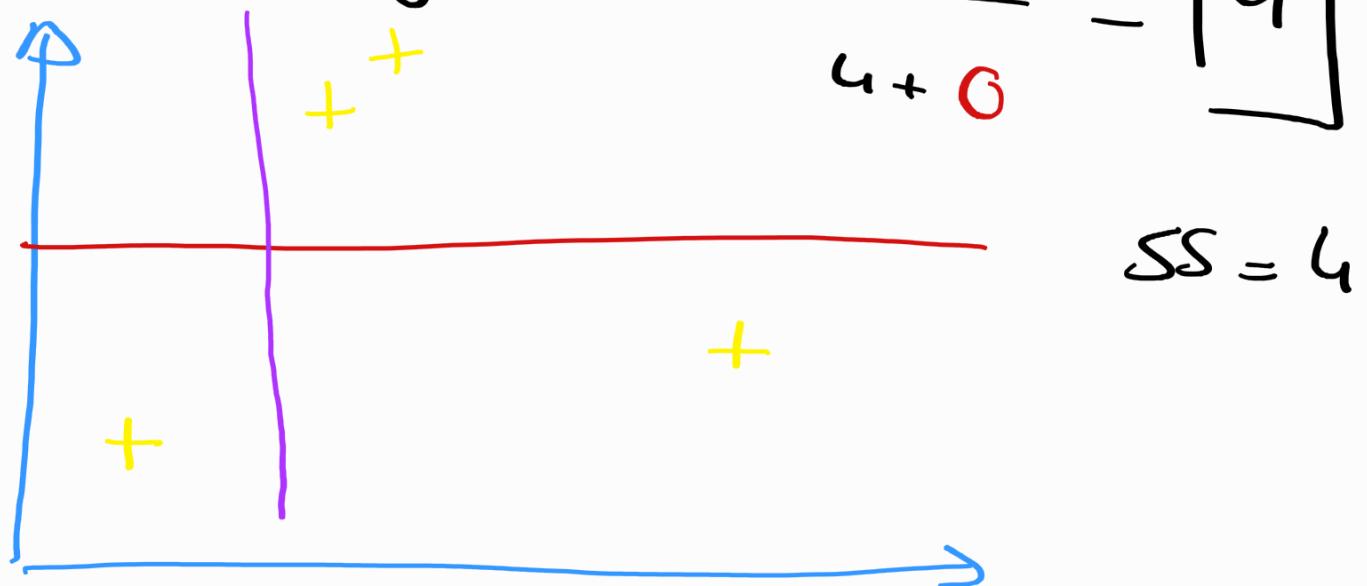
$$[-10,5 / 6,5 / 7,5 / -7,5]$$

Similarité score

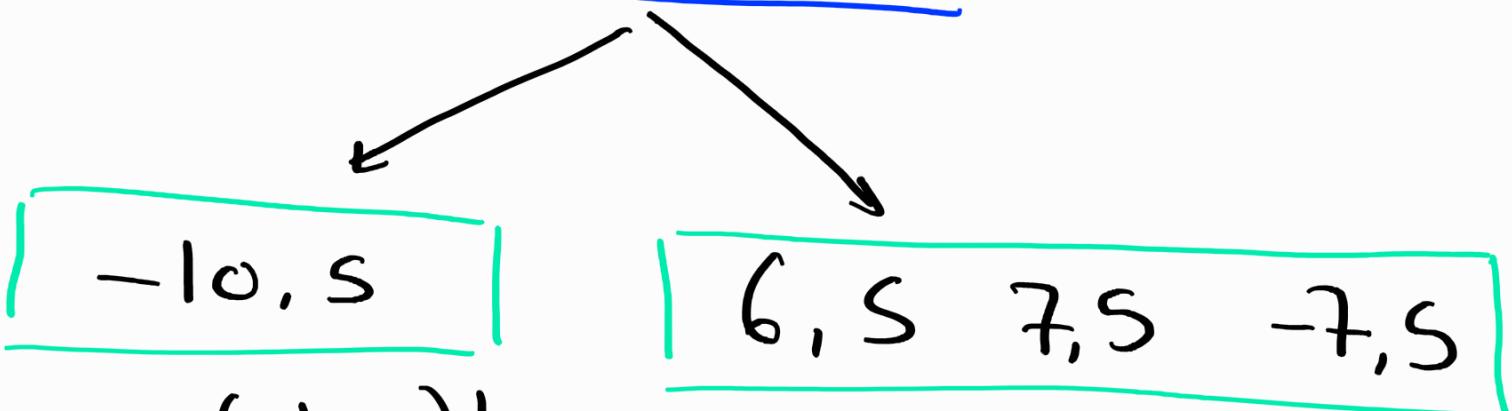
$$= \frac{\left( \sum_{i=1}^n \text{Residuals} \right)^2}{m + \lambda}$$

$$\frac{(-10,5 + 6,5 + 7,5 - 7,5)^2}{4 + 0}$$

Similarity score =  $\frac{(-4)^2}{4 + 0} = 4$



Do saq < 15



$$SS = \frac{(-10, S)^2}{1}$$
$$= 110, 25$$

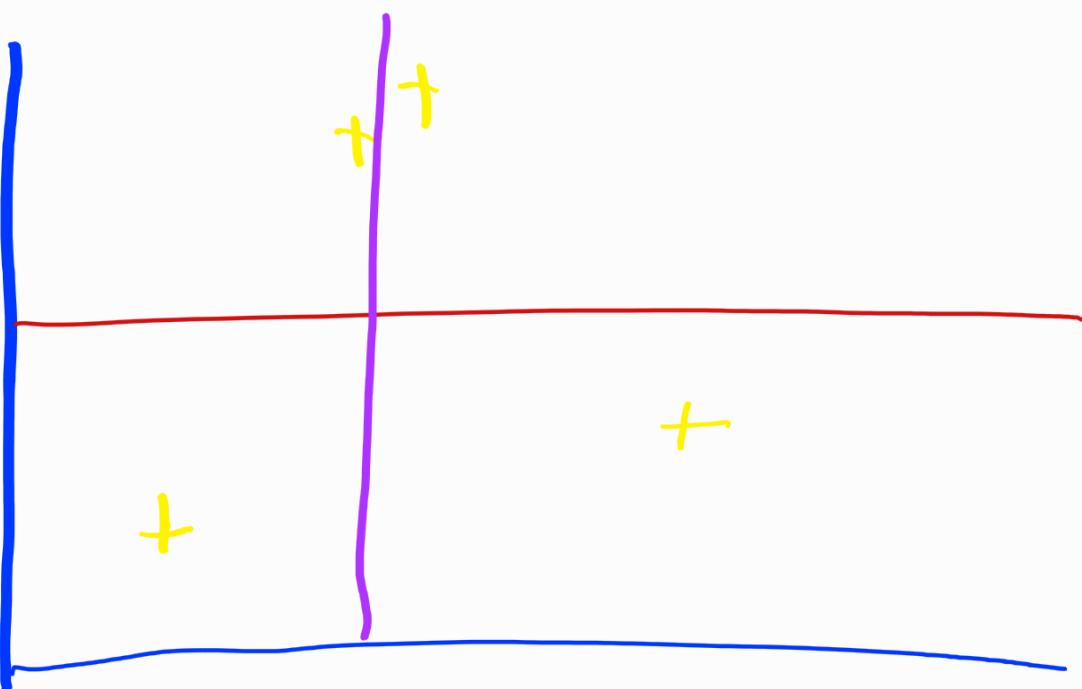
$$SS = \frac{(6, S + 7, S - 7, S)^2}{3}$$
$$= 14, 08$$

$$\text{Gain} = \text{left}_{ss} + \text{Right}_{ss} - \text{Root}_{ss}$$

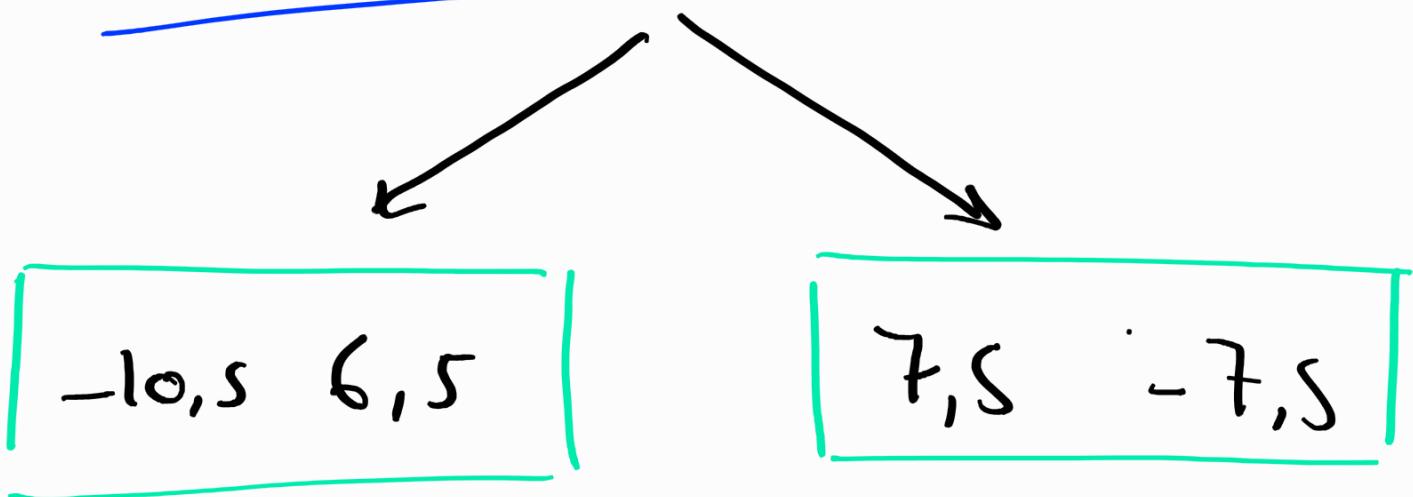
$$= 110, 25 + 14, 08 - 4$$

$$\boxed{\text{Gain}_1 = 120, 33}$$

let's see the gain for  
an other threshold



$-10, S \quad 6, S \quad 7, S \quad -7, S$



$$SS = 8$$

$$SS = 0$$

$$\frac{\text{Gain} = 8 + 0 - 4}{\text{Gain}_2 = 4}$$

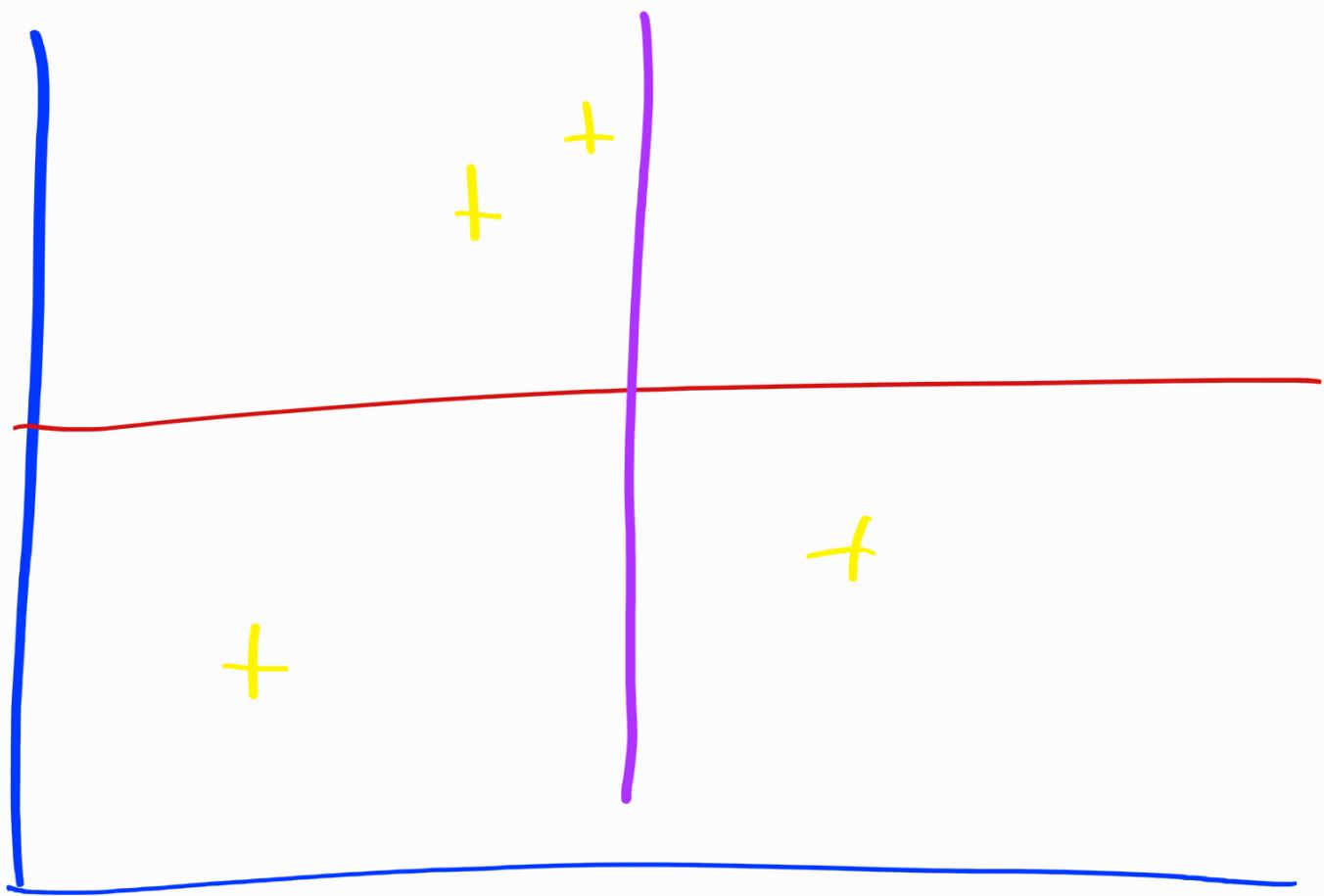
$$\text{Gain}_1 = 120,33$$

$$\text{Gain}_2 = 4$$

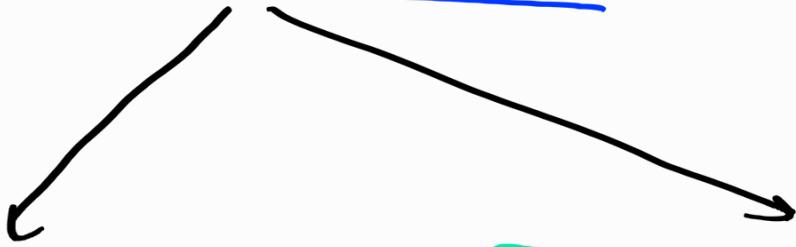
$$\Rightarrow \text{Gain}_1 > \text{Gain}_2$$

$$120,33 > 4$$

Gain<sub>1</sub> is better than Gain<sub>2</sub>



Dosage < 30



$$SS_1 = 4,08$$

$$SS_2 = 56,25$$

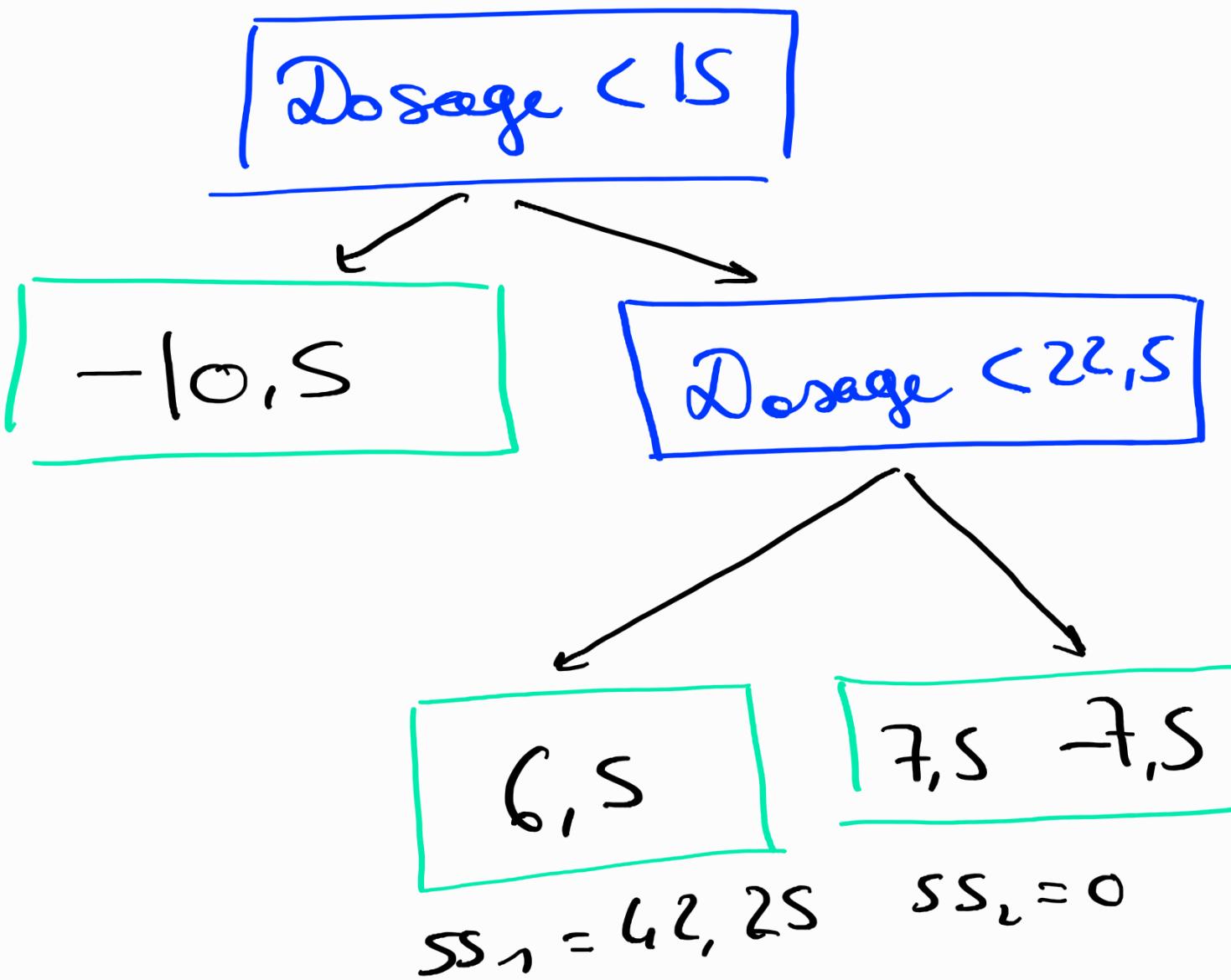
$$Gain_3 = 4,08 + 56,25 - 45 \cdot 56,33$$

$$Gain_3 = 56,33$$

$$Gain_2 < Gain_3 < Gain_1$$

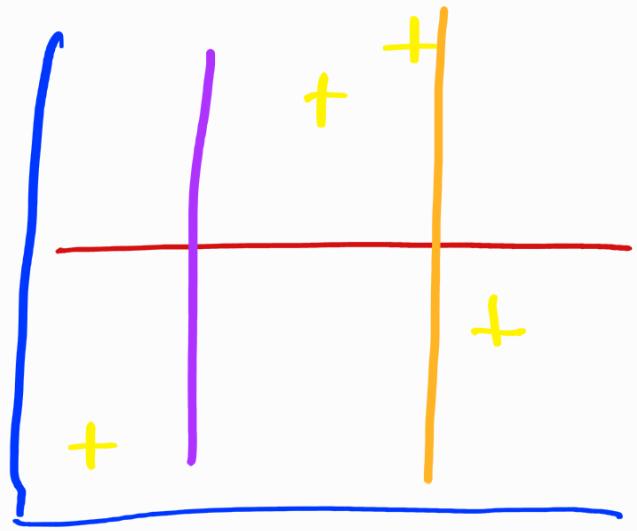
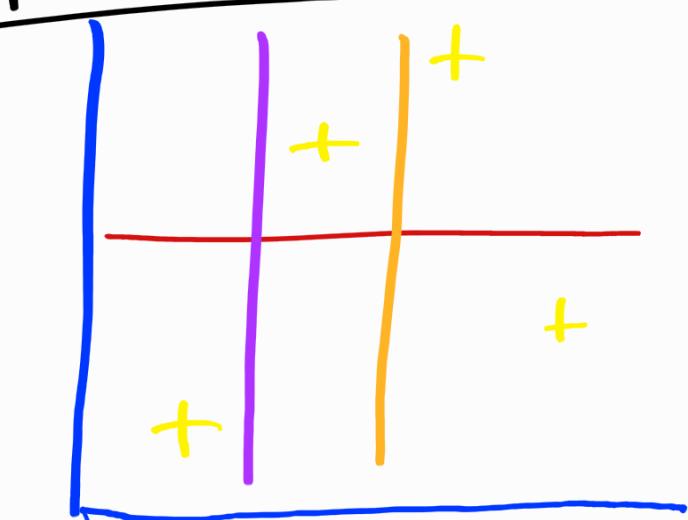
$$\Rightarrow 4 < 56,33 < 120,33$$

Dosage < 15 is better  
a splitting the obs.



$$\text{Gain} = 42,2S + 0 - 14,0S$$

$\text{Gain}_1 = 28,17$



Dosage < 15

-10, S

Dosage < 30

6, S 7, S

-7, S

$$SS_1 = 98$$

$$SS_2 = 56,25$$

$$Gain_2 = 98 + 56,25 - 16,02$$

$$Gain_2 = 140,17$$

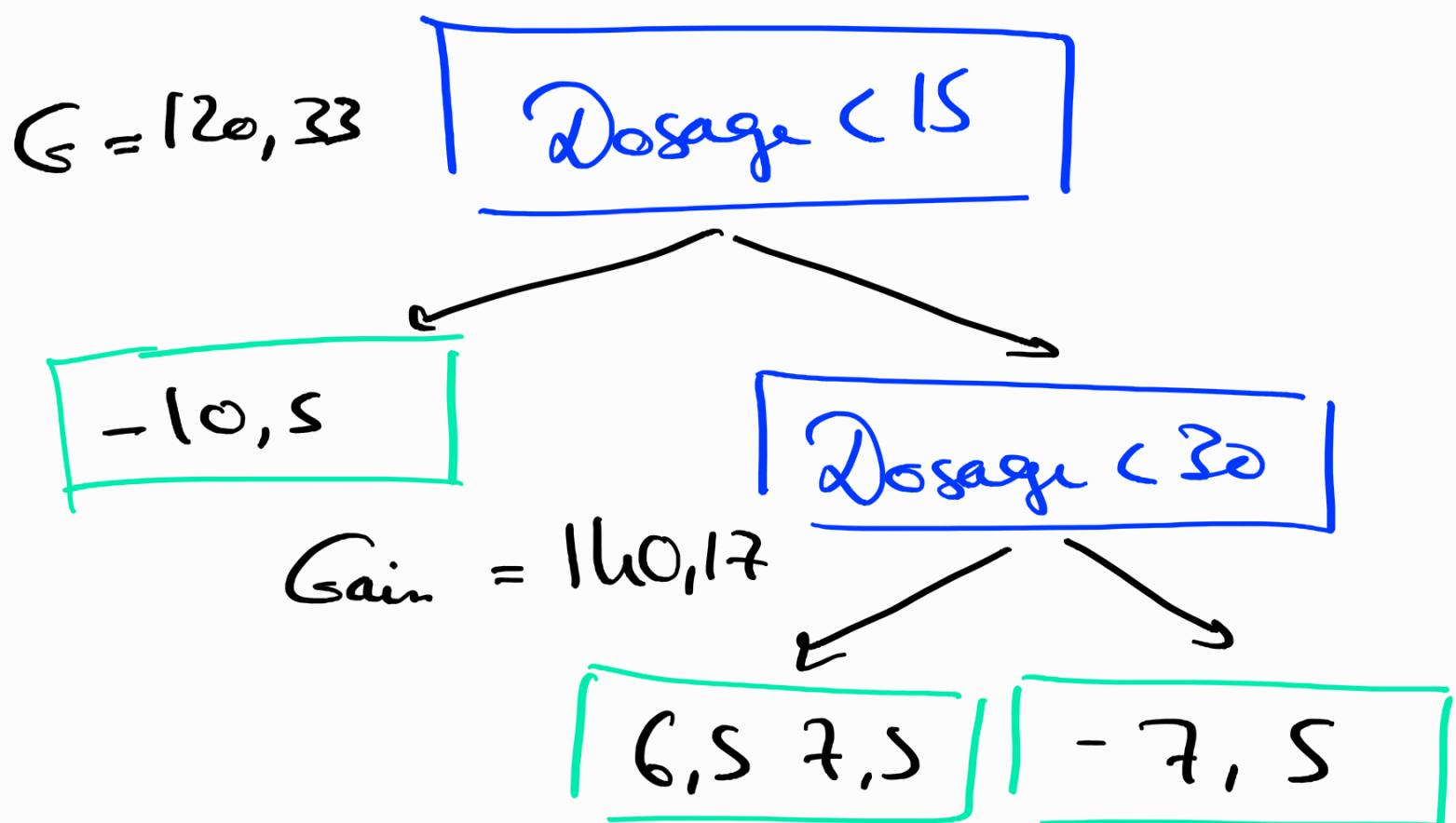
$$\Rightarrow Gain_2 > Gain_1$$

$$140,17 > 28,17$$

$\Rightarrow$  Gain<sub>2</sub> which is  
Dosage < 30 is the better  
threshold.

The tree is done

find tree is:



Let's fix  $\gamma = \underline{130}$

Gain -  $\gamma < 0$

Remove the branch.

$$140, 17 - 130 > 0$$

$\Rightarrow$  Do not remove the branch

$$\gamma = 150$$

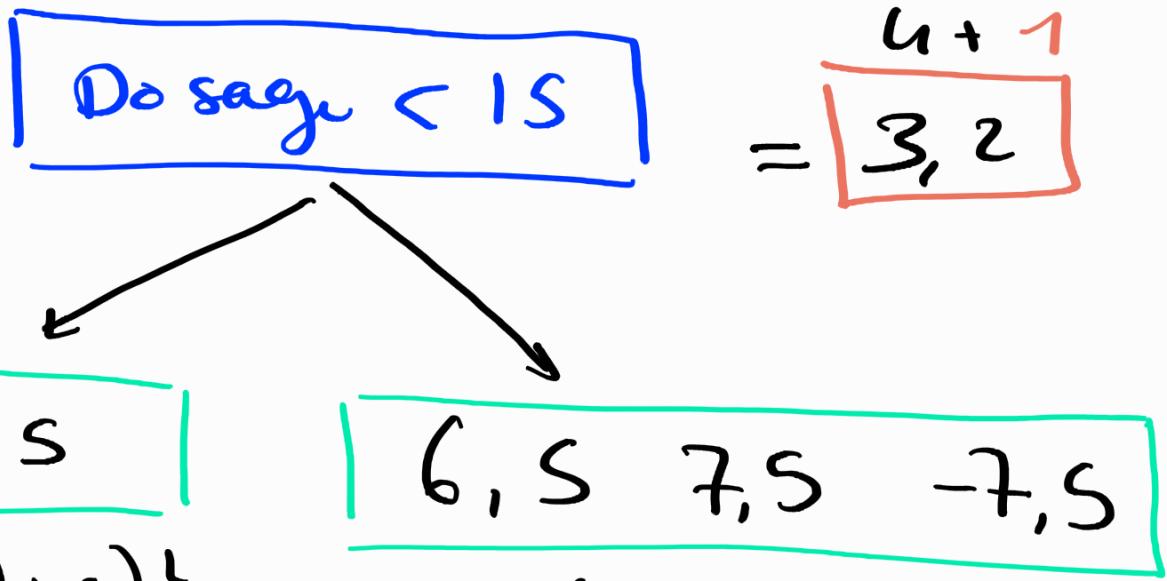
$\Rightarrow$  We remove the branch and there no predicate.

Let's fix  $\lambda = 1$

Remember  $\lambda$  is a regularization parameter, which means that it is intended to reduce the prediction's sensitivity to individual observation.

$$SS = \frac{(-10, S + 6, S + 7, S - 7, S)^2}{4 + 1}$$

$$= \boxed{3, 2}$$



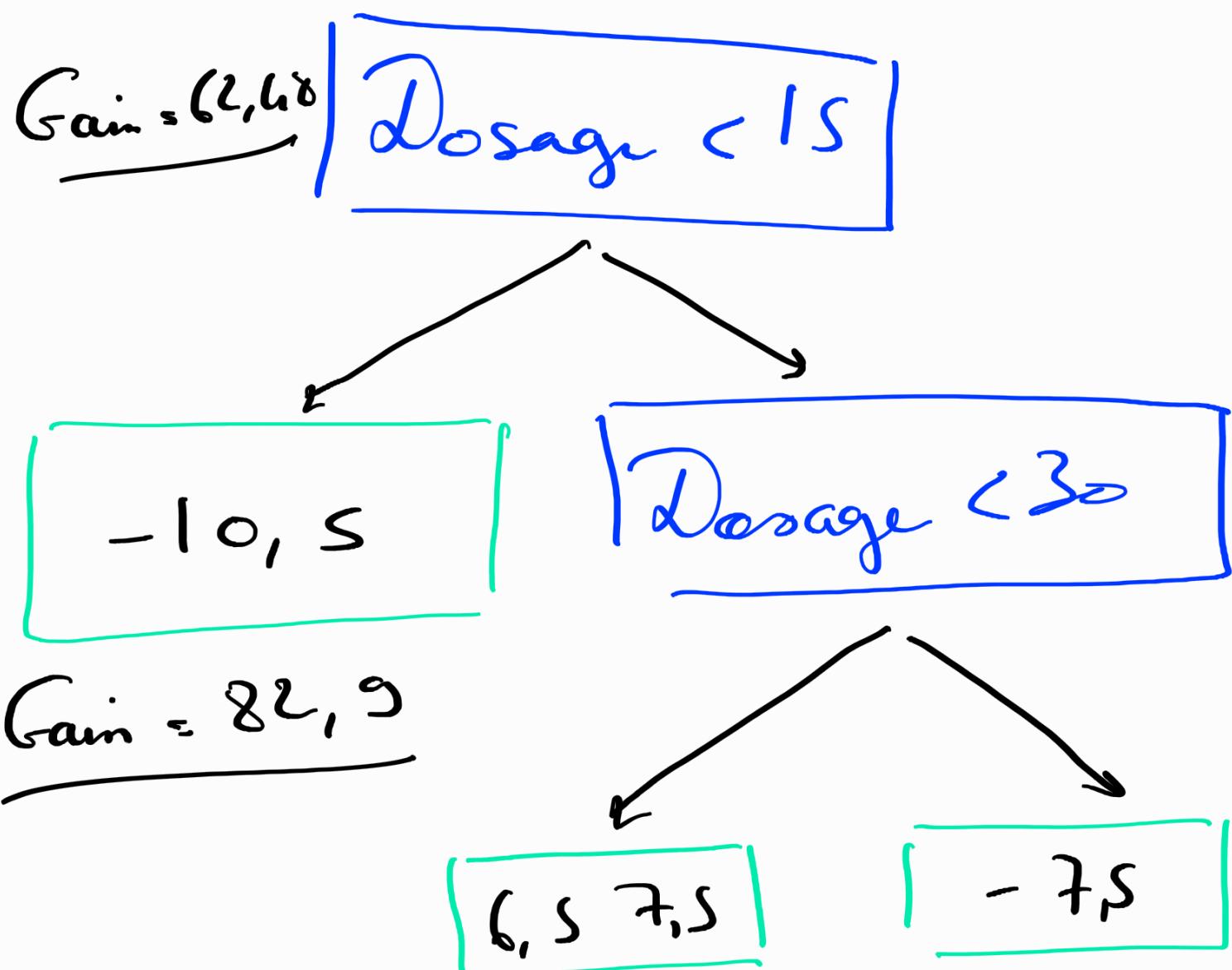
$$SS = \frac{(-10, S)^2}{1 + 1}$$

$$= 55, 12$$

$$SS = \frac{(6, S + 7, S - 7, S)^2}{3 + 1}$$

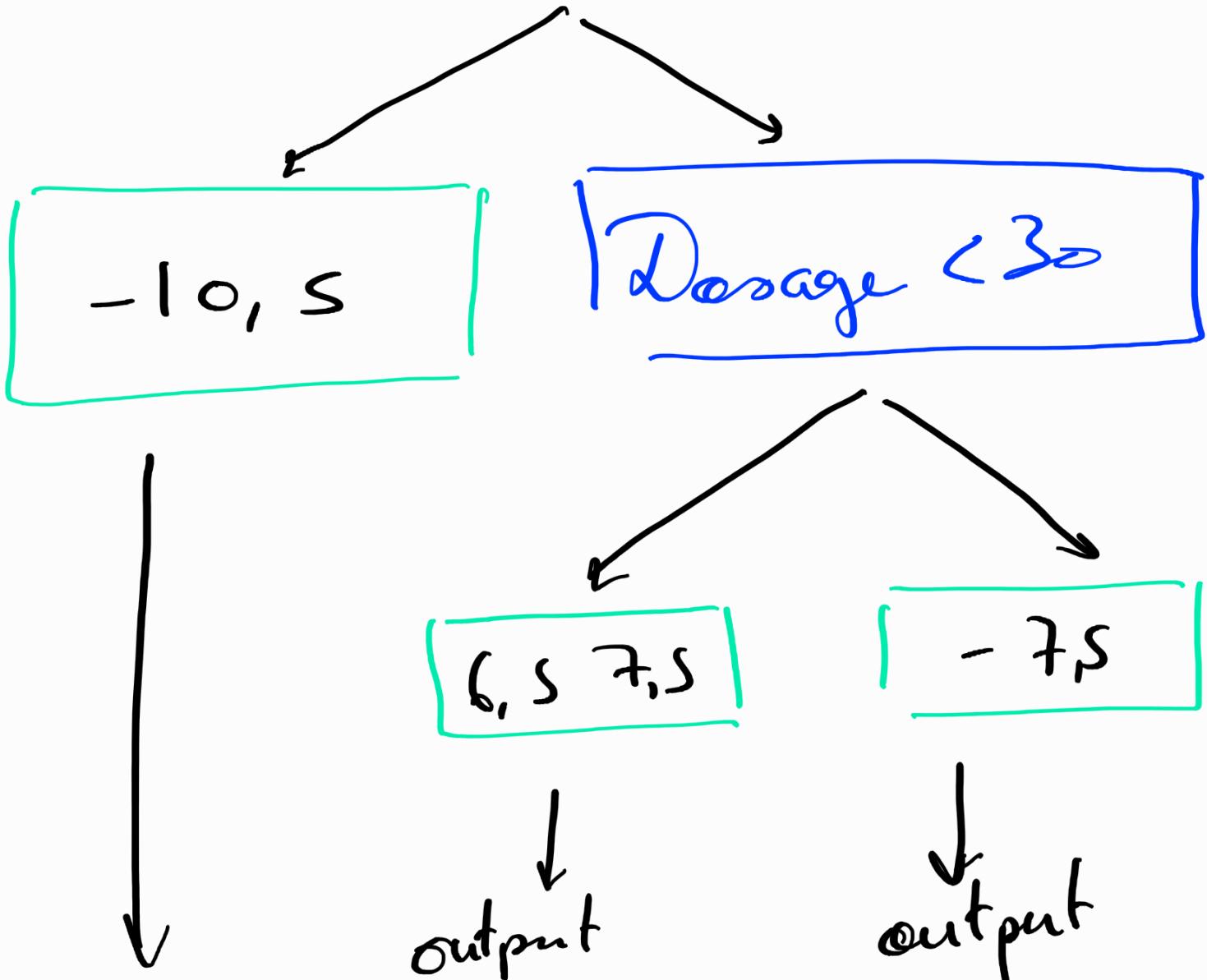
$$= 10, 56$$

$$\text{Gain} = SS_{12} + 10,56 - 3,2 \\ = 62,48$$



$\lambda > 1 \Rightarrow$  prevent overfitting.

| Dosage < 1S |



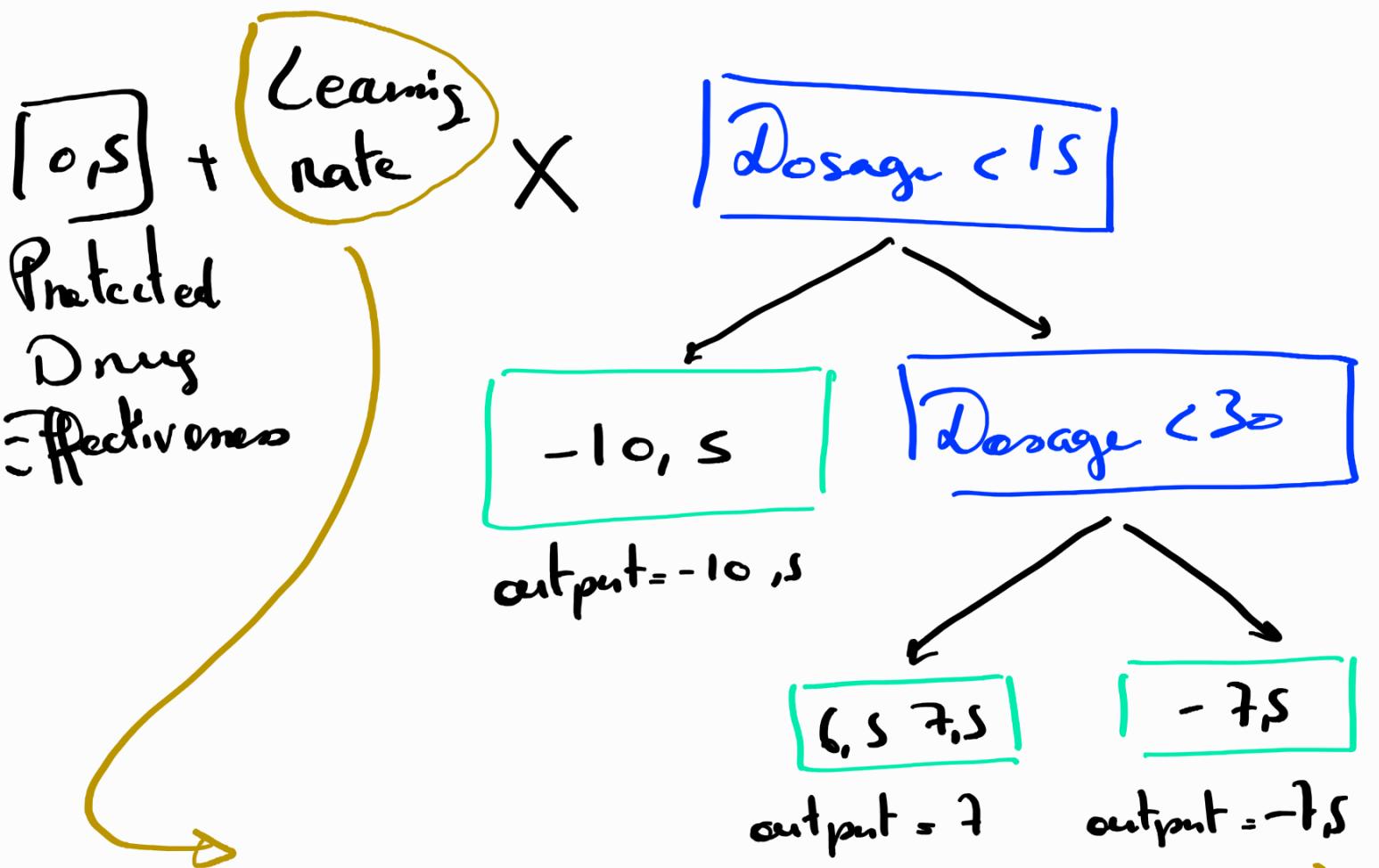
Output

$$= \frac{-10S}{1+0}$$

$$= -10, S$$

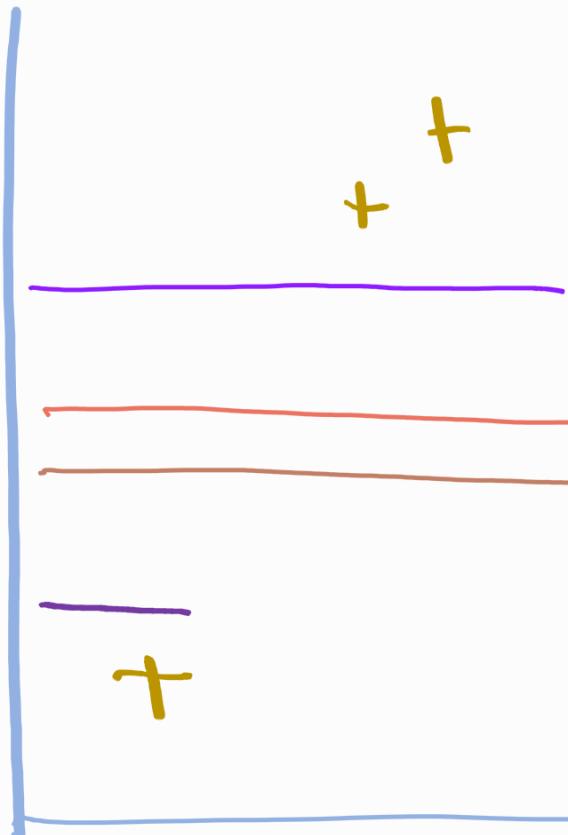
$$\begin{aligned} &= \frac{6, S + 7, S}{1+0} \\ &= 7 \end{aligned}$$

$$\begin{aligned} &= \frac{-7, S}{1+0} \\ &= -7, S \end{aligned}$$



Learning rate :  $\epsilon = 0,3$  (default value)

- $0,5 + (0,3 \times -10,5) = -2,65$
- $0,5 + (0,3 \times 7) = 2,6$
- $0,5 + (0,3 \times -7,5) = -1,75$



Continue to build trees with  
the same learning rate until  
the residual are super small or we  
have reached the maximum number