

sit with your clan if you can

CMPS 12B/M Introduction to Data Structures

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How fast is HighArray?

- How many steps does it take on average to do these operations for HighArray?
 - (Assume no duplicates allowed)
 - \blacksquare Let *n* be number of elements in array.
 - Insert
 - Delete
 - ▼ Find

What are we discovering?

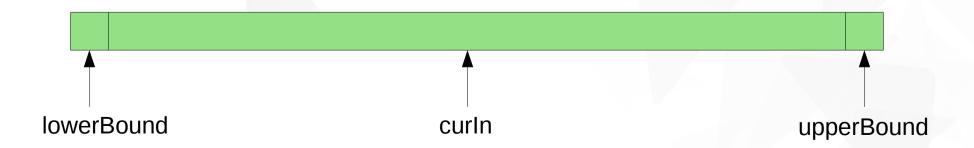
- Need to carefully define the thing we're counting
 - "step" is ambiguous
 - "comparison" or "array access" are better
- Insert is faster than delete
- ▼ Find is linear in size of array

How fast is OrderedArray?

- How many steps does it take on average to do these operations for OrderedArray?
 - (Assume no duplicates allowed)
 - \blacksquare Let *n* be number of elements in array.
 - Insert
 - Delete
 - ▼ Find

Binary Search

- You're looking for a needle in a haystack
- Compare needle to middle hay
 - If it matches, you're done
 - If it is smaller, then find the needle in the left haystack
 - If it is larger, then find the needle in the right haystack
- To keep track of where we're looking:
 - lowerBound, curln, upperBound
 - Keep going until lowerBound > upperBound



Questions

- How many comparisons will it take?
- Does it matter if we pick the "upper" middle or the "lower" middle?
- Experiment time
 - Run the algorithm for n=10
 - Each group pick randomly: upper/lower middle
 - Use seat row last digit for which number to search for, in:
 - $\mathbf{7}$ 0 1 2 3 4 5 6 7 8 9

Formula for Comparisons

■ What function is the number of comparisons as n gets bigger?

What function looks like this?

Worse case:

7	n=10	4	

Recurrence Relation

- Another way of thinking about the question...
 - Let T(n) be the function we're trying to find
- What happens when you double the number of businesses?
 - ▼ For OrderedArray:
 - **¬** T(2n) = ____ T(n) ____

You Can Solve Recurrences

- Techniques
 - Guess and check (the most powerful technique)
 - Look for patterns (linear, quadratic, logarithmic, exponential)
 - Ask Wolfram Alpha



Another Recurrence

- What about HighArray?
- How many comparisons does HighArray take?
 - **¬** T(2n) = ____ T(n) ____
 - Solve it using guess & check (since you already know the answer)

Comparing Algorithms

- If we know the exact problem size n
 - \neg Can directly compare $T_1(n)$ and $T_2(n)$ for different algorithms
- How do we compare algorithms more abstractly?
 - Different "classes" of algorithms
 - Grow bigger in n in different ways
 - Don't care so much about specific ratio with fixed problem size

Some Classes of Algorithms

- Examples:
 - Linear doubling the n makes it twice as big
 - Searching unordered array (average or worst case)
 - Constant changing n doesn't make it change
 - Inserting into an array without holes
- Our latest class:
 - Logarithmic doubling n makes it one bigger

Ignoring the Constant

- All linear algorithms have a formula like:
 - T(n) = K n
 - Average number of comparisons to find an element in an unordered array: 1/2 n
 - Worst case number of comparisons to find an element in an unordered array: n
- Key idea of Big O notation
 - **¬** Ignore the constant
 - All linear algorithms are in O(n)
 - O(something) is a set of functions that grow as n gets bigger like something

Big O

Some algorithms and running times

■ Linear search O(n)

■ Binary search O(log n)

■ Insert into unordered array O(1)

■ Insert into ordered array O(N)

■ Delete in unordered array O(N)

■ Delete in ordered array
O(N)

Simplifying into Big O

Suppose an algorithm always takes 3 comparisons no matter the size of the input.

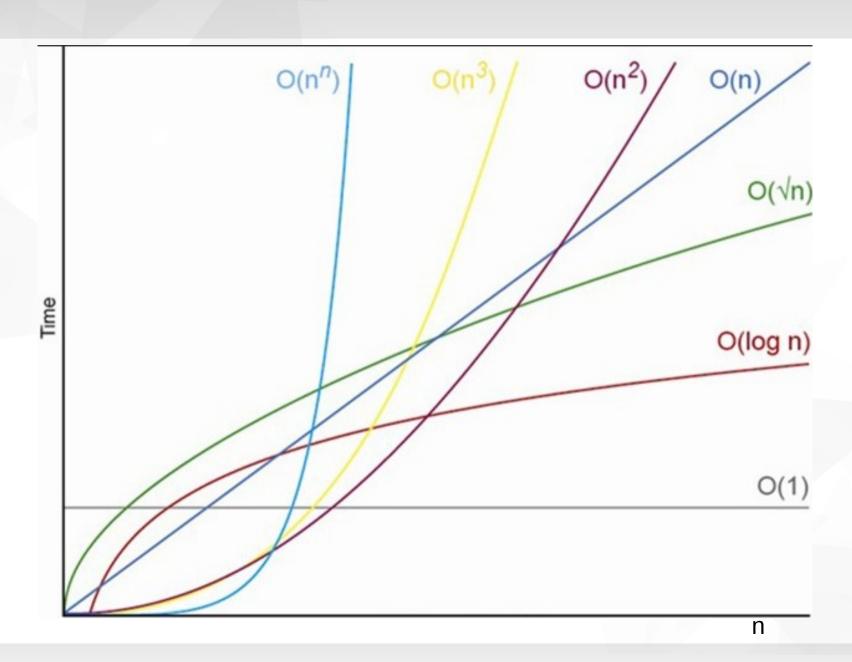
¬
$$T(n) = 3$$

Suppose an algorithm takes n comparisons to scan through an entire array, then does another n comparisons to scan it again

¬
$$T(n) = 2n$$

ignore any multiplicative constant

Complexities Graphed



Cheatsheet

Data Structure	Time Complexity							
	Average				Worst			
	Indexing	Search	Insertion	Deletion	Indexing	Search		
Basic Array	0(1)	0 (n)	-	-	0(1)	0 (n)		
Dynamic Array	0(1)	0 (n)	0 (n)	0(n)	0(1)	0 (n)		
Singly-Linked List	0(n)	0 (n)	0(1)	0(1)	0 (n)	0 (n)		
Doubly-Linked List	0(n)	0 (n)	0(1)	0(1)	0 (n)	0 (n)		
Skip List	0(log(n))	0(log(n))	0(log(n))	0(log(n))	0(n)	0 (n)		

http://bigocheatsheet.com/

A Business Problem

- Suppose we have a text file
 - One line per business
 - Business name, colon, phone number
- Need a program that:
 - Starts up, reads all businesses
 - Waits for queries that are business names
 - Prints out phone number for matching business
 - OR shows "NOT FOUND" if no business found
- Which data structure should we use?
 - How do we decide?
 - Does it even matter?

Simplest Thing

- Start with simplest thing
 - Put everything in an array

```
class Record {
    public String name;
    public String number;
class BusinessDatabase {
    // Database of all businesses
    private Record[] businesses;
    public Record parse(String txt) {
        // Parsing code here
    // Parse the input lines
    // Assuming one business per line
    public void parseData(String[] lines) {
        int numBusinesses = lines.length;
        businesses = new Record[numBusinesses];
        for(int i = 0; i < lines.length; i++) {</pre>
            Record rec = parse(lines[i]);
            businesses[i] = rec;
```

What about search?

■ To find a business:

```
// Search for a business
public String getPhoneNumber(String name) {
    for (int i = 0; i < businesses.length; i++) {
        if (name.equals(businesses[i].name)) {
            return businesses[i].number;
        }
    }
    return "NOT FOUND";
}</pre>
```

How many comparisons does it take to find a business if there are 1,000,000?

Which is better for problem?

- Decide between unordered and ordered array
 - Once data is all loaded and processed, which is better for searching?
 - ▼ For small numbers of businesses, probably doesn't matter
 - Logarithmic growth is slower as n increases
 - ▼ For 1,000,000 businesses, go with ordered array
- But how do we get the data into order?
 - Inserting each business would take O(n), for each business...

how do we order the data?

Simple Sorting

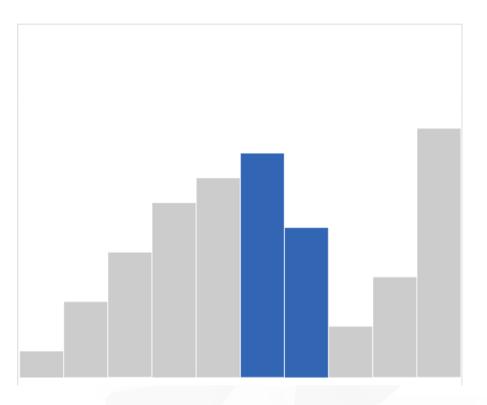
■ Well if you're sure, better be... GRYFFINDOR!

Sort Problem

- Suppose you had an unordered array, and wanted an ordered array
- Operations allowed:
 - Compare two items
 - Swap two items, or copy one item to a temp location
- All sorting algorithms do the same basic things
 - ▼ Produce ordered output using compares/swaps
 - Difference in the details

Bubble Sort

- Scan through left to right
 - Compare adjacent entries
 - If they are wrong way around, swap them
- If any swaps were made, loop back again
- No swaps made means you're done



http://www.algomation.com/player?algorithm=54162b10f3166302000a91f2

Bubble Sort in Java

- Examples/Chap03/BubbleSort/bubbleSort.java
- Observation:
 - ▼ Each run through, we know we have the biggest element to the right
 - So stop scanning once we hit the finished section on the right

Running Time of BubbleSort

- How many comparisons does optimized bubble sort make in the worst case?
 - **▼** For n=10:
 - **¬** Our variation: 9+9+9+9+9+9+9+9
 - With observation: 9+8+7+6+5+4+3+2+1

The End