

# CMPE 16 Homework 1

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1. Express each of the sets below by listing all of their elements when the set is finite, and otherwise listing at least 6 elements.

(a)  $\{9n - 7 : n \in \mathbb{Z}\}$

**Answer :**  $\{\dots, -7, 2, 11, 20, 29, 38 \dots\}$

(b)  $\{x \in \mathbb{Z} : 2x^2 - 7 < 43\}$

**Answer :**  $\{-4, -3, -2, -1, 0, 1, 2, 3, 4\}$

(c)  $\{x \in \mathbb{N} : 2x^2 - 7 \leq 43\}$

**Answer :**  $\{1, 2, 3, 4, 5\}$

(d)  $\{n \in \mathbb{Z} : 0 < n^2 - 4 < 38\}$

**Answer :**  $\{-7, -6, -5, -4, -3, 3, 4, 5, 6, 7\}$

(e)  $\{\sin \frac{n\pi}{2} : n \in \mathbb{Z} \text{ and } n \text{ is odd}\}$

**Answer :**  $\{1, -1\}$

(f)  $\{X \subseteq \{1,2,3,4\} : |X| = 2\}$

**Answer :**  $\{\{1, 2\}, \{1, 3\}, \{1, 4\}, \{2, 3\}, \{2, 4\}, \{3, 4\}\}$

(g)  $\{1,2,3\} \times \{1,2\}$

**Answer :**  $\{(1,1),(1,2),(2,1),(2,2),(3,1),(3,2)\}$

(h)  $\{1,2,3\} \times \mathbb{N} \times \emptyset$

**Answer :**  $\emptyset$

2. For each of the sets below give the size of the set if it is finite, and otherwise state that it is infinite.

(a)  $\{1,2,3\}$

**Answer :** 3

(b)  $\emptyset$

**Answer :** 0

(c)  $\{\emptyset\}$

**Answer :** 1

(d)  $\{\{\emptyset\}, \emptyset\}$

**Answer :** 2

(e) (Save me the trouble of having to rewrite the purposely tedious nested brackets)

**Answer :** 3

(f)  $\{\mathbb{N}, \emptyset, \mathbb{Z}\}$

**Answer :** 3

(g)  $\{1,2,3,4,5\} \times \{7,8,9\} \times \{10,11,12,13\}$

**Answer :** 60

(h) The power set of  $\{a,b,c,d,e,f\}$

**Answer :**  $2^6 = 64$

3. For the problem let  $A = \{3n + 4 \mid n \in \mathbb{N}\}$ ,  $B = \{-5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5\}$  and  $C = \{n^2 - 3 \mid n \in \mathbb{Z}\}$ . State whether each of the statements below is True or False and justify your answer.

(a)  $B \subseteq A$

**Answer** : False.  $0 \in B$  but  $0 \notin A$  Therefore  $B \not\subseteq A$

(b)  $C \subseteq \mathbb{N}$

**Answer** : False.  $-3 \in C$  but  $a > 0 \forall a \in \mathbb{N}$ . Therefore  $C \not\subseteq \mathbb{N}$

(c)  $A \subseteq \mathbb{Z}$

**Answer** : True,  $a \in \mathbb{N} \forall a \in A, \mathbb{N} \subseteq \mathbb{Z} \implies a \in \mathbb{Z} \forall a \in A$ , therefore  $A \subseteq \mathbb{Z}$

(d)  $A \subsetneq \mathbb{Z}$

**Answer** : True.  $a \in \mathbb{Z} \forall a \in A$ , also  $\exists x < 0 \in \mathbb{Z}$  while  $x < 0 \notin A$  therefore  $A \subsetneq \mathbb{Z}$

4. Give the power set of each of the sets below.

(a)  $\{1, 2, 3\}$

**Answer** :  $\{\{\emptyset\}, \{1\}, \{2\}, \{3\}, \{4\}, \{1, 2\}, \{1, 3\}, \{2, 3\}\}$

(b)  $\{\emptyset\}$

**Answer** :  $\{\emptyset\}$

(c)  $\{1, \mathbb{R}\}$

**Answer** :  $\{\emptyset, \{1\}, \{\mathbb{R}\}, \{1, \mathbb{R}\}\}$

(d)  $\{\emptyset, \{\emptyset\}\}$

**Answer** :  $\{\emptyset, \{\emptyset\}, \{\emptyset, \{\emptyset\}\}$  <sup>1</sup>

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<sup>1</sup>This one was confusing, the emptyset would appear twice so one occurrence should be removed because you can't have redundant items in a single set, I think ... ?