

CMPE 16 Lecture 3

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October 8, 2014

1 Set Operation

1.1 Intro

- For sets A and B , the \cup of A and $B = \{x : x \in A \text{ or } x \in B\}$
- The intersection of A and $B = \{x : x \in A \text{ and } x \in B\}$
- The difference of A and B , $A - B = \{x : x \in A \text{ and } x \notin B\}$
- $\mathbb{Z} - \mathbb{N} = \{x : x \in \mathbb{Z} \text{ and } x \leq 0\}$

1.2 Compliments

The complement of $A = \bar{A} = \{x : x \in \mathbb{U} \text{ and } x \notin A\}$

Notice that to perform a complement operation you need to understand what the universe is. The answer depends on whether the universe is \mathbb{R}^2 or \mathbb{N} .

- $A - B = A \cap \bar{B}$
- $A \cap B = \bar{\bar{A} \cup \bar{B}}$ (DeMorgans Law)
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Examples :

- $\sigma = \{2n + 1 : n \in \mathbb{Z} \text{ (odd numbers)}\}$
- $\mathbb{P} = \{n \in \mathbb{Z} : n > 1, n \text{ has no factor between } 1 \text{ and } n\}$
- $S = \{n^2 : n \in \mathbb{N}\} = \text{positive squares (0 is not in there)}$
- 9 is the only square that is a multiple of 9 false, $S \cap \mathbb{N} = \{9\}$
- $\mathbb{N} \cap \mathbb{P}$
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2 Index Sets

$\sum_{n=1}^{i-1} i = 1 + 2 + 3 \dots n$ So for instance, we could write the natural numbers $\mathbb{N} \cup_{i=1}^{\infty} \{i\}$
 $\mathbb{Z} = \{0\} \cup (\cup_{i=0}^{\infty})\{-i, i\}$