

- Non linearity induced by H operator :  
 $(Hx = (1 - \alpha)x + \alpha x^3)$ .
- Relinearization at outer loops level
- Influence of the  $\sigma^o$  and  $n_{obs}$

Full resolution, varying  $\alpha$  parameter with the same relinearization  
scheme :  $no = 4, ni = 6$ ,  
spectral interpolation and projective B matrix,  $\sigma^o = 0.01$

# Full resolution ; linear H ; $J$ vs $J^{nl}$

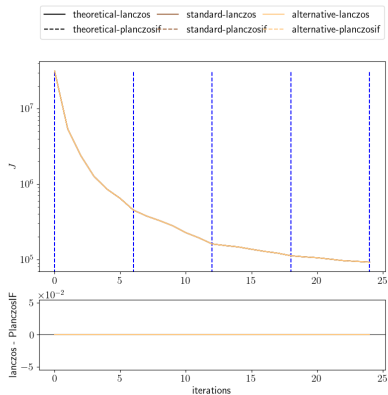


FIGURE -  $\alpha = 0$

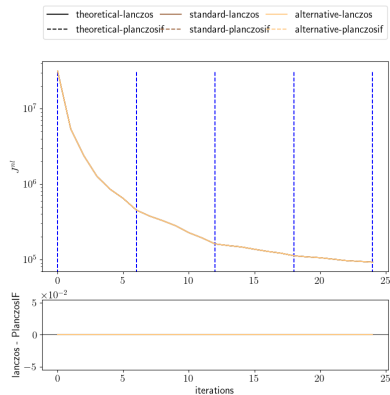


FIGURE -  $\alpha = 0$

# Full resolution ; non linear H ; $J$ vs $J^{nl}$

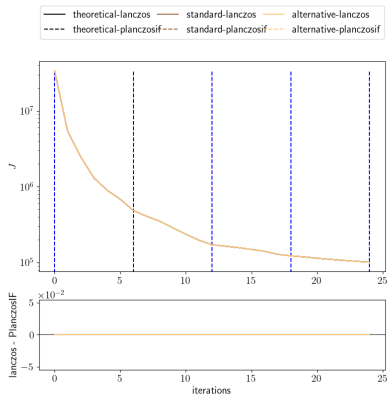


FIGURE -  $\alpha = 0.01$

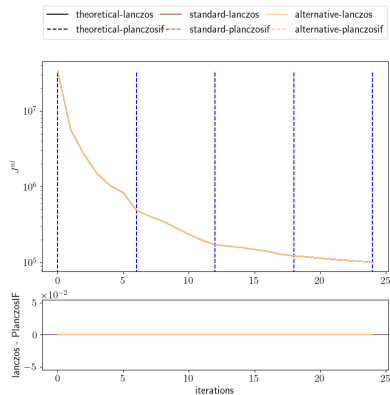


FIGURE -  $\alpha = 0.01$

# Full resolution ; non linear H ; $J$ vs $J^{nl}$

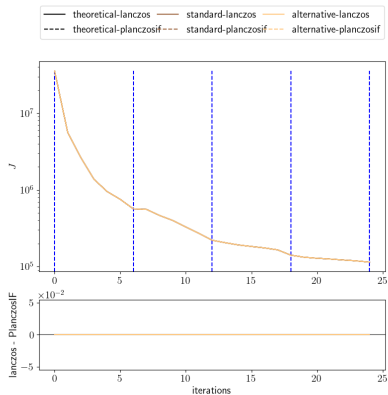


FIGURE -  $\alpha = 0.02$

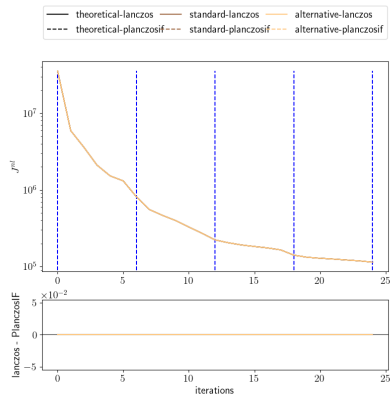


FIGURE -  $\alpha = 0.02$

# Full resolution ; non linear H ; $J$ vs $J^{nl}$

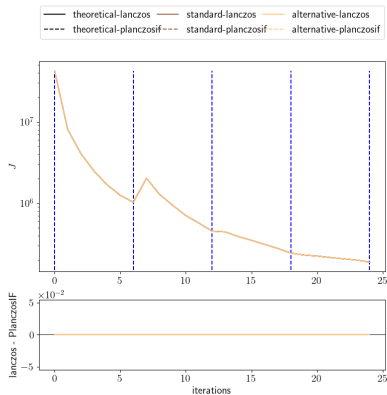


FIGURE –  $\alpha = 0.05$

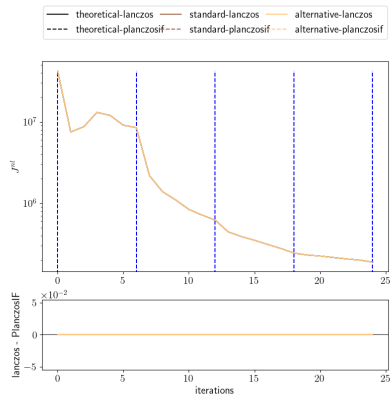


FIGURE –  $\alpha = 0.05$

# Full resolution ; non linear H ; $J$ vs $J^{nl}$

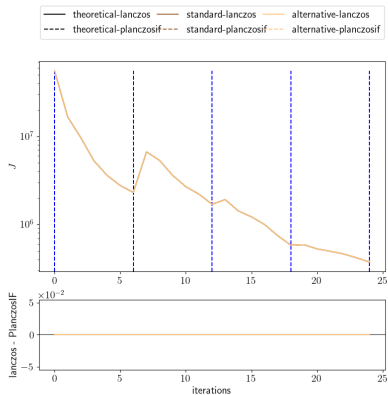


FIGURE -  $\alpha = 0.1$

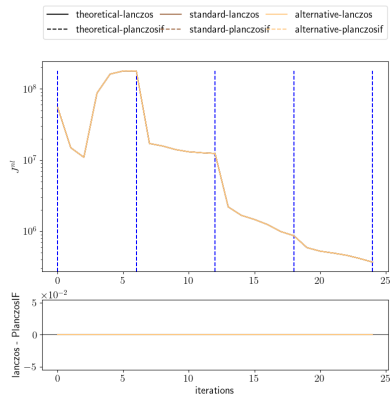


FIGURE -  $\alpha = 0.1$

# Full resolution ; non linear H ; $J$ vs $J^{nl}$

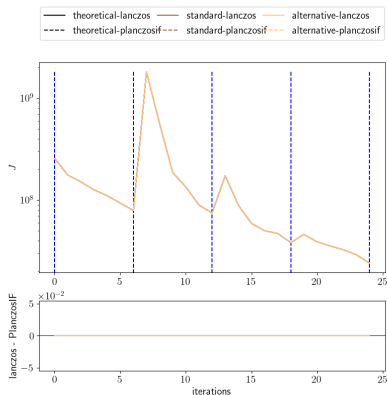


FIGURE -  $\alpha = 0.5$

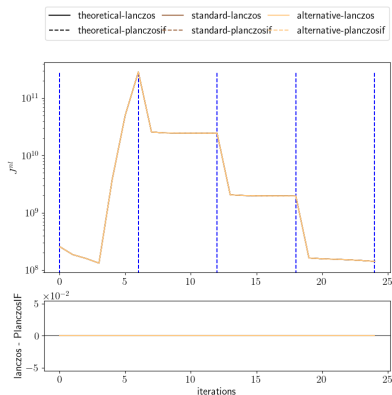


FIGURE -  $\alpha = 0.5$



# Full resolution ; non linear H ; $J$ vs $J^{nl}$

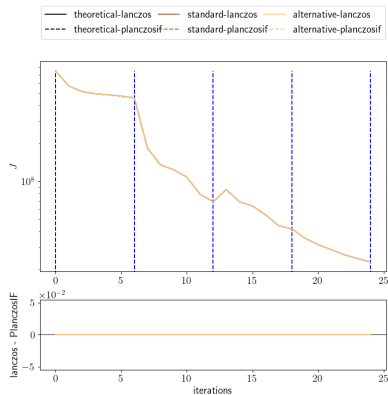


FIGURE -  $\alpha = 1$

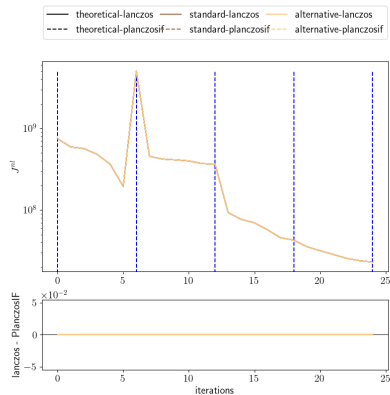


FIGURE -  $\alpha = 1$

# Conclusion on the non linearity induced by H

- Very sensitive to  $\alpha$  even for small values.
- The case with  $\alpha = 1$  seems better than the case with  $\alpha = 0.05...$   
→ What could be the reason for it?
- It seems that there are too much inner loops before relinearization but the iteration at which the "jump" occurs seems NOT correlated to the value of  $\alpha$ .

→ Need to study the number of inner iterations vs. outer iterations.

Full resolution, varying the number of inner and outer loops with a non linear H and the same total number of iterations ( $n_o \times n_i = 24$ ) (spectral interpolation and projective B matrix,  $\sigma^o = 0.01$ )

# Full resolution ; non linear H ( $\alpha = 0.05$ ) : $J^{nl}$

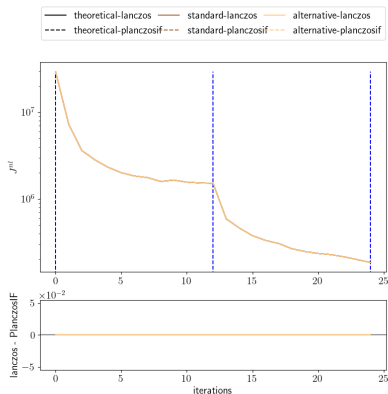


FIGURE -  $n_o = 2, n_i = 12$

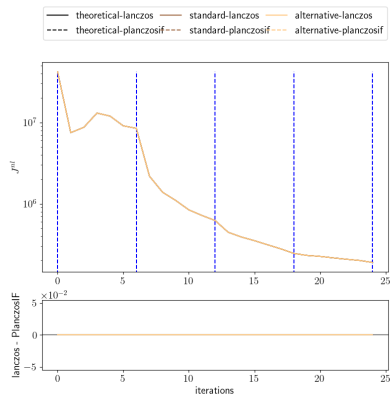


FIGURE -  $n_o = 4, n_i = 6$

# Full resolution ; non linear H ( $\alpha = 0.05$ ) : $J^{nl}$

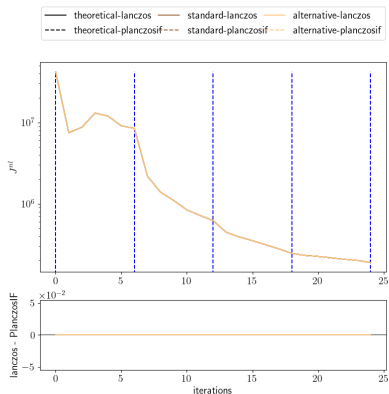


FIGURE –  $n_o = 4, n_i = 6$

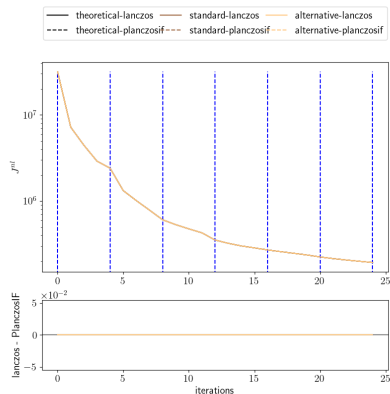


FIGURE –  $n_o = 6, n_i = 4$

# Full resolution ; non linear H ( $\alpha = 0.05$ ) : $J$

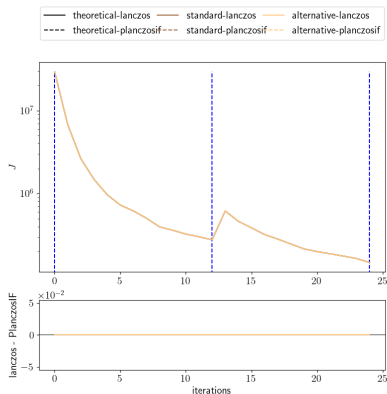


FIGURE –  $n_o = 2, n_i = 12$

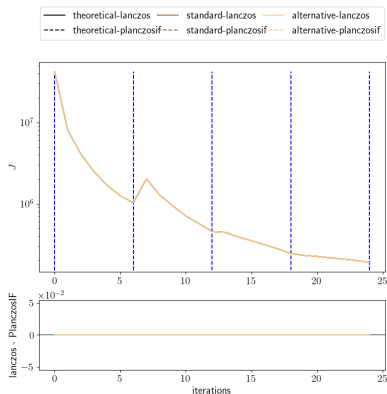


FIGURE –  $n_o = 4, n_i = 6$

# Full resolution ; non linear H ( $\alpha = 0.05$ ) : $J$

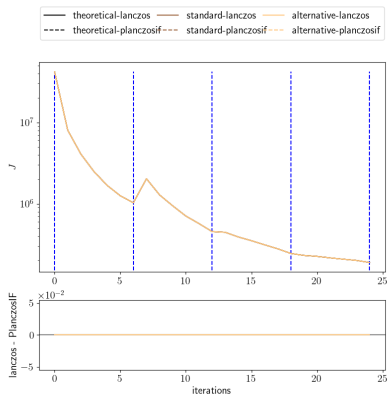


FIGURE –  $n_o = 4, n_i = 6$

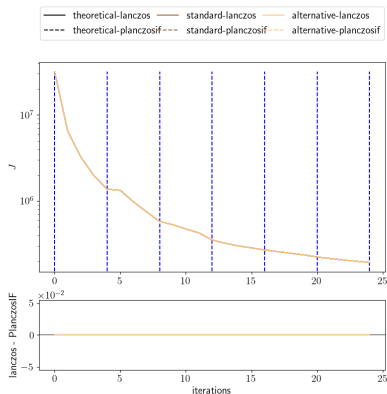


FIGURE –  $n_o = 6, n_i = 4$

# Full resolution ; non linear H ( $\alpha = 0.1$ ) : $J^{nl}$

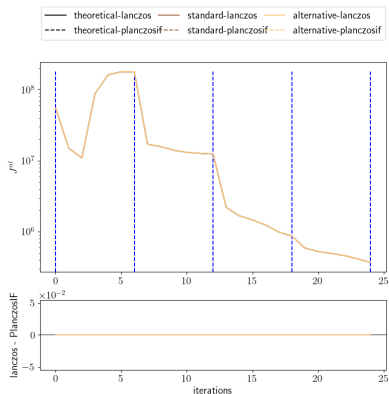


FIGURE –  $n_o = 4, n_i = 6$

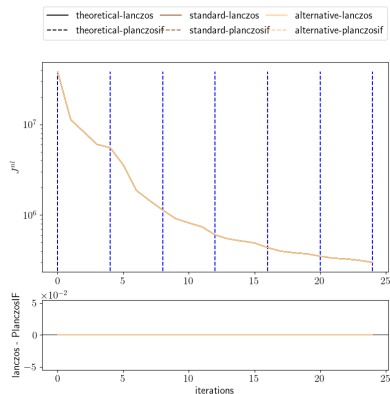


FIGURE –  $n_o = 6, n_i = 4$



# Full resolution ; non linear H ( $\alpha = 0.1$ ) : $J$

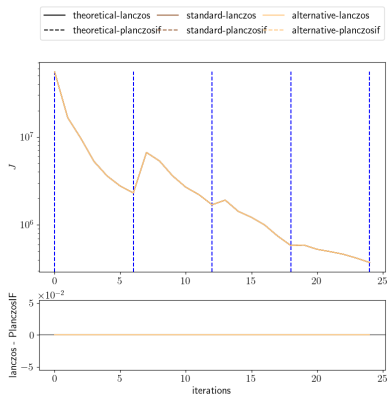


FIGURE –  $n_o = 4, n_i = 6$

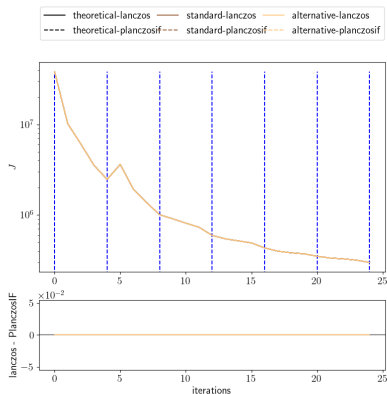


FIGURE –  $n_o = 6, n_i = 4$

# Full resolution ; non linear H ( $\alpha = 1$ ) : $J^{nl}$

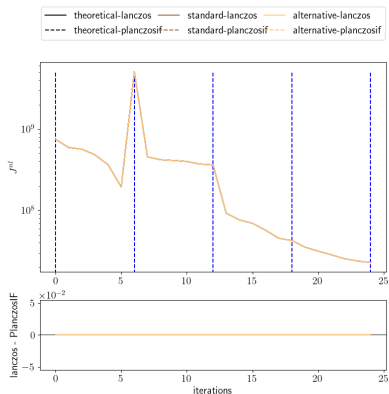


FIGURE –  $n_o = 4, n_i = 6$

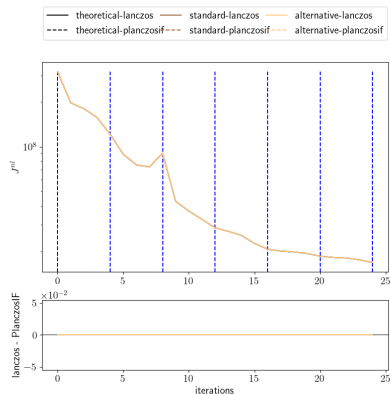


FIGURE –  $n_o = 6, n_i = 4$

# Full resolution ; non linear H ( $\alpha = 1$ ) : $J$

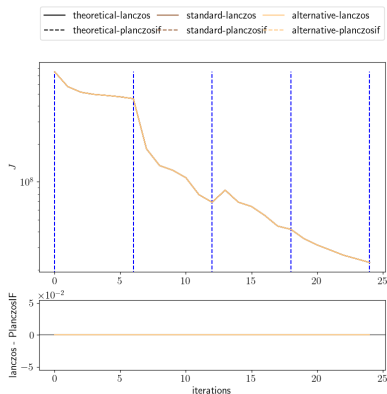


FIGURE –  $n_o = 4, n_i = 6$

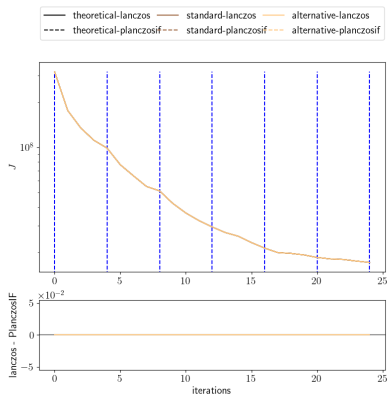


FIGURE –  $n_o = 6, n_i = 4$

# Conclusion on the number of inner and outer loops

- As expected, the assimilation scheme with the more outer loops is equal or better than the others.
- There is often a "jump" in the linear cost function which is not necessarily at the same iteration than the eventual "jump" in the non linear one.
- Problem : The firsts inner iterations in the first case with 12 inner iterations seems better than the case with 6 inner iterations whereas the case with 6 inner iterations seems better than the case with 6 inner iterations :  
→ The problem is too much dependant on the initial background and observation states that are randomly generated ( ? ) : there is a difference of  $10^7$  at the beggining !

# Short conclusion and questions :

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