# STAT 702 - Homework 2

Noah Javadi

2025 - 02 - 16

## Setup

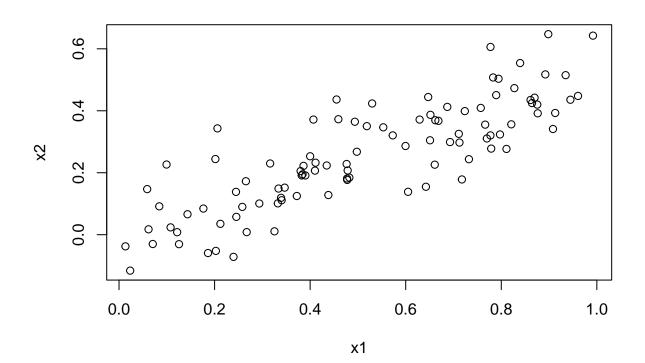
## Problem 14

```
set.seed(1)
x1 <- runif(100)
x2 <- 0.5 * x1 + rnorm(100) / 10
y <- 2 + 2 * x1 + 0.3 * x2 + rnorm(100)

#Correlation and scatterplot
cor(x1,x2)</pre>
```

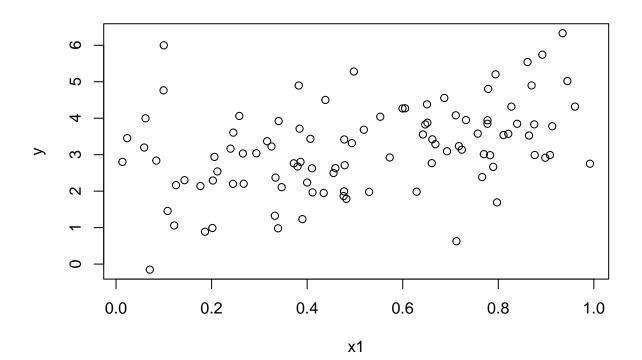
## [1] 0.8351212

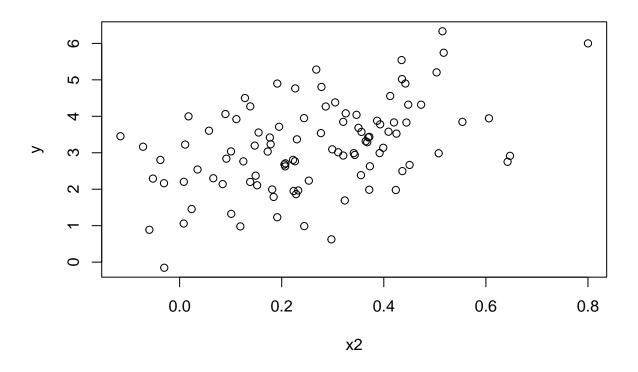
plot(x1,x2)



```
#Fitting full linear regression model
lm.p14 < - lm(y ~ x1 + x2)
summary(lm.p14)
##
## Call:
## lm(formula = y \sim x1 + x2)
##
## Residuals:
      Min
                1Q Median
                                3Q
                                       Max
## -2.8311 -0.7273 -0.0537 0.6338 2.3359
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                            0.2319
                                     9.188 7.61e-15 ***
## (Intercept)
                 2.1305
## x1
                 1.4396
                            0.7212
                                     1.996
                                             0.0487 *
## x2
                 1.0097
                            1.1337
                                     0.891
                                             0.3754
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.056 on 97 degrees of freedom
## Multiple R-squared: 0.2088, Adjusted R-squared: 0.1925
## F-statistic: 12.8 on 2 and 97 DF, p-value: 1.164e-05
#Fitting simple linear regression model with x1
lm.x1 \leftarrow lm(y \sim x1)
summary(lm.x1)
##
## Call:
## lm(formula = y \sim x1)
##
## Residuals:
       Min
                  1Q Median
                                            Max
## -2.89495 -0.66874 -0.07785 0.59221 2.45560
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
                            0.2307
                                    9.155 8.27e-15 ***
## (Intercept)
                2.1124
## x1
                 1.9759
                            0.3963
                                     4.986 2.66e-06 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.055 on 98 degrees of freedom
## Multiple R-squared: 0.2024, Adjusted R-squared: 0.1942
## F-statistic: 24.86 on 1 and 98 DF, p-value: 2.661e-06
#Fitting simple linear regression model with x2
lm.x2 < - lm(y ~ x2)
summary(lm.x2)
```

```
## Call:
## lm(formula = y \sim x2)
##
## Residuals:
##
                  1Q
                       Median
##
  -2.62687 -0.75156 -0.03598 0.72383
                                        2.44890
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 2.3899
                             0.1949
                                      12.26 < 2e-16 ***
## x2
                 2.8996
                             0.6330
                                       4.58 1.37e-05 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
\#\# Residual standard error: 1.072 on 98 degrees of freedom
## Multiple R-squared: 0.1763, Adjusted R-squared: 0.1679
## F-statistic: 20.98 on 1 and 98 DF, p-value: 1.366e-05
#Adding new values
x1 \leftarrow c(x1,0.1)
x2 \leftarrow c(x2,0.8)
y < -c(y,6)
#Plot new variables to determine relationship
plot(x1,y)
```





```
#Refitting full model
lm.p14 <- lm(y ~ x1 + x2)
summary(lm.p14)</pre>
```

```
##
## Call:
## lm(formula = y \sim x1 + x2)
##
## Residuals:
##
       Min
                  1Q
                     Median
                                    ЗQ
                                            Max
## -2.73348 -0.69318 -0.05263 0.66385
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
                 2.2267
                            0.2314
                                     9.624 7.91e-16 ***
## (Intercept)
## x1
                 0.5394
                            0.5922
                                     0.911 0.36458
## x2
                 2.5146
                            0.8977
                                     2.801 0.00614 **
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.075 on 98 degrees of freedom
## Multiple R-squared: 0.2188, Adjusted R-squared: 0.2029
## F-statistic: 13.72 on 2 and 98 DF, p-value: 5.564e-06
```

```
#Refitting simple linear regression with x1
lm.x1 \leftarrow lm(y \sim x1)
summary(lm.x1)
##
## Call:
## lm(formula = y \sim x1)
##
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
## -2.8897 -0.6556 -0.0909 0.5682 3.5665
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                 2.2569
                             0.2390
                                      9.445 1.78e-15 ***
## (Intercept)
## x1
                                      4.282 4.29e-05 ***
                 1.7657
                             0.4124
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.111 on 99 degrees of freedom
## Multiple R-squared: 0.1562, Adjusted R-squared: 0.1477
## F-statistic: 18.33 on 1 and 99 DF, p-value: 4.295e-05
#Refitting simple linear regression with x2
lm.x2 \leftarrow lm(y \sim x2)
summary(lm.x2)
##
## Call:
## lm(formula = y \sim x2)
##
## Residuals:
        Min
                  1Q
                      Median
                                     30
                                             Max
## -2.64729 -0.71021 -0.06899 0.72699
                                         2.38074
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 2.3451
                             0.1912 12.264 < 2e-16 ***
                 3.1190
                             0.6040
                                      5.164 1.25e-06 ***
## x2
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 1.074 on 99 degrees of freedom
## Multiple R-squared: 0.2122, Adjusted R-squared: 0.2042
## F-statistic: 26.66 on 1 and 99 DF, p-value: 1.253e-06
  a) The regression coefficients are 2 for beta_0, 2 for beta_1, and 0.3 for beta_2.
  b) 0.8424
```

c) The model with both x\_1 and x\_2 show a weak linear relationship to y. beta\_hat\_0 is 1.91, beta\_hat\_1 is 1.96, and beta\_hat\_2 is 0.549. The estimated coefficients should approach the true beta\_0, beta\_1, and beta\_2. For beta\_1, we can reject the null hypothesis where beta\_1 = 0. For beta\_2, we cannot reject the null hypothesis where beta\_2 = 0.

- d) This is a similar model to the full model previously analyzed. There is enough evidence to reject the null hypothesis for beta  $_1 = 0$ .
- e) This is a weaker model to the full model previously analyzed. There is not enough evidence to reject the null hypothesis for beta $_1 = 0$ .
- f) The results obtained in c-e do not contradict each other. The correlation between x1 and x2 show that x1 is the main predictor and adding x2 does not add much to describing the variability of y.
- g) We have introduced highly influential points to x1 and x2 which has changed the impact of x2 and the interpretation of each model. The point introduced to x1 is an outlier but not a high leverage point because it has a high residual, but not an extreme x value. Whereas the point introduced to x2 is not an outlier, but a high leverage point because it is in line with expected values, but has a large x value.

#### Problem 15

```
#?Boston

#Correlation matrix for all variables against crim
cor(Boston[-1],Boston$crim)
```

```
##
                   [,1]
## zn
           -0.20046922
            0.40658341
## indus
## chas
           -0.05589158
## nox
            0.42097171
           -0.21924670
## rm
## age
            0.35273425
           -0.37967009
## dis
## rad
            0.62550515
## tax
            0.58276431
## ptratio
            0.28994558
## lstat
            0.45562148
## medv
           -0.38830461
```

```
#Fitting simple linear regressions for each variable against crim
zn.lm <- lm(crim ~ zn,data = Boston)
indus.lm <- lm(crim ~ indus,data = Boston)
chas.lm <- lm(crim ~ chas,data = Boston)
nox.lm <- lm(crim ~ nox,data = Boston)
rm.lm <- lm(crim ~ rm,data = Boston)
age.lm <- lm(crim ~ age,data = Boston)
dis.lm <- lm(crim ~ dis,data = Boston)
rad.lm <- lm(crim ~ rad,data = Boston)
tax.lm <- lm(crim ~ tax,data = Boston)
ptratio.lm <- lm(crim ~ ptratio,data = Boston)
lstat.lm <- lm(crim ~ lstat,data = Boston)
medv.lm <- lm(crim ~ medv,data = Boston)</pre>
```

```
##
## Call:
## lm(formula = crim ~ zn, data = Boston)
##
## Residuals:
```

```
10 Median
                           3Q
     Min
## -4.429 -4.222 -2.620 1.250 84.523
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.45369 0.41722 10.675 < 2e-16 ***
              -0.07393
                          0.01609 -4.594 5.51e-06 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 8.435 on 504 degrees of freedom
## Multiple R-squared: 0.04019,
                                  Adjusted R-squared: 0.03828
## F-statistic: 21.1 on 1 and 504 DF, p-value: 5.506e-06
summary(indus.lm)
##
## Call:
## lm(formula = crim ~ indus, data = Boston)
## Residuals:
      Min
               1Q Median
                              30
                                     Max
## -11.972 -2.698 -0.736 0.712 81.813
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.06374
                          0.66723 -3.093 0.00209 **
## indus
              0.50978
                          0.05102 9.991 < 2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 7.866 on 504 degrees of freedom
## Multiple R-squared: 0.1653, Adjusted R-squared: 0.1637
## F-statistic: 99.82 on 1 and 504 DF, p-value: < 2.2e-16
summary(chas.lm)
##
## Call:
## lm(formula = crim ~ chas, data = Boston)
##
## Residuals:
     Min
             1Q Median
                           3Q
                                 Max
## -3.738 -3.661 -3.435 0.018 85.232
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.7444
                           0.3961 9.453
                                           <2e-16 ***
## chas
               -1.8928
                           1.5061 - 1.257
                                            0.209
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 8.597 on 504 degrees of freedom
```

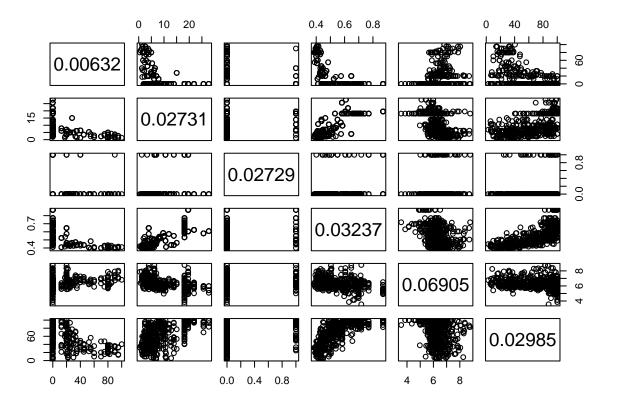
```
## Multiple R-squared: 0.003124, Adjusted R-squared: 0.001146
## F-statistic: 1.579 on 1 and 504 DF, p-value: 0.2094
summary(nox.lm)
## Call:
## lm(formula = crim ~ nox, data = Boston)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -12.371 -2.738 -0.974 0.559 81.728
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -13.720
                           1.699 -8.073 5.08e-15 ***
                            2.999 10.419 < 2e-16 ***
## nox
                31.249
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 7.81 on 504 degrees of freedom
## Multiple R-squared: 0.1772, Adjusted R-squared: 0.1756
## F-statistic: 108.6 on 1 and 504 DF, p-value: < 2.2e-16
summary(rm.lm)
##
## Call:
## lm(formula = crim ~ rm, data = Boston)
##
## Residuals:
     Min
             1Q Median
                           3Q
                                 Max
## -6.604 -3.952 -2.654 0.989 87.197
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 20.482
                            3.365 6.088 2.27e-09 ***
                -2.684
                            0.532 -5.045 6.35e-07 ***
## rm
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 8.401 on 504 degrees of freedom
## Multiple R-squared: 0.04807,
                                  Adjusted R-squared: 0.04618
## F-statistic: 25.45 on 1 and 504 DF, p-value: 6.347e-07
summary(age.lm)
##
## Call:
## lm(formula = crim ~ age, data = Boston)
## Residuals:
```

```
10 Median
                           3Q
     Min
## -6.789 -4.257 -1.230 1.527 82.849
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                          0.94398 -4.002 7.22e-05 ***
## (Intercept) -3.77791
                          0.01274 8.463 2.85e-16 ***
## age
               0.10779
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 8.057 on 504 degrees of freedom
## Multiple R-squared: 0.1244, Adjusted R-squared: 0.1227
## F-statistic: 71.62 on 1 and 504 DF, p-value: 2.855e-16
summary(dis.lm)
##
## Call:
## lm(formula = crim ~ dis, data = Boston)
## Residuals:
    Min
             1Q Median
                           30
## -6.708 -4.134 -1.527 1.516 81.674
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                           0.7304 13.006
## (Intercept) 9.4993
                                            <2e-16 ***
## dis
               -1.5509
                           0.1683 -9.213
                                            <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 7.965 on 504 degrees of freedom
## Multiple R-squared: 0.1441, Adjusted R-squared: 0.1425
## F-statistic: 84.89 on 1 and 504 DF, p-value: < 2.2e-16
summary(rad.lm)
##
## Call:
## lm(formula = crim ~ rad, data = Boston)
##
## Residuals:
               1Q Median
      Min
                               3Q
                                      Max
## -10.164 -1.381 -0.141 0.660 76.433
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.28716
                          0.44348 -5.157 3.61e-07 ***
                          0.03433 17.998 < 2e-16 ***
## rad
               0.61791
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 6.718 on 504 degrees of freedom
```

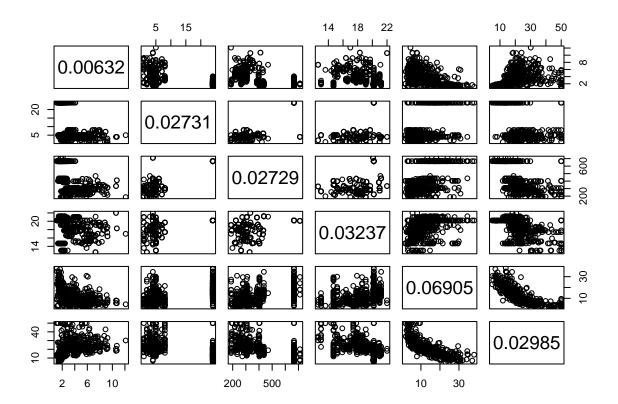
```
## Multiple R-squared: 0.3913, Adjusted R-squared: 0.39
## F-statistic: 323.9 on 1 and 504 DF, p-value: < 2.2e-16
summary(tax.lm)
## Call:
## lm(formula = crim ~ tax, data = Boston)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -12.513 -2.738 -0.194 1.065 77.696
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -8.528369
                          0.815809 -10.45
                                             <2e-16 ***
## tax
               0.029742
                         0.001847
                                     16.10
                                           <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.997 on 504 degrees of freedom
## Multiple R-squared: 0.3396, Adjusted R-squared: 0.3383
## F-statistic: 259.2 on 1 and 504 DF, p-value: < 2.2e-16
summary(ptratio.lm)
##
## Call:
## lm(formula = crim ~ ptratio, data = Boston)
##
## Residuals:
     Min
             1Q Median
                           3Q
                                 Max
## -7.654 -3.985 -1.912 1.825 83.353
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -17.6469
                           3.1473 -5.607 3.40e-08 ***
                           0.1694 6.801 2.94e-11 ***
## ptratio
               1.1520
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 8.24 on 504 degrees of freedom
## Multiple R-squared: 0.08407,
                                 Adjusted R-squared: 0.08225
## F-statistic: 46.26 on 1 and 504 DF, p-value: 2.943e-11
summary(lstat.lm)
##
## Call:
## lm(formula = crim ~ lstat, data = Boston)
## Residuals:
```

```
Min
               1Q Median
                               3Q
## -13.925 -2.822 -0.664 1.079 82.862
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.33054
                          0.69376 -4.801 2.09e-06 ***
              0.54880
                          0.04776 11.491 < 2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 7.664 on 504 degrees of freedom
## Multiple R-squared: 0.2076, Adjusted R-squared: 0.206
## F-statistic: 132 on 1 and 504 DF, p-value: < 2.2e-16
summary(medv.lm)
##
## lm(formula = crim ~ medv, data = Boston)
## Residuals:
   Min
             1Q Median
                           3Q
                                Max
## -9.071 -4.022 -2.343 1.298 80.957
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 11.79654
                          0.93419
                                    12.63
                                           <2e-16 ***
## medv
              -0.36316
                          0.03839
                                   -9.46
                                           <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 7.934 on 504 degrees of freedom
## Multiple R-squared: 0.1508, Adjusted R-squared: 0.1491
## F-statistic: 89.49 on 1 and 504 DF, p-value: < 2.2e-16
```

#Plots to confirm observations and linear relationships for each model against crim
plot(Boston[c(2:7)],Boston\$crim)



plot(Boston[c(8:13)],Boston\$crim)



```
#Fitting linear model for crim against all variables in data set
full.lm <- lm(crim ~ zn + indus + chas + nox + rm + age + dis + rad + tax + ptratio + lstat + medv,data
#Summary of the full model
summary(full.lm)
##
## Call:
## lm(formula = crim ~ zn + indus + chas + nox + rm + age + dis +
       rad + tax + ptratio + lstat + medv, data = Boston)
##
## Residuals:
```

1Q Median ## -8.534 -2.248 -0.348 1.087 73.923

Min

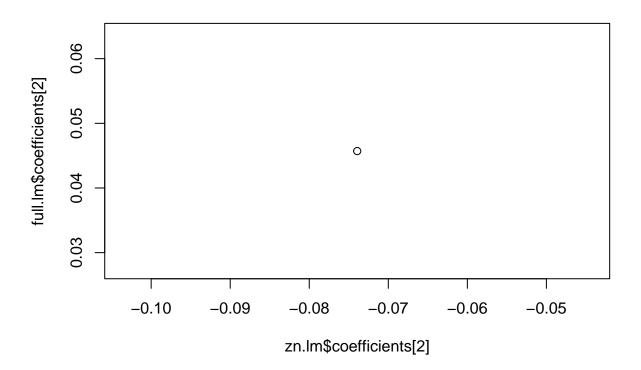
##

## rad

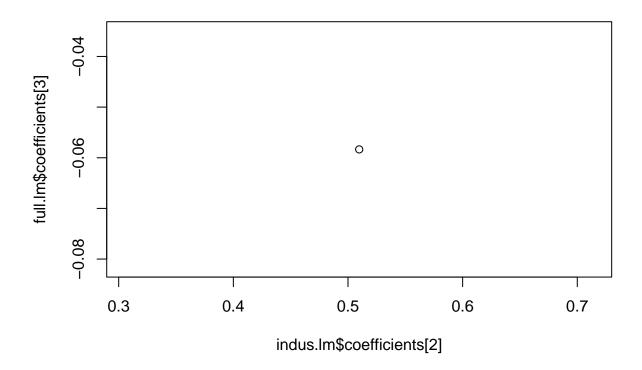
## (Intercept) 13.7783938 7.0818258 ## zn 0.0457100 0.0187903 2.433 0.015344 \* 0.0836351 -0.698 0.485709 ## indus -0.0583501 ## chas -0.8253776 1.1833963 -0.697 0.485841 ## nox -9.9575865 5.2898242 -1.882 0.060370 . ## rm 0.6289107 0.6070924 1.036 0.300738 -0.0008483 0.0179482 -0.047 0.962323 ## age ## dis 0.6124653 0.0875358 6.997 8.59e-12 \*\*\*

```
-0.0037756 0.0051723 -0.730 0.465757
## tax
                          0.1863598 -1.632 0.103393
## ptratio
              -0.3040728
## lstat
               0.1388006
                          0.0757213
                                      1.833 0.067398 .
## medv
              -0.2200564
                          0.0598240 -3.678 0.000261 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 6.46 on 493 degrees of freedom
## Multiple R-squared: 0.4493, Adjusted R-squared: 0.4359
## F-statistic: 33.52 on 12 and 493 DF, p-value: < 2.2e-16
```

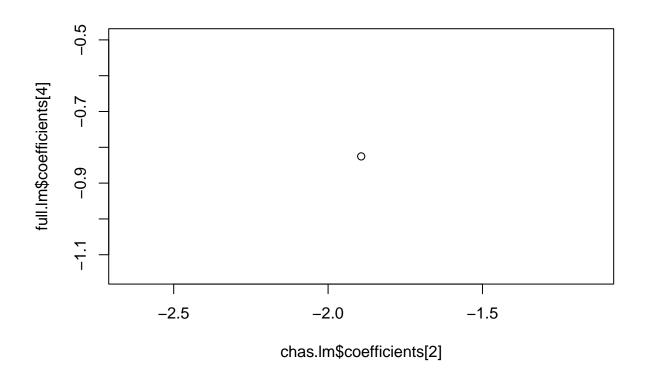
#Plots comparing univariate model coefficients against the full model coefficients plot(zn.lm\\$coefficients[2],full.lm\\$coefficients[2])



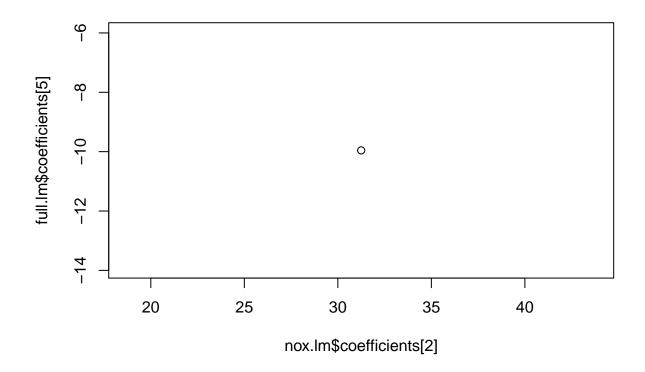
plot(indus.lm\$coefficients[2],full.lm\$coefficients[3])



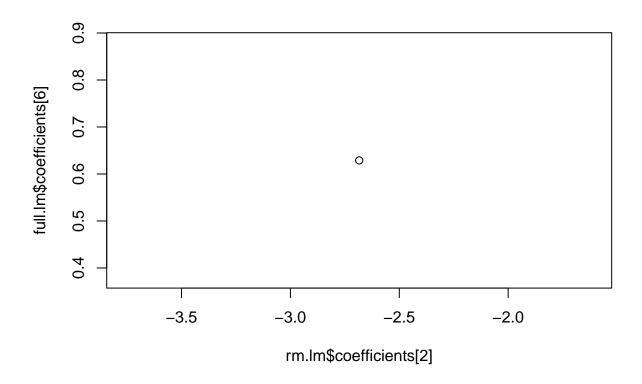
plot(chas.lm\$coefficients[2],full.lm\$coefficients[4])



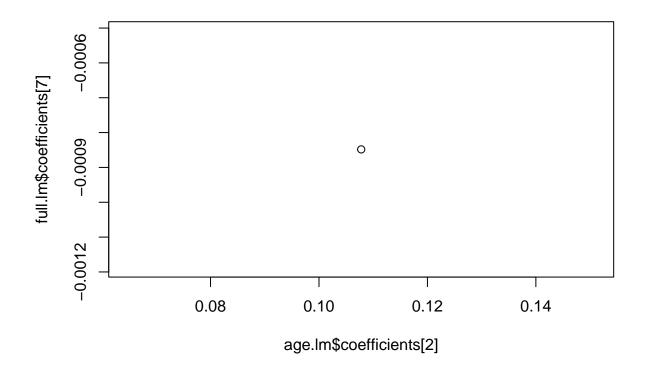
plot(nox.lm\$coefficients[2],full.lm\$coefficients[5])



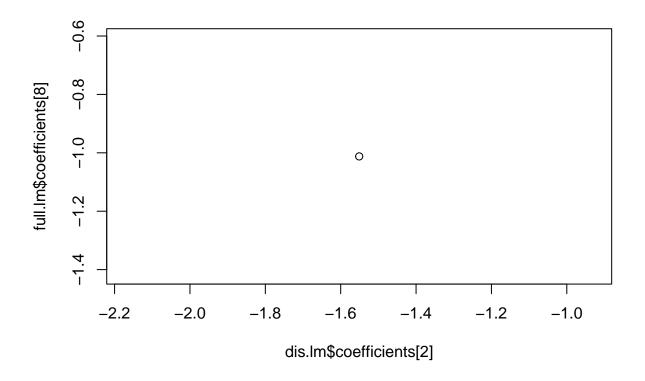
plot(rm.lm\$coefficients[2],full.lm\$coefficients[6])



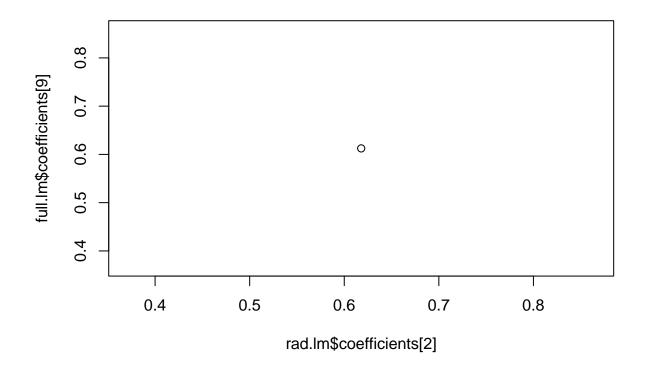
plot(age.lm\$coefficients[2],full.lm\$coefficients[7])



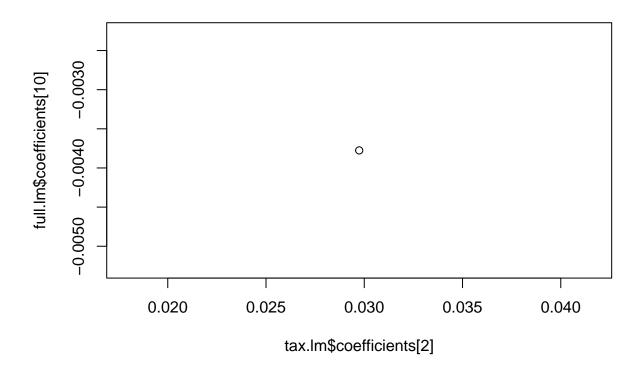
plot(dis.lm\$coefficients[2],full.lm\$coefficients[8])



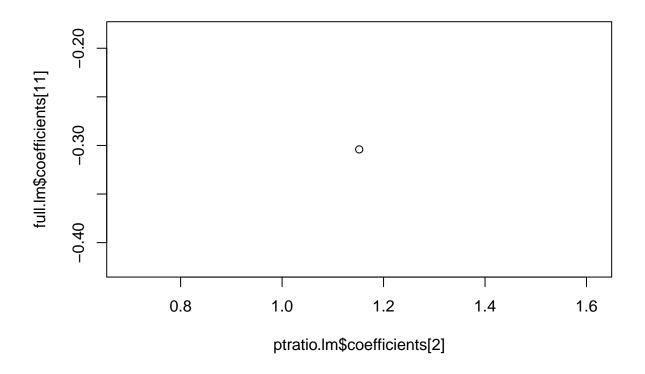
plot(rad.lm\$coefficients[2],full.lm\$coefficients[9])



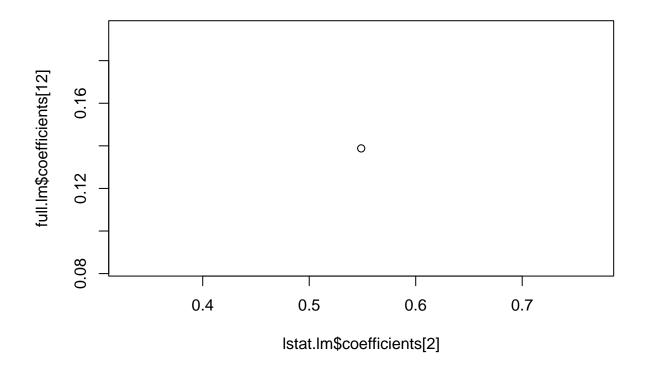
plot(tax.lm\$coefficients[2],full.lm\$coefficients[10])



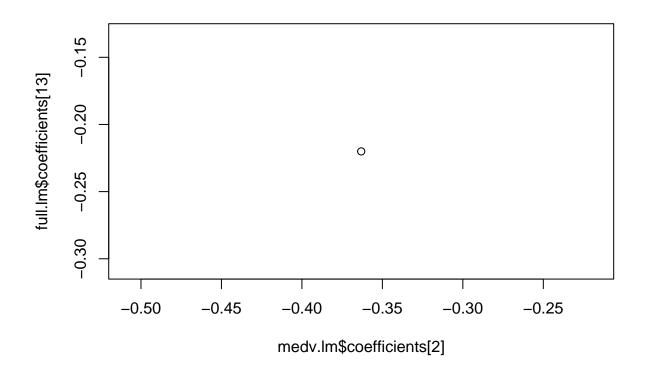
plot(ptratio.lm\$coefficients[2],full.lm\$coefficients[11])



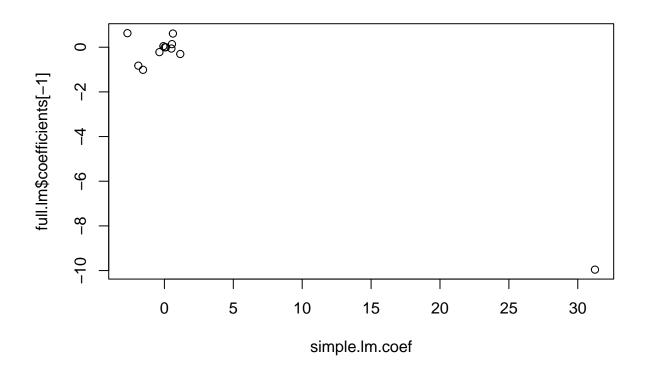
plot(lstat.lm\$coefficients[2],full.lm\$coefficients[12])



plot(medv.lm\$coefficients[2],full.lm\$coefficients[13])



simple.lm.coef <- c(zn.lm\$coefficients[2],indus.lm\$coefficients[2],chas.lm\$coefficients[2],nox.lm\$coefficients[-1])



```
#chas only factor with 2 levels. Fitting nonlinear models against crim
zn.nlm <- lm(crim ~ poly(zn,3),data = Boston)
indus.nlm <- lm(crim ~ poly(indus,3),data = Boston)
nox.nlm <- lm(crim ~ poly(nox,3),data = Boston)
rm.nlm <- lm(crim ~ poly(rm,3),data = Boston)
age.nlm <- lm(crim ~ poly(age,3),data = Boston)
dis.nlm <- lm(crim ~ poly(dis,3),data = Boston)
rad.nlm <- lm(crim ~ poly(rad,3),data = Boston)
tax.nlm <- lm(crim ~ poly(tax,3),data = Boston)
ptratio.nlm <- lm(crim ~ poly(ptratio,3),data = Boston)
lstat.nlm <- lm(crim ~ poly(lstat,3),data = Boston)
medv.nlm <- lm(crim ~ poly(medv,3),data = Boston)</pre>
```

```
##
## lm(formula = crim ~ poly(zn, 3), data = Boston)
##
## Residuals:
      Min
              1Q Median
                            3Q
                                  Max
## -4.821 -4.614 -1.294 0.473 84.130
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
                             0.3722
                                      9.709 < 2e-16 ***
## (Intercept)
                  3.6135
```

```
## poly(zn, 3)1 -38.7498
                            8.3722 -4.628 4.7e-06 ***
## poly(zn, 3)2 23.9398
                            8.3722 2.859 0.00442 **
## poly(zn, 3)3 -10.0719
                            8.3722 -1.203 0.22954
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 8.372 on 502 degrees of freedom
## Multiple R-squared: 0.05824,
                                  Adjusted R-squared: 0.05261
## F-statistic: 10.35 on 3 and 502 DF, p-value: 1.281e-06
summary(indus.nlm)
##
## Call:
## lm(formula = crim ~ poly(indus, 3), data = Boston)
## Residuals:
     Min
             1Q Median
##
                           3Q
## -8.278 -2.514 0.054 0.764 79.713
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
                                0.330 10.950 < 2e-16 ***
## (Intercept)
                     3.614
## poly(indus, 3)1 78.591
                                7.423 10.587 < 2e-16 ***
## poly(indus, 3)2 -24.395
                                7.423 -3.286 0.00109 **
## poly(indus, 3)3 -54.130
                                7.423 -7.292 1.2e-12 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 7.423 on 502 degrees of freedom
## Multiple R-squared: 0.2597, Adjusted R-squared: 0.2552
## F-statistic: 58.69 on 3 and 502 DF, p-value: < 2.2e-16
summary(nox.nlm)
##
## lm(formula = crim ~ poly(nox, 3), data = Boston)
##
## Residuals:
     Min
             1Q Median
                           3Q
                                 Max
## -9.110 -2.068 -0.255 0.739 78.302
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  3.6135
                             0.3216 11.237 < 2e-16 ***
## poly(nox, 3)1 81.3720
                             7.2336 11.249 < 2e-16 ***
## poly(nox, 3)2 -28.8286
                             7.2336 -3.985 7.74e-05 ***
## poly(nox, 3)3 -60.3619
                             7.2336 -8.345 6.96e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 7.234 on 502 degrees of freedom
```

```
## Multiple R-squared: 0.297, Adjusted R-squared: 0.2928
## F-statistic: 70.69 on 3 and 502 DF, p-value: < 2.2e-16
summary(rm.nlm)
##
## Call:
## lm(formula = crim ~ poly(rm, 3), data = Boston)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                     Max
## -18.485 -3.468 -2.221 -0.015 87.219
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                           0.3703
                                   9.758 < 2e-16 ***
                3.6135
## poly(rm, 3)1 -42.3794
                           8.3297 -5.088 5.13e-07 ***
## poly(rm, 3)2 26.5768
                           8.3297
                                    3.191 0.00151 **
## poly(rm, 3)3 -5.5103
                           8.3297 -0.662 0.50858
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8.33 on 502 degrees of freedom
## Multiple R-squared: 0.06779, Adjusted R-squared: 0.06222
## F-statistic: 12.17 on 3 and 502 DF, p-value: 1.067e-07
summary(age.nlm)
##
## lm(formula = crim ~ poly(age, 3), data = Boston)
##
## Residuals:
##
             1Q Median
   Min
                           3Q
                                Max
## -9.762 -2.673 -0.516 0.019 82.842
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                           0.3485 10.368 < 2e-16 ***
## (Intercept)
                 3.6135
                                     8.697 < 2e-16 ***
## poly(age, 3)1 68.1820
                            7.8397
## poly(age, 3)2 37.4845
                            7.8397
                                     4.781 2.29e-06 ***
## poly(age, 3)3 21.3532
                            7.8397
                                     2.724 0.00668 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 7.84 on 502 degrees of freedom
## Multiple R-squared: 0.1742, Adjusted R-squared: 0.1693
## F-statistic: 35.31 on 3 and 502 DF, \, p-value: < 2.2e-16
summary(dis.nlm)
```

##

```
## Call:
## lm(formula = crim ~ poly(dis, 3), data = Boston)
## Residuals:
      Min
               1Q Median
                               3Q
## -10.757 -2.588 0.031
                            1.267 76.378
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  3.6135
                             0.3259 11.087 < 2e-16 ***
## poly(dis, 3)1 -73.3886
                             7.3315 -10.010 < 2e-16 ***
## poly(dis, 3)2 56.3730
                             7.3315
                                     7.689 7.87e-14 ***
## poly(dis, 3)3 -42.6219
                             7.3315 -5.814 1.09e-08 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 7.331 on 502 degrees of freedom
## Multiple R-squared: 0.2778, Adjusted R-squared: 0.2735
## F-statistic: 64.37 on 3 and 502 DF, p-value: < 2.2e-16
summary(rad.nlm)
##
## lm(formula = crim ~ poly(rad, 3), data = Boston)
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -10.381 -0.412 -0.269
                            0.179 76.217
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                  3.6135
                             0.2971 12.164 < 2e-16 ***
## poly(rad, 3)1 120.9074
                             6.6824 18.093 < 2e-16 ***
## poly(rad, 3)2 17.4923
                             6.6824
                                      2.618 0.00912 **
## poly(rad, 3)3
                 4.6985
                             6.6824
                                     0.703 0.48231
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 6.682 on 502 degrees of freedom
                       0.4, Adjusted R-squared: 0.3965
## Multiple R-squared:
## F-statistic: 111.6 on 3 and 502 DF, p-value: < 2.2e-16
summary(tax.nlm)
##
## Call:
## lm(formula = crim ~ poly(tax, 3), data = Boston)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -13.273 -1.389
                   0.046
                            0.536 76.950
##
```

```
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                             0.3047 11.860 < 2e-16 ***
## (Intercept)
                  3.6135
## poly(tax, 3)1 112.6458
                             6.8537 16.436 < 2e-16 ***
## poly(tax, 3)2 32.0873
                             6.8537
                                      4.682 3.67e-06 ***
                             6.8537 -1.167
## poly(tax, 3)3 -7.9968
                                               0.244
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 6.854 on 502 degrees of freedom
## Multiple R-squared: 0.3689, Adjusted R-squared: 0.3651
## F-statistic: 97.8 on 3 and 502 DF, p-value: < 2.2e-16
summary(ptratio.nlm)
##
## Call:
## lm(formula = crim ~ poly(ptratio, 3), data = Boston)
##
## Residuals:
##
     Min
             1Q Median
                           3Q
                                 Max
## -6.833 -4.146 -1.655 1.408 82.697
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       3.614
                                  0.361 10.008 < 2e-16 ***
                      56.045
                                  8.122
                                          6.901 1.57e-11 ***
## poly(ptratio, 3)1
## poly(ptratio, 3)2
                     24.775
                                  8.122
                                          3.050 0.00241 **
## poly(ptratio, 3)3 -22.280
                                  8.122 -2.743 0.00630 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 8.122 on 502 degrees of freedom
## Multiple R-squared: 0.1138, Adjusted R-squared: 0.1085
## F-statistic: 21.48 on 3 and 502 DF, p-value: 4.171e-13
summary(lstat.nlm)
##
## Call:
## lm(formula = crim ~ poly(lstat, 3), data = Boston)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -15.234 -2.151 -0.486
                            0.066 83.353
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               0.3392 10.654
                    3.6135
                                                <2e-16 ***
## poly(lstat, 3)1 88.0697
                               7.6294 11.543
                                                <2e-16 ***
## poly(lstat, 3)2 15.8882
                               7.6294
                                       2.082
                                                0.0378 *
## poly(lstat, 3)3 -11.5740
                                                0.1299
                               7.6294 -1.517
```

## ---

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 7.629 on 502 degrees of freedom
## Multiple R-squared: 0.2179, Adjusted R-squared: 0.2133
## F-statistic: 46.63 on 3 and 502 DF, p-value: < 2.2e-16</pre>
```

#### summary(medv.nlm)

```
##
## Call:
## lm(formula = crim ~ poly(medv, 3), data = Boston)
## Residuals:
##
      Min
                1Q
                   Median
                                3Q
                                       Max
##
  -24.427
           -1.976
                   -0.437
                             0.439
                                    73.655
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
                                              < 2e-16 ***
                     3.614
                                0.292
                                       12.374
## (Intercept)
## poly(medv, 3)1
                  -75.058
                                6.569 - 11.426
                                               < 2e-16 ***
## poly(medv, 3)2
                    88.086
                                6.569
                                       13.409
                                              < 2e-16 ***
## poly(medv, 3)3
                   -48.033
                                6.569
                                      -7.312 1.05e-12 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.569 on 502 degrees of freedom
## Multiple R-squared: 0.4202, Adjusted R-squared: 0.4167
## F-statistic: 121.3 on 3 and 502 DF, p-value: < 2.2e-16
```

- a) For chas (which is a binary variable), there is no linear relationship. However, for the remaining continuous variables there appears to be some weak linear relationships (as supported by the correlation column as well). The rad variable has the strongest linear relationship to crim and from the p-values chas is the only variable that we cannot reject the null hypothesis of beta 1 = 0.
- b) There is very little increase in variability accounted for by the full model compared to the rad simple linear regression. For the zn, dis, rad, and medv variables we can reject the null hypothesis of beta\_j = 0.
- c) The simple linear model for crim and rad is very close to the variability explained by the full model.
- d) There seems to be some nonlinear relationship between rad, tax, and medv and crim, but the remaining models do not seem to have a strong association to crim.