

LDA

# Remember

Generative process  $\neq$  inference algorithm

- ▶ Examples from the course so far?

# Today

LDA – we've learned generative process so far

- ▶ In words, what are the parameters we want to estimate?

# Notation

Known quantities:

$N$  documents

$V$  unique number of words

$M_i$  words in document  $i$

$w_{ij}$  indicates  $j$ th word in document  $i$

Unknown:

$z_{ij} \in 1, \dots, K$  indicates topic of word  $j$  in document  $i$

$\theta_i$  is length  $K$  vector indicating topic proportions in document  $i$

$\phi_k$  is length  $V$  vector of word probabilities, aka topic  $k$

## Another look at LDA generative process

- ▶ For each topic  $k \in [1, K]$  draw  $\phi_k \sim \text{Dirichlet}(\beta)$
- ▶ For each document  $i \in [1, N]$ :
  - ▶ Draw a distribution over topics  $\theta_i \sim \text{Dirichlet}(\alpha)$
  - ▶ For each word index  $j \in [1, M_i]$ :
    - ▶ Draw a topic assignment  $z_{ij} \sim \text{Multinomial}(1, \theta_i)$
    - ▶ Draw a word  $w_{ij} \sim \text{Multinomial}(1, \phi_{z_{ij}})$

# Multinomial

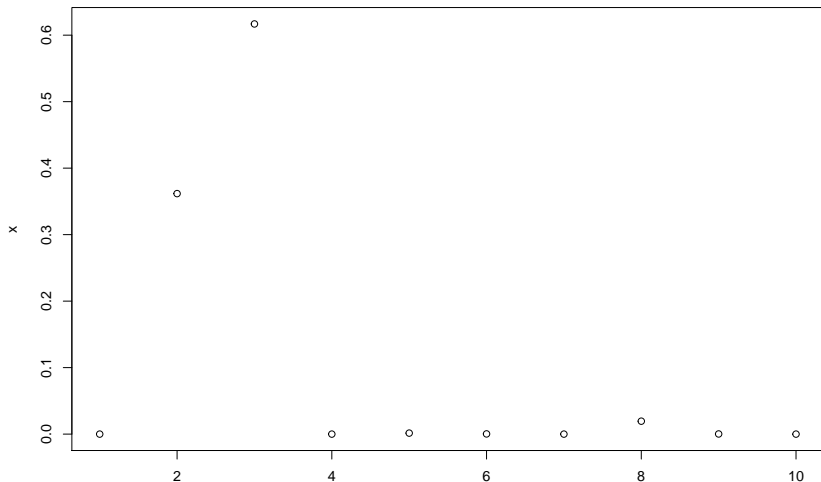
```
rmultinom(n = 1, size = 1, prob = rep(1/3, 3))
```

```
##      [,1]  
## [1,]    0  
## [2,]    1  
## [3,]    0
```

# Dirichlet

Think of it as a distribution over probability distributions

```
library(MCMCpack)
x <- rdirichlet(n = 1, alpha = rep(.1, 10))
plot(x = 1:10, y = x)
```



## Use in LDA

We use dirichlet distribution twice in LDA DGP—what for?



## Use in LDA

We use dirichlet distribution twice in LDA DGP—what for?

1. To draw  $\phi_k$  – distribution over words in vocab (aka topic  $k$ )
2. To draw  $\theta_i$  – distribution over  $k$  topics in document  $i$

# Helpful note

Hyperparameters are really *vectors*, but since what's mainstream is to use symmetric Dirichlet distributions, notation is abused and shown as a scalar

- ▶  $\phi_k \sim \text{Dirichlet}(\beta)$ 
  - ▶  $\beta$  actually length  $V$  vector
- ▶  $\theta_i \sim \text{Dirichlet}(\alpha)$ 
  - ▶  $\alpha$  actually length  $K$  vector

## Example

Assume  $V = 500$ ,  $K = 3$ ,  $\alpha = .1$ , and  $\beta = .01$

```
## how do we draw a topic? (phi_k)
```

```
#rdirichlet(n = 1, alpha = ???)
```

```
## how do we draw a distribution over topics? (theta_i)
```

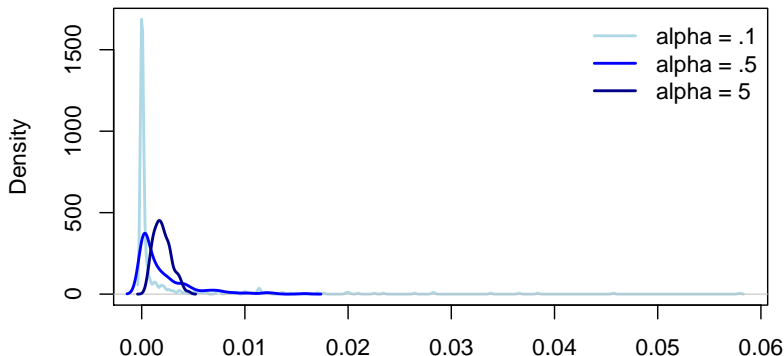
```
#rdirichlet(n = 1, alpha = ???)
```

# Why small hyperparameters?

Look at this for a second and describe what we're seeing. Recall  $V = 500$

```
set.seed(109123)
phi1 <- rdirichlet(n = 1, alpha = rep(.1, 500))
phi2 <- rdirichlet(n = 1, alpha = rep(.5, 500))
phi3 <- rdirichlet(n = 1, alpha = rep(5, 500))
```

## Random draws from dirichlet distributions with varying alpha

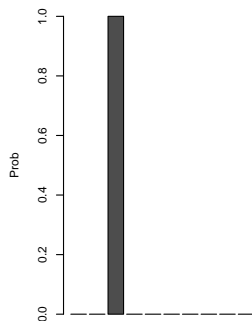


# Why small hyperparameters?

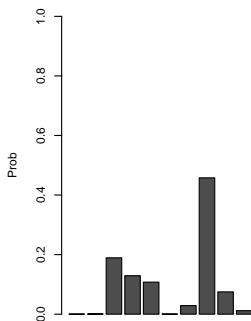
Look at this for a second and describe what we're seeing. Let's say  $K = 10$ .

```
set.seed(109123)
theta1 <- rdirichlet(n = 1, alpha = rep(.01, 10))
theta2 <- rdirichlet(n = 1, alpha = rep(.5, 10))
theta3 <- rdirichlet(n = 1, alpha = rep(5, 10))
```

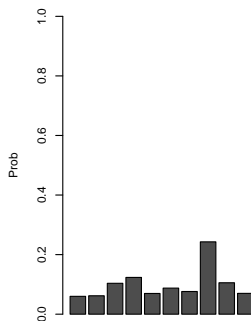
Random draw, alpha=.01



Random draw, alpha=.5



Random draw, alpha=5



## Last thing

The meaning of hyperparameters varies with the the dimensions of the data and  $K$ .

- ▶ In other words,  $\alpha = .1$  means something different depending on the data. You'll sometimes see advise/defaults as  $1/K$ .
- ▶ Think Bayesian
  - ▶ Dirichlet( $\alpha$ ) – our prior beliefs about how the topics in our documents are distributed (... dominated by one topic? ... a mixture over most topics?)
  - ▶ Dirichlet( $\beta$ ) – our prior beliefs about how our topics are defined (... a few distinctive words? ... a mixture of most of the words?)
- ▶ But of course, everything we know about priors applies, like priors can be overwhelmed with enough information from the data