

Exercise 5

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1 Read Chapter 3.1-3.5 from Haykin's book; summarize or sketch your insights in mind-map or an outline or a summary.

- Rosenblatt proved that given linearly separable data, a perceptron is proven to converge.
- Least mean square algorithm is the backbone of linear adaptive filters
- Adaptive filtering
 - m dimensional input produces scalar output
 - data equally distributed
 - data can be spread over space (snapshot) or over time (uniformly spaced in time)
 - Filtering process produces the output and error signals
 - Adaptive process involves adjustments based on errors
 - Error correction is an optimization problem
- Unconstrained optimization techniques
 - Optimal solution is gradient of cost function equal to 0
- Steepest descent
 - converges slowly
 - size of η produces overdamped response when small, under when large
- Newton method
 - needs to be twice continuously differentiable wrt w to form hessian
 - converges quickly and generally not subject to underdamped behavior of steepest descent
 - Needs to be positive definite matrix, however there is no guarantee of that.

- Gauss Newton method

Only requires jacobian of the error vector as opposed to hessian of cost function

Jacobian product must be non singular

- Least mean squares

Inverse of the learning rate η is the

weight vector traverses random trajectory in contrast with steepest descent

The stability of the system is determined by choosing an appropriate η for x

Model independent, therefore robust

Needs approx 10x the dimensionality iterations to converge

2 (3.1)

2.1 (a)

2.2 (b)

3 (3.2)

4 (3.4)

5 (3.8)

5.1 (a)

5.2 (b)

5.3 (c)