

Sensitivity and Backgrounds of Phase-I and II of the COMET Experiment

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A dissertation submitted to Imperial College London
for the degree of Doctor of Philosophy

Abstract

Declaration

This dissertation is the result of my own work, except where explicit reference is made to the work of others, and has not been submitted for another qualification to this or any other university. This dissertation does not exceed the word limit for the respective Degree Committee.

Benjamin Edward Krikler

Acknowledgements

Contents

1. Theory	2
2. The COMET Experiment	3
2.1. Overview of Signal and Backgrounds	4
2.2. General Experimental Techniques	6
2.2.1. Proton Beam Energy and Production Target	6
2.2.2. Particle Transport through Bent Solenoids	8
2.2.3. Stopping Target Material and Beam Pulsing	9
2.3. COMET Phase-I	13
2.4. COMET Phase-II	14
2.5. Schedule and Status	16
3. Offline Software and The COMET Simulation	18
4. Phase-II Optimisation	19
4.1. Optimisation Strategy	20
4.2. Optimisation Goals	21
4.3. Production Target Optimisation	21
4.3.1. Configuration	21
4.3.2. Length Scan	23
4.3.3. Radius scan	25
4.3.4. Final Result	25
5. Phase-II Signal Sensitivity	28
6. Phase-II Backgrounds	29
A. Drifts in a Bent Solenoid	30
A.1. Uniform Solenoidal Field	30
A.2. Field in a Bent Solenoid	30

Contents	1
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A.3. Drift Calculation	31
A.3.1. Gradient Drift	31
List of Acronyms	34
Bibliography	35

Chapter 1.

Theory

Chapter 2.

The COMET Experiment

The aim of the COMET experiment is to search for COherent Muon to Electron Transitions with a single-event-sensitivity of around 3×10^{-17} . This amounts to an improvement of four orders of magnitude compared to the current limit [2] which requires some significant changes to the way the experiment operates.

The general experimental goals of COMET are to:

- stop many muons in aluminium,
- have a high signal acceptance,
- suppress potential background sources to well below a single event.

At the level of sensitivity desired for COMET these requirements translate to the need for:

- a very high intensity muon beam,
- a thin stopping target and low material budget detector,
- a low energy muon beam,
- a pulse beam and relatively low-Z stopping target.

Realising these goals requires many new experimental techniques and as such COMET has decided to operate in two stages, Phase-I and Phase-II. Phase-II will realise the final objective of 3×10^{-17} , whilst Phase-I aims for a measurement with sensitivity of 3×10^{-15} but also to understand the beam and backgrounds to improve our understanding of Phase-II. In order to understand both phases a simple appreciation of the types of backgrounds that must be considered is valuable, so I shall first give an overview of these.

Type	Background	Predicted number of events during run	
		Phase-I [5]	Phase-II [3]
Intrinsic	Muon Decay-in-Orbit	0.01	0.15
	Radiative Muon Capture	0.00056	< 0.001
	μ^- Capture w/ n Emission	< 0.001	< 0.001
	μ^- Capture w/ Charged Part. Emission	< 0.001	< 0.001
Prompt	Radiative Pion Capture	0.00023	0.05
	Beam Electrons	0.00083	< 0.1*
	Muon Decay in Flight	≤ 0.0002	< 0.0002
	Pion Decay in Flight	≤ 0.00023	< 0.0001
	Neutron Induced	—	0.024
	Other beam induced B.G.	$< 2.8 \times 10^{-6}$	—
Delayed	Delayed Radiative Pion Capture	~ 0	0.002
	Anti-proton Induced	0.007	0.007
	Other delayed B.G.	~ 0	—
Cosmic	Cosmic Ray Muons	—	0.002
	Electrons from Cosmic Ray Muons	< 0.0001	0.002
Total background		0.019	0.34
Signal (Assuming $B = 1 \times 10^{-16}$)		0.31	3.8

Table 2.1.: ((*CHECK: UPDATE Phase-I values with TDR 2016*)) Backgrounds for COMET Phase-I [5] and Phase-II [3]. Prompt backgrounds arise by protons that occur in between bunches and are therefore suppressed by the extinction factor. For Phase-I, the recently measured value of 10^{-12} was used for the extinction factor, but for Phase-II the older expectation of 10^{-9} was used.

2.1. Overview of Signal and Backgrounds

μ - e conversion is experimentally attractive because its signal is so simple: a single monoenergetic electron at close to the muon mass of 105 MeV/c, given by:

$$E_e = M_\mu - E_{\mu,\text{binding}} - E_{\text{recoil}} \quad (2.1)$$

where $M_\mu = 105.66$ MeV/c² is the muon mass, $E_{\mu,\text{binding}}$ the binding energy of the muon in the ground state of the muonic atom, and E_{recoil} is the kinetic energy of the recoiling

nucleus. In the aluminium target used for COMET (see section 2.2.3) the electron energy is $E_e = 104.97$ MeV.

Background rates must be kept well below the signal sensitivity if an observation is to be confidently identified as signal, or if meaningful limits are to be set. Given the desired sensitivity of COMET is 3×10^{-15} at Phase-I and 3×10^{-17} by Phase-II, background rates must be kept equally rare.

Table 2.1 summarizes the results of previous studies for background rates at Phase-I and Phase-II. There are predominantly four main groups of background sources: intrinsic, prompt, delayed and cosmic sources.

Intrinsic processes are those that arise from muons stopping in the target and will therefore always be present regardless of how well you make your muon beam and detector. Of these, the dominant background is muon decay in orbit (DIO), which is the standard model process of a muon decaying to an electron, emitting two neutrinos in the process. Although the decay of a free muon cannot produce electrons with energy greater than half the muon mass, once bound to a nucleus the neutrinos can be configured to carry almost no kinetic energy away, such that only the nucleus and electron are important in the end-point configuration. It can immediately be seen then the kinematics of the end-point configuration for muon decay-in-orbit are the same as for μ - e conversion, and indeed a tail in the spectrum of electrons coming from muon DIO extends all the way up to this point. Fig. ?? shows the spectrum of electrons from muon DIO in aluminium where it can be seen that the high energy tail does reach up to about 105 MeV/c, but with a very steeply falling rate.

((CHECK: Figure for DIO spectrum on log / lin scales from 2011 paper, or 2015 paper?))

Delayed and prompt processes can come from impurities in the muon beam, the key difference being the timing with respect to the proton beam arrival. For example, pions reaching the stopping target region are dangerous since they can produce high energy gamma rays which can pair produce to create 105 MeV electrons. Since pion capture against a nucleus is extremely fast (less than 1 ns) the timing of pion-induced backgrounds is determined solely by the arrival time of pions into the target region. In order to reach this region without decaying, the pions must be relatively high momentum of about 60 MeV/c or greater. As a result, backgrounds from pion capture are typically expected close to the arrival of protons at the production target. These sort of prompt processes are suppressed by using a pulse proton beam (discussed in more depth later)

and ensuring very few protons in between pulses. Should a pion in the beam arrive at the target region with a large delay then the timing of the proton beam is not a useful method for suppressing this. Possible causes of this against which must be mitigated is the mirroring of particles in the magnetic field or by production of pions and high-energy electrons from antiprotons. At a given momentum, antiprotons travel considerably more slowly than muons or pions given their considerably larger mass. Other beam related issues include the decay of muons and pions to electrons. An electron of 100 MeV/c can be produced by muons or pions with greater than 70 or 50 MeV/c respectively, and so the flux of higher energy particles must be removed.

Finally cosmic backgrounds arise from high energy muons that pass through the building and enter the detector or beamline. Events where a muon decays to an electron which is then detected as 105 MeV are counted as backgrounds. In particular, muons that produce high energy electrons close to the target are dangerous since cuts on the reconstructed direction and position will be less effective.

2.2. General Experimental Techniques

2.2.1. Proton Beam Energy and Production Target

The muon beam used in COMET is produced as the decay products of a secondary pion beam created by protons striking a target. If maximising the muon intensity were the only concern, then both the proton beam energy and atomic mass of the target material would also be maximised since the pion production cross section grows with these two parameters. However, the need to suppress background rates and maintain the mechanical and operational stability of the target constrain both of these parameters.

In particular, protons with more than 5.6 GeV (***CHECK: Target dependence? Correct?***) striking a stationary target have sufficient energy to produce antiprotons which travel relatively slowly (see 2.2.3) and can produce backgrounds. Since the antiproton yield grows very quickly above this threshold, it has been chosen to use protons with 8 GeV kinetic energy.

For Phase-II running, the main ring will operate at 7 μA so that a beam power of 56 kW is achieved. Phase-I on the other hand will use a lower beam intensity of 0.4 μA or 3.2 kW.

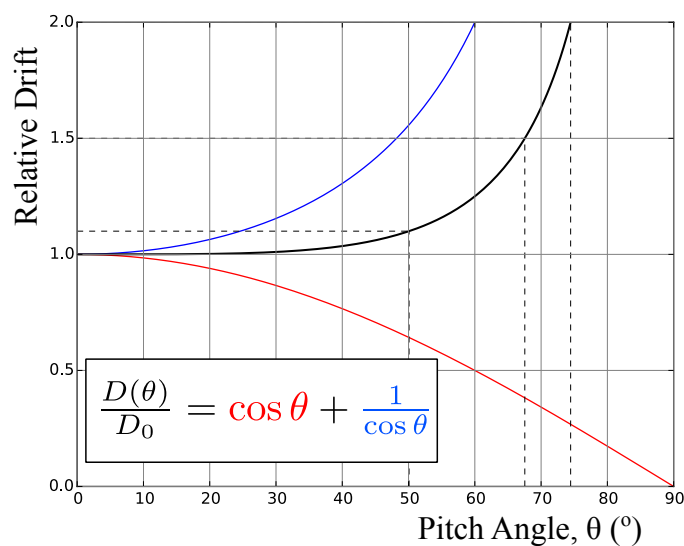


Figure 2.1.: Angular dependence of the magnitude of vertical drift in a bent solenoid field. The total variation (black) remains below 10% for pitch angles below 50°.

A heavy metal target is preferable since it improves the pion yield, in particular tungsten since it is relatively cheap compared to other options. However, at the beam powers under consideration, a metal target would melt, such that we must actively cool the target. Such will be the approach in Phase-II, however for simplicity Phase-I will run with a radiatively cooled graphite target.

((CHECK: Figure for pion vs. antiproton production cross-section for different proton energies and/or target materials))

Finally, only those pions and muons emitted in the backwards direction with respect to the proton beam are captured and transported to the muon beamline. This is a strong way to reduce the high-energy components of the muons and pions distributions since the yield for low momentum pions in the forward and backwards direction is similar, whilst the high energy tail is greatly suppressed in the backwards direction. At this time however, there is a dearth of experimental measurements for pion production in the backwards direction with 8 GeV protons on a graphite or tungsten target. Fig. ?? shows a measurement of the cross section for pion production with 10 GeV protons on tantalum (which is adjacent to tungsten on the periodic table).

2.2.2. Particle Transport through Bent Solenoids

Both Phase-I and II make use of bent solenoids to help select particles of a particular momentum. In bent solenoids, a dispersion occurs that is proportional to the momentum and charge of the particle passing through it.

Charged particles moving through a straight solenoid follow a helical trajectory, orbiting a point that moves parallel to the solenoidal axis with constant velocity fixed by the longitudinal momentum of the particle. The frequency that the particle rotates about this point (betatron frequency or frequency of gyration) is determined by the transverse momentum.

By comparison, if a charged particle moves through a solenoid channel that has been bent, the particle can still be considered to orbit a point, only now the motion of that point can be shown to drift vertically, out of the plane of bending. This drift arises from the gradient introduced to the field by bending the solenoid but also from the non-rectilinear coordinate system of the field lines. The total drift, D , of a particle with mass and charge m and q respectively through a solenoid bent with a fixed radius of curvature, R , is given by:

$$D = \frac{1}{qB} \left(\frac{s}{R} \right) \frac{p_L^2 + 0.5p_T^2}{p_L} \quad (2.2)$$

$$= \frac{1}{qB} \left(\frac{s}{R} \right) \frac{p}{2} \left(\cos \theta + \frac{1}{\cos \theta} \right) \quad (2.3)$$

where B is the magnetic field strength¹, s is the distance travelled through the solenoid, p the momentum of the particle, with longitudinal and transverse components with respect to the solenoid axis, p_L and p_T respectively. The pitch angle, θ , is a property of the helical trajectory taken by the particle and defined as:

$$\theta = \tan^{-1} \left(\frac{p_T}{p_L} \right) \quad (2.4)$$

See Appendix A for a derivation of equations (2.2) and (2.3). The angular dependence of this equation is shown in Fig. 2.1 where it can be seen that for angles below 50 degrees the variation in the drift is less than 10%, such that the drift is determined almost completely by the momentum of particles up to these angles.

¹Strictly speaking, B is the field strength along the path of the centre of gyration, which is constant for a fixed transverse distance from the focus of the bent solenoid.

Bent solenoids are used to disperse high-energy muons and pions in the muon beam for both Phase-I and II, and as a spectrometer system for electrons coming from the stopping target in Phase-II, which will both be described in more detail below.

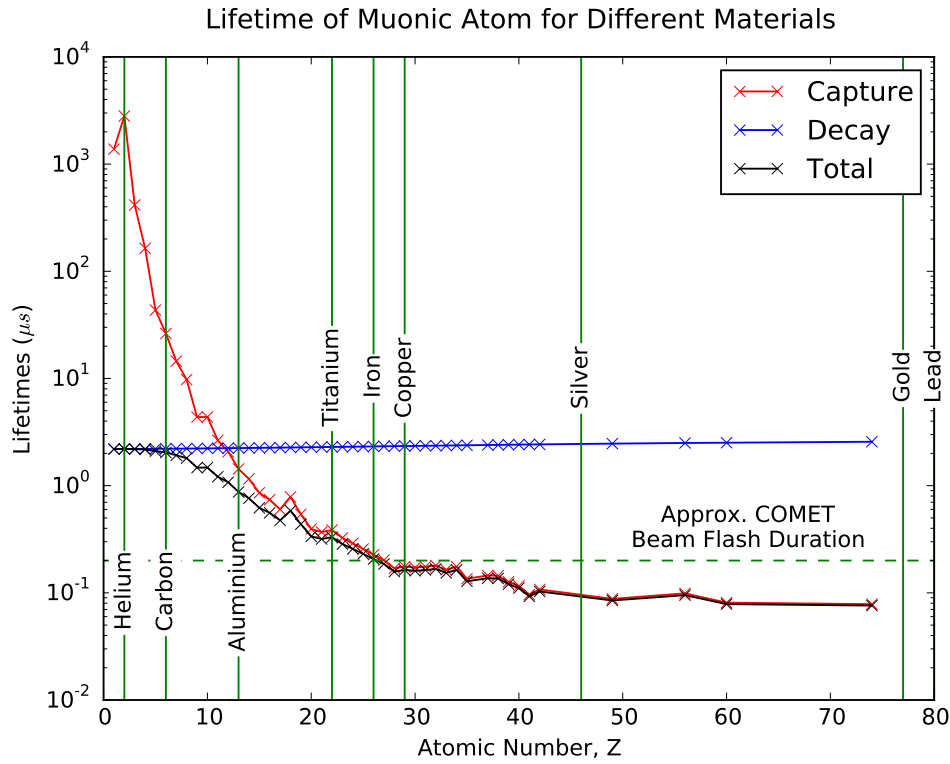
Since the drift is proportional to the momentum of the particle, those particles with zero momentum would remain on axis, whilst particles of interest (105 MeV electrons in the Phase-II electron spectrometer and around 40 MeV/c muons in the muon beam line) drift to the sides. To overcome this issue, a vertical component to the field lines is introduced. If the solenoid were straight the axis of a particle's helical trajectory would follow the field line. A vertical component would therefore cause the trajectories to move upwards with the field line itself. The same result is true in a bent solenoid and since the drift this introduces is not proportional to momentum a vertical component can be used to select at which momentum particles remain on-axis. Two techniques have been considered to introduce this vertical component: tilting the solenoid coils themselves, or adding additional dipole coils around the solenoids. COMET has opted to pursue the latter, using a special, proprietary winding technique developed by Toshiba to introduce a vertical component by placing additional conductor around the other solenoid coils. Since the current through these dipole coils can be altered separately to the solenoid coils, this approach has the advantage that the two can be tuned against the other so that the optimal dipole field can be found whilst running and or the acceptance can be shifted to another momentum or charge to study backgrounds. Additional collimator material can also be introduced to remove particles with undesirable momentum.

2.2.3. Stopping Target Material and Beam Pulsing

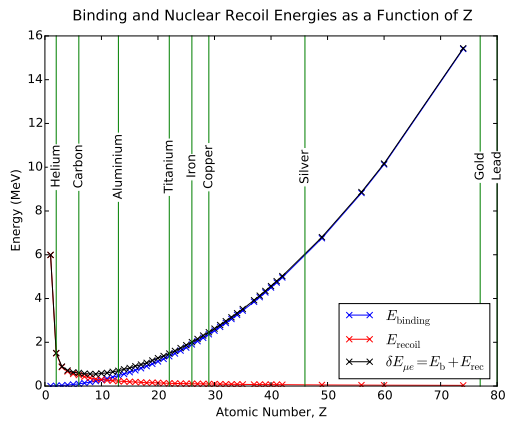
The combination of using backwards going pions and the long, bent-solenoid transport channel is already effective at removing potential background issues. In addition to these however, there is one further method which helps both to reduce beam-related backgrounds and improve the detector occupancy and reconstruction requirements: the use of a pulsed proton beam with a relatively light stopping target.

Since the signal process is coherent, its cross section grows roughly as the square of the number of nucleons (or protons, depending on the model)² until the muon is contained almost completely within the nucleus at which point the rate levels off. It is therefore desirable to use a high-Z target in order to increase the probability of conversion

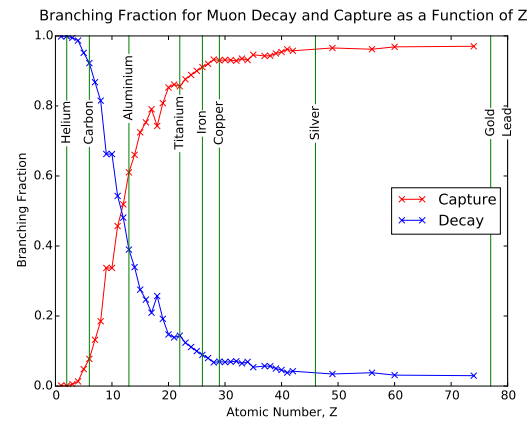
²Although this growth is offset by the normalisation to the capture rate which is incoherent and grows linearly with the number of nucleons, so that the conversion rate itself is roughly linear.



(a) Lifetimes



(b) End-point Shift



(c) Branching Fraction

Figure 2.2.: The effect of changing the atomic number on the branching ratio, lifetime and electron energy spectrum end-point. For the branching ratio and lifetime plots, the partial rate for muon nuclear capture and decay-in-orbit are shown separately. The capture and decay rates are taken from the Geant4 [1] parametrisation for stopped negative muons. Only elements for which at least 1 isotope uses a measured value are plotted. The values for the end-point energy level are calculated using the Bohr model for the muon ground-state binding energy.

and indeed SINDRUM-II used both lead and gold targets, with its most stringent limit coming on gold [2].

However, as the nucleus gets larger, the lifetime of the muonic atom falls steeply due to the increase in the nuclear capture rate. This is illustrated in Fig. 2.2 where it can be seen that for elements heavier than iron ($Z > 26$) the muon lifetime is less than 200 ns. The COMET beamline produces a beam flash that lasts for about 200 ns after the arrival of a proton at the production target. This means that for targets heavier than iron timing information can not be used to distinguish particles coming from the beam or from the decay of a muon stopped in the target.

Whilst these are the two dominant factors in deciding the target material, other factors like the mechanical stability, cost, isotopic purity and the stability of the daughter nuclei following muon capture on the target must also be considered. Accordingly, titanium and aluminium are considered the two most viable target materials. Titanium, in which the muon lifetime is about 330 ns, would be considerably harder to measure μ - e conversion so at this stage the COMET experiment is focussed on using aluminium where the muon lifetime is about 864 ns [4].

The J-PARC accelerator has buckets separated by 550 ns, although separations of multiples of this number can in principle be achieved. For COMET running the intention is to fill every other bucket so that a separation of $1.17 \mu\text{s}$ is achieved. Fig. ?? shows the beam timing schematically. A window from about 700 to 1100 ns after the proton beam arrival is then used to look for signal events, by which time most of the beam flash should have passed whilst signal events remain probable.

Having a well-defined bunch structure is crucial for this scheme to work. Protons arriving in between bunches would produce (a fragment of) beam flash that could include high energy muons or pions which could result in background electrons arriving within the timing window. The extinction factor quantifies the chance of this and is given by:

$$R_{\text{Extinction}} = \frac{N(p \text{ between bunches})}{N(p \text{ per bunch})} \quad (2.5)$$

Original estimates were made assuming $R_{\text{Extinction}}$ was around 10^{-9} [3] (about 1 out-of-time proton for every 7 bunches) although recent measurements have been able to demonstrate extinction at a level of 10^{-12} [?] (about 1 out-of-time proton for every 7100 bunches).

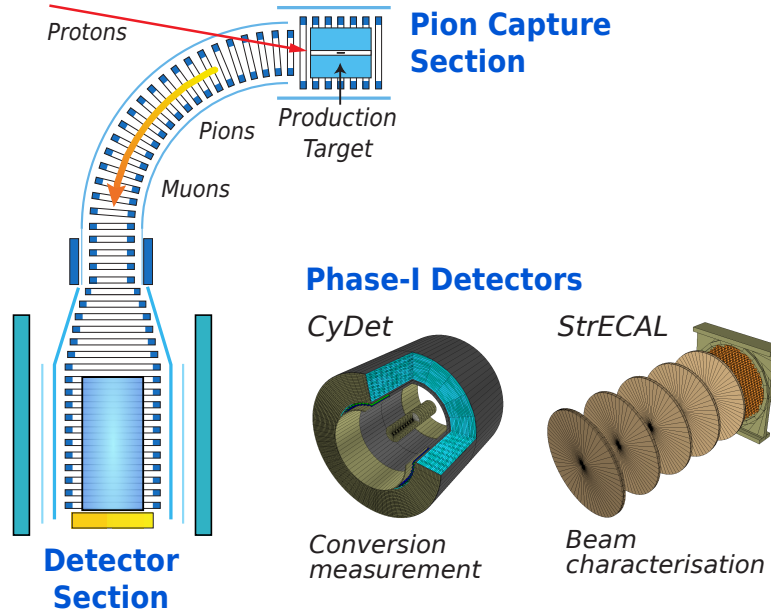


Figure 2.3.: Schematic layout of COMET Phase-I.

The bunch structure is initially defined by the linac at J-PARC which accelerates protons up to 600 MeV. The J-PARC Rapid Cycling Synchrotron (RCS) then takes these protons up to 3 GeV where up to two buckets can be stored at a time, although for COMET only one bunch at a time will be filled. The protons are then injected into the J-PARC Main Ring (MR) which accelerates them up the final energy of 8 GeV and is capable of storing up to 9 buckets at once. Using the Linac chopper alone would not be sufficient to keep the extinction factor since stray protons tend to drift into the unfilled buckets. Achieving the high extinction factor then is possible only by using the injection kicker from the RCS to the MR in a ‘double-kick’ mode. The kicker excitation length is set to two buckets (so that the RCS is completely emptied into the MR). The kicker is then activated again immediately after the first filled bunch has performed a complete rotation of the MR such that protons that had diffused into the second bunch of the RCS are now kicked away. Thus only four out of the nine buckets in the MR are filled and all other buckets are kept empty.

2.3. COMET Phase-I

Phase-I will see the construction of the COMET hall, the production target capture solenoids, the first 90 degrees of the bent muon transport solenoid, and the detector solenoid. The beamline is shown schematically in Fig. 2.3 where the two interchangeable detector systems can also be seen.

There are two key goals to Phase-I:

1. measure μ - e conversion at a sensitivity of 3×10^{-15} ,
2. prepare for Phase-II by measuring the beam profile, particle yields and background rates, and prototype the detector technology.

Since the dynamics of bent solenoids are complicated, it is important to study the beam as close to the production target as possible. However, due to the high radiation environment, it is important that the detector and electronics be kept well shielded. Phase-I will therefore measure the beam after the first 90 degrees of bent solenoid using the same detector system to be used in Phase-II, namely the Straw tube tracker and Electromagnetic Calorimeter ([StrECAL](#)) detector – a series of Straw Tracker stations followed by an ECAL all sitting in the beam.

However, since the [StrECAL](#) detector will be hit by the full force of the muon beam, it would not be feasible to conduct a μ - e conversion search using this detector. As such, for Phase-I a second detector, known as the Cylindrical Detector ([CyDet](#)) will be used for this purpose. The [CyDet](#) uses a Cylindrical Drift Chamber to reconstruct the trajectories of charged particles and a pair of Cherenkov and Scintillation counters (one upstream and one down) to trigger the read-out of the system. The [CyDet](#) escapes the issue of the beam flash that the [StrECAL](#) would face at Phase-I since only the outer region is instrumented. Since the detector sits in a 1 T solenoid field (and both the detector and solenoid are co-axial), particles follow helical trajectories with the radius of gyration determined by the transverse momentum of the particle. The beam is introduced in the centre and typically remains in an envelope of 15 cm whilst the stopping target sits in the centre of the detector with a radius of 10 cm. As such the detector itself is geometrically blind to charged particles in the beam and electrons coming from muon [DIO](#) in the target with momentum less than 60 MeV/c which make up the majority of the [DIO](#) spectrum. To reconstruct the longitudinal position of the particle's trajectory an all-stereo configuration is used in the Cylindrical Drift Chamber, where each layer is

rotated in the opposite direction compared to the previous layer by an angle of 4° with respect to the solenoid axis.

Because the Phase-I detector sits much closer to the stopping target, there is greater exposure to hadrons emitted following nuclear capture of the stopped negative muons, such as protons, deuterons, alpha particles and so on. Despite being emitted with kinetic energies of a few tens of MeV, momenta above 60 MeV are readily achieved given the large mass of these particles. For similar reasons these particles are typically very heavily ionising, so if left unchecked could readily dominate the occupancy of the Cylindrical Drift Chamber (CDC). The AlCap experiment has shown that for muon capture on Al-27 nuclei, the emission of a proton occurs for about 3% of every muon capture [6]. At this level, it is believed that no specific shielding is required beyond the carbon inner wall of the CDC needed to contain the gas mixture.

Four layers of scintillation bars will surround the outside of the detector to provide a veto for cosmic ray events. The most dangerous event would be a high energy muon reaching the target and decaying to a 105 MeV electron which is then detected. Dedicated cosmic runs will be performed prior to operation with a beam in order to understand the flux of cosmic muons. Since the neutron flux from

2.4. COMET Phase-II

Since chapter 4 presents an in-depth optimisation of the design of Phase-II, I shall only give a brief introductory overview here, most of which is based on the design as laid out in the CDR [3].

COMET Phase-II will be the final stage of the experiment. It will extend the muon beamline built in for Phase-I by an extra 90° , and add two extra solenoid sections: one to hold the stopping target, and a second 180° bent solenoid with a large aperture of 60 cm radius. This layout is shown in Fig. 2.4. The bent solenoid after the stopping target acts both as a spectrometer, but also to remove the low energy DIO electrons which otherwise could significantly increase the hit rate in the detector. The final detector system for Phase-II will use the StrECAL from Phase-I but probably with thinner diameter straw tubes, thinner straw material, and more tracking stations in order to improve the energy resolution.

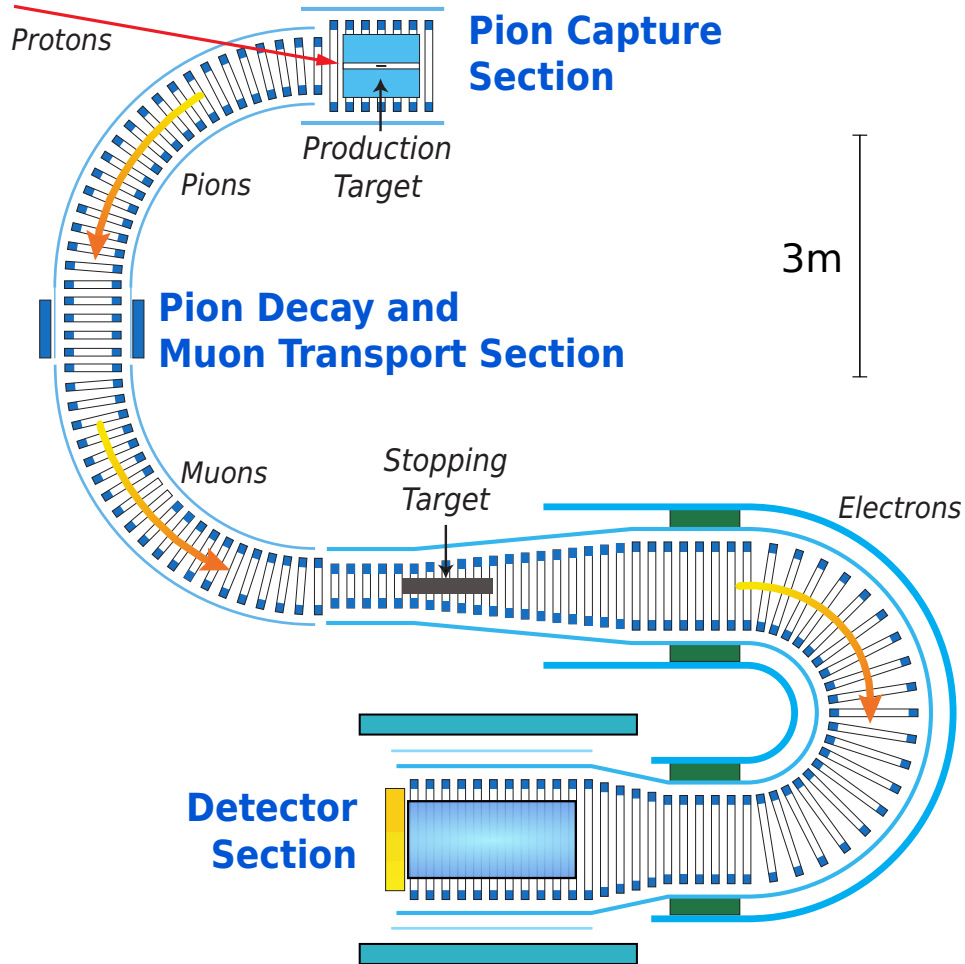


Figure 2.4.: Schematic layout of COMET Phase-II. The 8 GeV proton beam enters from the top-left, producing (amongst other things) pions. Pions and muons travelling backwards with respect to the proton beam are then transported around 180 degrees of bent solenoid, during which time most of the pions decay producing an intense muon beam. About 40% of these muons then stop in the stopping target (centre of image). Any electrons coming from μ - e conversion are then transported through another 180 degrees of bent solenoid into the detector system.

The stopping target itself has typically been designed as thin disks of aluminium, followed by a beam blocker. Even including the growth of the beam envelope as it passes from the 3 T field in the bent muon transport solenoids to the 1 T of the bent electron spectrometer solenoid the beam blocker removes all line-of-sight between the entrance of the electron spectrometer and the muon transport solenoids so that most of the beam flash is prevented from reaching the detector. The tapering of the field occurs almost

completely across the target itself with the intention that signal electrons heading initially upstream will be magnetically mirrored back towards the detector.

As for Phase-I, an active cosmic ray veto will prevent triggering on events caused by cosmic muons. At least the detector solenoid will be covered, but there is some scope

2.5. Schedule and Status

The overall schedule for the COMET experiment is shown in Fig. 2.5. Phase-I is due to start data taking in Japanese Fiscal Year (JFY) 2018 so that construction and development is well underway.

At the time of writing, with regards to the facility, the building to house the experiment is now finished attached to the side of the existing Hadron Hall at the Japanese Proton Accelerator Research Complex (J-PARC). Cooling and power supplies are being installed and the shielding for the concrete hatch area is being produced. In the mean time the development of the new beamline to extract protons from the MR and deliver them to the COMET area is being installed. In particular, the Lambertson magnet which directs the protons towards COMET rather than the existing Hadron Hall has been built. For the muon beamline, the Phase-I section of the bent muon transport solenoids has been built and installed and is now under commissioning studies. Construction of the detector solenoid has also begun with the capture solenoids around the production target

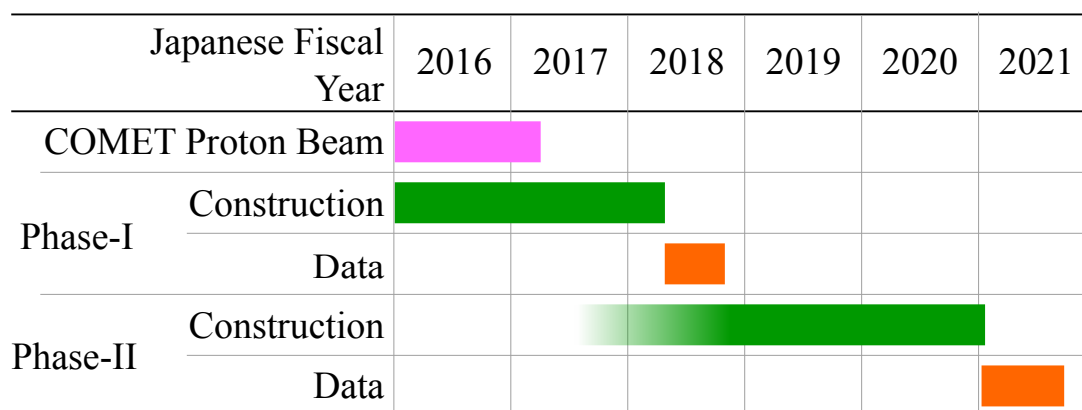


Figure 2.5.: A summarised timeline for the COMET experiment including Phase-I and Phase-II based on the 2016 TDR [?]. At the time of writing, construction of the detector solenoid is underway as well as the final stages of the facility.

soon to begin. A selection of photographs that show the construction of the facility and installation of the bent transport solenoid are shown in Fig. ??.

Much of the recent activity for the collaboration has been on the design and construction of the detector systems. Beam tests to understand the performance and resolution of prototype ECAL crystals, straw tubes and the CDC have taken place. For the StrECAL, production of all 2500 Phase-I straws has been completed and procurement of the LYSO! (LYSO!) crystals for the ECAL is under way with some 200 or so crystals already purchased. Aging tests of the straw tubes are under way with straws under pressure and tension are being held for a long duration at KEK. Analysis of beam-test data is underway to understand the position resolution for a given straw, and the energy resolution of the ECAL, although better than 5% resolution for 105 MeV electrons has already been shown. Fig. ?? shows photographs of the prototypes and beam test set-ups of the Straw Tube Tracker and the ECAL.

In the meantime the full CDC has been strung, with some 20,000 wires less than 10 microns thick (*(CHECK: is this the correct wire size)*) being inserted. Every wire has had its tension checked using a vibrational resonance method, which showed some -- (*(CHECK: How many wires needed to be replaced)*) wires were too loose and have since been replaced. Currently the inner wall of the CDC is being inserted so that leak tests can begin shortly. Fig. ?? shows photographs from the stringing of the CDC. In parallel, cosmic ray tests have been used to study the performance of CDC prototypes and analysis of the data is under way to deduce the X-T curve for the CDC cells.

Chapter 3.

Offline Software and The COMET Simulation

Chapter 4.

Phase-II Optimisation

1. Before a substantial sensitivity estimate can be made, need a solidly optimised design
2. Aiming for 3×10^{-17} within a single year of running
3. Designs previously optimised [?], and these results are used as nominal design / starting point
4. Fresh optimisation using new software / simulation, updated fieldmaps, physics lists and geometry
5. Some aspects fixed already since Phase-I under construction: Experiment hall, Torus1, detector solenoid, fieldmap and coil parameters?
6. Key areas for optimising:
 - 6.1. Production target dimensions
 - 6.2. Torus1 dipole field strength
 - 6.3. Torus2 dipole field strength
 - 6.4. Electron spectrometer dipole field strength
 - 6.5. collimator shapes and locations
 - 6.6. stopping target and beam blocker position and form
 - 6.7. DIO blockers on spectrometer

4.1. Optimisation Strategy

7. Take some aspects as fixed

8. Limit scope and approach:

8.1. Ideally, each aspect optimised in combination to maximise signal acceptance and reduce background

8.2. How decoupled are each section?

8.3. In practise such an optimisation is not easy to do, instead aim to produce a baseline optimisation so that all backgrounds / issues can be identified

8.4. This can then form basis for further optimisation, with perhaps a smarter more integrated approach

9. Method:

9.1. Production target optimisation

9.1.1. Maximise muon and pion yield between 0 and 80 MeV at entrance to muon beamline

9.1.2. Parameters to vary: target length, target radius

9.2. Muon beam optimisation

9.2.1. Maximise muon stopping rate in stopping target

9.2.2. Minimise pion stopping rate

9.2.3. vary dipole along TS2 and TS4

9.2.4. vary Collimators: TS2 and at TS3

9.3. Electron spectrometer optimisation

9.3.1. Optimise dipole to increase signal acceptance

9.3.2. Optimise DIO blockers so DIO rate per straw is less than 1 kHz

9.3.3. Vary solenoidal field to increase separation?

9.4. Stopping target / beam blocker optimisation

9.4.1. Maximise reflection of signal electrons from upstream by tuning target position

9.5. Detector optimisation

4.2. Optimisation Goals

10. Set sensitivity goal and optimise to reach this

11. Single event sensitivity only considers signal acceptance, but also need to understand backgrounds in terms of final confidence limit that can be set

4.3. Production Target Optimisation

In the Phase-II Conceptual Design Report ([CDR](#)), the production target is given as being 16 cm in length and 4 mm in radius [?]. Since then, there have been changes to the magnetic field in this region, as well as the lengths and locations of solenoids, shielding and beam-pipe, and the proton beam. Previous studies have looked at comparing the Tungsten target proposed for Phase-II to other materials [?], and also drawn a comparison between MARS [?], Geant4 [?] and the limited data available.

The goal in this study then is to optimise the production target with the up-to-date configurations. This study aims to maximise the total muon and pion yield below 80 MeV at the entrance to the Torus1 bent solenoid, by varying the radius and length of the production target.

4.3.1. Configuration

Table [4.1](#) gives the key parameters for the beam input and other aspects of this simulation. The location and orientation of the target were held fixed, since the proton beamline is fixed with respect to the muon beam axis. Once a realistic proton beam becomes available, these values would also benefit from optimisation, however. During the scan over length, the back face of the target was kept 8 cm away from the muon beam since the radiation shielding has previously been optimised, and since beyond this the magnetic field will no longer be able to capture the pions and muons produced.

It must be noted that at this point in time there is a appreciable uncertainty in the proton beam profile and position. In particular, whilst the proton beamline upstream has

Proton Beam	
Horizontal spread, σ_x	5.8 mm
Vertical spread, σ_y	2.9 mm
Mean energy, μ_E	8.01 GeV
Energy spread, σ_E	0.135 MeV
Target	
Material	Tungsten
Orientation	10° between target's principal axis and the muon beam axis.
Location	Back face fixed 8 cm away from muon beam axis.
Length	16 cm in CDR. Varied in steps of 4 cm from 4 to 32 cm.
Radius	4 mm in CDR. Varied from 2 to 10 cm in steps of 2 cm and from 10 to 30 cm in steps of 4 cm.
Software configuration	
Packages	heads/1512w51_develop(3a0ee59)__3_UNCOMMITTED__
Externals	heads/Patch_Geant4-G4MultiLevelLocator(11fc8f0)
Fieldmap	160104 ((<i>CHECK:</i>))
Sample Sizes	
Length scan	3e5 Protons on Target (POT) (30 runs of 1e4)
Radius scan	4.9e5 POT (49 runs of 1e4)
Final scan	

Table 4.1.: Key parameters in the configuration of the Production Target optimisation.

been well delivered, the effect of the magnetic field and necessary dipole and quadrupole magnetics are still being studied by the proton beam-line group. The beam profile is given in the Phase-I Technical Design Report ([TDR](#)) as having a Gaussian profile and energy distribution, but no divergence or location is given. The effect of the proton beam distribution on the overall sensitivity shall therefore be considered later on.

Protons originated from a plane (distributed as a two dimensional Gaussian across this surface) but since there is therefore some scope to tune the proton beam's position, the input particle plane was moved to remain 1 cm away from the front surface of the target. Since the aim is to maximise the muon and pion yield by varying only the length and radius, shifting the proton beam input plane in this way removes any variation of target acceptance due to divergences of the proton beam in the magnetic field.

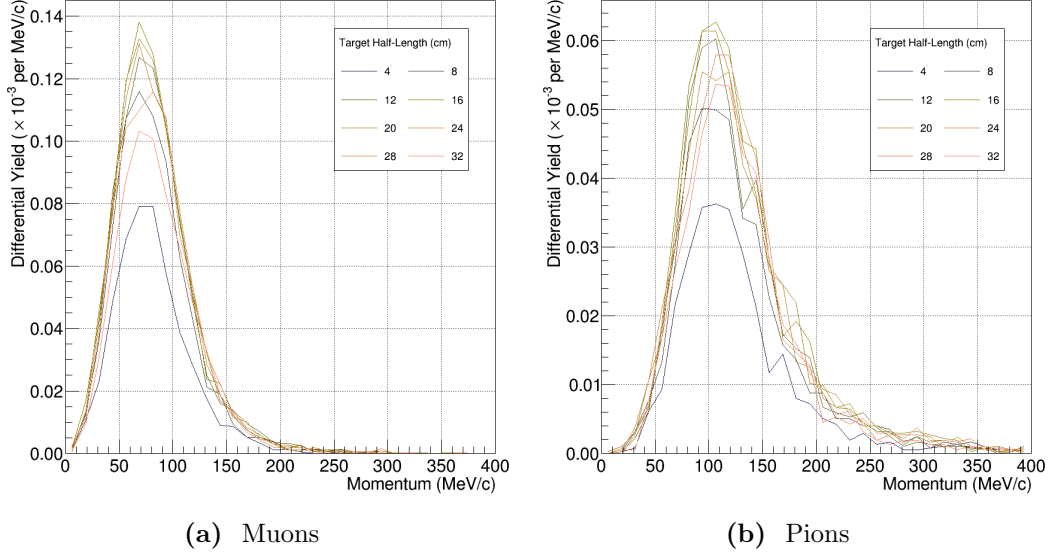


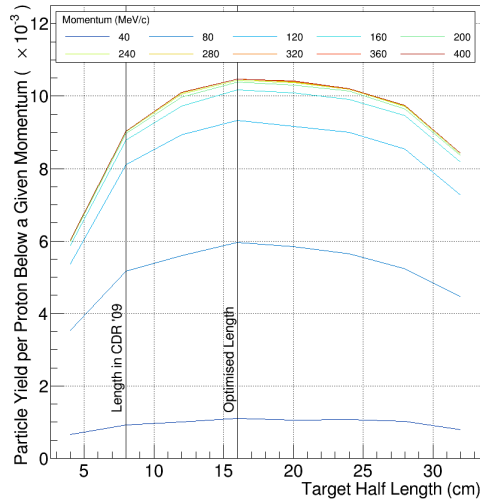
Figure 4.1.: Change to momentum distributions at the entrance to the first 90 degrees of the bent muon beam solenoid for different target lengths. Target length is given as half-length which is the Geant4 convention.

4.3.2. Length Scan

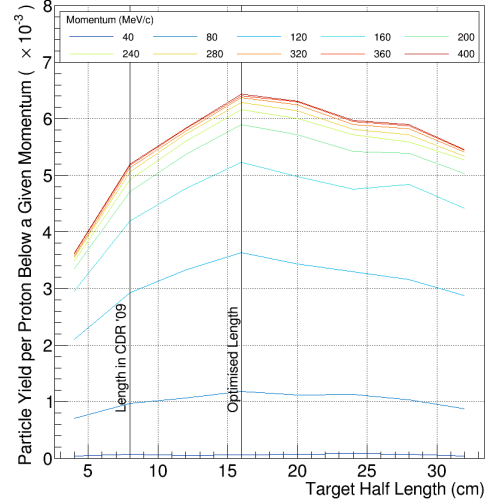
Different length targets were simulated with $3e5$ POT per length. Target length was varied in steps of 4 cm from 4 to 32 cm, whilst the target radius was held fixed at the CDR value of 4 mm.

Fig. ?? shows the momentum distributions of pions and muons for different target lengths. Target length is given as half-length which is the Geant4 convention. Fig. 4.2 then shows these distributions integrated up to different momentum. From these plots it can be seen that for both muons and pions, the optimum target length occurs around a total length of 32 cm.

Additionally it can be seen from Fig. 4.3 that the shape of the momentum distributions changes only weakly as a function of the target length. These plots were produced by normalising the integrated momentum contours of Fig. 4.2 to the total integral below 400 MeV. As a result, it is possible that the actual shape variation is even weaker than apparent here, since in the present sample size, the high momentum tail is not well sampled at small target lengths, such that a skew in the normalisation might occur.

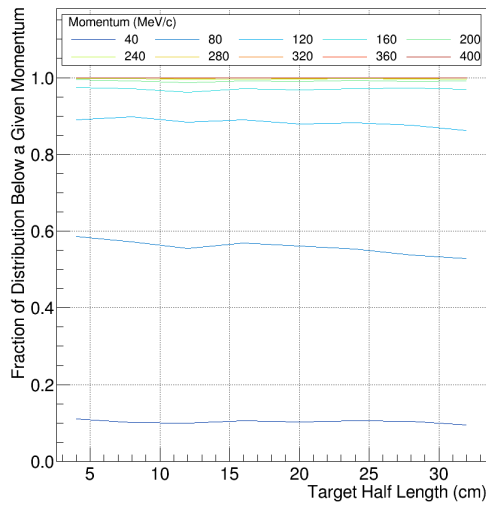


(a) Muons

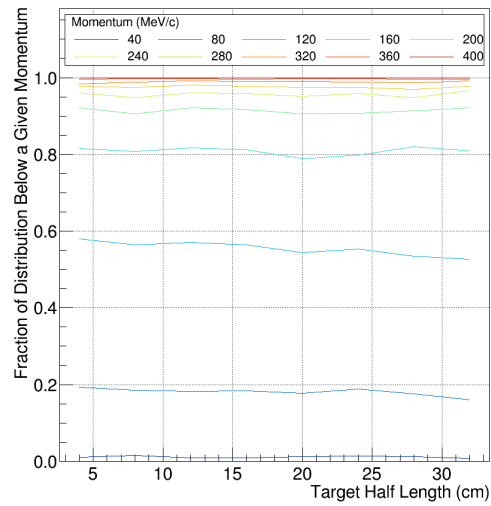


(b) Pions

Figure 4.2.: Integrated muon and pion yields up to a certain momentum at the entrance to the first 90 degrees of the bent muon beam solenoid as a function of target length.



(a) Muons



(b) Pions

Figure 4.3.: Change in the momentum distribution of muons and pions at the entrance to the first 90 degrees of the bent muon beam solenoid as a function of target length.

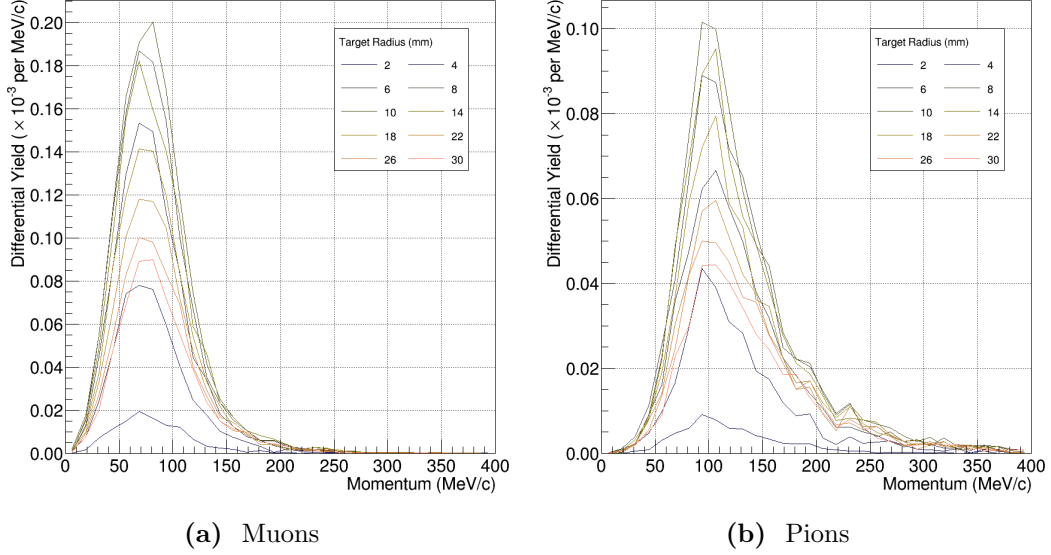


Figure 4.4.: Change to momentum distributions at the entrance to the first 90 degrees of the bent muon beam solenoid for different target radii.

4.3.3. Radius scan

In parallel to the length optimisation scan, different radii targets were also simulated. Targets with radii of 2, 4, 6, 8, 10, 14, 18, 22, 26, and 30 mm were tested. The target length was held at the CDR value of 16 cm in total.

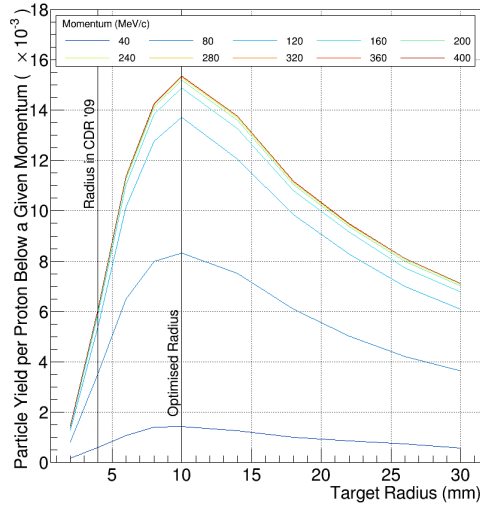
The results of these scans can be seen in Fig. ?? and Fig. 4.5, where it can be seen that a maximum in both the muon and pion yields at the entrance to the Torus1 section is achieved at a radius of about 10 mm. As in the length scan, the shape variation of the momentum distributions is rather weak as a function of target radius.

4.3.4. Final Result

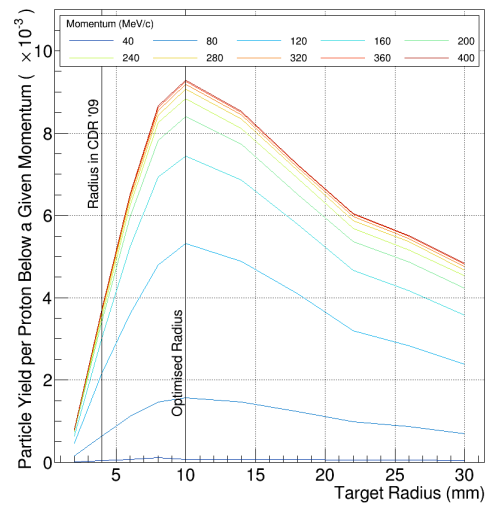
Since the length and radius scan were performed in parallel, a final cross check was performed where the optimal radius was confirmed at the optimised target length. The integrated spectrum is shown in Fig. ?? where it can be seen that the optimum radius once the target length is increased to 32 cm is still 10 mm.

12. Figure comparing Phase-II to Phase-I

13. Conclusions

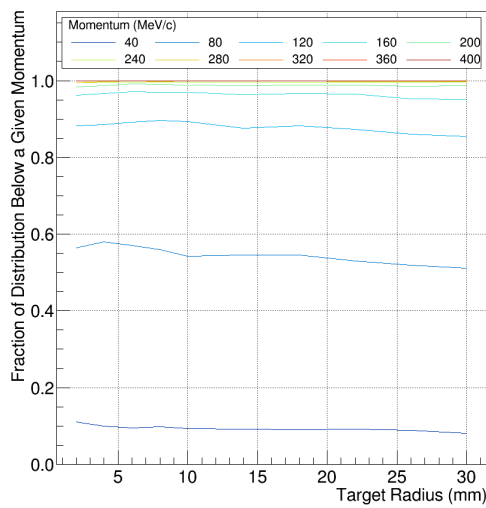


(a) Muons

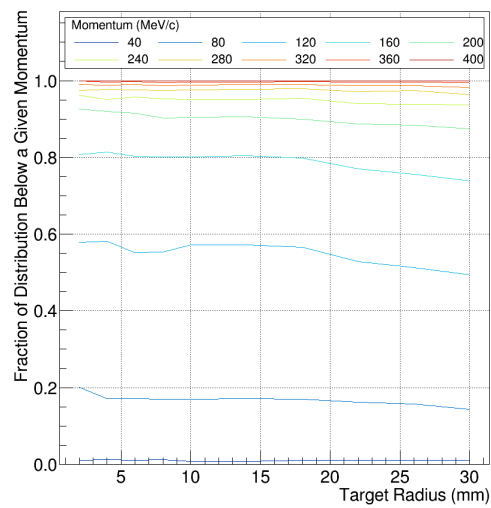


(b) Pions

Figure 4.5.: Integrated muon and pion yields up to a certain momentum at the entrance to the first 90 degrees of the bent muon beam solenoid as a function of target radius.



(a) Muons



(b) Pions

Figure 4.6.: Change in the momentum distribution of muons and pions at the entrance to the first 90 degrees of the bent muon beam solenoid as a function of target radius.

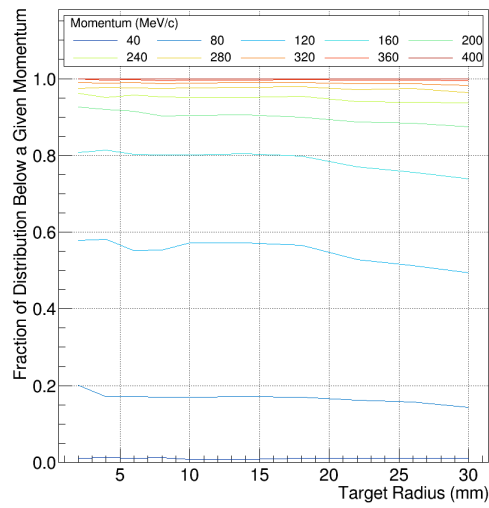


Figure 4.7.: Comparison of the combined muon and pion yield at the entrance to Torus1 for Phase-I (blue) and Phase-II (red).

Chapter 5.

Phase-II Signal Sensitivity

Chapter 6.

Phase-II Backgrounds

Appendix A.

Drifts in a Bent Solenoid

The Lorentz force:

$$\frac{d\vec{p}}{dt} = \frac{q}{m} \vec{p} \times \vec{B} \quad (\text{A.1})$$

A.1. Uniform Solenoidal Field

B field is uniform and parallel to axis of solenoid. Define the Larmor frequency, ω , and radius, a , as:

$$a = \frac{\gamma m \vec{v} \times \vec{B}}{q B^2} = \frac{p_T}{q B} \quad (\text{A.2})$$

$$\omega = \frac{q B}{m} \quad (\text{A.3})$$

A.2. Field in a Bent Solenoid

Producing a cylindrical solenoid channel can be imagined as directly bending that of a normal uniform and linear one. By symmetry it can be seen that any gradient introduced to the magnetic field can only be radially, in the plane of the bending. Further, by considering Ampere's law with a current loop in the plane of bending formed by two radial straight lines (with length $|r - R| < L$, where R and L are the bending and aperture radii of the solenoid channel) and an arc, it can be seen that the variation in

the field is given by:

$$\frac{\vec{\nabla} B}{B} = \frac{1}{r} \hat{r} \quad (\text{A.4})$$

((*CHECK: Sketch or figure?*))

A.3. Drift Calculation

There are two sources of drift in a bent solenoid: the gradient in the field, and the centrifugal force arising from the circular coordinate system needed to describe the field lines. The two can be treated separately in the sense that the motion of a particle moving through a field with straight field lines but with a transverse gradient given by $\nabla B/B \propto 1/r$ would be described by an equation of motion equivalent to that from the first source of drift in the bent solenoid system. Similarly, a system with a uniform field but field lines that follow circular paths would exhibit drift equivalent to the second component mentioned above.

A.3.1. Gradient Drift

“Grad-B” drift is well described in text books, but in the interest of completeness a short derivation shall be given here. The drift arising due to the gradient in the field can be treated as a perturbation of the motion of the particle in a uniform solenoidal field. The total velocity \vec{V} , is given by:

$$\vec{V} = \vec{v} + \vec{v}_g, \quad (\text{A.5})$$

where \vec{v} is the unperturbed velocity of the particle in the transverse plane, and \vec{v}_g is the velocity arising due to the gradient in the field.

Treating the field as a Taylor expansion:

$$\vec{B}(\vec{r}) = \vec{B}_0 + (\vec{r} \cdot \nabla)|_{\vec{r}=0} \vec{B} + \dots \quad (\text{A.6})$$

and substituting equations (A.5) and (A.6) into the Lorentz force, gives:

$$m \frac{d(\vec{v} + \vec{v}_g)}{dt} = q(\vec{v} + \vec{v}_g) \times \left(\vec{B}_0 + (\vec{r} \cdot \nabla)|_{\vec{r}=0} \vec{B} \right) \quad (\text{A.7})$$

$$(\text{A.8})$$

so that to first order, the perturbing velocity is given by:

$$\frac{d\vec{v}_g}{dt} = \frac{q}{m} \left(\vec{v} \times (\vec{r} \cdot \nabla)|_{\vec{r}=0} \vec{B} + \vec{v}_g \times \vec{B}_0 \right) \quad (\text{A.9})$$

Since we are only interested in steady-state solutions where \dot{v}_g is close to zero, the above equation gives:

$$\vec{v}_g = \frac{q}{m} \frac{\vec{B}_0 \times \left(\vec{v} \times (\vec{r} \cdot \nabla)|_{\vec{r}=0} \vec{B} \right)}{B_0^2} \quad (\text{A.10})$$

which by considering the form after time averaging becomes:

$$\langle \vec{v}_g \rangle_t = \frac{\vec{B}_0 \times \left(\vec{v} \times (\vec{r} \cdot \nabla)|_{\vec{r}=0} \vec{B} \right)}{B_0^2} \quad (\text{A.11})$$

List of Acronyms

CDC Cylindrical Drift Chamber

CDR Conceptual Design Report

CyDet Cylindrical Detector

DIO decay in orbit

JFY Japanese Fiscal Year

J-PARC the Japanese Proton Accelerator Research Complex

MR J-PARC Main Ring

POT Protons on Target

RCS J-PARC Rapid Cycling Synchrotron

StrECAL Straw tube tracker and Electromagnetic Calorimeter

TDR Technical Design Report

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