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Towards Reinforcement Learning of Invariants for Model Checking of Interlockings

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Abstract—The application of formal methods to verify that railway signalling systems operate correctly is well established within academia and is beginning to see real applications in industry. However, the uptake is yet to make a substantial impact due to current approaches often producing so-called false positives that cause the need for lengthy manual analysis during verification. It is accepted that so-called invariants, properties which hold for all scenarios in which a signalling system operates, can help reduce the number of such false positives. These invariants are often bespoke, manually designed properties created by experienced engineers and automating their generation remain a challenge. In this work we present first steps towards using reinforcement learning to explore state spaces of signalling systems and to generate a dataset of state sequences from which we envisage invariants could be mined.

Results and what they suggest

1. Introduction

Model checking is a formal verification technique stemming from the need to systematically check whether certain properties hold for different configurations (states) of a given system. Given a transition system T and a formula (or property) F, model checking attempts to verify through refutation that $s \vdash F$ for every system state $s \in T$, such that $T \vdash F$.

The application of model checking in order to verify railway interlockings is well established within academia and is beginning to see real applications in industry. As early as 1995, Groote et al. [1] applied formal methods to verify an interlocking for controlling the Hoorn-Kersenbooger railway station. Newer approaches to interlocking verification have also been proposed in recent years [2], [3], [4]. This includes work by Linh et al. which explores the verification of interlockings written in a similar language to Ladder Logic using SAT-based model checking. In spite of this, such approaches still lack widespread use within the Rail industry.

In particular, one of the limitations of such model checking solutions is that verification can fail due to over approximation, typically when using techniques such as inductive verification []. Inductive verification fails to consider whether system states which violate a given property are

indeed reachable by the system from a defined intital configuration. These false positive often require manual inspection. One solution is to introduce so-called invariants to suppress false positives [5]. Invariants are properties that hold for subregions of the state space. The aim is to introduce invariants that help bound the region of reachable states when model checking. However generating sufficiently strong invariants automatically is complex [].

In this work we take first steps towards using machine learning to generate invariants by providing a first formal mapping of interlocking based state spaces to a reinforcement learning environment. We then explore how such state spaces can be generated in a controlled manner to test the scalability of our approach on environments where the number of reachable states is known. Finally we provide an analysis of how various reinforcement learning algorithms can be used to effectively explore state spaces in terms of their coverage. We see this as a first step towards mining invariants from such state spaces as this approach would indeed require reasonable coverage. Finally we reflect upon future works in directing our approach to improve exploration and learn invariants from a dataset of state sequences generated by our RL agents.

2. Preliminaries

We now briefly discuss model checking of railway interlockings and reinforcement learning. For further details we refer the reader to [6], [7] and [8] respectively.

2.1. Ladder Logic & Interlockings

Interlockings serve as a filter or 'safety layer' between inputs from railway operators, such as route setting requests, ensuring proposed changes to the current railway state avoid safety conflicts. As a vital part of any railway signalling system, interlockings are critical systems regarded with the highest safety integrity level (SIL4) according to the CEN-ELEC 50128 standard.

Ladder logic is a graphical language widely used to program Programmable Logic Controllers [?] and in particular the Siemens interlocking systems we consider in this work. From an abstract perspective, ladder logic diagrams can be represented as propositional formulae. Here we follow the definition of James et al— [?]. A ladder logic rung

consists of the following entities. Coils represent boolean values that are stored for later use as output variables from the program. A coil is always the right most entity of the rung and its value is computed by executing the rung from left to right. Contacts are the boolean inputs of a rung, with open and closed contacts representing the values of un-negated and negated variables respectively. The value of a coil is calculated when a rung fires, making use of the current set of inputs – input variables, previous output variables, and output variables already computed for this cycle – following the given connections. A horizontal connection between contacts represents logical conjunction and a vertical connection represents logical disjunction.

A interlocking executes such a program froim top-tobottom over and over, indefinitely.

More formally, following [?] a ladder logic program is constructed in terms of disjoint finite sets I and C of input and output/state variables. We define $C' = \{c' \mid c \in C\}$ to be a set of new variables in order to denote the output variables computed by the interlocking in the current cycle.

Defn 1. Ladder Logic Formulae: A ladder logic formula ψ is a propositional formula of the form

$$\psi \equiv ((c_1' \leftrightarrow \psi_1) \land (c_2' \leftrightarrow \psi_2) \land \dots \land (c_n' \leftrightarrow \psi_n)$$

Where each conjunct represents a rung of the ladder, such that the following holds for all $i, j \in \{1, ..., n\}$:

- $c'_i \in C'$ (i.e. c' is a coil)
- $i \neq j \rightarrow c_i' \neq c_j'$ (i.e. coils are unique) $vars(\psi_i) \subseteq I \cup \{c_1', \dots, c_{i-1}'\} \cup \{c_i, \dots, c_n\}$ (i.e. the output variable c_i' of each rung ψ_i , may depend on $\{c_i,\ldots,c_n\}$ from the previous cycle, but not on c_i with j < i, due to the nature of the ladder logic implementation, those values are overridden.)

2.2. Transistion Systems and Model Checking for Ladder Logic

For this work, we have concentrated on trying to produce invariants for the approaches taken by Kanso et al. [6] and James et al. [7]. Here we include their model of ladder logic based railway interlocking programs as we use this as a basis for defining a learning environment.

Builiding upon the propositional representation of a ladder logic program given in Section ??, we can define, following [?], the semantics of a ladder logic program in terms of labelled transition systems.

Let $\{0,1\}$ represent the set of boolean values and let

$$Val_I = \{\mu_I \mid \mu_I : I \to \{0, 1\}\} = \{0, 1\}^I$$
$$Val_C = \{\mu_C \mid \mu_C : C \to \{0, 1\}\} = \{0, 1\}^C$$

be the sets of valuations for input and output variables.

The semantics of a ladder logic formula ψ is a function that takes the two current valuations and returns a new valuation for output variables.

$$[\psi]: Val_I \times Val_C \to Val_C$$

 $[\psi](\mu_I, \mu_C) = \mu'_C$

where μ'_C is computed as follows: the value of each variable c_i is computed using the *i*th rung of the ladder, ψ_i , using the valuations μ_C and mu_I from the last cycle and the current valuations restricted to those evaluated be fore the current variable. We refer the reader to [?] for full details.

Defn 2. Ladder Logic Labelled Transition System: We define the labelled transition system $LTS(\psi)$ for a ladder logic formula ψ as the tuple $(Val_C, Val_I, \rightarrow, Val_0)$ where

- $Val_C=\{\mu_C|\mu_C:C\rightarrow\{0,1\}\}$ is a set of states. $Val_I=\{\mu_I|\mu_I:I\rightarrow\{0,1\}\}$ is a set of transition
- $\bullet \to \subseteq Val_C \times Val_I \times Val_c \text{ is a labelled transition relation, where } \mu_C \xrightarrow{\mu_I} \mu_C' \text{ iff } [\psi](\mu_I,\mu_C) = \mu_C'.$
- $Val_0 \subseteq Val_C$ is the set of initial states.

We write $s\xrightarrow{t} s'$ for $(s,t,s')\in R$. A state s is called reachable if $s_0\xrightarrow{t_0} s_1\xrightarrow{t_1}\dots\xrightarrow{t_{n-1}} s_n$, for some states $s_0,\dots,s_n\in Val_C$, and labels $t_0,\dots,t_{n-1}\in Val_I$ such that $s_0 \in Val_0$.

add figure example

2.3. Reinforcement Learning and MDPs

Reinforcement Learning (RL) is a machine learning paradigm with demonstrably impressive capacity for modelling sequential decision making problems as the optimal control of some incompletely-known Markov Decision Process (MDP) [9].

Defn 3 Markov Decision Process A finite discounted Markov Decision Process M is a five tuple $\langle S, \mathcal{A}, P_a(s, s'), R_a(s, s'), \gamma \rangle$, where

- S, is a finite set of states, known as the observation space or state space, representing the environment at discrete time steps.
- A, describes the action space; a set of actions performable at discrete time steps, used to compute new states from the observation space.
- $P_a(s,s') = Pr(s_{t+1} = s'|s_t,a_t)$, describe state transition probabilities. The likelihood of observing state s_{t+1} given action a_t is taken from state s_t .
- $R_a(s,s')$ is a reward function feeding a scalar signal back to the agent at each time step t.
- $\gamma \in [0,1]$ is a discount scalar successively applied at each time step.

In an RL setting we refer to the MDP as our environment, \mathcal{E} where through simulation, software agents sample actions $a \in \mathcal{A}$, observe changes in states, $s \in S$ and learn to optimise learning some objective based on rewards, r issued over discrete time steps t. Simulation can be continuous, where agents indefinitely interact with the environment until some termination criterion is met, such as reaching some reward threshold. Alternatively tasks may be episodic, where training is conducted over a sequence of episodes, defined by a finite number of time steps. An agent's trajectory, $\tau = (s_1, a_1, r_1, s_2, a_2, r_2, ..., s_h, a_h, r_h)$, summarises experience accumulated over a single episode or continuous training run. Here, h refers to the horizon; a time step beyond which rewards are no longer considered. Rewards observed from time step t up to some terminal time step T are denoted $G_t = \sum_{i=t}^T \gamma^{i-t} r_i$, and referred to as the return. The discount factor $\gamma \in [0,1]$ applies to successive rewards at each time step to help enumerate returns over a potentially infinite horizon. Thereafter, learning may conclude having achieved adequate performance or resume from some initial state following an environment reset.

Two principle challenges of RL are those of prediction and control. The first refers to approximating the value function used to estimate state values v(s) or state-action values q(s,a), describing the benefit of being in that state. Values are differentiable and updated based on an empirical average, known as the expectation, taken over observed returns, $\mathbb{E}[G_t|S_t=s,A_t=a]$. Observed returns depend on the action(s) sampled at discrete time steps. The second challenge of control concerns optimising this selection process via the policy $\pi(a|s)$; a probability distribution mapping states to actions most likely to maximise the reward objective. Ultimately an optimal value function will converge to an optimal policy []. In practice to scale with complex environments these functions are parametric and approximated with gradient-based methods, such as stochastic gradient ascent.

Determining the reachable state space for LLPs is often intractable, making the complete MDP model unknown to us without computing all transitions. Consequently we trial several gradient-based learning methods. Policy gradient methods [] utilise parameterised policies which update with respect to their parameter vector and objective function []. Actor-critic methods also approximate a parametric value function, separating the learning of action selection from value estimates. In this work we explore the efficacy of basic Deep Q-Networks [11], Proximal Policy Optimisation (PPO) [12], Advantage Actor-Critic (A2C) and its asynchronous counterpart (A3C) [8] in navigating our set of generated LLPs.

3. Mapping Formal Methods to Reinforcement Learning

Explain why the LTS in James et al. [17] uses four elements, but we ignore ...

3.1. Ladder Logic Markov Decision Process

We now define the finite Markov Decision Process (MDP), or environment $\mathcal E$ used to represent the LLP. A Ladder Logic MDP $M(\psi)$ is a five tuple, where $S=V_I\cup V_C$, observation space to represent the MDP state at discrete time steps. $\mathcal A=V_I$, describes the action space; a set of formally defined actions which change the observation space. $P_a(s,s')=Pr(s_{t+1}=s'|s_t,a_t)$, describing the likelihood of observing state s_{t+1} given action a_t taken from state s_t . $R_a(s,s')$ is a reward function fed back to the agent

at each time step γ is a discount scalar applied to the reward estimates for future time steps.

Explain relation between transition probabilities and state transitions

Subsequently the environment unfolds as a set of reachable states for the respective LLP. As workers improve their value estimates according to the reward function, a balance is maintained between stochastic action sampling for exploration and predicted actions from the policy network.

Aiming to maximise state space coverage we implement a reward scheme which positively rewards novel observations and dissuade loops with negative reward and episode termination. Training episodes spawn agents at some initial state, either with all variables set to 0 or from some randomly sampled state from a set of previous observations. Workers are initialised with separate environment instances to accumulate experience independently. A global set of observations is asynchronously updated by workers periodically to compile shared experiences. Early stopping terminates training if a set number of consecutive model updates do not improvement in terms of coverage or reward. Second, training ends in our artificially generated programs if all reachable states have been observed at least once. To aid exploration, on episode resets we randomly initialise workers in some previously visited state, as demonstrated in [23].

4. Related Work

Here we briefly highlight key contributions within related literature, addressing the invariant finding problem for interlocking programs and contemporary RL strategies for environment exploration.

4.1. Invariant Finding

Overview of IC3, other invariant finding techniques for interlockings

From software engineering techniques [24], [25] to hybrid methods incorporating machine learning [26], researchers have proposed various approaches to invariant finding with varying degrees of success.

4.2. Exploration in Reinforcement Learning

Game testing, applied algorithms to 3D environment, postition and player movement used as observations with aim of state coverage for bug finding. FPS paper [27] applies vanilla PPO with no reset logic to identify game exploits. HMI paper [28] apply curiosity function based on an empirical count of state-action pairs to maximise traversal of state transitions over a deterministiv finite state automaton navigation model. Uses vanilla Q-learning with e-greedy exploration. Similar use in web testing [29] simulate user actions to navigate web application, tracking 'uncertain' state transitions for backtracking. Also use vanilla

Q-learning and count-based reward scaling during for Q-function updates. [30] decompose exploration tasks over large, adaptive and partially observable environments into two sub-problems - adaptive exploration policy for region selection and separate policy for exploitation of an area of interest. Others [31] incorporate recurrent networks in policy design, using temporality to recall the performance of past actions and their subsequent consequences according to the reward function. ACER algorithm used to make the A3C algorithm off-policy and constrain updates with TRPO like parameter updates. [32] apply a range of state-of-the-art learning algorithms to help robot navigation in procedurally generated environments. PPO found to have near human-driver level performance, recalling which states are 'expensive' to reach, minimising the frequency of rediscovery.

Existing works have illustrated the efficacy of RL methods in learning such heuristics over large graph structures [33], distributing learning for accelerated performance [34] and prioritising novelty when exploration unfamiliar environments [23], [35], [36].

Reinforcement learning for state exploration

5. Results

We now present a set of results from applying our approach to a series of generated LLPs, modelled as learning environments.

5.1. Environment Generation

Given exhaustive search of large state spaces is often computationally intractable, we have generated a set of LLPs where the number of reachable states and recurrence reachability diameter are known. This has enabled us to analyse the performance of our approach against well understood state spaces. Using existing models of ladder logic structures as a base template [7], we derive progressively larger programs by sequentially introducing additional rungs. This way a constrained yet predictable pattern of growth is devised. If $|S(p_i)|$ represents the number of reachable states for a program p_i , a subsequently generated program p_{i+1} with one additional rung, has $2|S(p_i)|+1$ reachable states. Through a series of training runs on each environment we record the number of states observed by workers to gauge the overall state space coverage.

Introduce DQN, A2C and PPO

Tried DQN on smaller environments to test the viability of RL in our problem formulation and it solved them (with respect to our reward objective) within an acceptable time frame. DQN doesn't scale well and is too sensitive to hyperparameter tuning. buffer size environment dependent, training delay and gradient step size contingent on complexity of learnable function, which we'd expect to increase with environment size. Algorithm is also off-policy - trains from experiences generated by old (presumably less optimal) policies. Exploration is goverend explicitly by the epsilongreedy strategy and guaranteed to anneal toward a minimum

threshold over a significant number timesteps - this could happen with large regions of an environment unobserved. Methods exist to improve the sample efficiency and learning stability, such as Prioritised experience replay or dueling DQN.

We also try two Actor critic methods, Advantage actorcritic (A2C) and its asynchronous counterpart (A3C) to improve sample efficiency in distributing environment interaction among several workers. Having several workers and an on-policy learning algorithm removes need of replay memory and training delay to accumulate sufficient experience. Actor and critic networks, approximating the behaviour policy and value function, providee better convergence guarantees at the cost of some additional complexity. Paired with randomised reset logic both algorithms accumulate experience faster than Vanilla DQN, achieving good coverage on a range of medium to large state spaces. They are susceptible to parameter updates pushing the model into an unfamiliar region of policy space from which subsequent updates are unable to recover, potentially triggering model collapse.

We then move to trust region methods which constrain the magnitude of gradient updates within some clip range or according to KL-divergence between the current and most recent policy parameters, making the model more resilient to collapse.

5.2. Discussion

Elaborate on the efficacy of approach - is it actually promising?

Add results on some Loch Ness interlocking examples

Preliminary results applying our approach to a number of generated programs are outlined in [ref results]. 'Actions' referenced in column 3 refer to the number of possible assignments over input variables in each LLP. 'K', refers to the greatest number of steps taken before repeating observations n the environment, across all workers.

Coverage metrics are expectedly maximised for environments with a small number of reachable states with acceptable levels of coverage for programs with more than 1e5 states. Interestingly, we observed longer training durations occasionally increased coverage beyond a certain threshold. It is possible workers learn an optimal search strategy within a subregion of the state space. Additionally, performance in terms of max k and states reached increased by approx. 5% when decreasing the total number of episodes from 3e5 to 1.5e5 episodes.

Fix scientific notation

This may be a product of random episode initialisation spawning workers in more desirable states where stochastic action sampling happened to lead to unfamiliar subregions of the environment.

Performance plots illustrating the cumulative reward which failed to maximise coverage often increased linearly before collapsing to some suboptimal reward.

Include performance plots

This may be due to tendencies for large network updates to shift the network gradients into a bad local minima, from which performance does not recover within the allotted training duration. The on-policy nature of actor critic means trajectories generated via an old policy are no longer sampled during minibatch updates for the current policy, thus biasing behaviour to the most recent model updates and introducing sample inefficiency. Adding experience replay [37] may help avoid this in future applications

Given the A3C algorithm requires workers to asynchronously update their shared network every $T_{\rm max}$ steps or on episode termination, larger values for $T_{\rm max}$ consolidate more information regarding worker trajectories before applying gradient updates to their local network. We found the most significant improvements to performance in terms of coverage metrics and increasing the k bound when introducing workers to larger environments, was lower update frequencies and random start state initialisation. Prior to these adjustments workers, irrespective of their number, seldom covered 80% of most smaller environments. Similarly, for the largest environment with 2^{50} states, coverage improved from 3.2% to 41.48%

6. Conclusion & Future Work

In this paper we have applied a basic asynchronous deep reinforcement learning method to maximise program state coverage, motivated by a reward scheme

Sentence?

. some promising preliminary results but limited in its capacity to scale across large observation spaces.

In light of our findings, we aim to improve several aspects of our approach, predominantly concerning learning stability, sample efficiency and training speed. Experience replay for distributed learning may improve on-policy bias and sample efficiency.

The low dimensionality of our state spaces representation may allow us to introduce count-based exploration models to dampen the reward issued for states repeatedly observed [35]. Intrinsic motivation has also illustrated successes in environment exploration [38].

Applying IMPALA [39] to improve both sample efficiency over A3C and robustness to network architectures and hyperparameter adjustments. The adoption of a Long Short-Term Memory model (LSTM) also improves performance given GPU acceleration is maximised on larger batch updates.

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References

- [1] J. F. Groote, S. F. van Vlijmen, and J. W. Koorn, "The safety guaranteeing system at station hoorn-kersenboogerd," in *COMPASS'95 Proceedings of the Tenth Annual Conference on Computer Assurance Systems Integrity, Software Safety and Process Security'*. IEEE, 1995, pp. 57–68.
- [2] A. Fantechi, W. Fokkink, and A. Morzenti, "Some trends in formal methods applications to railway signaling," Formal methods for industrial critical systems: A survey of applications, pp. 61–84, 2012.
- [3] A. Ferrari, G. Magnani, D. Grasso, and A. Fantechi, "Model checking interlocking control tables," in *FORMS/FORMAT 2010*. Springer, 2011, pp. 107–115.
- [4] A. E. Haxthausen, M. L. Bliguet, and A. A. Kjær, "Modelling and verification of relay interlocking systems," in *Monterey Workshop*. Springer, 2008, pp. 141–153.
- [5] M. Awedh and F. Somenzi, "Automatic invariant strengthening to prove properties in bounded model checking," in 2006 43rd ACM/IEEE Design Automation Conference, 2006, pp. 1073–1076.
- [6] K. Kanso, F. Moller, and A. Setzer, "Automated verification of signalling principles in railway interlocking systems," *Electronic Notes* in *Theoretical Computer Science*, vol. 250, no. 2, pp. 19–31, 2009.
- [7] P. James, A. Lawrence, F. Moller, M. Roggenbach, M. Seisenberger, A. Setzer, K. Kanso, and S. Chadwick, "Verification of solid state interlocking programs," in *International Conference on Software En*gineering and Formal Methods. Springer, 2013, pp. 253–268.
- [8] V. Mnih, A. P. Badia, M. Mirza, A. Graves, T. P. Lillicrap, T. Harley, D. Silver, and K. Kavukcuoglu, "Asynchronous methods for deep reinforcement learning," 2016.
- [9] R. S. Sutton and A. G. Barto, Reinforcement learning: An introduction. MIT press, 2018.
- [10] M. Geist and O. Pietquin, "Algorithmic survey of parametric value function approximation," *IEEE Transactions on Neural Networks and Learning Systems*, vol. 24, no. 6, pp. 845–867, 2013.
- [11] V. Mnih, K. Kavukcuoglu, D. Silver, A. Graves, I. Antonoglou, D. Wierstra, and M. Riedmiller, "Playing atari with deep reinforcement learning," arXiv preprint arXiv:1312.5602, 2013.
- [12] J. Schulman, F. Wolski, P. Dhariwal, A. Radford, and O. Klimov, "Proximal policy optimization algorithms," 2017.
- [13] T. Schaul, J. Quan, I. Antonoglou, and D. Silver, "Prioritized experience replay," arXiv preprint arXiv:1511.05952, 2015.
- [14] D. Silver, A. Huang, C. J. Maddison, A. Guez, L. Sifre, G. Van Den Driessche, J. Schrittwieser, I. Antonoglou, V. Panneershelvam, M. Lanctot *et al.*, "Mastering the game of go with deep neural networks and tree search," *nature*, vol. 529, no. 7587, pp. 484–489, 2016
- [15] O. Vinyals, I. Babuschkin, W. M. Czarnecki, M. Mathieu, A. Dudzik, J. Chung, D. H. Choi, R. Powell, T. Ewalds, P. Georgiev *et al.*, "Grandmaster level in starcraft ii using multi-agent reinforcement learning," *Nature*, vol. 575, no. 7782, pp. 350–354, 2019.
- [16] S. Gu, E. Holly, T. Lillicrap, and S. Levine, "Deep reinforcement learning for robotic manipulation with asynchronous off-policy updates," in 2017 IEEE international conference on robotics and automation (ICRA). IEEE, 2017, pp. 3389–3396.
- [17] M. Bloesch, J. Humplik, V. Patraucean, R. Hafner, T. Haarnoja, A. Byravan, N. Y. Siegel, S. Tunyasuvunakool, F. Casarini, N. Batchelor *et al.*, "Towards real robot learning in the wild: A case study in bipedal locomotion," in *Conference on Robot Learning*. PMLR, 2022, pp. 1502–1511.
- [18] N. Mazyavkina, S. Sviridov, S. Ivanov, and E. Burnaev, "Reinforcement learning for combinatorial optimization: A survey," *Computers & Operations Research*, vol. 134, p. 105400, 2021.

- [19] C. J. Watkins and P. Dayan, "Q-learning," *Machine learning*, vol. 8, no. 3, pp. 279–292, 1992.
- [20] Y. LeCun, Y. Bengio, and G. Hinton, "Deep learning," nature, vol. 521, no. 7553, pp. 436–444, 2015.
- [21] S. M. Kakade, "A natural policy gradient," Advances in neural information processing systems, vol. 14, 2001.
- [22] J. Schulman, S. Levine, P. Moritz, M. I. Jordan, and P. Abbeel, "Trust region policy optimization," 2017.
- [23] C. Gordillo, J. Bergdahl, K. Tollmar, and L. Gisslén, "Improving playtesting coverage via curiosity driven reinforcement learning agents," arXiv preprint arXiv:2103.13798, 2021.
- [24] M. L. Case, A. Mishchenko, and R. K. Brayton, "Automated extraction of inductive invariants to aid model checking," in *Formal Methods in Computer Aided Design (FMCAD'07)*. IEEE, 2007, pp. 165–172.
- [25] S. Bensalem, Y. Lakhnech, and H. Saidi, "Powerful techniques for the automatic generation of invariants," in *International Conference* on Computer Aided Verification. Springer, 1996, pp. 323–335.
- [26] P. Garg, D. Neider, P. Madhusudan, and D. Roth, "Learning invariants using decision trees and implication counterexamples," ACM Sigplan Notices, vol. 51, no. 1, pp. 499–512, 2016.
- [27] J. Bergdahl, C. Gordillo, K. Tollmar, and L. Gisslén, "Augmenting automated game testing with deep reinforcement learning," in 2020 IEEE Conference on Games (CoG), 2020, pp. 600–603.
- [28] Y. Cao, Y. Zheng, S.-W. Lin, Y. Liu, Y. S. Teo, Y. Toh, and V. V. Adiga, "Automatic hmi structure exploration via curiositybased reinforcement learning," in 2021 36th IEEE/ACM International Conference on Automated Software Engineering (ASE), 2021, pp. 1151–1155.
- [29] Y. Zheng, Y. Liu, X. Xie, Y. Liu, L. Ma, J. Hao, and Y. Liu, "Automatic web testing using curiosity-driven reinforcement learning," in 2021 IEEE/ACM 43rd International Conference on Software Engineering (ICSE), 2021, pp. 423–435.
- [30] A. Peake, J. McCalmon, Y. Zhang, D. Myers, S. Alqahtani, and P. Pauca, "Deep reinforcement learning for adaptive exploration of unknown environments," in 2021 International Conference on Unmanned Aircraft Systems (ICUAS), 2021, pp. 265–274.
- [31] K. G. S. Apuroop, A. V. Le, M. R. Elara, and B. J. Sheu, "Reinforcement learning-based complete area coverage path planning for a modified htrihex robot," *Sensors*, vol. 21, no. 4, 2021. [Online]. Available: https://www.mdpi.com/1424-8220/21/4/1067
- [32] D. I. Koutras, A. C. Kapoutsis, A. A. Amanatiadis, and E. B. Kosmatopoulos, "Marsexplorer: Exploration of unknown terrains via deep reinforcement learning and procedurally generated environments," *Electronics*, vol. 10, no. 22, 2021. [Online]. Available: https://www.mdpi.com/2079-9292/10/22/2751
- [33] S. Manchanda, A. Mittal, A. Dhawan, S. Medya, S. Ranu, and A. Singh, "Learning heuristics over large graphs via deep reinforcement learning," arXiv preprint arXiv:1903.03332, 2019.
- [34] M. Hoffman, B. Shahriari, J. Aslanides, G. Barth-Maron, F. Behbahani, T. Norman, A. Abdolmaleki, A. Cassirer, F. Yang, K. Baumli et al., "Acme: A research framework for distributed reinforcement learning," arXiv preprint arXiv:2006.00979, 2020.
- [35] G. Ostrovski, M. G. Bellemare, A. van den Oord, and R. Munos, "Count-based exploration with neural density models," 2017.
- [36] T. Haarnoja, A. Zhou, P. Abbeel, and S. Levine, "Soft actor-critic: Off-policy maximum entropy deep reinforcement learning with a stochastic actor," 2018.
- [37] Z. Wang, V. Bapst, N. Heess, V. Mnih, R. Munos, K. Kavukcuoglu, and N. de Freitas, "Sample efficient actor-critic with experience replay," 2017.
- [38] R. Houthooft, X. Chen, Y. Duan, J. Schulman, F. D. Turck, and P. Abbeel, "Vime: Variational information maximizing exploration," 2017.

[39] L. Espeholt, H. Soyer, R. Munos, K. Simonyan, V. Mnih, T. Ward, Y. Doron, V. Firoiu, T. Harley, I. Dunning, S. Legg, and K. Kavukcuoglu, "Impala: Scalable distributed deep-rl with importance weighted actor-learner architectures," 2018.