



The number of flops in my algorithm is $2n^3 + n^2$ for each term. $(n^2)(2n-1)$ multiplications and additions to multiply the last term by A, n^2 divisions to divide by k, and n^2 additions to add the new term to the previous sum of terms. For $n=1000$, 2,001,000,000 flops per term are computed. Dividing the time to compute each exp(A) by their respective k terms, then taking the mean, the time to compute exp(A) is approximated at $k \cdot 0.5910$ seconds (at $3.3855e+09$ flops/second).

Round off error accumulates with the huge number of flops in multiplying 1000x1000 Matrices. It also occurs when dividing by a large factorial, causing an element to become less than machine epsilon.

Using the slope at the steepest linear piece of the relative error in 2-norm plot, $k=60$ to $k=80$, gives $\log_{10}(\epsilon) = -0.3198k + 25.06$. The error bound is $\max(\epsilon \leq 10^{(25.06)} \cdot (10^{(-0.3198)})^k, \epsilon = 10^{-3.645})$.