```
In [255...
          using JuMP, Gurobi, LinearAlgebra, CSV, DataFrames, Pkg, Distances, Plots
In [262...
          centers = CSV.read("centers.csv", DataFrame, header=false);
          centers2 = CSV.read("centers2.csv", DataFrame, header=false);
          landfills = CSV.read("landfills.csv", DataFrame, header=false);
          landfills2 = CSV.read("landfills2.csv", DataFrame, header=false);
          q = CSV.read("q.csv", DataFrame, header=false);
          q2 = CSV.read("q2.csv", DataFrame, header=false);
          stations = CSV.read("stations.csv", DataFrame, header=false);
          stations2 = CSV.read("stations2.csv", DataFrame, header=false);
In [263...
          first(centers, 5);
In [264...
          first(landfills, 5);
In [265...
          rename!(centers,:Column1 => "xco");
          rename!(centers,:Column2 => "yco");
          rename!(landfills,:Column1 => "xco");
          rename!(landfills,:Column2 => "yco");
          rename!(q,:Column1 => "waste" );
          rename!(stations,:Column1 => "xco");
          rename!(stations,:Column2 => "yco");
In [266...
          dmatx = pairwise(Euclidean(), centers.xco, landfills.xco);
          dmaty = pairwise(Euclidean(), centers.yco, landfills.yco);
          dmat = sqrt.((dmatx.^2)+(dmaty.^2));
```

A.a

The objective function is simply minimizing the overall distance that all waste is moved. In effect, it attempts to make the waste be disposed in the most efficient

manner. This assumes that all waste transportation is equal and linear. In essence, there is no cost saving for moving waste in bulk.

Constraint 2 ensures that all the waste at centers is transported to a landfill.

Using the big-M method, contraint 3 ensures that waste is only transported to those landfills which are built.

Constraint 4 makes it so that only 5 landfills are built.

Constraint 5 makes it so that waste is a positive value. This assumes waste can only flow in one direction from a center to a landfill.

Constraint 6 makes it so that landfills are either fully built or not. This assumes that all landfills are the same size and serve the same functionality.

A.b

```
In [267...
    mod = JuMP.Model(JuMP.optimizer_with_attributes(() -> Gurobi.Optimizer(), "MIPGap" => 0.0001))
    set_optimizer_attribute(mod, "OutputFlag", 0)

    @variable(mod, z[j=1:15], Bin)
    @variable(mod, x[i=1:50, j=1:15]>=0)

@constraint(mod, [i=1:50], sum(x[i,j] for j=1:15)== q[i,1])
@constraint(mod, [i=1:50, j=1:15], x[i,j] <= 10000000*z[j])
@constraint(mod, sum(z[j] for j=1:15)<=5)

@objective(mod, Min, sum(sum(dmat[i,j]*x[i,j] for j=1:15) for i=1:50))

optimize!(mod)</pre>
```

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The total distance traveled by the waste is 840,487.52

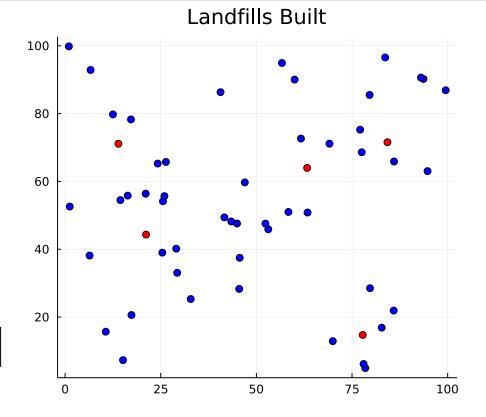
```
In [268...
           objective_value(mod)
Out[268... 840487.5240012797
In [269...
           x = value.(x);
In [270...
           z1=value.(z)
Out[270... 15-element Vector{Float64}:
           -0.0
            0.0
            1.0
            1.0
           -0.0
           -0.0
            1.0
           -0.0
           -0.0
           -0.0
            0.0
            0.0
            1.0
            1.0
           -0.0
In [271...
           built_ind = [3,4,7,13,14];
```

Landfills are built at the following coordinates:

| | XCO | ycc |
|---|---------|---------|
| | Float64 | Float64 |
| 1 | 21.163 | 44.33′ |
| 2 | 63.265 | 63.989 |
| 3 | 77.801 | 14.727 |
| 4 | 84.261 | 71.562 |
| 5 | 13.93 | 71.108 |
| | | |

```
plot(lf_b.xco, lf_b.yco, seriestype = :scatter, color = "red", title = "Landfills Built", label = "Landfills", l plot!(centers.xco, centers.yco, seriestype = :scatter, color = "blue", label = "Centers")
```

Out[273...



B

Landfills Centers

```
In [274...
    dmatx_ct = pairwise(Euclidean(), centers.xco, stations.xco);
    dmaty_ct = pairwise(Euclidean(), centers.yco, stations.yco);
    dmat_ct = sqrt.((dmatx_ct.^2)+(dmaty_ct.^2));

In [275...
    dmatx_tl = pairwise(Euclidean(), stations.xco, landfills.xco);
    dmaty_tl = pairwise(Euclidean(), stations.yco, landfills.yco);
    dmat_tl = sqrt.((dmatx_tl.^2)+(dmaty_tl.^2));
```

B.c

Formulation

Sets

```
i=1,\dots,50 centers s=1,\dots,50 potential transfer stations j=1,\dots,15 potential landfills
```

Parameters

```
q_i amount of waste generated at center i d_{ij} \ (\mbox{Euclidean}) \ distance \ \mbox{between center} \ i \ \mbox{and potential landfill} \ j d_{is} \ (\mbox{Euclidean}) \ distance \ \mbox{between center} \ i \ \mbox{and transfer station} \ s d_{sj} \ (\mbox{Euclidean}) \ \mbox{distance} \ \mbox{between transfer station} \ s \ \mbox{and landfill} \ j
```

Variables

 $z_j = 1$ if landfill j is built

 $t_s=1$ if transfer station s is built

 x_{ij} amount of waste transported from center i to landfill j

 a_{is} amount of waste transported from center i to transfer center s

 b_{sj} amount of compacted waste transported from transfer center s to landfill j

$$egin{aligned} min_{z,x,ta,b} & \sum_{i=1}^{50} \sum_{j=1}^{15} d_{ij} x_{ij} + \sum_{i=1}^{50} \sum_{s=1}^{50} d_{is} a_{is} + \sum_{s=1}^{50} \sum_{j=1}^{15} d_{sj} b_{sj} + 1000 \sum_{s=1}^{50} t_s \ x_{ij} & \leq 10000000 * z_j \quad orall i,j \ \sum_{j=1}^{15} z_j & \leq 5 \ \sum_{j=1}^{15} x_{ij} + \sum_{s=1}^{50} a_{is} & = q_i \quad orall i \ \sum_{j=1}^{50} a_{is} & = \sum_{j=1}^{15} b_{sj} \quad orall i,s,j \end{aligned}$$

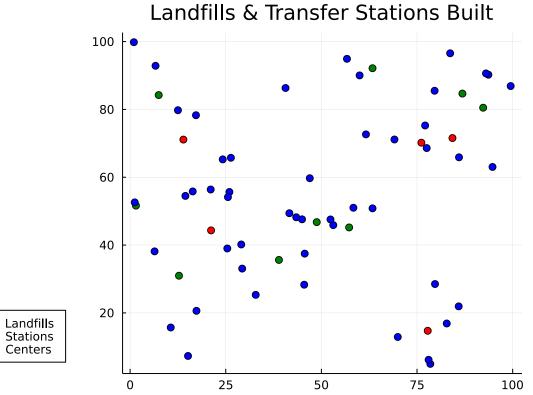
 $b_{sj} \leq 1000000 * z_j \quad \forall s, j$

$$local host: 8888/nbconvert/html/Desktop/One Drive-Massachusetts\ Institute\ of\ Technology/AE/HWs/Pset3/PSet_3_code-Copy1.ipynb?download=false-false$$

$$egin{aligned} \sum_{i=1}^{50} a_{is} & \leq 2000 t_s \quad orall i, s \ & x_{ij}, a_{is}, b_{sj} \leq 0 \ & z_j, t_s \in \{0, 1\} \end{aligned}$$

```
In [276...
                         mod2 = JuMP.Model(JuMP.optimizer with attributes(() -> Gurobi.Optimizer(), "MIPGap" => 0.0001))
                         set optimizer attribute(mod2, "OutputFlag", 0)
                         #OLD VARIABLES
                         #if landfill j is built
                          @variable(mod2, z[j=1:15], Bin)
                          #amount of waste transported from center i to landfill j
                          @variable(mod2, x[i=1:50,j=1:15]>=0)
                         #NEW VARIABLES
                         #if transfer station s is built
                          @variable(mod2, t[s=1:50], Bin)
                          #amount of waste transported from center i to trasnfer station s
                          @variable(mod2, a[i=1:50,s=1:50]>=0)
                          #amount of waste transported from center i to trasnfer station s
                          @variable(mod2, b[s=1:50, j=1:15] >= 0)
                         #OLD CONSTRAINTS
                          #@constraint(mod2, [i=1:50], sum(x[i,j] for j=1:15) == q[i,1]) modified for reformulation
                          @constraint(mod2, [i=1:50, j=1:15], x[i,j] \le 1000000*z[j])
                          @constraint(mod2, sum(z[j] for j=1:15) \le 5)
                          #NEW CONSTRAINTS
                          #ensure that all waste is taken care of
                          (constraint(mod2, [i=1:50], sum(x[i,j] for j=1:15) + sum(a[i,s] for s=1:50) == q[i,1])
                         #conservation of flow for transfer stations
                          \{(s, t), (s, t), (s,
                          #transfer station t cannot serve landfill j unless landfill j is built
                          \{constraint(mod2, [s=1:50, j=1:15], b[s,j] \le 1000000*z[j]\}
                          (constraint(mod2, [i=1:50, s=1:50], sum(a[i,s] for i=1:50) <= 2000 *t[s])
```

```
\texttt{@objective}(\texttt{mod2}, \texttt{Min}, \texttt{sum}(\texttt{dmat}[\texttt{i},\texttt{j}] * \texttt{x}[\texttt{i},\texttt{j}] \texttt{ for } \texttt{i} = 1:50, \texttt{j} = 1:15)
                                    sum(dmat_ct[i,s]*a[i,s] for i = 1:50, s = 1:50)
                                    sum(dmat_tl[s,j]*b[s,j] for s = 1:50, j = 1:15)/2
                                    sum(10000*t[s] for s=1:50))
           optimize!(mod2)
           Academic license - for non-commercial use only - expires 2022-08-19
In [277...
           objective value(mod2)
Out[277... 808642.7541913458
In [279...
            z = value.(z);
In [280...
           t = value.(t);
In [281...
           built 1 ind2 = [2,3,7,13,14]
           lf b2 = landfills[built 1 ind2,:];
In [282...
           built t ind2 = findall(>(.5), t)
            ts b2 = stations[built t ind2,:];
In [283...
           plot(lf b2.xco, lf b2.yco, seriestype = :scatter, color = "red", title = "Landfills & Transfer Stations Built",
           plot!(ts b2.xco, ts b2.yco, seriestype = :scatter, color = "green", label = "Stations")
           plot!(centers.yco, centers.yco, seriestype = :scatter, color = "blue", label = "Centers")
Out[283...
```



B.d

9 transfer stations were created.

```
In [284... round(sum(t))
Out[284... 9.0
```

35.12% of waste in compacted.

```
In [285... x = value.(x);
```

```
11/21/21,5:11 PM
    In [286... sum(x)

Out[286... 31665.669999999587

In [287... a = value.(a);

In [288... sum(a)

Out[288... 17137.500000000487

In [289... dist1 = sum(dmat*z1)
```

```
In the first scenario, the total distance traveled was 11,946.95. In
the second scenario the total distance significantly increased to
41,153.68
```

```
In [245... print(dist1, " ")
print(dist2)

11946.954019037625 41153.67660407018
```

The transportation costs of the first scenario is 840,487.52 and the second scenario is 718,642.75

```
In [246... print(objective_value(mod), " ") print(objective_value(mod2)-sum(10000*t))

840487.5240012797 718642.7541913444
```

The total costs of the first scenario is 840,487.52 and with the

dist2 = sum(dmat*z)+sum(dmat ct*t)+sum(t'*dmat tl);

transfer stations in the second scenario is 808,642.75.

```
In [247...
          print(objective value(mod), " ")
          print(objective value(mod2))
         840487.5240012797 808642.7541913458
In [290...
          rename!(centers2,:Column1 => "xco");
          rename!(centers2,:Column2 => "yco");
          rename!(landfills2,:Column1 => "xco");
          rename!(landfills2,:Column2 => "yco");
          rename!(stations2,:Column1 => "xco");
          rename!(stations2,:Column2 => "yco");
          rename!(q2,:Column1 => "waste");
In [291...
          dmatx = pairwise(Euclidean(), centers2.xco, landfills2.xco);
          dmaty = pairwise(Euclidean(), centers2.yco, landfills2.yco);
          dmat = sqrt.((dmatx.^2)+(dmaty.^2));
```

C.e

```
mod3 = JuMP.Model(JuMP.optimizer_with_attributes(() -> Gurobi.Optimizer(),"MIPGap" => 0.0001))

set_optimizer_attribute(mod2, "OutputFlag", 0)

#OLD VARIABLES
#if landfill j is built
@variable(mod3, z[j=1:15], Bin)
#amount of waste transported from center i to landfill j
@variable(mod3, x[i=1:40,j=1:15]>=0)

#NEW VARIABLES
#if transfer station s is built
@variable(mod3, t[s=1:50], Bin)
#amount of waste transported from center i to transfer station s
@variable(mod3, a[i=1:40,s=1:50]>=0)
#amount of waste transported from center i to transfer station s
@variable(mod3, b[s=1:50,j=1:15]>=0)
```

```
#OLD CONSTRAINTS
 \#\emptysetconstraint(mod3, [i=1:40], sum(x[i,j] for j=1:15)== q[i,1]) modified for reformulation
  \{\text{constraint}(\text{mod3}, [i=1:40, j=1:15], x[i,j] \le 1000000*z[j]\}
  @constraint(mod3, sum(z[j] for j=1:15) \le 5)
 #NEW CONSTRAINTS
 #ensure that all waste is taken care of
  (x_{i,j}) = (x_{i,j}) + (x_{
 #conservation of flow for transfer stations
  (constraint(mod3, [i=1:40, s=1:50, j=1:15], sum(a[i,s] for i=1:40) == sum(b[s,j] for j=1:15))
  #transfer station t cannot serve landfill j unless landfill j is built
  (\text{constraint}(\text{mod3}, [s=1:50, j=1:15], b[s,j] \leq 1000000*z[j])
  \{\text{constraint}(\text{mod3}, [i=1:40, s=1:50], \text{sum}(a[i,s] \text{ for } i=1:40) \le 2000 \times t[s]\}
  \texttt{@objective}(\texttt{mod3}, \texttt{Min}, \texttt{sum}(\texttt{dmat}[\texttt{i},\texttt{j}] * \texttt{x}[\texttt{i},\texttt{j}] \texttt{ for } \texttt{i} = 1:40, \texttt{j} = 1:15)
                                               sum(dmat ct[i,s]*a[i,s] for i = 1:40, s = 1:50)
                                               sum(dmat tl[s,j]*b[s,j] for s = 1:50, j = 1:15)/2
                                               sum(10000*t[s] for s=1:50))
 optimize!(mod3)
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Gurobi Optimizer version 9.1.2 build v9.1.2rc0 (mac64)
Thread count: 8 physical cores, 8 logical processors, using up to 8 threads
Optimize a model with 33391 rows, 3415 columns and 1737315 nonzeros
Model fingerprint: 0x0e70716b
Variable types: 3350 continuous, 65 integer (65 binary)
Coefficient statistics:
    Matrix range
                                        [1e+00, 1e+06]
    Objective range [1e-01, 1e+04]
    Bounds range
                                        [0e+00, 0e+00]
    RHS range
                                        [5e+00, 3e+03]
Presolve removed 31900 rows and 0 columns
Presolve time: 0.82s
Presolved: 1491 rows, 3415 columns, 10115 nonzeros
Variable types: 3350 continuous, 65 integer (65 binary)
Root relaxation: objective 9.744086e+05, 243 iterations, 0.01 seconds
        Nodes
                                       Current Node
                                                                                       Objective Bounds
                                                                                                                                                    Work
  Expl Unexpl
                                  Obj Depth IntInf | Incumbent
                                                                                                          BestBd
                                                                                                                              Gap | It/Node Time
                       0 974408.621
          0
                                                           0 25
                                                                                             - 974408.621
                                                                                                                                                             0s
Η
                        0
                                                                     1454438.7026 974408.621 33.0%
                                                                                                                                                             0s
Η
          0
                        0
                                                                     1127090.2538 974408.621 13.5%
                                                                                                                                                            0s
```

```
0 1023606.60
                              35 1127090.25 1023606.60
                                                        9.18%
                                                                      1s
                               1096781.9600 1023606.60
                                                        6.67%
                                                                      1s
Η
          0 1024986.37
                            35 1096781.96 1024986.37 6.55%
                                                                      1s
          0 1039198.76
                              36 1096781.96 1039198.76 5.25%
                                                                      1s
                              37 1096781.96 1040138.98 5.16%
          0 1040138.98
                                                                      1s
                               1096628.8849 1040138.98 5.15%
                                                                      1s
Η
                               1085833.6282 1040138.98 4.21%
                                                                      1s
                               1077900.7407 1040138.98 3.50%
                                                                      1s
    0
                               1076788.4380 1040138.98 3.40%
                                                                      1s
          0 1050914.20
                          0 41 1076788.44 1050914.20 2.40%
                                                                      1s
          0 1051161.47
                          0 40 1076788.44 1051161.47 2.38%
                                                                      1s
          0 1051175.88
                          0 41 1076788.44 1051175.88 2.38%
                                                                      1s
          0 1058913.66
                          0 31 1076788.44 1058913.66 1.66%
                                                                      1s
                          0 29 1076788.44 1061498.21 1.42%
                                                                      1s
          0 1061498.21
          0 1061498.21
                          0 30 1076788.44 1061498.21 1.42%
                                                                      1s
Cutting planes:
 Gomory: 1
 Implied bound: 32
 MTR: 35
 Flow cover: 39
Explored 1 nodes (634 simplex iterations) in 1.23 seconds
Thread count was 8 (of 8 available processors)
Solution count 6: 1.07679e+06 1.08583e+06 1.09663e+06 ... 1.45444e+06
Optimal solution found (tolerance 1.00e-04)
Best objective 1.076788438001e+06, best bound 1.076788438001e+06, gap 0.0000%
```

The daily total cost of region B is \$1,076,788.44.

```
In [293... objective_value(mod3)
Out[293... 1.0767884380013323e6

In [294... t = value.(t);
    z = value.(z);
    i_t = findall(>(.5), t)
    i_z = findall(>(.5), z)
    ts_b3 = stations2[i_t,:];
    lf_b3 = landfills2[i_z,:];
```

User-callback calls 242, time in user-callback 0.00 sec

Transfer Stations are built at the following coordinates:

In [296... ts_b3

Out[296... 8 rows × 2 columns

| | хсо | усо |
|---|---------|---------|
| | Float64 | Float64 |
| 1 | 175.68 | 65.393 |
| 2 | 133.12 | 78.404 |
| 3 | 162.59 | 70.408 |
| 4 | 172.01 | 96.693 |
| 5 | 158.35 | 8.6711 |
| 6 | 187.25 | 64.139 |
| 7 | 127.51 | 43.675 |
| 8 | 116.65 | 48.425 |

Landfills are built at the following coordinates:

In [297... lf_b3

Out[297... 5 rows × 2 columns

| | хсо | усо |
|---|---------|---------|
| | Float64 | Float64 |
| 1 | 170.73 | 89.923 |
| 2 | 107.54 | 70.32 |
| 3 | 130.56 | 30.882 |
| 4 | 135.89 | 90.798 |

 xco
 yco

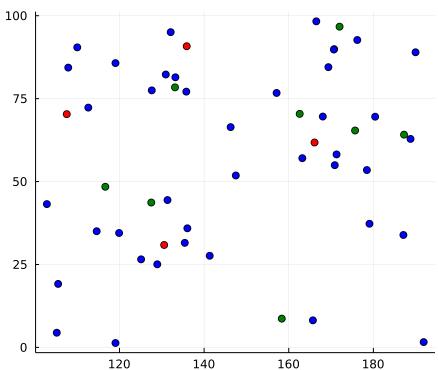
 Float64
 Float64

 5
 166.1
 61.775

```
plot(lf_b3.xco, lf_b3.yco, seriestype = :scatter, color = "red", title = "Landfills & Transfer Stations Built", plot!(ts_b3.xco, ts_b3.yco, seriestype = :scatter, color = "green", label = "Stations") plot!(centers2.xco, centers2.yco, seriestype = :scatter, color = "blue", label = "Centers")
```

Out[295...

Landfills & Transfer Stations Built



C.f

Landfills Stations Centers

```
append!(stations, stations2);
append!(landfills, landfills2);
append!(centers, centers2);
append!(q,q2);
```

```
In [299...
          dmatx = pairwise(Euclidean(), centers.xco, landfills.xco);
          dmaty = pairwise(Euclidean(), centers.yco, landfills.yco);
          dmat = sqrt.((dmatx.^2)+(dmaty.^2));
          dmatx ct = pairwise(Euclidean(), centers.xco, stations.xco);
          dmaty ct = pairwise(Euclidean(), centers.yco, stations.yco);
          dmat ct = sqrt.((dmatx ct.^2)+(dmaty ct.^2));
          dmatx tl = pairwise(Euclidean(), stations.xco, landfills.xco);
          dmaty tl = pairwise(Euclidean(), stations.yco, landfills.yco);
          dmat tl = sqrt.((dmatx tl.^2)+(dmaty tl.^2));
In [300...
          print(size(stations), size(landfills), size(centers), size(q))
          (100, 2)(30, 2)(90, 2)(90, 1)
In [301...
          mod4 = JuMP.Model(JuMP.optimizer with attributes(() -> Gurobi.Optimizer(), "MIPGap" => 0.0001))
          set optimizer attribute(mod4, "OutputFlag", 0)
          #OLD VARIABLES
          #if landfill j is built
          @variable(mod4, z[j=1:30], Bin)
          #amount of waste transported from center i to landfill j
          @variable(mod4, x[i=1:90, j=1:30] >= 0)
          #NEW VARTABLES
          #if transfer station s is built
          @variable(mod4, t[s=1:100], Bin)
          #amount of waste transported from center i to trasnfer station s
           @variable(mod4, a[i=1:90, s=1:100] >= 0)
          #amount of waste transported from center i to trasnfer station s
          @variable(mod4, b[s=1:100,j=1:30]>=0)
          #OLD CONSTRAINTS
          \#\emptysetconstraint(mod4, [i=1:90], sum(x[i,j] for j=1:30)== q[i,1]) modified for reformulation
          (constraint(mod4, [i=1:90, j=1:30], x[i,j] \le 1000000*z[j])
          @constraint(mod4, sum(z[j] for j=1:30) \le 10)
          #NEW CONSTRAINTS
          #ensure that all waste is taken care of
          (x_{i,j}) = (x_{i,j}) + x_{i,j}  for (x_{i,j}) = (x_{i,j}) + x_{i,j}  for (x_{i,j}) = (x_{i,j}) + x_{i,j}  for (x_{i,j}) = (x_{i,j}) + x_{i,j} 
          #conservation of flow for transfer stations
           @constraint(mod4, [i=1:90, s=1:100, j=1:30], sum(a[i,s] for i=1:90)==sum(b[s,j] for j=1:30))
```

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The total cost of the combined regions is \$1,865,384.50

```
In [302... objective_value(mod4)

Out[302... 1.8653845034414863e6

In [303... t = value.(t);
    z = value.(z);
    i_t = findall(>(.5), t)
    i_z = findall(>(.5), z)
    ts_b3 = stations[i_t,:];
    lf_b3 = landfills[i_z,:];
```

Transfer Stations are built at the following coordinates:

```
In [304... ts_b3

Out[304... 15 rows × 2 columns

xco yco
Float64 Float64

1 85.45 19.15
```

| | хсо | усо |
|----|---------|---------|
| | Float64 | Float64 |
| 2 | 63.366 | 92.143 |
| 3 | 61.369 | 50.405 |
| 4 | 83.286 | 14.437 |
| 5 | 38.906 | 35.617 |
| 6 | 12.781 | 30.966 |
| 7 | 48.784 | 46.765 |
| 8 | 1.5279 | 51.627 |
| 9 | 7.478 | 84.236 |
| 10 | 86.416 | 6.6111 |
| 11 | 35.57 | 52.772 |
| 12 | 119.09 | 38.195 |
| 13 | 181.62 | 31.085 |
| 14 | 187.25 | 24.887 |
| 15 | 187.25 | 64.139 |

Landfills are built at the following coordinates:

In [305... lf_b3

Out[305... 10 rows × 2 columns

| | хсо | усо |
|---|---------|---------|
| | Float64 | Float64 |
| 1 | 76.138 | 70.191 |
| 2 | 21.163 | 44.331 |
| 3 | 13.93 | 71.108 |

| | хсо | усо |
|----|---------|---------|
| | Float64 | Float64 |
| 4 | 171.94 | 8.2604 |
| 5 | 102.13 | 78.974 |
| 6 | 170.73 | 89.923 |
| 7 | 108.11 | 11.864 |
| 8 | 130.56 | 30.882 |
| 9 | 135.89 | 90.798 |
| 10 | 166.1 | 61.775 |

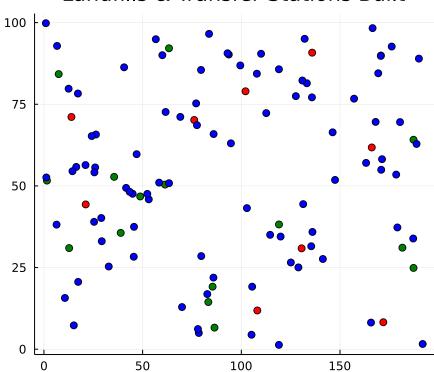
In [306...

```
plot(lf_b3.xco, lf_b3.yco, seriestype = :scatter, color = "red", title = "Landfills & Transfer Stations Built",
plot!(ts_b3.xco, ts_b3.yco, seriestype = :scatter, color = "green", label = "Stations")
plot!(centers.xco, centers.yco, seriestype = :scatter, color = "blue", label = "Centers")
```

Out[306...

Landfills Stations Centers





In [307... x=value.(x)Out[307... 90×30 Matrix{Float64}: 0.0 538.56 0.0 910.83 0.0 969.95 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 18.0 0.0 961.35 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 955.27 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 855.61 0.0 2234.3 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0

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   In [312...
             cl = sum(sum(x[1:50,15:30],dims = 2))
  Out[312... 5172.849999999999
   In [313...
             cl = sum(sum(x[50:90,1:15],dims = 2))
  Out[313... 1033.1
    In [ ]:
```