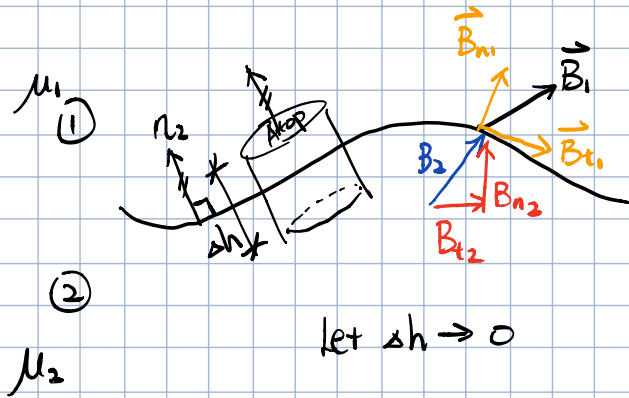


# magnetic boundary conditions at interface b/w 2 media.



1. Apply "Gauss" law for magnetostatics

$$\oint_S \vec{B} \cdot d\vec{s} = 0$$

$$\int_{\text{side}} + \int_{\text{top}} + \int_{\text{bottom}} = 0$$

$$B_{n1} A_{\text{top}} - B_{n2} A_{\text{bottom}} = 0$$

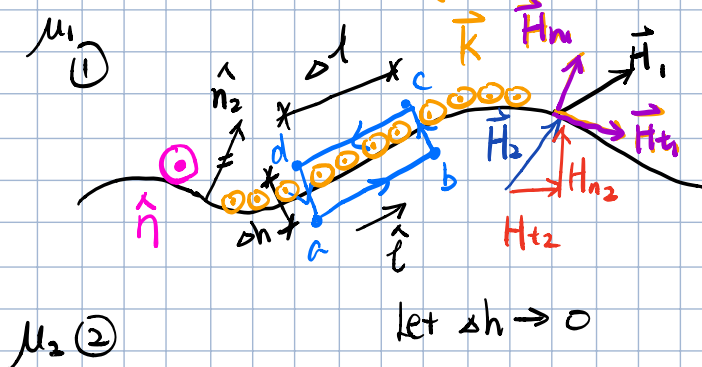
$$B_{n1} = B_{n2}$$

normal comp. of  $\vec{B}$  continuous.

$$\hat{n}_1 \cdot \vec{B}_1 = \hat{n}_2 \cdot \vec{B}_2$$

B.C. #1

surface current density.



Ampere's Law

$$\oint_C \vec{H} \cdot d\vec{\ell} = I$$

current enclosed in C

$$\int_a^b + \int_b^c + \int_c^d + \int_d^a$$

$$\vec{H}_2 \cdot \Delta l \hat{\ell} - \vec{H}_1 \cdot \Delta l \hat{\ell} = \underbrace{\vec{K} \cdot \Delta l \hat{n}}_{\text{only get normal component of } K}$$

only get normal component of  $K$

$$\hat{\ell} = \hat{n} \times \hat{n}_2$$

$$\Delta l \hat{\ell} \cdot (\vec{H}_2 - \vec{H}_1) = \vec{K} \cdot \Delta l \hat{n}$$

$$\Delta l (\hat{n} \times \hat{n}_2) \cdot (\vec{H}_2 - \vec{H}_1) = \vec{K} \cdot \Delta l \hat{n}$$

$$\therefore \vec{A} \cdot (\vec{B} \times \vec{C}) = \vec{B} \cdot (\vec{C} \times \vec{A})$$

$$\oint \vec{H} \cdot (\hat{n}_2 \times (\vec{H}_2 - \vec{H}_1)) = \vec{K} \cdot \oint \vec{H}$$

$$\hat{n}_2 \times (\vec{H}_2 - \vec{H}_1) = \vec{K}$$

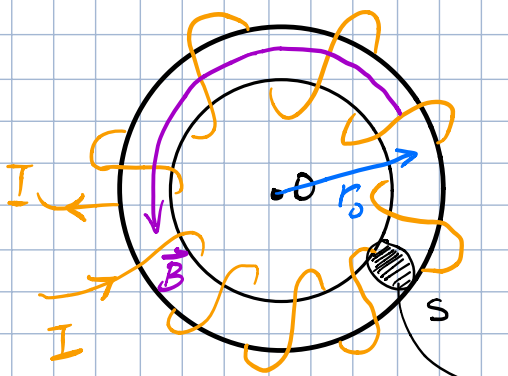
$H$  is discontinuous across boundary.

Special Case: if medium ① & ② are dielectrics

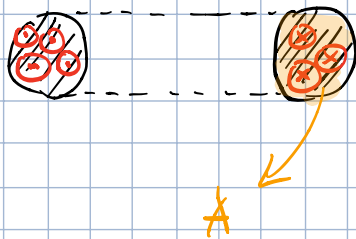
$$H_{2t} - H_{1t} = 0$$

## Inductance

Recall: magnetic flux  $\phi$



flux passed through  $S$



$$\vec{H} = \frac{NI}{2\pi r} \hat{\phi}$$

$$\vec{B} = \mu \vec{H}$$

$$= \hat{\phi} \frac{\mu NI}{2\pi r}$$

$$\phi = \iint_S \vec{B} \cdot d\vec{S}$$

$$= \iint_S \hat{\phi} \frac{\mu NI}{2\pi r} \cdot \hat{\phi} ds$$

means  $\vec{B}$  is uniform  $\left\{ \begin{array}{l} \text{Assume that mean radius of the} \\ \text{toroid } r_0 \gg \text{cross sectional} \\ \text{dimensions of toroid.} \end{array} \right.$

$$\approx \frac{\mu NI}{2\pi r} \cdot A$$

Flux linkage.  $\Delta$  = product of the # of turns and flux linking each of them.

$$\Lambda = N\psi$$

Define inductance

$$L = \frac{\Lambda}{I} = \frac{N\psi}{I} \quad [H]$$

$$\text{toroid: } L = \frac{\mu N^2 A_{\text{cross}}}{2\pi r_o} \quad [H]$$

Example: Solenoid.

