

SIT221: Data Structures and Algorithms

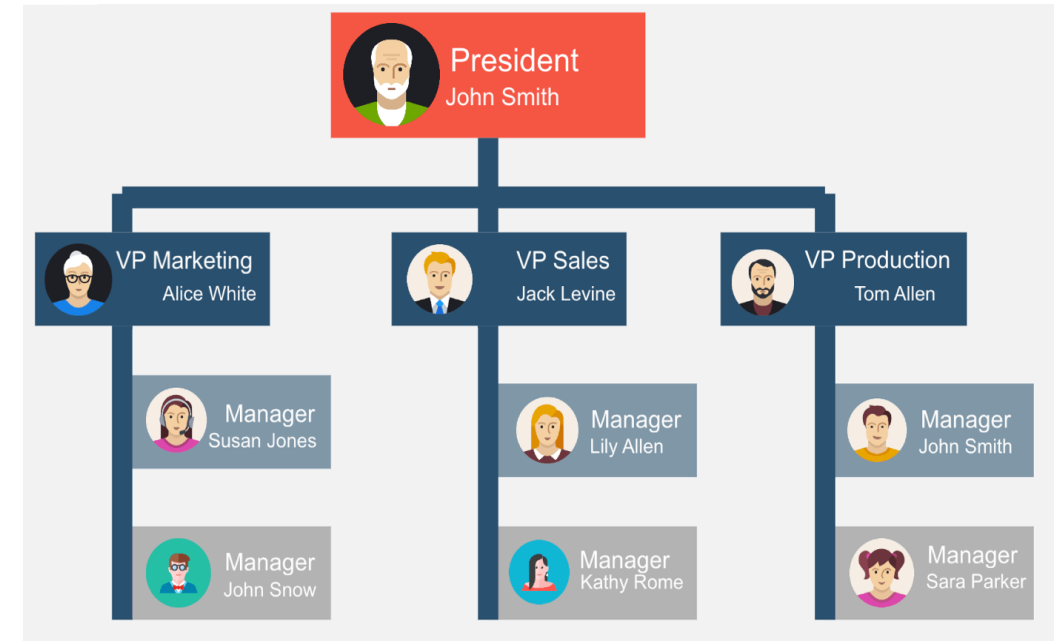
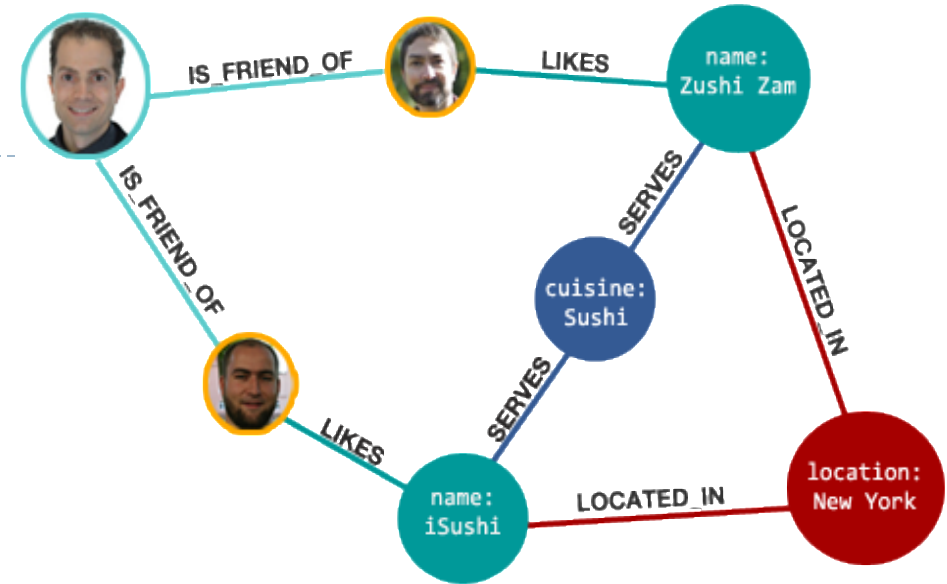
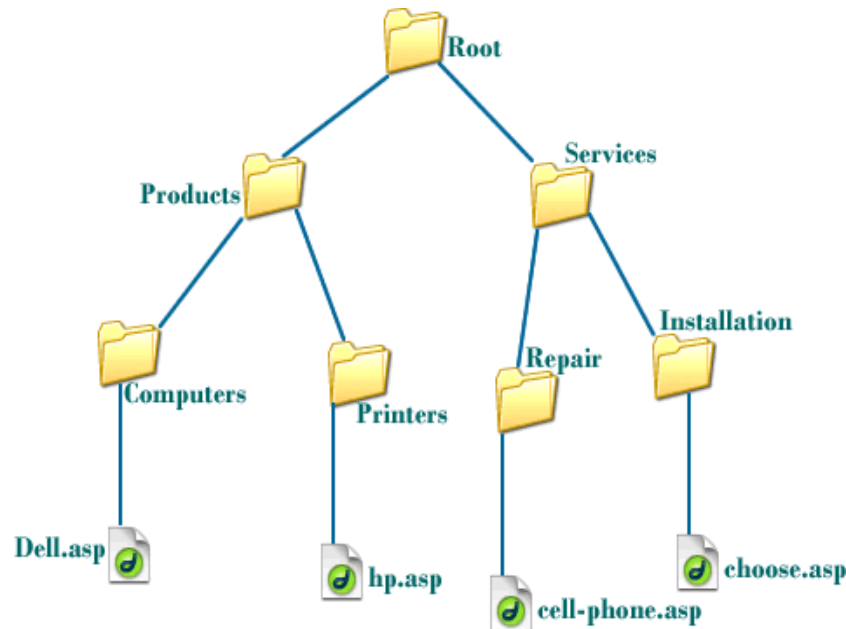
Lecture 8: Graphs

Week 7 recording for prac

Week 7	Week 7 - prac - recording_1	Week 7 - prac	26/08/2017 4:11 pm	00:39:42	...
Week 4	SIT221 - Data Structures And Algorithms - recording_1	SIT221 - Data Structures And Algorithms	3/08/2017 11:22 am	00:42:34	...
Week 3	SIT221 - Data Structures And Algorithms - recording_1	SIT221 - Data Structures And Algorithms	27/07/2017 10:55 am	00:40:01	...
Week 2	Week 2 - prac - recording_1	Week 2 - prac	20/07/2017 11:01 am	00:31:17	...

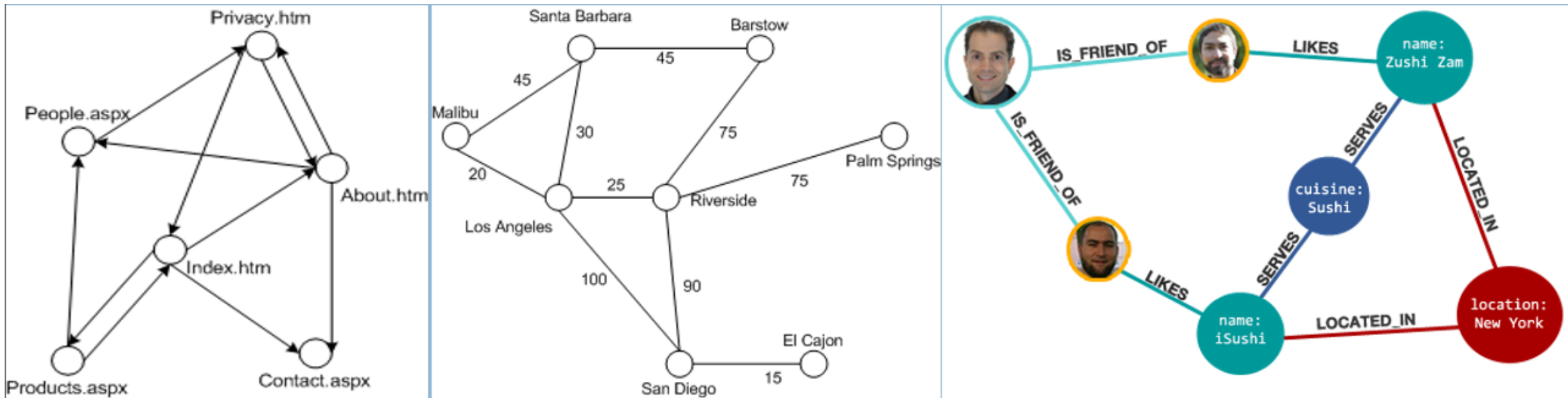
Non-linear data structures

- ▶ Values are not arranged in order, many next/previous nodes.
 - ▶ Hierarchical data (last week)
 - ▶ Network data (this week)



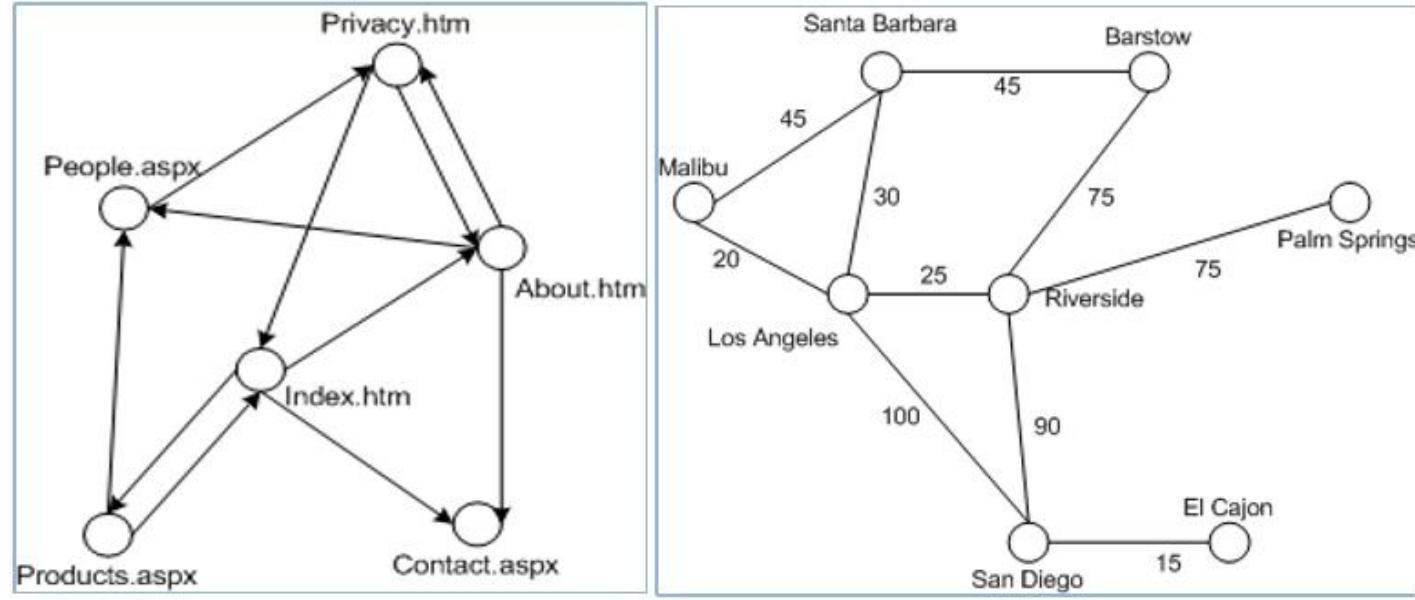
Motivation

- ▶ How can we store data of this type in memory?



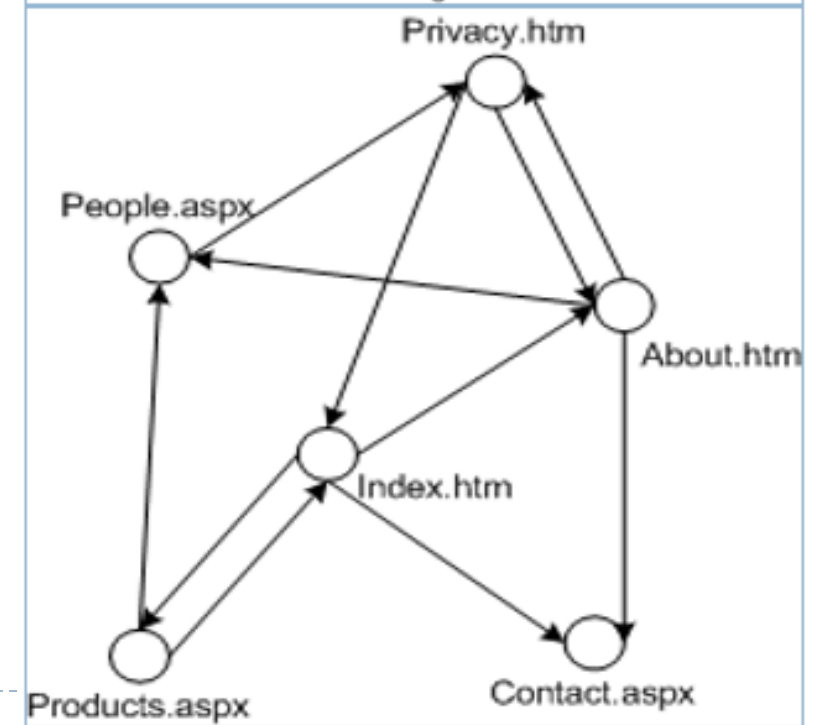
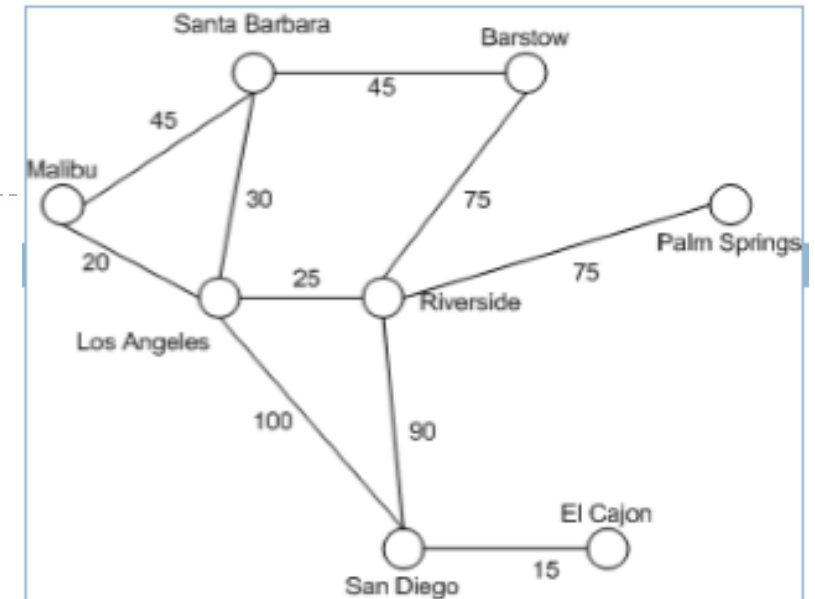
Graph data

- ▶ What are the key elements in this diagram?
 - ▶ Nodes/vertices, e.g. pages, individuals, etc.
 - ▶ Links/edges, e.g. to represent navigations from one page to another, route from a city to another, etc.
- ▶ Thus, any graph can be described as: Vertices & edges
- ▶ **$G = (V, E)$**

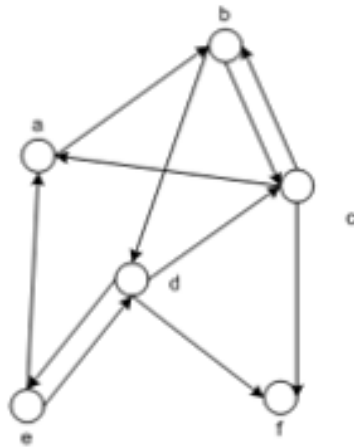


Graph data (cont)

- ▶ Are all graphs the same? NO
- ▶ Graphs can be directed or undirected
- ▶ Edges may have weights
- ▶ Graphs can be sparse (few links/edges) or dense (to many edges) or even fully connected (every two nodes are connected by a link)



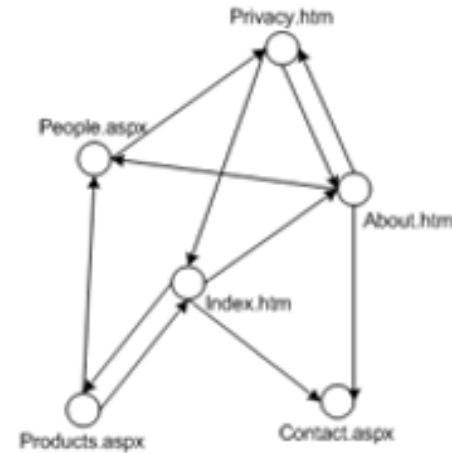
How to represent a graph?



Directed Graph (a)

	a	b	c	d	e	f
a		✓				
b			✓	✓		
c		✓				✓
d			✓		✓	✓
e	✓			✓		
f						

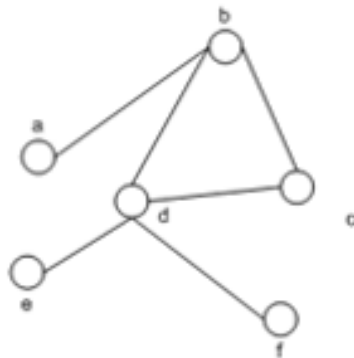
Adjacency Matrix Representation (a)



Directed Graph (a)

Set of nodes	Nodes' Adjacency lists		
Index.htm	Products.aspx	Contact.aspx	About.htm
About.htm	Privacy.aspx	Products.aspx	People.aspx
Privacy.htm	Index.htm	About.htm	
Contact.aspx			
Products.aspx	People.aspx	Index.htm	
People.aspx	Privacy.htm		

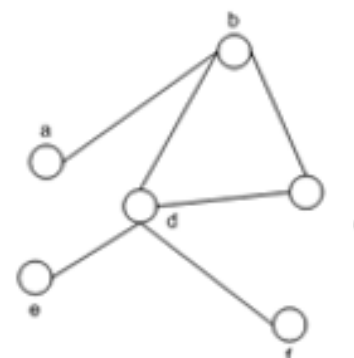
Adjacency List Representation (a)



Undirected Graph (b)

	a	b	c	d	e	f
a		✓				
b	✓		✓	✓		
c		✓		✓		
d		✓	✓		✓	✓
e				✓		
f				✓		

Adjacency Matrix Representation (b)



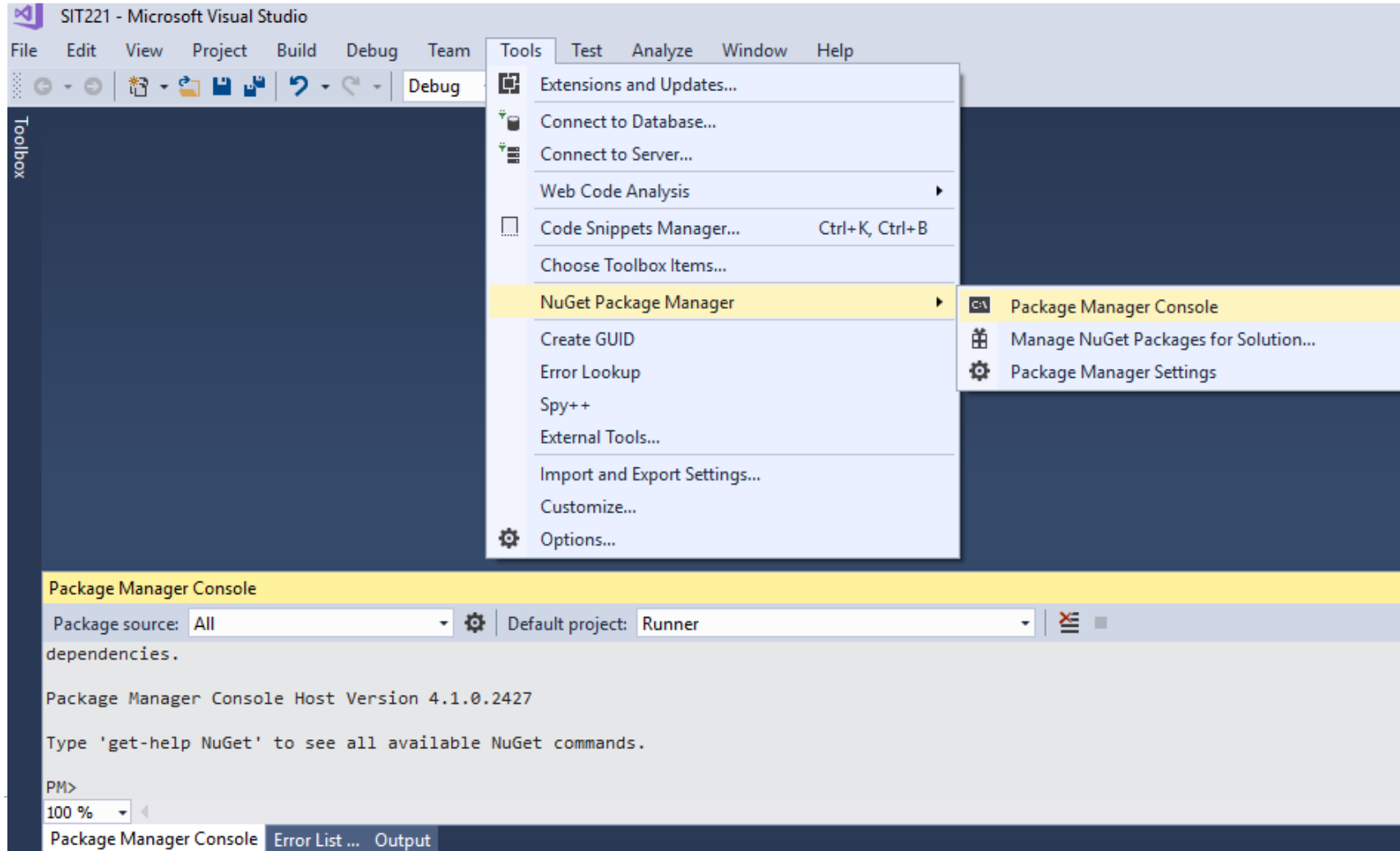
Undirected Graph (b)

Set of nodes	Nodes' Adjacency lists		
a	b		
b	a	d	c
c	b	d	
d	b	e	f
e	d		
f	d		

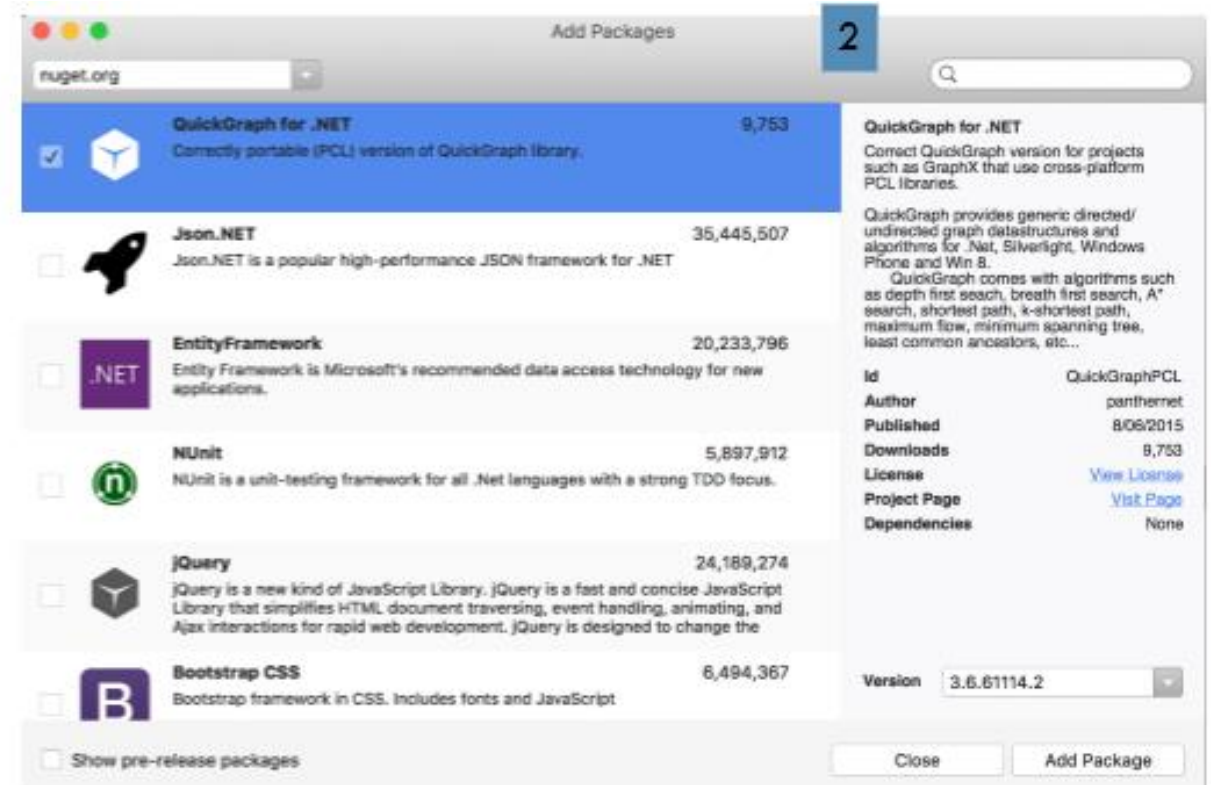
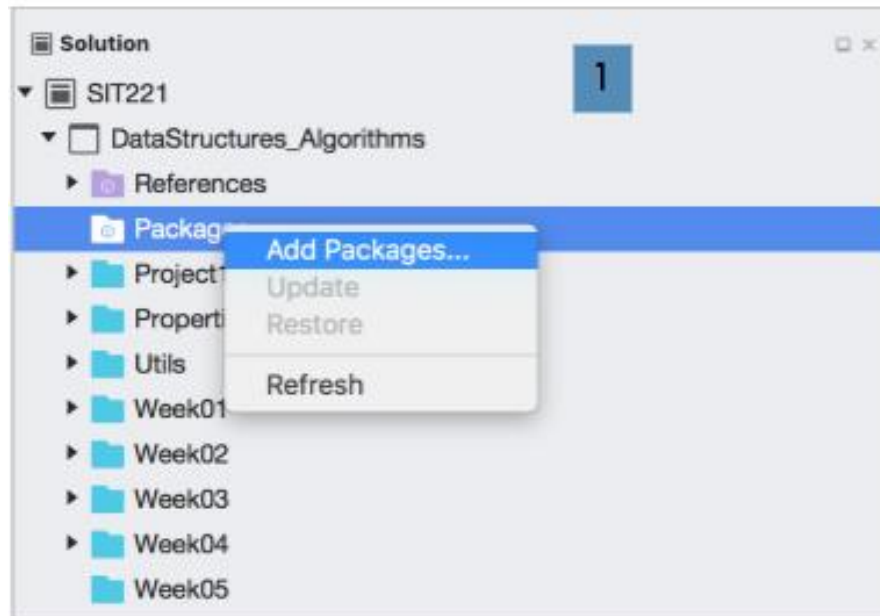
Adjacency List Representation (b)

Using library

- Visual Studio 2017 <http://quickgraph.codeplex.com/>



Using library



Example 1

- ▶ A graph of cities

- ▶ Let's create a bi-directional graph

```
var trafficNetwork = new BidirectionalGraph<NOTETYPE, Edge<NOTETYPE>>>();
```

- ▶ If we want each node is named by a city name

- ▶ NOTETYPE: `string`

```
var trafficNetwork = new BidirectionalGraph<string, Edge<string>>>();
```

Example 2

- ▶ A graph of integers

```
BidirectionalGraph<int, Edge<int>> integersGraph = new  
BidirectionalGraph<int , Edge<int>>();
```

Example 3

- ▶ A graph of POIs

```
BidirectionalGraph<PointOfInterest, GraphEdge<PointOfInterest>>  
POIsGraph = new BidirectionalGraph<PointOfInterest ,  
GraphEdge<PointOfInterest>>();
```

- ▶ GraphEdge class is a user-defined class that enables adding description and distance/time to any edge (you will see this in next week prac)

Adding nodes in a graph

► trafficNetwork

//Let's add Australia big cities

```
trafficNetwork.AddVertex("Melbourne");
```

```
trafficNetwork.AddVertex("Sydney");
```

```
trafficNetwork.AddVertex("Brisbane");
```

```
trafficNetwork.AddVertex("Adelaide");
```

```
trafficNetwork.AddVertex("Perth");
```

```
trafficNetwork.AddVertex("Melbourne"); //what would happen here?
```

Adding nodes in a graph

► integersGraph

```
integersGraph.AddVertex(1);  
integersGraph.AddVertex(2);  
integersGraph.AddVertex(3);  
integersGraph.AddVertex(4);
```

Adding nodes in a graph

- ▶ POIsGraph

```
var poi = ... // similar to week07 prac  
POIsGraph.AddVertex(poi);
```

Adding edges in a graph

//new Edge<string>(Source, Target)

```
trafficNetwork.AddEdge(new Edge<string>("Melbourne", "Sydney"));  
trafficNetwork.AddEdge(new Edge<string>("Melbourne", "Brisbane"));  
trafficNetwork.AddEdge(new Edge<string>("Sydney", "Brisbane"));
```

//Let's add Edges between two POIs

```
POIsGraph.AddEdge(new GraphEdge<PointOfInterest> { Source = OBJ_POI1 , Target = OBJ_POI2 , Description = "Description of route from POI1 to POI2", Distance = 100 });
```


Displaying graph nodes and edges

// Let's display all graph nodes

```
foreach (var vertex in trafficNetwork.Vertices)
    Console.WriteLine(vertex);
```

// Let's display all edges

```
foreach (var edge in trafficNetwork.Edges)
    Console.WriteLine(edge);
```

// Let's display each node and it's edges

```
foreach (var vertex in trafficNetwork.Vertices)
    foreach (var edge in trafficNetwork.OutEdges(vertex)) //you can use InEdges
        Console.WriteLine(edge);
```

Graph Applications

- ▶ Traffic/Navigation
- ▶ PageRanking – Search Engines
- ▶ Social media – Facebook/Twitter
- ▶ Computer Networks/routing
- ▶ Dependencies – in your code/unit pre-requisites
- ▶ Project management – critical path analysis
- ▶ Graphical models (machine learning)