

# Analyse spatiale multi-échelles de données écologiques avec adespatial

Stéphane Dray

Rencontres R - 2017

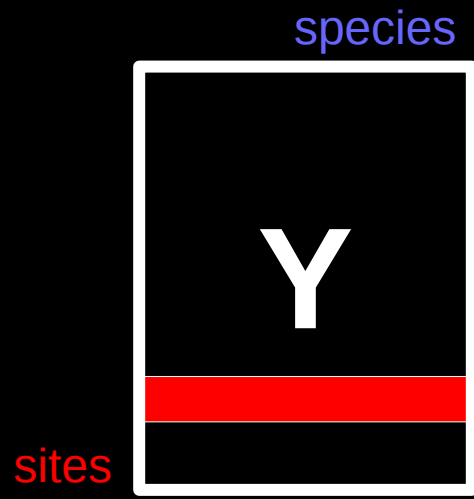
# Ecological communities



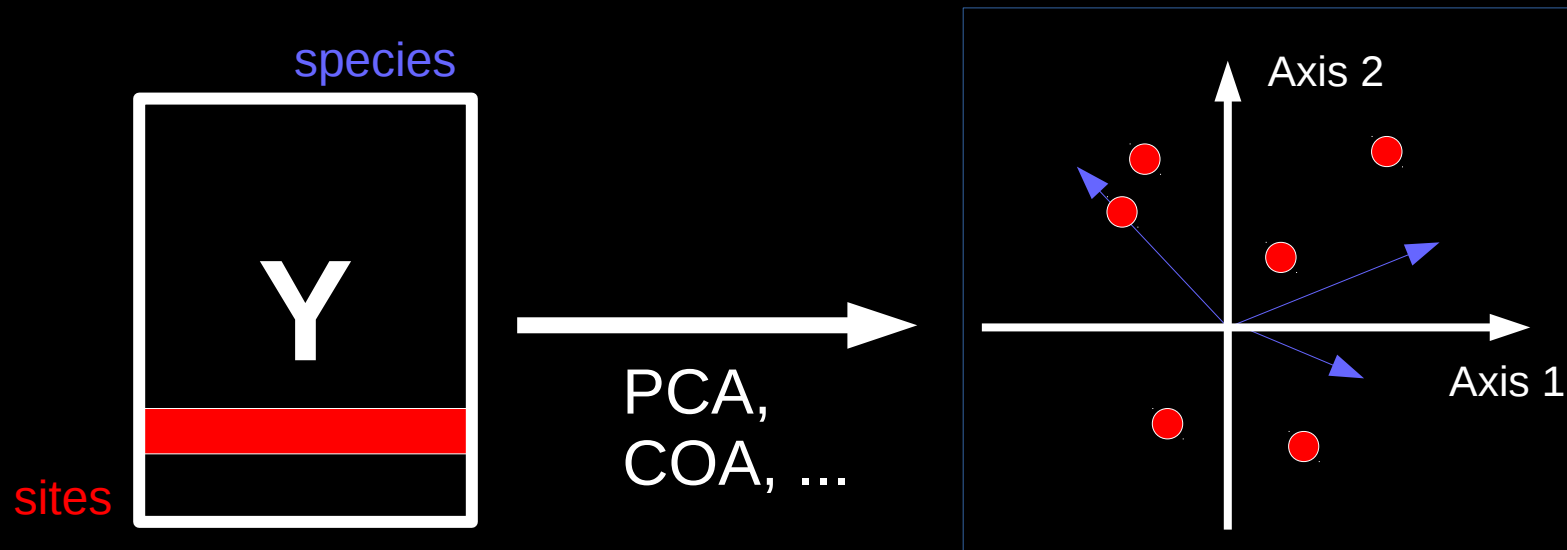
# Community ecology

- Describe communities (species assemblages)
- Study how their composition vary (in space or time)
- Identify factors/processes behind these patterns

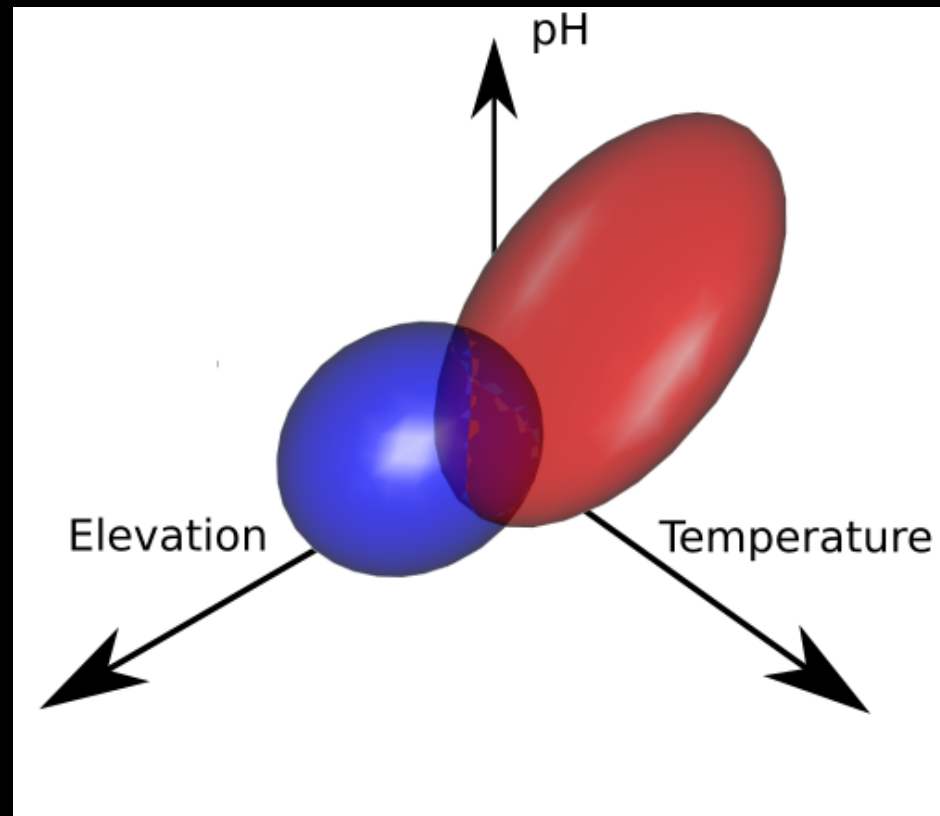
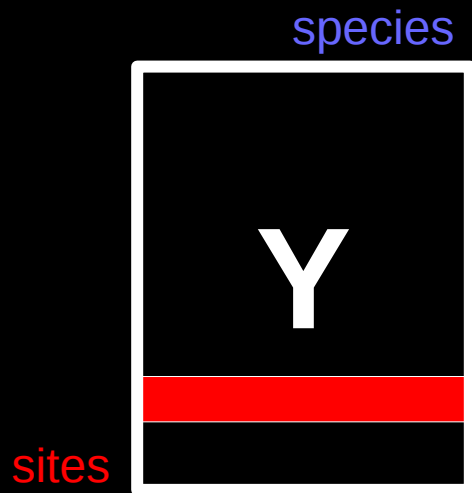
# One-table ordination



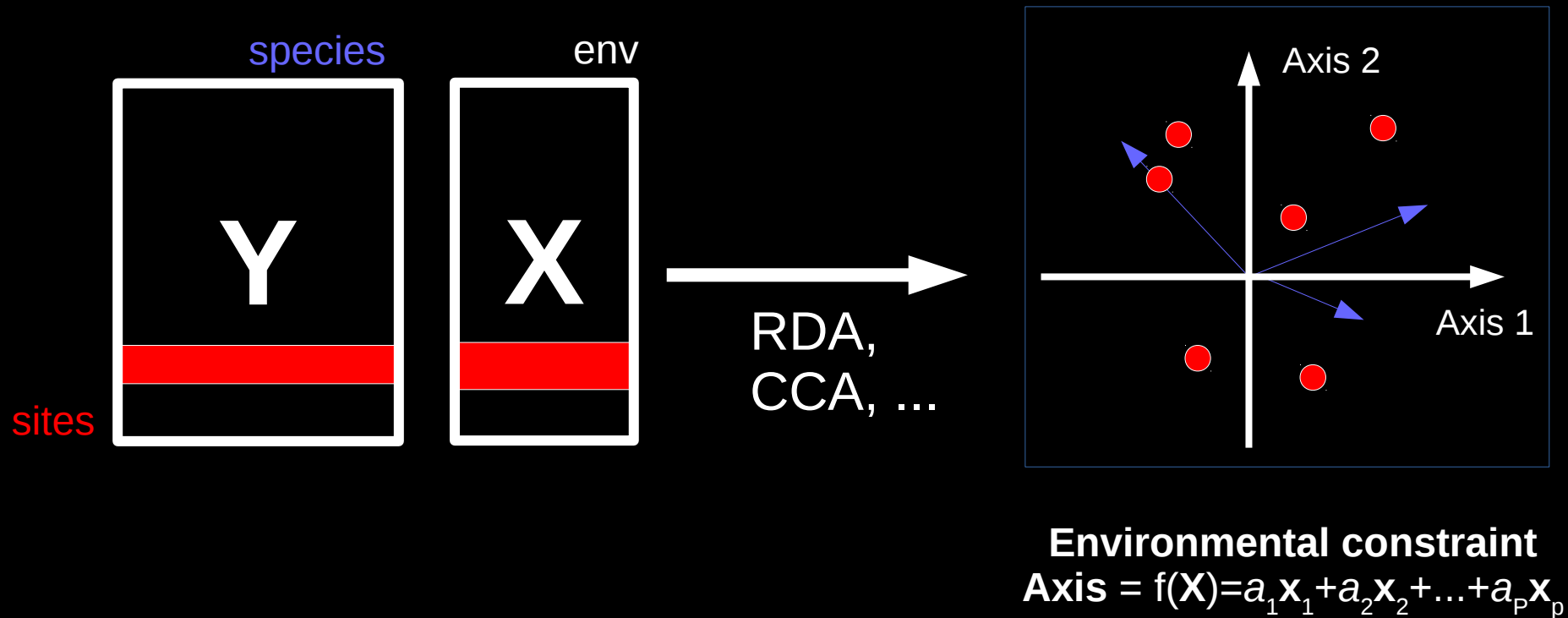
# One-table ordination



# The niche theory



# Two-tables ordination



# Spatial patterns as proxies

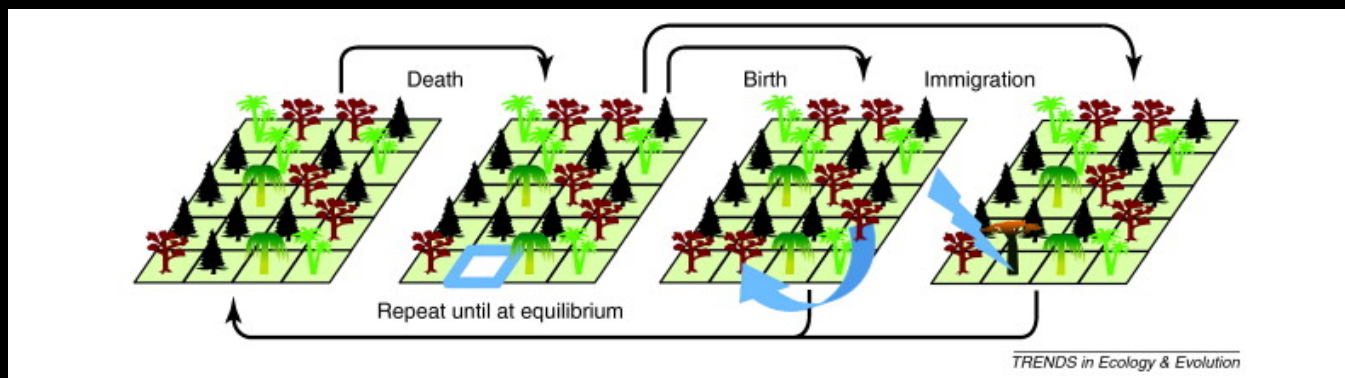
- Some missing environmental variables
- Other ecological processes could act



# Spatial patterns as proxies

- Some missing environmental variables
- Other ecological processes could act

Species are equivalent, only stochastic events



Hubbell (2001)

Rosindell et al. (2011) TREE

# Spatial patterns as proxies

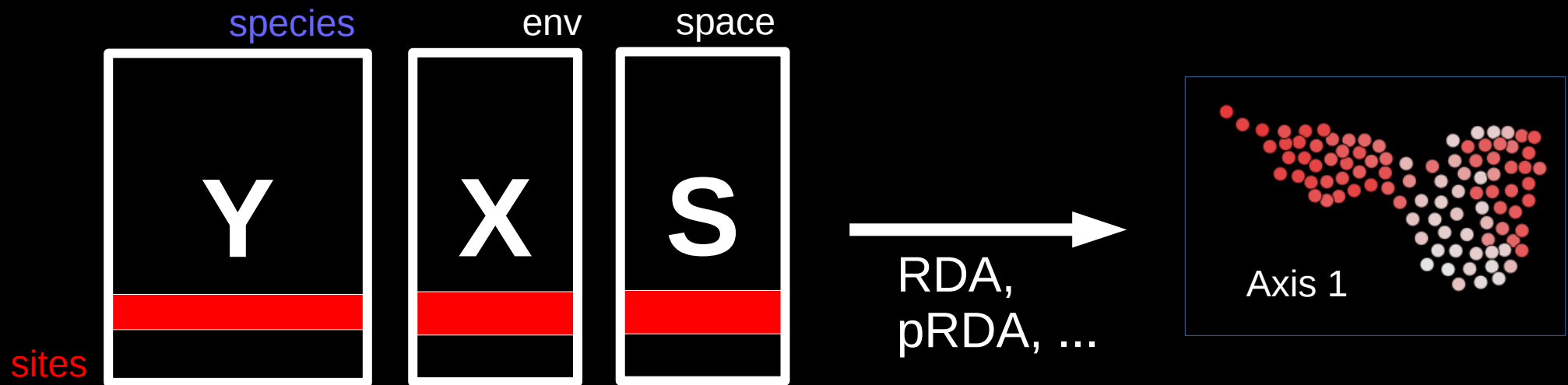
- Some missing environmental variables
- Other ecological processes could act
- Spatial structures as proxies of unmeasured variables / unknown processes

*Ecology*, 90(1), 2009, pp. 46–56  
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Beyond description: the active and effective way  
to infer processes from spatial patterns

ELIOT J. B. MCINTIRE<sup>1,4</sup> AND ALEX FAJARDO<sup>2,3</sup>

# Spatial patterns



- Spatial patterns linked to environment ( $Y \sim X \leftrightarrow S$ )
- Spatial patterns due to other factors ( $Y|X \leftrightarrow S$ )
- Which scales?

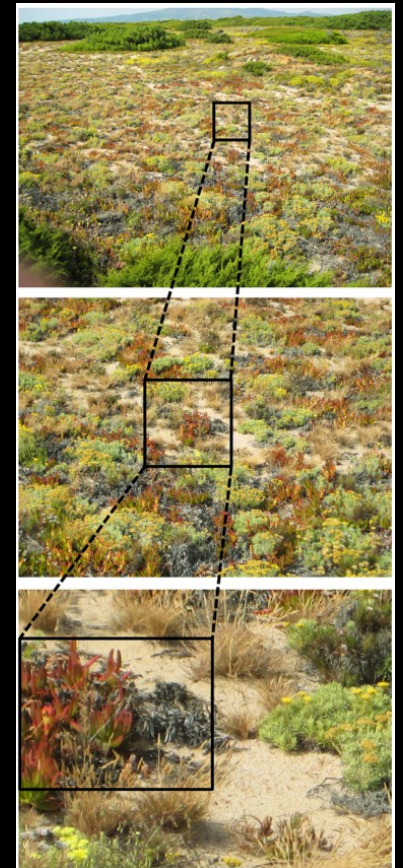
# How integrate spatial information?

- Mapping (Goodall, 1954)
- Spatial weights (Moran, 1954)
- Spatial predictors:
  - Polynomials (Gittins, 1968)
  - PCNM (Borcard & Legendre, 2002)
  - MEM (Dray et al, 2006)
  - AEM (Blanchet et al, 2008)

# How integrate spatial information?

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- Table: sites x variables
- Variables = scales
- Orthonormal predictors



2008

# SEDAR

Spatial Ecological Data Analysis with  Workshop

2012

## REVIEWS

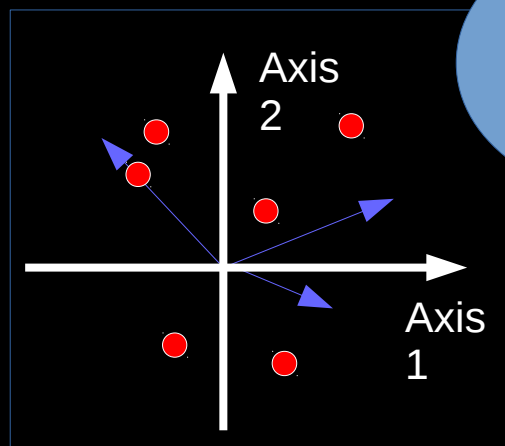
*Monographs*, 82(3), 2012, pp. 257–275  
by the Ecological Society of America

### Community ecology in the age of multivariate multiscale spatial analysis

S. DRAY,<sup>1,16</sup> R. PÉLISSIER,<sup>2,3</sup> P. COUTERON,<sup>2</sup> M.-J. FORTIN,<sup>4</sup> P. LEGENDRE,<sup>5</sup> P. R. PERES-NETO,<sup>6</sup> E. BELLIER,<sup>7,8</sup>  
R. BIVAND,<sup>9</sup> F. G. BLANCHET,<sup>10</sup> M. DE CÁCERES,<sup>11</sup> A.-B. DUFOUR,<sup>1</sup> E. HEEGAARD,<sup>12</sup> T. JOMBART,<sup>1,13</sup> F. MUNOZ,<sup>2</sup>  
J. OKSANEN,<sup>14</sup> J. THIOULOUSE,<sup>1</sup> AND H. H. WAGNER<sup>15</sup>

2015

`adespatial` 0.0-1 on CRAN



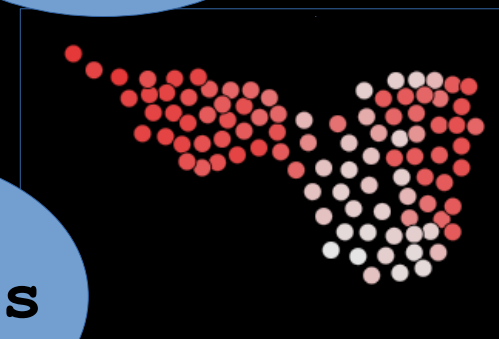
ade4

sp

adespatial

spdep

adegraphics



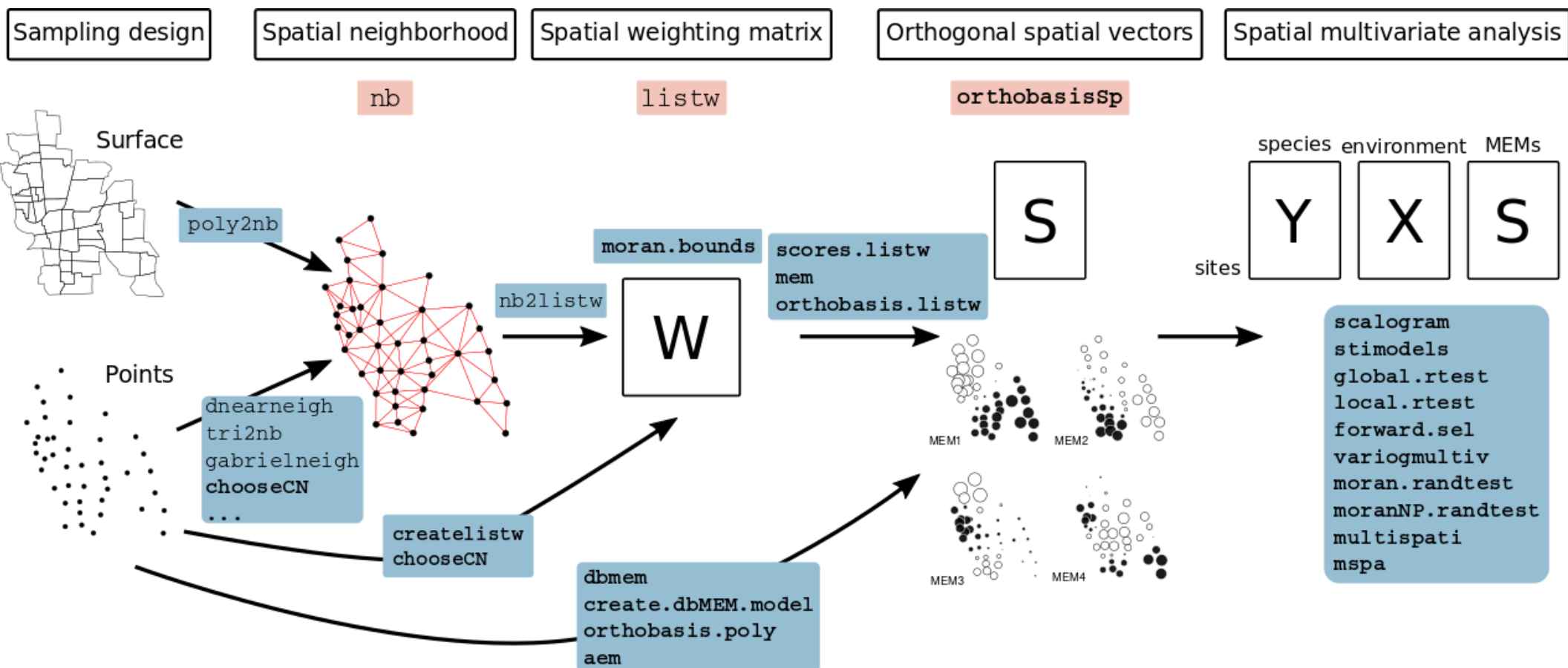
maptools

vegan

multivariate

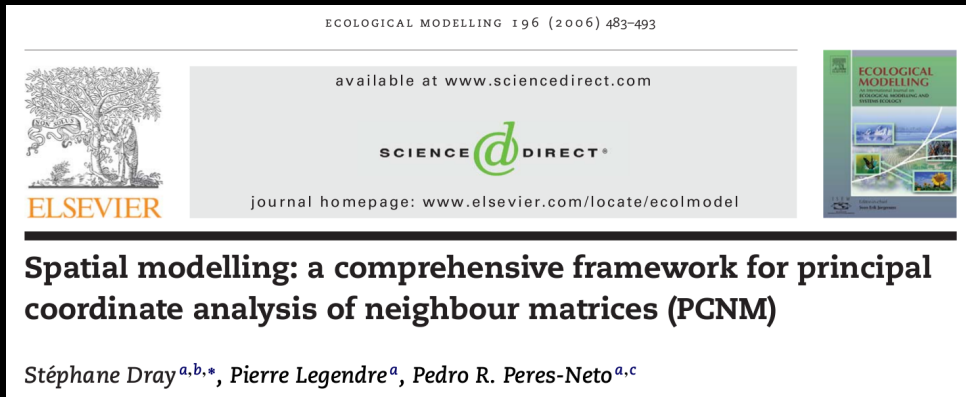
spatial

# adespatial: an overview

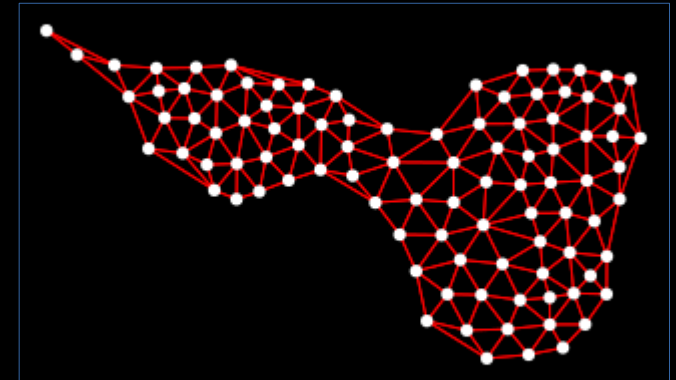
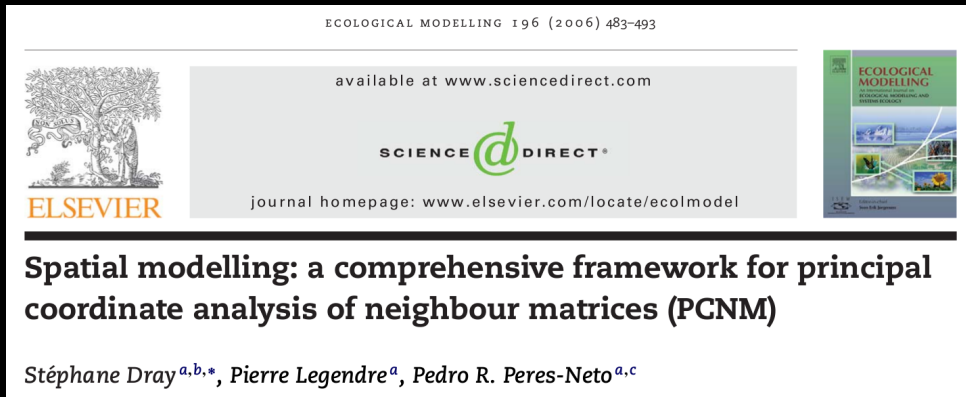




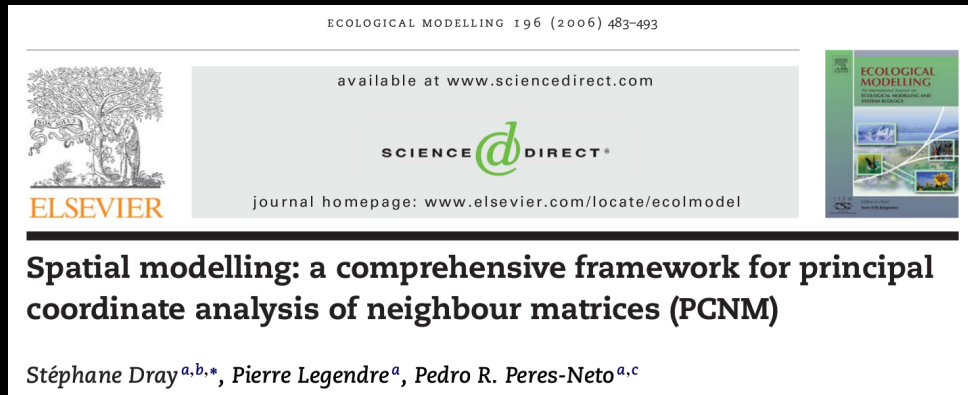
# Space as a graph (spatial weights matrix)



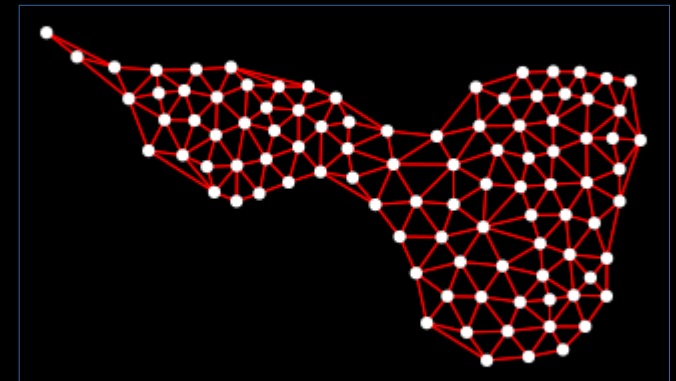
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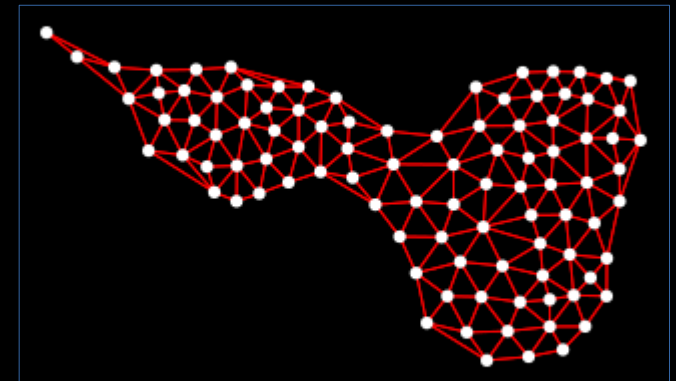
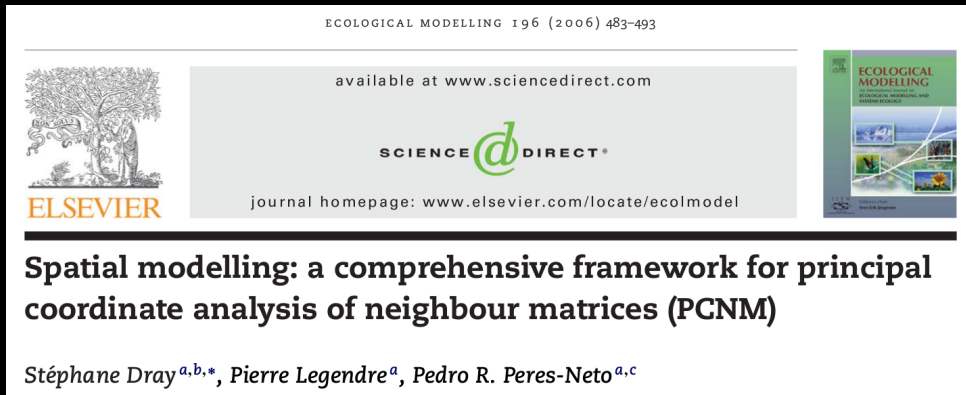
# Space as a graph (spatial weights matrix)



$$\mathbf{W} = \begin{bmatrix} 0 & 1 & \dots & 0 \\ 1 & 0 & \dots & 1 \\ \vdots & \vdots & \dots & \vdots \\ 0 & 1 & \dots & 0 \end{bmatrix}$$



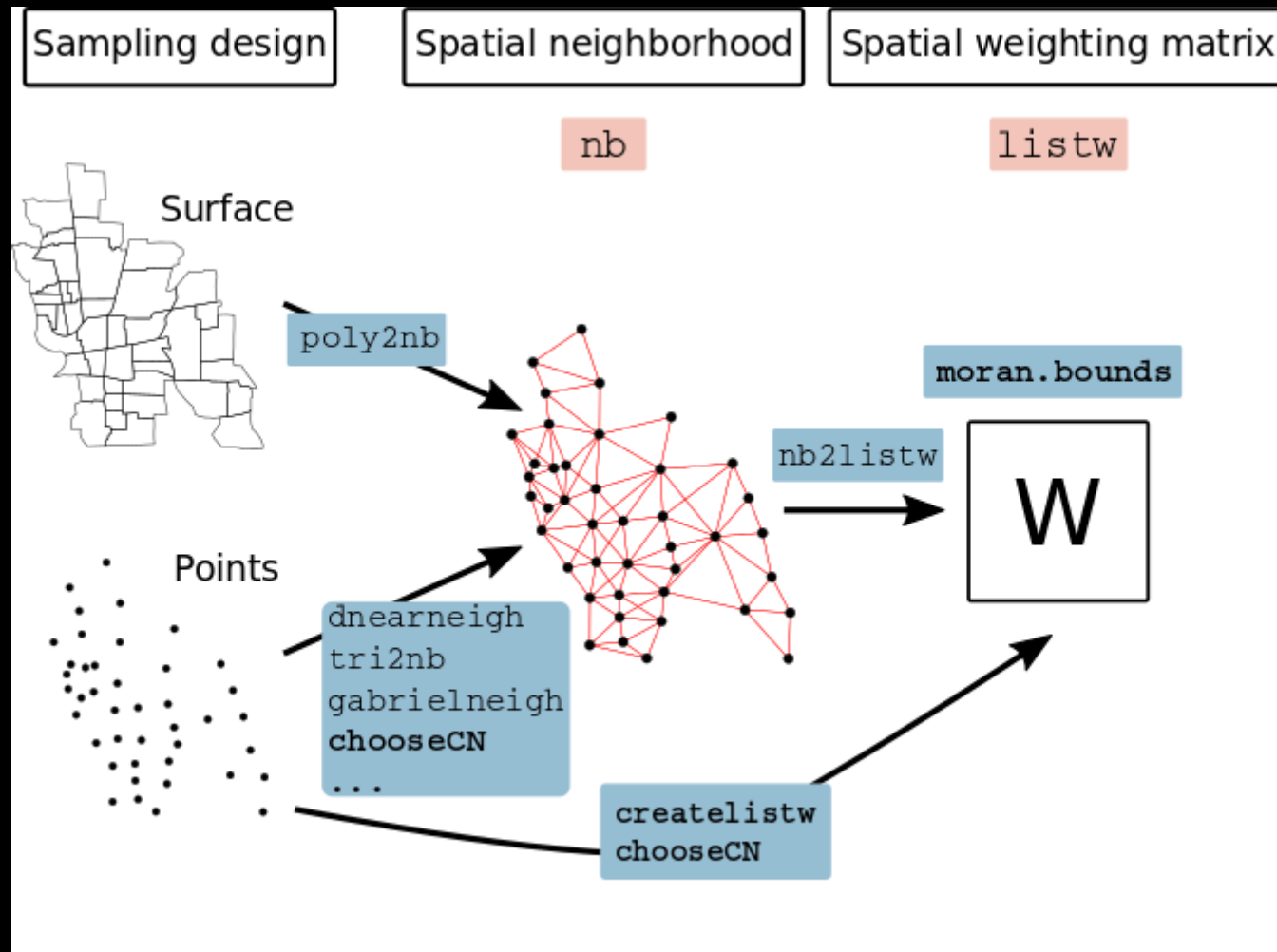
# Space as a graph (spatial weights matrix)



$$\mathbf{W} = \begin{bmatrix} 0 & 1 & \dots & 0 \\ 1 & 0 & \dots & 1 \\ \vdots & \vdots & \dots & \vdots \\ 0 & 1 & \dots & 0 \end{bmatrix}$$

$$MC(\mathbf{x}) = \frac{n}{\mathbf{1}_n^\top \mathbf{W} \mathbf{1}_n} \frac{\mathbf{x}^\top \mathbf{H} \mathbf{W} \mathbf{H} \mathbf{z}}{\mathbf{z}^\top \mathbf{H} \mathbf{H} \mathbf{z}} = \frac{n \sum_{i,j} w_{ij} (x_i - \bar{x})(x_j - \bar{x})}{\sum_{i,j} w_{ij} \sum_i (x_i - \bar{x})^2}$$

# From spatial sampling to weights



# createlistw

## Generate R code to create a spatial weighting matrix

### nb options

#### Sp object or coordinates:

xyir

#### Graph type:

Gabriel

Delaunay

Gabriel

Relative

Minimum spanning tree

Distance

K-nearest

### listw options

#### Standardization style:

W

#### General weights:

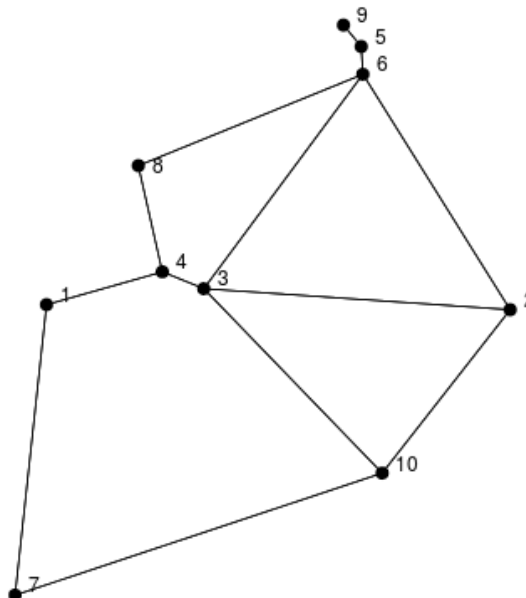
$1 - d/\max(d)$

### R code (copy & paste in the R console):

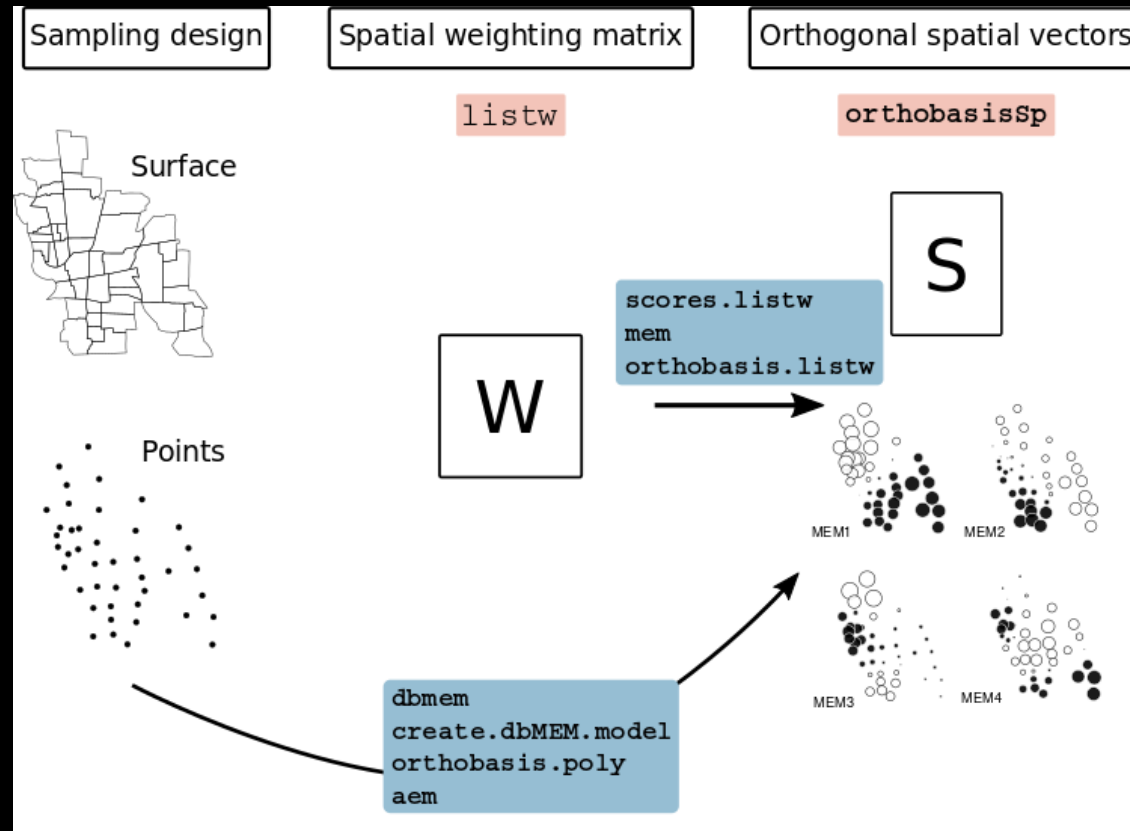
```
library(adespatial);library(sp);library(spdep);  
nb <- chooseCN(coordinates(xyir), type = 2, plot.nb = FALSE)  
distnb <- nbdists(nb, xyir)  
fdist <- lapply(distnb, function(x) 1 - x/max(dist(xyir)))  
lw <- nb2listw(nb, style = 'W', glist = fdist, zero.policy = TRUE)
```

### Display summary

☒ no ☐ yes



# From weights to spatial predictors



## orthobasisSp

- `plot`, `summary`, `print` methods
- inherits from `data.frame`

# Moran's Eigenvector Maps

$$\mathbf{HWHV} = \mathbf{V}\mathbf{\Lambda}$$

Eigenvectors are orthogonal and maximize Moran's coefficient :

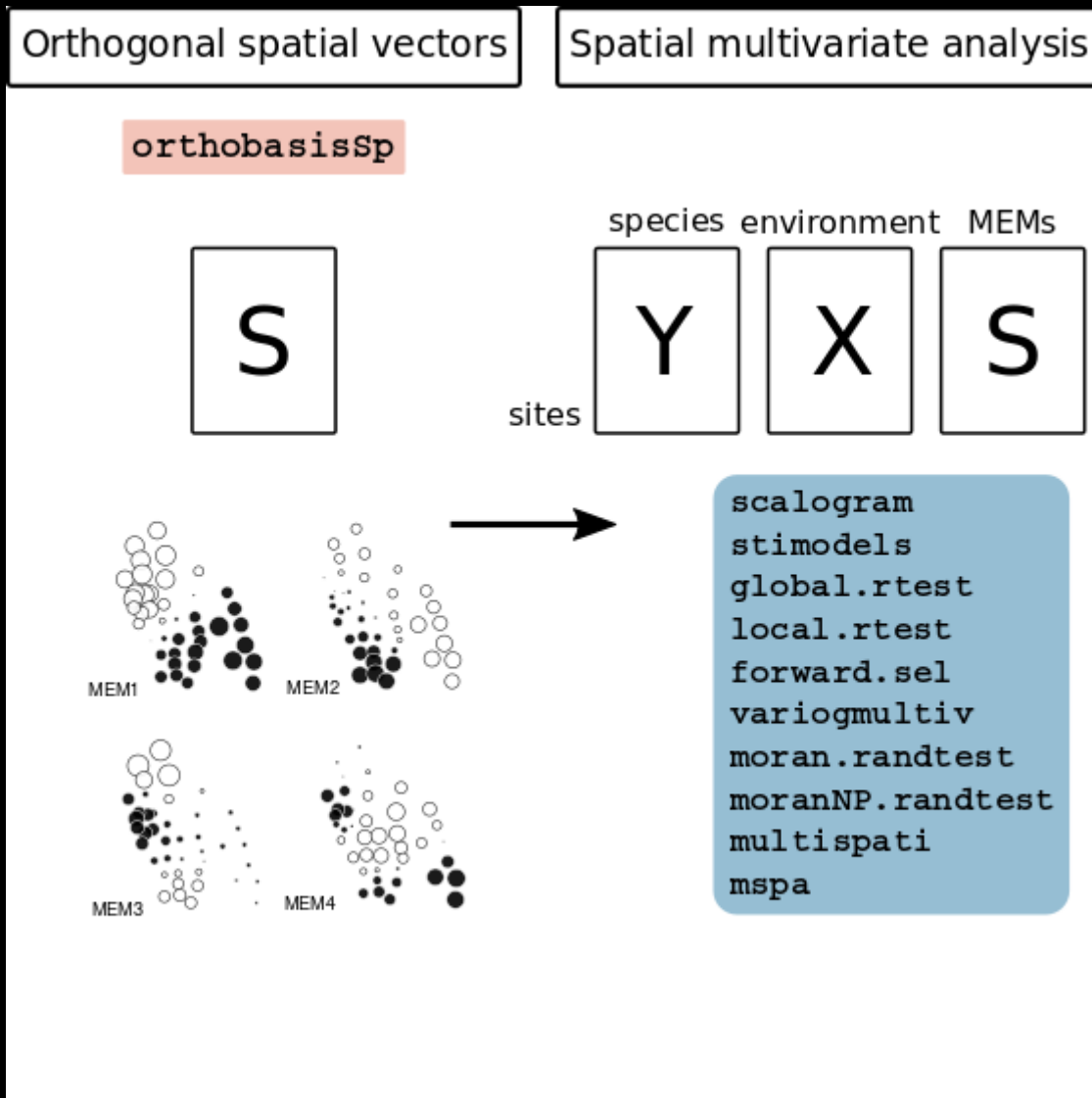
$$MC(\mathbf{v}_i) = \lambda_i$$

```
mymem <- mem(mylistw)  
plot(mymem[,c(1,2,10,69)], xy)
```





# Spatial multiscale/multivariate methods



# Univariate multiscale methods

- Moran's Index: `moran.randtest(x, mylistw)`
- Positive/Negative decomposition: `moranNP.randtest(x, mylistw)`

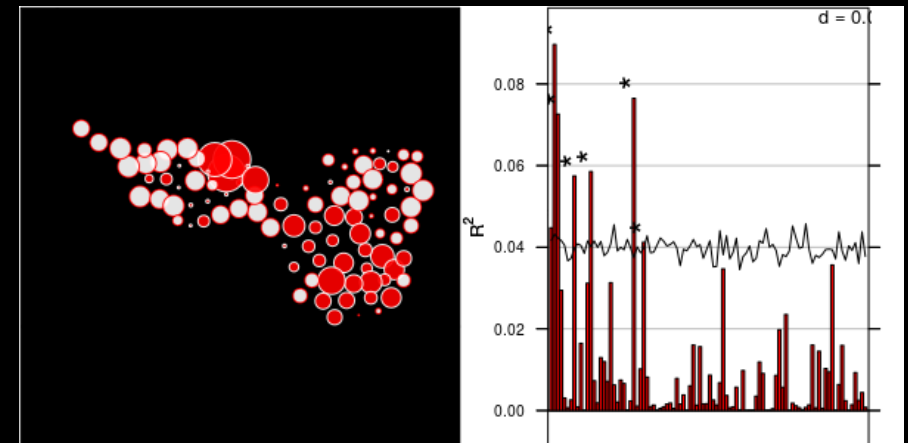
$$MC(\mathbf{x}) = \sum_{i=1}^{n-1} \lambda_i \text{cor}^2(\mathbf{x}, \mathbf{v}_i)$$

Dray (2011) Geographical Analysis

- Multiscale decomposition:

`scalogram(x, mymem)`  
`mspa(mypca, mymem)`

$$\sum_{i=1}^{n-1} \text{cor}^2(\mathbf{x}, \mathbf{v}_i) = 1$$



Dray et al (2012) Ecological Monographs  
 Jombart, Dufour & Dray (2009) Ecography

# Spatial multivariate methods

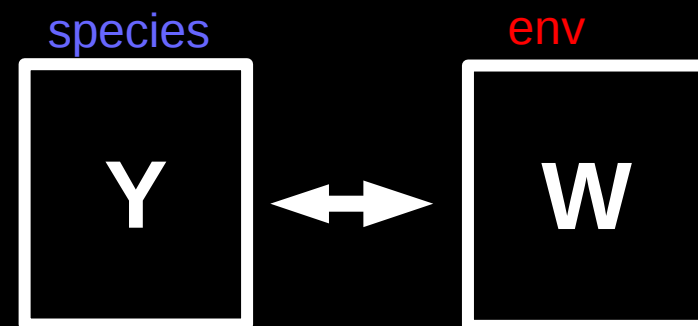
- Multivariate autocorrelation: `global.rtest(Y, mylistw)`

Jombart et al (2008) Heredity

- Spatial multivariate analysis:

`multispati(mypca, mylistw)`

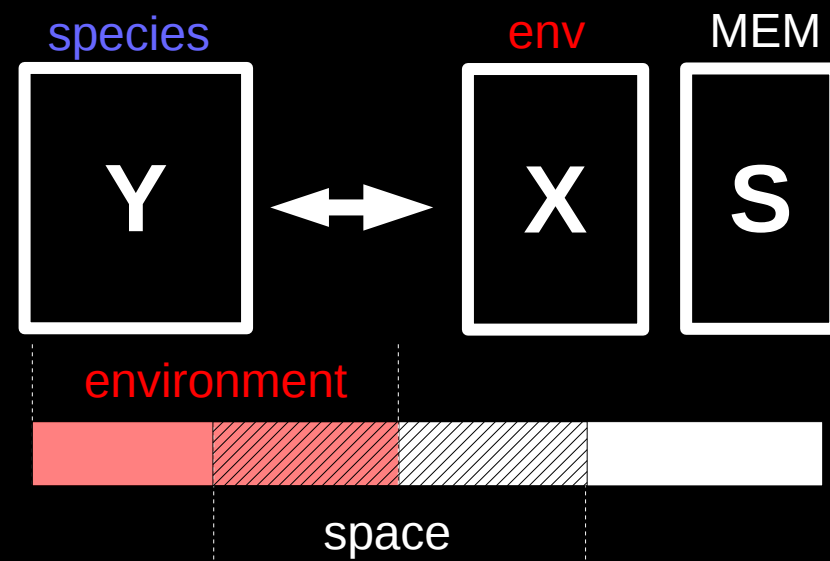
Dray et al (2008) Journal of Vegetation Science



- Constrained ordination/Variation partitioning:

`pcaiv(mypca, mymem)`  
`varpart(Y, X, mymem)`

Dray et al (2012) Ecological Monographs



# The two faces of spatial autocorrelation

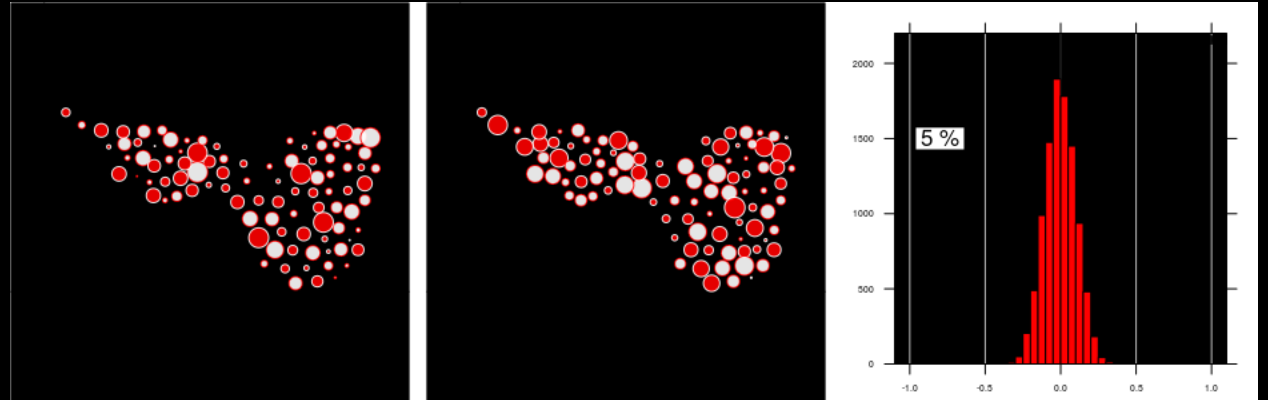


Proxies for unmeasured processes

Non-independent observations

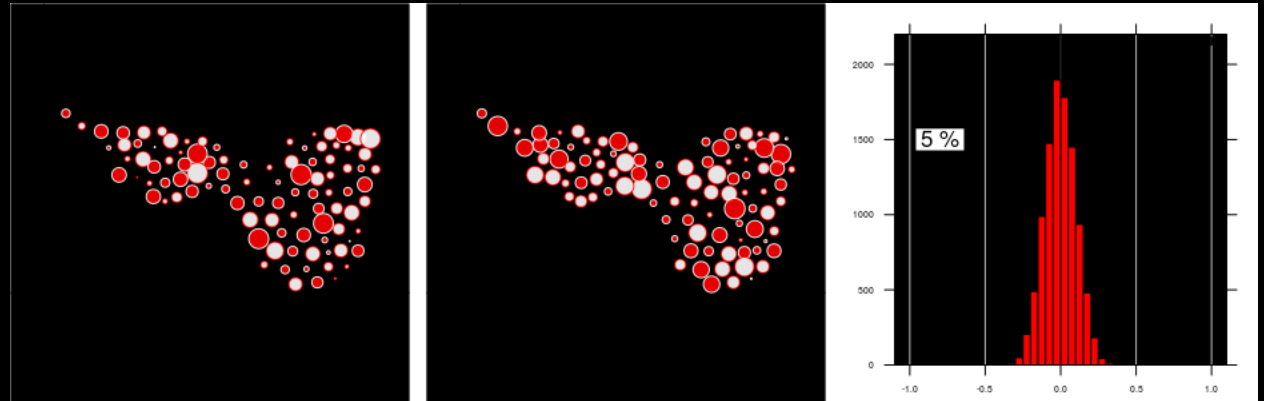
# Inference and spatial autocorrelation

- No spatial structure

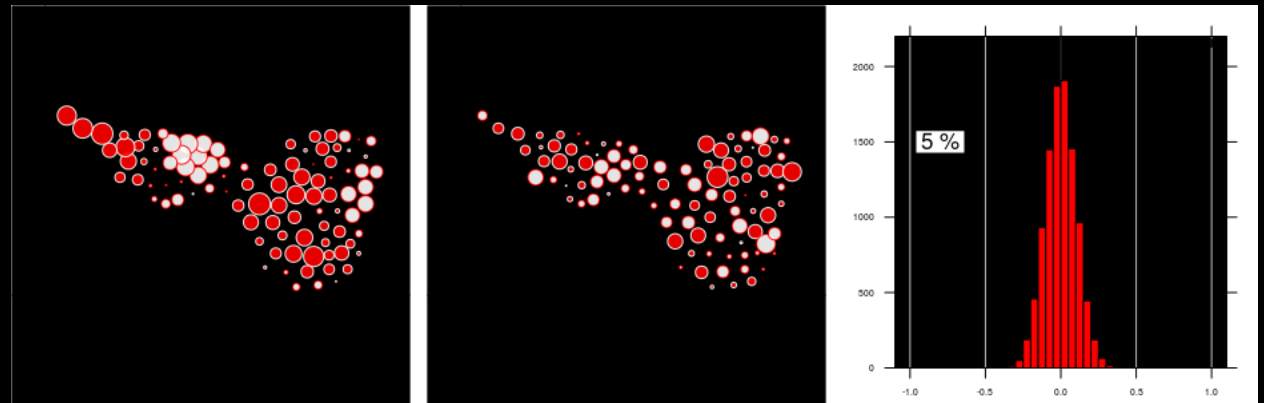


# Inference and spatial autocorrelation

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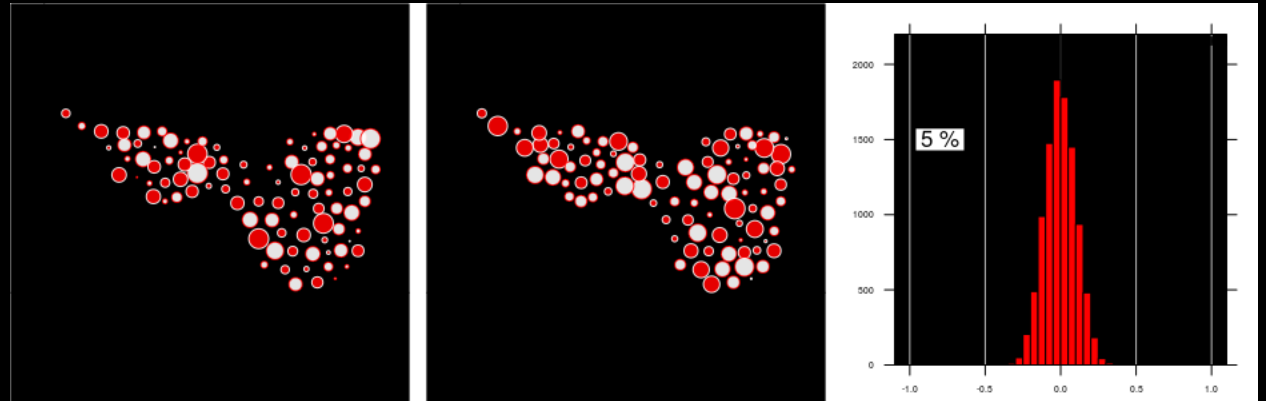


- One spatial structure



# Inference and spatial autocorrelation

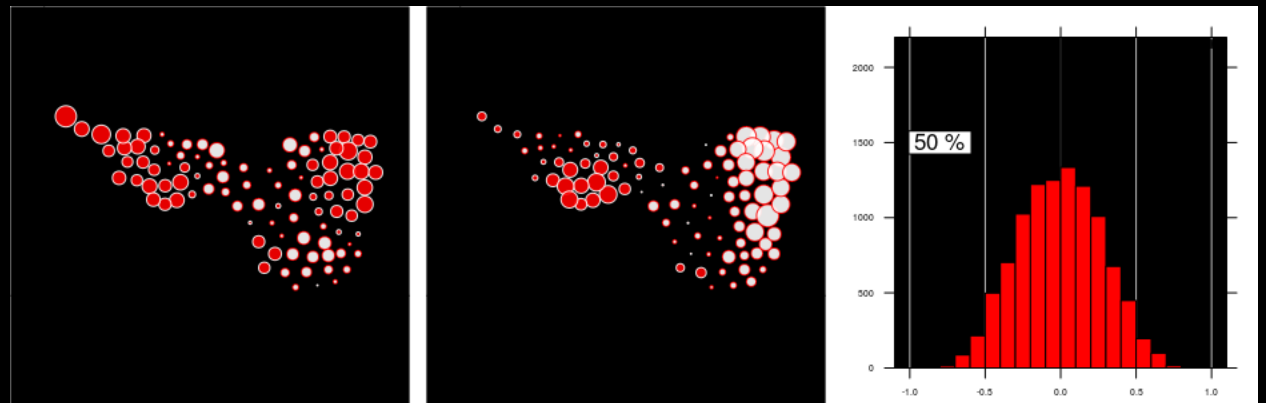
- No spatial structure



- One spatial structure

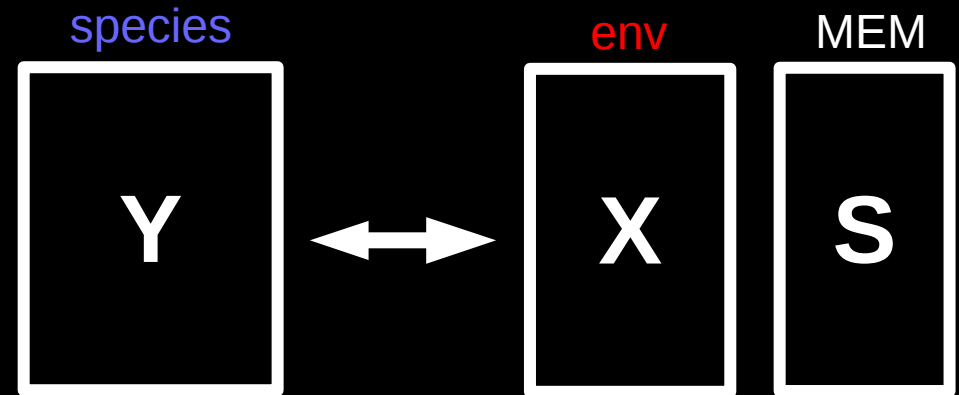


- Two independent spatial structures



# Consequences in ordination

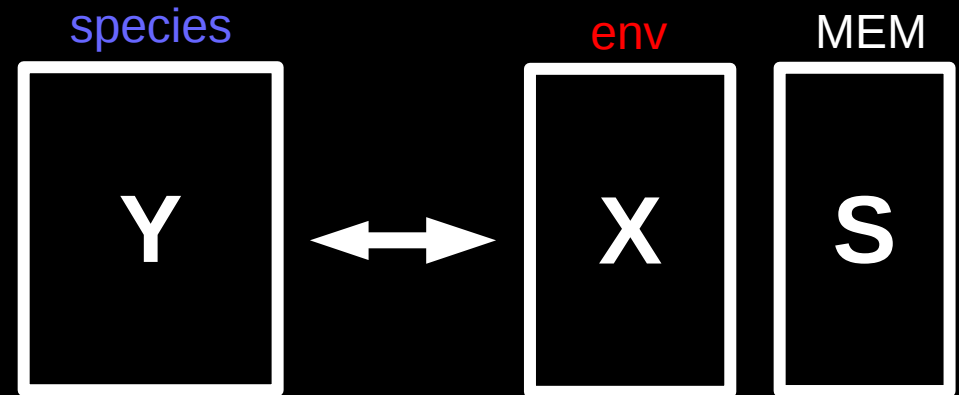
- X and Y independents  
X and Y spatially structured



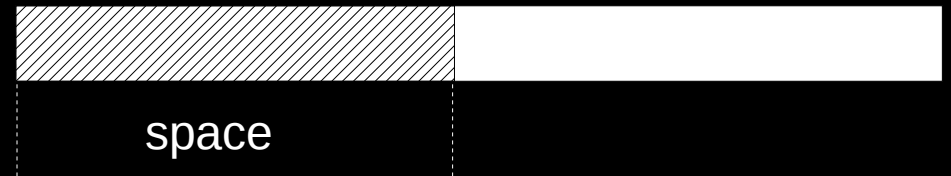


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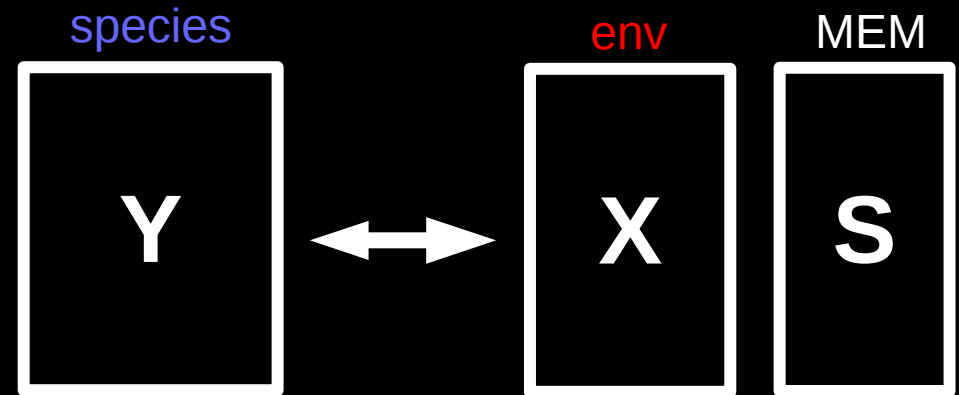


- In theory

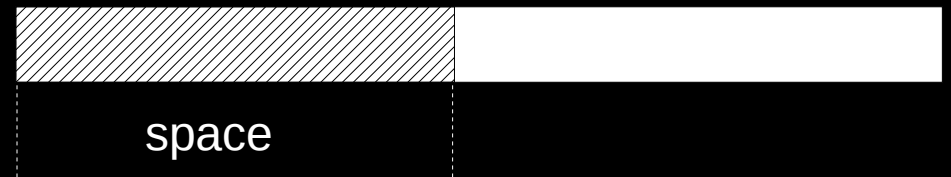


# Consequences in ordination

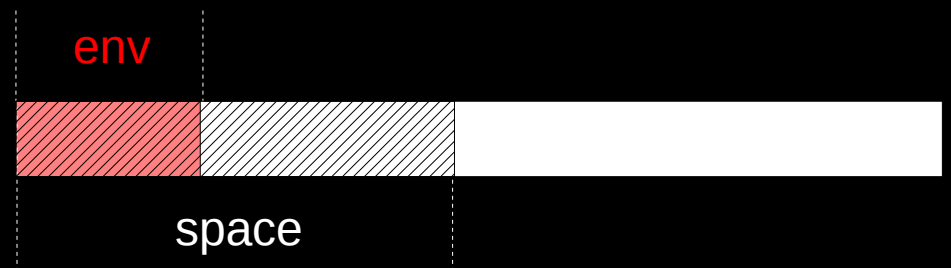
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- In theory

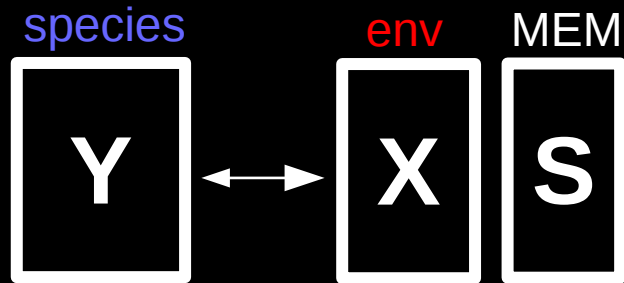


- In practice

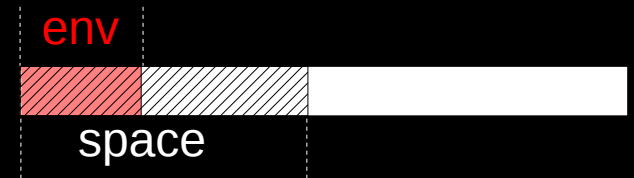


# Constrained null models

- Observed data

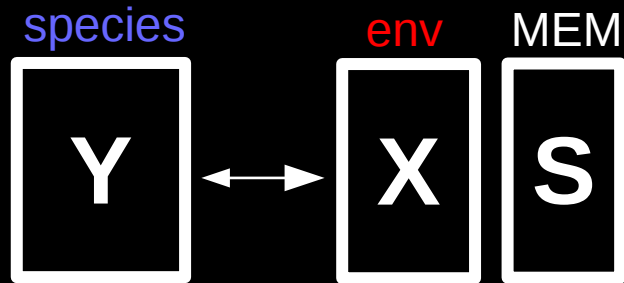


Obs :

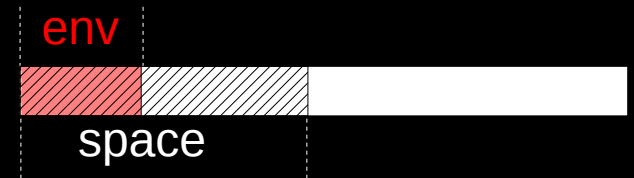


# Constrained null models

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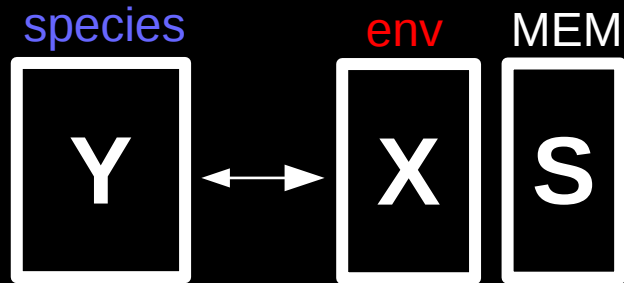
Obs :



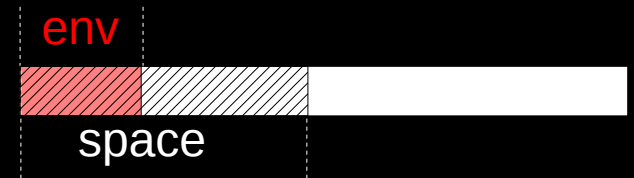
- Simulated data

# Constrained null models

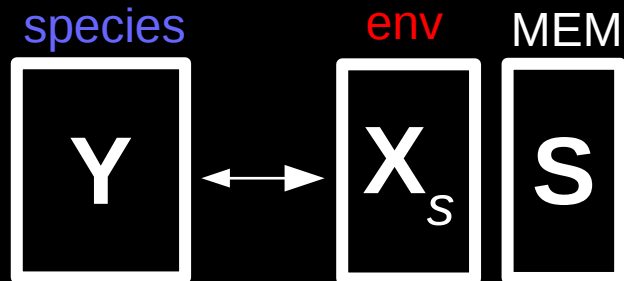
- Observed data



Obs :



- Simulated data

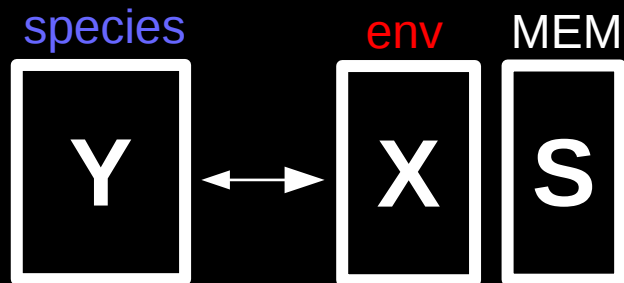


Sim 1 :

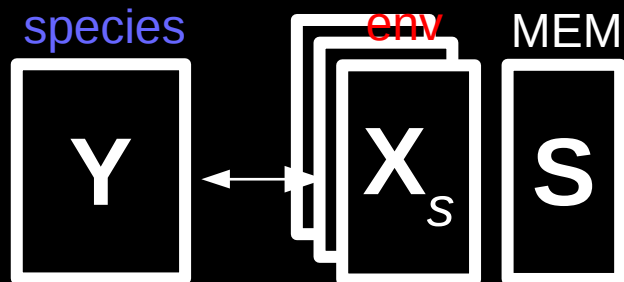


# Constrained null models

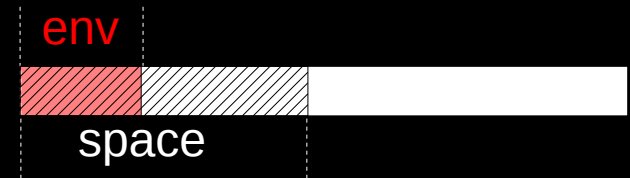
- Observed data



- Simulated data



Obs :



Sim 1 :



Sim 2 :



⋮

⋮

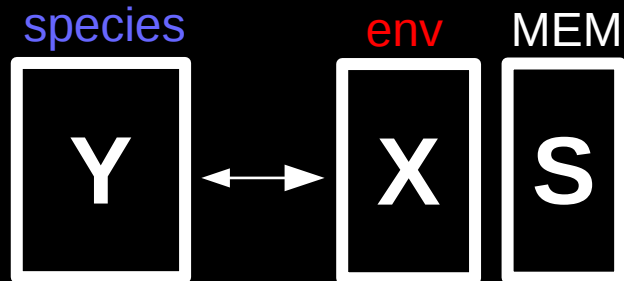
⋮

Sim 999 :

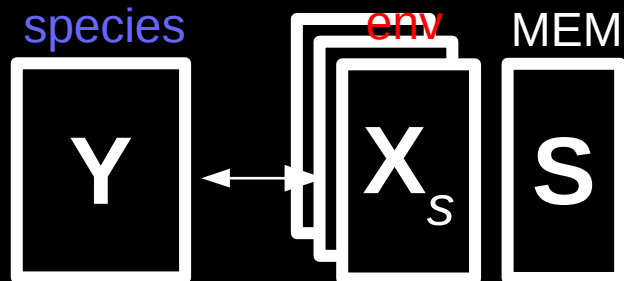


# Constrained null models

- Observed data



- Simulated data

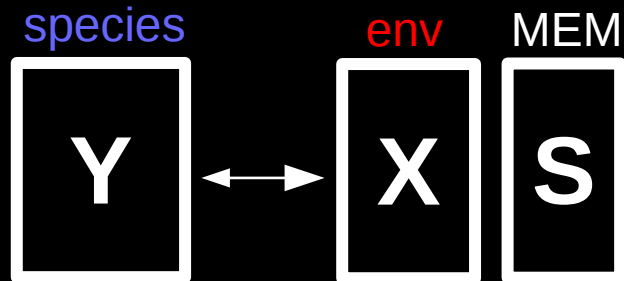


- Comparison

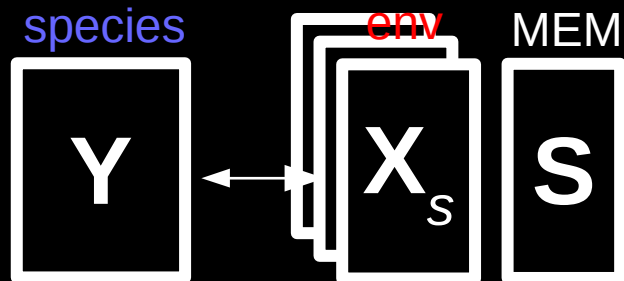


# Constrained null models

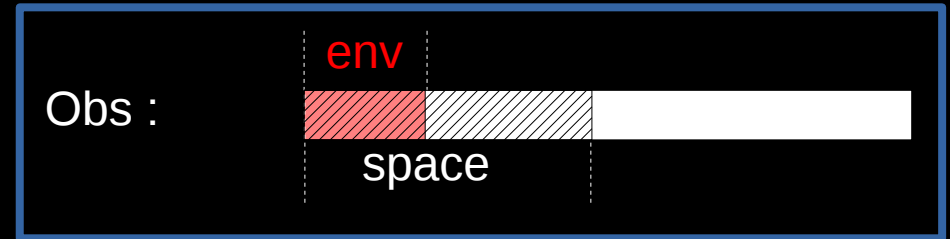
- Observed data



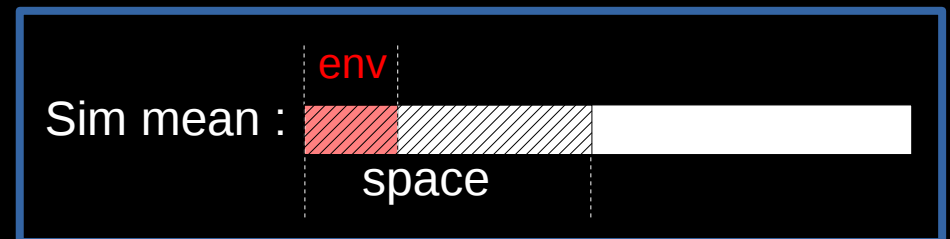
- Simulated data



- Comparison



⋮  
⋮  
⋮





# Moran spectral randomization

Moran's coefficient decomposition :

$$MC(\mathbf{x}) = \sum_{i=1}^{n-1} \lambda_i \text{cor}^2(\mathbf{x}, \mathbf{v}_i)$$

Variable decomposition:

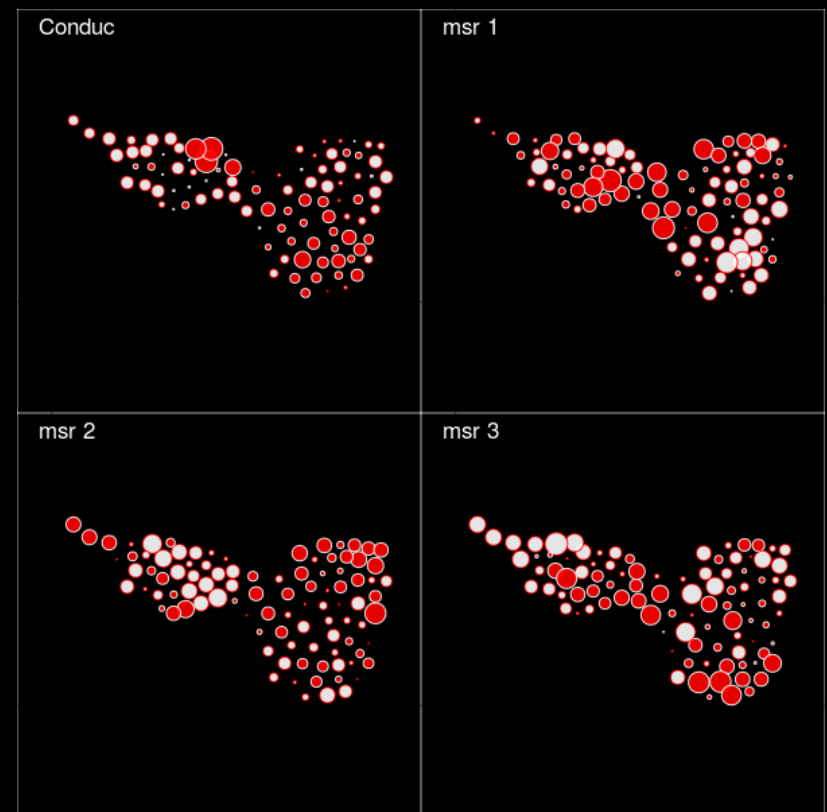
$$\mathbf{x} = \bar{x} + s(\mathbf{x}) \sum_{i=1}^{n-1} \text{cor}(\mathbf{x}, \mathbf{v}_i) \mathbf{v}_i$$

Random replicates:

$$\mathbf{x}_{sim} = \bar{x} + s(\mathbf{x}) \sum_{i=1}^{n-1} a_i \mathbf{v}_i$$

with  $a_i = \pm \text{cor}(\mathbf{x}, \mathbf{v}_i)$

**msr** (**X**, **mymem**)





Pierre Legendre



Guillaume Larocque



Thibaut Jombart



Helene Wagner



Daniel Borcard



Guillaume Blanchet

Naima Madi

Guillaume Guenard

GitHub

<https://github.com/sdray/adespatial>

Vignette

```
vignette("tutorial", package =  
        "adespatial")
```