#### Invariance and Variability of Synonymy Networks

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#### Exploring lexical networks

#### Multidisciplinary team, University of Toulouse: CNRS, IRIT, CLLE-ERSS

- ► NLP: resources building and consolidation: **Wisigoth** [Sajous et al., 2010]
- ► IR, networks of documents and labels: **KODEX** (Quaero) [Navarro et al., 2011]
- ► Cognition: lexicon learning dynamics and medical application [Gaume et al., 2008], metaphor resolution (SLAM)[Desalle et al., 2010]
- Linguistics: lexical networks and language typology [Gaume et al., 2009], Franco-Taiwan project M3

#### Today: issue of comparing the many lexical networks:

- ► High variability of synonymy networks at the edge level...
- ► Reliable resource comparison criterion ?



#### Comparing graphs' vertices

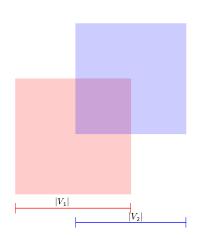
$$|V_1|$$

$$G_1 = (V_1, E_1), \quad G_2 = (V_2, E_2)$$

Lexical coverage :

$$R_{\bullet} = \frac{|V_{1} \cap V_{2}|}{|V_{2}|} \qquad P_{\bullet} = \frac{|V_{1} \cap V_{2}|}{|V_{1}|}$$
$$F_{\bullet} = 2 \cdot \frac{R_{\bullet} \cdot P_{\bullet}}{R_{\bullet} + P_{\bullet}}$$

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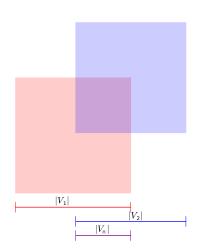


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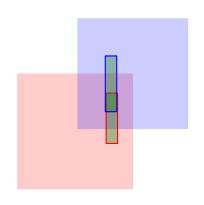
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Reduce graphs to common vertices,

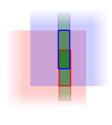
Consider graph as a synonymy judgment,

Use **Kappa** to measure inter judge agreement:

$$K_{\updownarrow}(G'_1, G'_2) = \frac{(p_0 - p_e)}{(1 - p_e)}$$

$$p_0 = \frac{1}{\omega} \cdot (|E'_1 \cap E'_2| + |\overline{E'_1} \cap \overline{E'_2}|)$$

$$p_e = \frac{1}{\omega^2} \cdot (|E'_1| \cdot |E'_2| + |\overline{E'_1}| \cdot |\overline{E'_2}|)$$



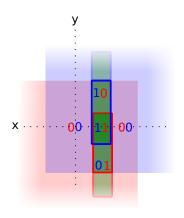
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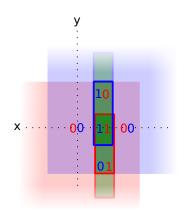
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### Experiment: Comparison of 7 synonymy resources

5 French dictionaries:

(General purpose, paper dictionaries)

- ► Bailly
- ▶ Benac
- Bertaud
- ▶ Larousse
- ▶ Robert

#### 2 English resources:

- Wiktionary
- ► Princeton Wordnet

	n	m	$\langle k \rangle$	n <sub>lcc</sub>	m <sub>lcc</sub>	С	$L_{lcc}$	λ	r <sup>2</sup>
$Bai_V$	3082	3648	2.46	2774	3417	0.04	8.24	-2.33	0.94
$Ben_V$	3549	4680	2.73	3318	4528	0.03	6.52	-2.10	0.96
Ber <sub>V</sub>	6561	25177	7.71	6524	25149	0.13	4.52	-1.88	0.93
Larv	5377	22042	8.44	5193	21926	0.17	4.61	-1.94	0.88
$Rob_V$	7357	26567	7.48	7056	26401	0.12	4.59	-2.01	0.93
$PWN_V$	11529	23019	6.3	6534	20806	0.47	5.9	-2.4	0.90
$Wik_V$	7339	8353	2.8	4285	6093	0.11	8.9	-2.4	0.94

### Results: A Weak Agreement ...

<i>K</i> <sub>↓</sub>	Ben <sub>V</sub>	$Ber_V$	Lar <sub>V</sub>	$Rob_V$	Wik <sub>V</sub>
Bai <sub>V</sub>	0.583	0.309	0.255	0.288	
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Ber <sub>V</sub>			0.416	0.538	
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# What's wrong ??

▶ Why do resources describing the same lexicon appear so different ?

## The picture metaphor (1/2)



Hawthorne bridge, Portland

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Hawthorne bridge, Portland



Each even pixel painted in black...

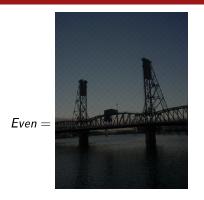


Each **odd** pixel painted in black...

# The picture metaphor (2/2)



## The picture metaphor (2/2)





#### Can you see a difference ?

however...  $sim(A, B) \approx 0$ , when computed at **pixel level**.

### Similarly on graphs: take a step back!

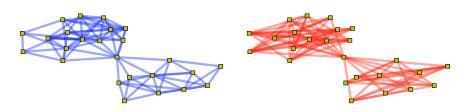
Weak agreement at the **edge level** 

a stronger agreement at a coarser grain level...

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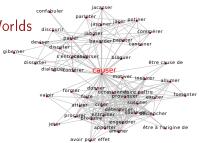


As for the pictures: **no edge in common** between these two graphs.

### How can we look at our graph at different grain levels?

#### Lexical Networks: Hierarchical Small Worlds

- Low density
- Short paths
- Heavy tailed degree distribution
- High clustering coefficient: dense zones



#### Random Walks

- ▶ Idea: if (u, v) are in the same "cluster", they may not be adjacent, but many shorth paths lead from u to v.
  - Random walkers tend to be trapped into clusters,
  - Note: possible approach for clustering

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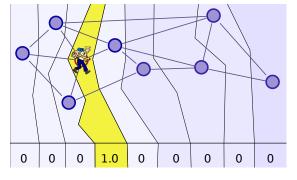
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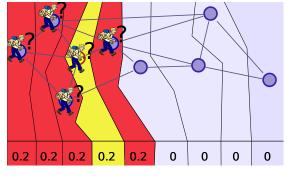
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- $\bullet$  start from a node u,
- walk to a neighbour with equal probability,
- walk to a neighbour with equal probability
- etc...

$$t = 0$$
,  $P^{t}(u, *) = [0, 0, 0, 1.0, 0, 0, 0, 0, 0]$ 

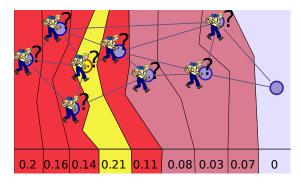




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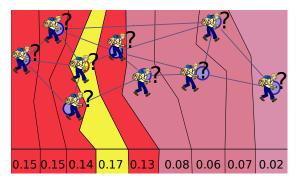
$$t = 1$$
,  $P^{t}(u, *) = [0.2, 0.2, 0.2, 0.2, 0.2, 0, 0, 0, 0, 0]$ 





- start from a node u,
- walk to a neighbour with equal probability,
- walk to a neighbour with equal probability,
- etc..

$$t = 2$$
,  $P^{t}(u, *) = [0.2, 0.16, 0.14, 0.21, 0.11, 0.08, 0.03, 0.07, 0]$ 



- start from a node u,
- walk to a neighbour with equal probability,
- walk to a neighbour with equal probability,
- etc...

$$t = 3$$
,  $P^{t}(u, *) = [0.15, 0.15, 0.14, 0.17, 0.13, 0.08, 0.06, 0.07, 0.02]$ 

#### Strong and weak confluence

▶ **Long walks**: probability of reaching a node v only depends on v's degree:

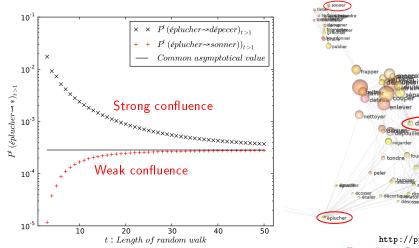
$$\lim_{t \to \infty} P^t(u, v) = \frac{\deg(v)}{\sum_{n \in V} \deg(n)} = \pi_v \tag{1}$$

- ▶ **Short walks**: high probability of staying in a dense zones:
  - $P_t(u, v) > \pi_v$  if u et v in the same cluster: strong confluence
  - $P_t(u, v) < \pi_v$  otherwise: weak confluence

## Illustration of weak and strong confluence (1/2)

Confluences, in  $Rob_V$ , between:

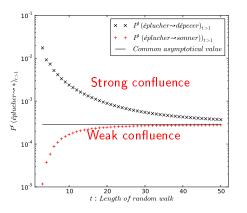
éplucher (peel)  $\leftrightarrow$  dépecer (tear apart) and éplucher (peel)  $\leftrightarrow$  sonner (ring).



décomposer

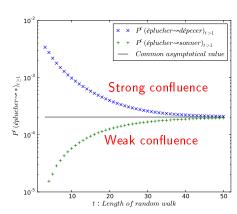
### Illustration of weak and strong confluence (2/2)

In Robert: éplucher (peel)  $\leftrightarrow$  dépecer (tear apart) éplucher (peel)  $\leftrightarrow$  sonner (ring)

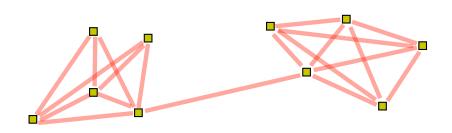


#### In Larousse:

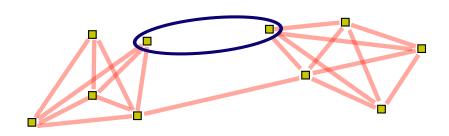
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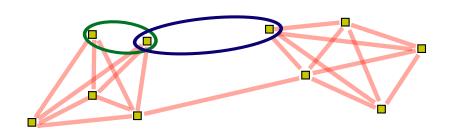
Synonymy	Confluence	
No	weak	Unrelated
No	strong	Potential synonyms
Yes	weak	Shortcut
Yes	strong	Strong synonyms



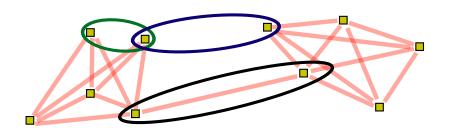
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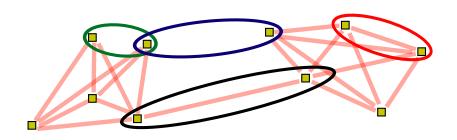
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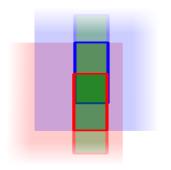


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#### Negotiation:

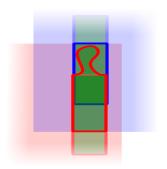
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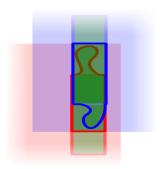
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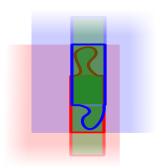
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#### Experimental set up

- ▶ Negociation between pairs of graphs (same POS, same language),
- ▶ Shortest "interesting" walks: t = 2,
- Measure Kappa of graphs after negociation,
- ► Control experiment: negociation of *random graphs* (same edge agreement).

	K <sub>⊥</sub>	$Ben_V$	$Ber_V$	Lar <sub>V</sub>	$Rob_V$	$Wik_V$
	ori.	0.583	0.309	0.255	0.288	
Bai <sub>V</sub>	acc.	0.777	0.572	0.603	0.567	
Daily	ori. r.	0.583	0.309	0.256	0.288	
	acc. r.	0.585	0.313	0.262	0.293	
	ori.		0.389	0.276	0.293	
Pon	acc.		0.657	0.689	0.636	
Ben <sub>V</sub>	ori. r.		0.390	0.276	0.294	
	acc. r.		0.392	0.283	0.301	
	ori.			0.416	0.538	
Por	acc.			0.838	0.868	
Ber <sub>V</sub>	ori. r.			0.417	0.539	
	acc. r.			0.434	0.549	
	ori.				0.518	
Lar	acc.				0.852	
Lar <sub>V</sub>	ori. r.				0.518	
	acc. r.				0.529	
	ori.					0.247
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- ▶ Note: order is not maintained!

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1 00100	ori. r.
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- ► From weak to medium agreement,
- ► Control: random networks fail to improve
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	ori.			0.416	0.538	
Par	acc.			0.838	0.868	
Ber <sub>V</sub>	ori. r.			0.417	0.539	
	1	I	l	1.434	0.549	

- ► From medium to strong agreement,
- ► From weak to medium agreement,
- ► Control: random networks fail to improve.
- ► Note: order is not maintained!

$PWN_V$	acc.		
	ori. r.		
	acc r		

0.247
0.540
0.247

0.518

0.852 0.518

0.529

#### Conclusions and Perspectives

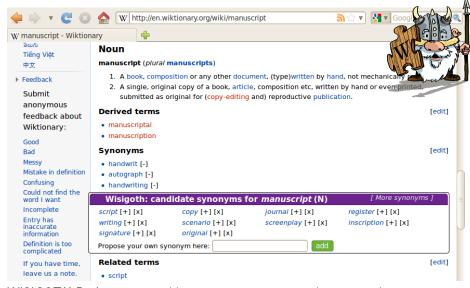
# Global agreement on semantic structures of resource despite pair by pair synonymy variability:

► Semantic disagreemet between structurally different resources

#### Perspectives and applications:

- Merging resources: between union and intersection, filtering shortcuts,
- Evaluating resources:
   Semantic agreement of new resources with (sets of) established resources,
- Bilingual semantic comparison:
   via translation bigraph, SMAC of graphs of different languages,
- ► Semi-automatic **enrichment** of Wiktionary by confluence.

## Application to semi-automatic enrichment of Wiktionary



WISIGOTH Project: http://redac.univ-tlse2.fr/wisigoth/

# Thank you!

Any question?

Desalle, Y., Gaume, B., and Duvignau, K. (2010).

Slam : Solutions lexicales automatique pour métaphores.

CoRR, abs/1002.4820.



Gaume, B., Duvignau, K., Prévot, L., and Desalle, Y. (2008).

Toward a Cognitive Organization for Electronic Dictionaries, the Case for Semantic Proxemy.

In Proceedings of the Workshop on Cognitive Aspects of the Lexicon (COGALEX 2008), pages 86–93, Manchester.



Gaume, B., Duvignau, K., and Vanhove, M. (2009).

Semantic Associations and Confluences in Paradigmatic Networks.

In Vanhove, M., editor, From Polysemy to Semantic Change: Towards a Typology of Lexical Semantic Associations, pages 233–264. John Benjamins Publishing.



Navarro, E., Chudy, Y., Gaume, B., Cabanac, G., and Pinel-Sauvagnat, K. (2011).

Kodex ou comment organiser les résultats d'une recherche d'information par détection de communautés sur un graphe biparti ?

In CORIA'11, Avignon, pages 25-40. ARIA.



Sajous, F., Navarro, E., Gaume, B., Prévot, L., and Chudy, Y. (2010).

Semi-automatic endogenous enrichment of collaboratively constructed lexical resources: Piggybacking onto wiktionary.

In Loftsson, H., Rögnvaldsson, E., and Helgadóttir, S., editors, Advances in NLP, volume 6233 of LNCS, pages 332–344. Springer Berlin / Heidelberg.