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EasyOCaml: Concepts, Implementation and Technicalities

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Abstract

OCaml is not a language well suited for beginners or teaching programming, because error messages are sometimes hard to understand without some practice. *EasyOCaml* equips the OCaml system with a new type checker for a reasonable subset of the *OCaml* language and an adapted parser to make error messages more descriptive. Plugins for reporting errors can be loaded at runtime, to produce output for different settings. Furthermore, *EasyOCaml* adds language levels and teach packs (similar to those of *DrScheme*) to make the language a good choice for teaching programming. All this is integrated in the original OCaml system.

This report describes the ideas and formal and notional foundations of *EasyOCaml* as well as its implementation as a manual and guide to further development.

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1 Objectives and Introduction

Objective Caml (Leroy et al., 2008) is a programming language which unifies functional, imperative and object oriented concepts in a ML-like language with a powerful and sound type system. Its main implementation (<http://caml.inria.fr>) ships with a platform independent byte code compiler and an efficient machine code compiler and there are a lot of existing libraries, which make it a great multi purpose programming language.

Up to now, OCaml is not a language well suited for *learning* and *teaching programming*: It has a very rich type system, but type errors are reported only with few information on the underlying reasons. Some practice is necessary to manage these. On the other hand, OCaml comes with tools (e.g. Stolpmann's *findlib*) which make it easy to handle libraries for developers, but it lacks a fool-proof system to use primed code in programming lessons.

The objectives of this work are, in large, to make OCaml a programming language better suited for beginners and to teach programming. We achieve this by

- improving OCaml's error messages by providing a modified parser and a new type checker.
- equipping OCaml with an infrastructure to make it adaptable for teaching programming, in means of restricting the supported features of the language, or providing code and the startup environment in a simple way of distribution (language levels).
- integrating all that into OCaml's original toplevel and compiler system to take advantage of existing libraries and OCaml's code generation facilities.

The project is hosted at <http://easyocaml.forge.ocamlcore.org> where an online demo of EasyOCaml's type inference and language levels can be found, too.

1.1 Similar Projects

There are some projects which heavily influenced our work:

Haack and Wells (2004) have described and implemented a technique to produce more descriptive type error messages in a subset of SML. Their work is seminal for constraint based type checking with attention on good error reporting and builds the foundation for EasyOCaml's type checker.

Helium (Heeren et al., 2003) is a system for teaching programming in Haskell. In a similar manner, type checking is done via constraint solving. Furthermore, it features detailed error messages including hints how to fix errors based on certain heuristics.

Finally, *DrScheme* (Felleisen et al., 1998) is a programming environment for the Scheme language that is build for teaching programming. It has introduced the concept of language levels and teach packs to restrict the syntax and broaden functionality especially for exercises.

EasyOCaml uses and combines ideas of all these project for the attempt to make *OCaml* better suited for learning and teaching programming.

1.2 Supported Language

EasyOCaml targets to be usable not only for the very first steps in programming, so it supports a reasonable subset of the *OCaml* language. This language can be characterized as “Caml without module declarations”, hence its designation *Caml_m*.

Unlike simpler functional programming languages like *Scheme* with only a single syntactic category *expression*, *OCaml* makes a distinction between *structure items*, *expressions* and *patterns*.

Here is the supported language features in more detail, which also can be pruned by teach packs. See section 7 for a complete grammar.

Structure items

OCaml programs consist of a list of *structure items*, which are used to declare values, types and exceptions. Expressions occur only as a part of structure items. *EasyOCaml* supports

- Optionally parametrized *type declarations* of type synonyms, records with optionally mutable fields and variant types.
- *exception declarations* like in *OCaml*.
- optionally recursive (**rec**) and multiple (**and**) *value declarations*, where binding occur with arbitrary patterns. Note, that a language level can coerce require type annotations of those toplevel value declarations.
- Toplevel evaluations. Note that the toplevel evaluation of **e** is just syntactic sugar for **let _ = e**.

Core types

Direct combinations of existing types are called *core types* in *OCaml*. *EasyOCaml* allows as core types primitive types (**int**, **char**, **string** and **float**), free and bound type variables, type arrows (types of functions), tuples and type constructors, i.e. application of parametrized types.

Expressions

Expressions are parts of a program that can be evaluated to a *OCaml* value. *EasyOCaml* supports simple expressions that can be found in *MiniML*, too, like variables, functions, infix operators, conditionals and variable binding.

Despite those, it features construction of tuples, records and variants, conditionals with optional **else** branch, **while** and **for** loops, sequences of expressions, exception handling (throwing and catching) as well as type annotations.

Patterns

In *EasyOCaml*, pattern matching is possible in every place where it works in *OCaml*, i.e. value matching (`match ... with pat -> ... | ...`), in variable bindings (`let pat = ...`), in functional abstractions with `function` (`function pat -> ... | ...`) and exception catching (`try ... with pat -> ... | ...`).

Pattern matching works for every possible value in *EasyOCaml*, i.e. primitive values, tuples, variants and records¹.

Goals of this report

This report is split in a less formal part I which is easily readable and a more formal part which acts as a reference for the user and developer. This report has four goals:

Firstly to present *EasyOCaml* and the concepts used in and developed for it (target audience: the users) through section 2–5. Then, it describes the usage of the programs `ecam1` and `ecam1c` for usage in section 6. Afterwards it combines the concepts with the actual implementation and describes its architecture in code (target audience: the developers) in section 8. Finally, formal foundations for the type checker are given the section 9 (target audience: the interested readers).

¹version 0.49 lacks the implementation for pattern matching on the latter

Part I

Concepts and design

2 Constraint Based Type Inference

The type inference currently used by OCaml has the algorithm \mathcal{W} by Milner (1978) at its core. Although it is very efficient and broadly extended to OCaml's requirements, it lacks sort of a memory: For example, inferring the type of a variable is done by accumulating (unifying) information on its usages while traversing the abstract syntax tree (AST). Broadly spoken, a type constructor clash is detected as the usage just inspected contradicts the information collected so far. Therefore, OCaml's type checker cannot report any *reasons* for a type error but reports only the location where the error became obvious to the type checker. Much work while debugging type errors in OCaml comprises of manually searching for other usages of the mis-typed variable in the program which might have lead to the type constructor clash.

2.1 Haack & Wells

Haack and Wells (2004) describe an algorithm which exceeds the algorithm \mathcal{W} in two ways: Firstly, every type error report contains information on exactly those locations in the program which are essential to the error, by means of dropping it would vanish the error. Secondly, it is able to report all type errors in a program at once (whilst locations which are involved in several type errors are most notable the source of the errors, by the way).

In a sense, algorithm \mathcal{W} does two things at once while traversing the AST: it generates type information on the variables and unifies it with existing type information anon. Haack & Wells' algorithm works by separating these steps.

During *constraint generation* every node of the AST gets annotated with a type variable. While traversing the AST, information on these type variables is collected from the usage of each node. This information is stored as a set of constraints on the type variables.

The intention is the following: If they are *unifiable* the resulting substitution represents a valid typing of the program with respect to the type variables of the nodes.

Otherwise, the program has at least one type error. But now, the collected type information is still available as a set of constraints and enables the algorithm to reexamine the errors in a second stage of *error enumeration and minimization*: Error enumeration is basically done by systematically removing constraints grounded at one program location from the constraint set and running unification again. Haack and Wells (2004) also present an iterative version of this algorithm which is implemented in EasyOCaml. Although it avoids recomputation of the same errors over and over again, error enumeration has nevertheless exponential time consumptions. Thus error enumeration delimited to a given time amount which can be specified by a environment variable (see 6.2).

The result of error enumeration is a set of errors, each represented as a complete set of locations whose nodes in the AST have to the error (*complete* in being a superset of the locations which caused the type error). By application of error minimization on each error, the algorithm further guarantees *minimality* of the reported errors in the sense that removing the constraints annotated with a location would vanish the error itself.

In addition to type errors, Haack and Wells' technique also enables the type checker to collect unbound variables in the program while generating. Their types are assumed as a free variable to avoid a type error, but unbound variables are reported with the type errors after error enumeration.

2.2 Extensions for EasyOCaml

Haack and Wells (2004) comes with constraint generation rules only for *MiniML*, i.e. variables, infix operations, functional abstraction, application and local polymorphic variable bindings. This is good to describe the algorithms involved, but we had to extend it to the language *Caml_m* as loosely described in section 1.2 and more formally in section 7. I will describe the constraint generation rules for *EasyOCaml* by example here, take a look into section 9 for the complete set of rules.

In the following, Δ always denotes an environment for variables, record fields and variant constructors, with access by $\Delta|_{\text{id}}$, $\Delta|_{\text{var}}$, $\Delta|_{\text{rec}}$ and $\Delta|_{\text{var}}$ respectively. To capture the possibility to *declare* values and types, constraint generation rules for structure items have the form

$$\Delta; \text{strit} \Downarrow_s \langle \Delta', C, u \rangle.$$

Δ denotes the environment which contains declarations in the program so far, *strit* denotes the current structure item. Δ' denotes the environment Δ extended by declarations in *strit* and C is a set of constraints collected in *strit*. Finally, u is a set of errors in *strit* which are described in 3.1.

This is the rule for the declaration of a variant type:

$$\frac{\text{VARIANT DECL} \quad \Delta' = \Delta|_{\text{var}}[t \mapsto \{\langle K_1, ty_1 \rangle^{l_1}, \dots, \langle K_n, ty_n \rangle^{l_n}\}^{l_l}]}{\Delta; (\text{type } t = K_1 \text{ of}^{l_1} ty_1 \mid \dots \mid K_n \text{ of}^{l_n} ty_n)^l \Downarrow_s \langle \Delta', \emptyset, \emptyset \rangle}$$

It just extends the current environment Δ with the variant constructors K_1 to K_n with the given types.

...

EasyOCaml features type annotations of the form $(\text{t}:\text{ct})$. OCaml's current type checker ignores the type annotations whilst unification by using the term's inferred type and only checks its validity later on. So type inference and error reporting makes no use of the type annotations itself. In contrast, EasyOCaml assumes terms to have the denoted type while type checking, type checks the term isolated and tests the validity afterwards by proving that the annotated type is a subtype of the inferred type.

...

EasyOCaml facilitates references and mutable data.

...

EasyOCaml collects as many errors as possible.

- records ...
- variants ...
- type annotations ...
- references ...

See section 9 for a complete list of inference rules used in *EasyOCaml*.

3 Errors and Error Reporting Adaptability

EasyOCaml is essentially build for teaching programming . A such special attention is paid to the way errors are reported to achieve the following goals:

Firstly, errors should provide a right amount of details, too few information is of course insufficient, but also too much information can be confusing. So, for example in type constructor clashes exactly those locations are reported, which are essential to the error. Delivering more information on the reasons of type errors is exactly what *EasyOCaml*'s type checker is made for.

Secondly, error reporting should be adaptable: For a beginner, reading errors in a foreign language can distract or even prevent him from understanding an error. Furthermore, the error output should be adaptable in its overall structure to serve as the input for different kinds of presentation, e.g. plain text on command line or HTML to display it in a web browser.

The last section has explained the improvements of *EasyOCaml* to type error messages. I will describe the changes to the parser to build a foundation to include more information with the parsing errors below and the error adaption possibilities subsequently.

3.1 Errors in *EasyOCaml*

3.2 New Errors for *Camlp4*

As mentioned, *EasyOCaml* parses its input with a *Camlp4* parser. Unfortunately, *Camlp4*'s error messages are hard coded in English and never represented in data. This is because *Camlp4* is a OCaml stream parser in its core, and this requires parsing errors to be reported as exceptions which only allow just a string for information².

Nevertheless, we supplied *Camlp4* with a new error reporting system, up to now just to make error reporting adaptable, but it should be possible now to augment the information of parse errors with more information on the state of the parser. A parsing error³ is one of the following:

²exception `Stream.Error` of `string`

³type `ParseError.t`

`Expected (entry, opt_before, context)` is raised if when the parser stuck while parsing a phrase: `entry` describe the categories of the possible, expected sub-phrases, `opt_before` might describe the category of the entry just parsed and `context` denotes the category of the phrase which contains the entry.

`Illegal.begin sym` is raised when the parser is not able to parse the top categories described by `sym`.

`Failed` is raised only in `Camlp4.Struct.Grammar.Fold`.

`Specific_error err` Beside the generic parsing errors just mentioned, it is possible to extend the parsing errors per language by “artificial” errors which are specific to a language, e.g. curried constructor in OCaml, which is not represented in the grammar but checked in code. (further errors for EasyOCaml are specified in subsection 8.8.)

How are these errors represented in the string information of the stream error? Not without a hack, which is luckily hidden behind the interface of `Camlp4`: Internally, the parsing exception contains a string of the format “<msg>\000<mrsh>” where <msg> is the usual `Camlp4` error message and <mrsh> is the marshalled parsing error as just described. This string is again decomposed in the interface function for parsing⁴, and reported as a parsing error⁵ to the user.

And so `Camlp4`’s parsing errors now represented in data to apply error reporting adaptabilities and to further extend it to contain more informations.

3.3 Adaptability

For internationalization of error messages and different structures of error messages for different display settings, EasyOCaml provides adaptability of error messages by a plugin system. Error reporting plugins should use `EzyError`’s internationalized functions to output the error’s description (`EzyErrors.print*_desc`) to keep them uniform but can print it any structure: Currently, a plain text format is default and a HTML printer which highlights the locations of an error in source code and a XML/Sexp printer for usage in an IDE are delivered with EasyOCaml.

The user can register an error printer via the command line flag `-easyerrorprinter`. The module is dynamically linked and registers itself with `EzyErrors.register` where appropriate functions are overwritten.

The following section describes the tools which EasyOCaml provides specifically for teaching programming.

⁴function `Camlp4.Struct.Grammar.Entry.action_parse`

⁵type `ParseError.t`

4 Language Levels and Teachpacks

Language levels are a facility to describe the initial state of the EasyOCaml compiler or toplevel system in means of the environment which is accessible to the user and the available syntax. Language levels are useful for teaching programming, as they can be designed just for specific exercises – probably providing an easy interface to some advanced API and restrictions on the syntactic elements taught so far, to avoid syntax errors regarding unknown syntactic elements.

Here is in more detail, what language levels can define: The available *syntactic features*. One can specify the syntactic elements which are allowed for patterns, expressions, structure items and type declarations, in high detail. Currently, most of these restrictions are implemented by deleting the according entries from the grammar (thanks to the power of Camlp4!). However, some features like mandatory type annotations for toplevel values are checked afterwards while importing the AST to EasyOCaml's AST.

Settings of *path inclusion* and *object loading and opening*. Teach packs can specify the directories which are included for searching objects, just like the `-I` command line flag. A teach pack can contain objects itself and the specification which have to be loaded (just like putting them on the command line). Furthermore, teach packs can specify which modules are opened on startup.

Teach packs can specify the settings for path inclusion and object loading. Whereas only one language level can be loaded, teach packs can extend a possible language level.

The user can specify which language level and teach pack to use by the `-easylevel` and `-easyteachpack` command line parameter respectively. EasyOCaml then searches for it in the following directories:

The idea of teach packs and language levels is taken from DrScheme. See <http://docs.plt-scheme.org/drsch> for more information.

5 Forecast and Conclusion

EasyOCaml in version 0.5 is not yet full ready for action. For version 1.0, we will add installation procedures for language levels and teachpacks. Furthermore, we will equip the errors with more informations such that error reporting plugins can use certain heuristics to give hints how to fix an error (i.e. to pass the variable environment to check misspellings for unbound variable errors). In a long term, a dynamically typed interpreter would be great for the very first lessons in programming without the need to think about types as well as support for module declarations to make EasyOCaml ready in our daily programming.

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Part II

Manual, formalities and implementation

6 The user interface (manual)

This section describe the extensions of the `ocaml` and `ocamlc` programs.

6.1 Command line parameters

There are some command line flags to control *EasyOCaml*:

`-easy` This flag enables *EasyOCaml* and is obligatory for usage of all other command line flags described here. It enables an alternative type checking algorithm wich gives more information on the type errors.

`-easyteachpack <teachpack>` Enables a teachpack named `<teachpack>`.

6.2 Environment variables

`EASYOCAML_ENUM_TIMEOUT` The real value controls the maximal amount of time *EasyOCaml* may use to enumerate type errors (note, that the underlying algorithm has exponential time consumptions).

6.3 The EasyOCaml directory

EasyOCaml searches for language levels and teachpacks in a designated configuration directory.

There is a global and a user configuration directory. First, *EasyOCaml* searches the user then the global configuration directory. Here's how the global configuration directory is determined (in descending preference):

1. Environment variable `EASYOCAML_GLOBAL_DIR`
2. Compile-time option

Here's how the user configuration directory is determined (in descending preference):

1. Environment variable `EASYOCAML_USER_DIR`
2. `$HOME/.easyocaml`

EasyOCaml's configuration directory must have the following structure:

```
language-levels/level-1
                  level-2
                  ...
teachpacks/tp-1
              tp-2
              ...
```

Each language level and teach pack contains a module `LANG_META` which is loaded into EasyOCaml.

The diagram illustrates the LR(0) automaton for the grammar. It consists of several states (boxes) and transitions (arrows):

- States:**
 - `prim_type` (top left)
 - `type_var` (top left, below `prim_type`)
 - `core_type` (middle left)
 - `core_type` (middle right)
 - `core_type` (bottom left)
 - `core_type` (bottom middle)
 - `longident` (bottom right)
- Transitions:**
 - From the start state (implied by an incoming arrow) to `prim_type` and `type_var`.
 - From `core_type` (middle left) to `core_type` (middle right) on the symbol `*`.
 - From `core_type` (middle right) to `core_type` (middle left) on the symbol `*`.
 - From `core_type` (middle left) to `core_type` (bottom left) on the symbol `(`.
 - From `core_type` (bottom left) to `core_type` (bottom middle) on the symbol `(`.
 - From `core_type` (bottom middle) to `core_type` (bottom left) on the symbol `,`.
 - From `core_type` (bottom middle) to `core_type` (middle right) on the symbol `,`.
 - From `core_type` (middle right) to `core_type` (bottom middle) on the symbol `,`.
 - From `core_type` (bottom middle) to `core_type` (middle right) on the symbol `,`.
 - From `core_type` (middle left) to `longident` on the symbol `longident`.
 - From `core_type` (bottom left) to `longident` on the symbol `longident`.
 - From `core_type` (bottom middle) to `longident` on the symbol `longident`.
 - From `core_type` (middle right) to `longident` on the symbol `longident`.

8 Details of the Implementation

8.1 Outline of EasyOCaml's Pipeline

Here is a rough outline of EasyOCaml's pipeline which is quite similar for both the compiler and the toplevel:

1. Command line flags are evaluated to check the “`-easy`” flag and an error printer and possibly load a teach pack and/or language levels. See section 6.1 for information on the command line flags.
2. `EzyCamlgrammar` parses the AST from the input, possibly respecting restrictions from the language level which yields an `EzyAst.imported_structure`.
3. `EzyGenerate` generates constraints from the AST (involving type information from the default environment and modules loaded by command line or teach packs/language levels). This yields a quadruple `generated_structure * AtConstrSet.t * PostProcess.t` where
 - `generated_structure` is the AST annotated with type variables and unique identifiers.
 - `AtConstrSet.t` is a set of constraints on the type variables in the AST.
 - `PostProcess.t` is build gradually during constraint generation and contains sets of different types of errors (from `EzyErrors`) as well as checks which can only processed after constraint unification (i.e. type annotations)
 - `EzyEnv.t` is used to keep track of local variables and after constraint generation contains information on the global types and values of the program.
4. `EzyTyping.solve` tries to solve the generated constrains. If solving succeeds, the program is typed by a substitution on the variables in the generated AST and the environment and contains type errors otherwise.
5. The last step, reimporting the `EzyEnrichedAst.generated_structure` with typing information given by type substitution to OCaml's original typed tree is not yet done. We type the code again with OCaml's original type checker and compare the result to verify its correctness.

The goal of this section is to describe roughly the modules implemented for EasyOCaml and locate functions for the EasyOCaml's steps in 1.

8.2 Utilities and Miscellaneous

Two rather independent modules for code used in EasyOCaml

EzyUtils Functionality which is not specific to EasyOCaml, but extends the standard library (String, Set, Map). It contains also code copies from existing Libraries (from Core: Option, Monad, T2, T3, T4, such that EasyOCaml adds no dependencies

at bootstrap time) and new code for Logging and some more (lexical comparison, tools on functions).

EzyMisc EasyOCaml-specific code which is used at different locations in the project.

EzyOcamlmodules Extensions of the modules from the standard OCaml system (e.g. Location, Path, Longident, Types, ...) as well as sets and maps over these.

The rest of the modules contains the code for the EasyOCaml implementation:

8.3 Error Reporting

EasyOCaml offers sophisticated facilities to represent errors, to allow as detailed error reporting as possible. Furthermore, new error reporting plugins can be registered.

EzyErrorReportUtils Code for type error slicing (described in Haack & Wells), i.e. slicing an AST to only contain nodes from locations given in a set, substituting the rest with ellipses.

EzyErrors Representation (types) of errors which can occur in EasyOCaml, functions for pretty printing errors as well as functions for error reporting plugins to register themselves.

8.4 Teachpacks and Language Levels

EzyConfig Constants of the teach pack system (e.g. the name of the module describing the teach pack or language level) and functions to find a teach pack or language level in the file system.

EzyDynload Superset of functionality for loading teach packs and language levels (used by EzyLang)

EzyLang Functions for loading language levels and teach packs (used by EzySetup)

EzyTeachpack Shortcut to EzyFeatures and registering of the teach pack. Actual teach packs should only need to link against this module.

EzyLangLevel Shortcut to EzyFeatures and registering of the language level. Actual language levels should only need to link against this module.

EzySetup Process command line flags regarding language levels and teach packs and provide the actual setup of features, modules, included directories and object files given by teach packs and language levels to other parts of EasyOCaml.

8.5 Abstract Syntax Tree

The following modules contain representation, manipulation, parsing and restrictions on EasyOCaml's AST.

EzyFeatures In EasyOCaml, the available syntax can be restricted. This module contains types to describe these restrictions and some functions to generate defaults (i.e. settings where everything is forbidden or allowed).

EzyAsttypes Adaption of Asttypes from the standard OCaml system.

EzyAst Representation of the AST in EasyOCaml. Each node is parametrized on some data it contains. This is `unit` for a parsed tree and typing information (mainly the type variable) for a parsed tree after constraint generation. Furthermore, each syntactic category can be some “dots” which is only used in type error slicing.

EzyCamlgrammar The EasyOCaml Parser as a Camlp4 extension of `Camlp4OCamlParser`. It just deletes some entries in the latter (partially depending on the given features).

EzyEnrichedAst This module directly belongs to **EzyAst** but we had to outsource it because of module dependencies between **EzyErrors**. It contains

- definitions of the AST after constraint generation import functions from
- OCaml's standard Parsetree respecting given restrictions from **EzyFeatures**
- comparison of two ASTs which is used to compare OCaml's typing and EasyOCaml's typing afterwards

8.6 Type Constraints

EzyTypingCoreTypes Contains base types for the constraints and their generation, closely related to the data described in Haack & Wells (type variables, types, type substitutions, intersection types, type environments)

EzyConstraints Here are constraints annotated with only one location (`AtConstr.t`) and constraints with sets of locations (`Constr.t`) defined, as well as set and maps of those. Furthermore a derived environment as described in Haack & Wells is defined.

EzyGenerate There is a function for every syntactic category to generate constraints and/or errors.

8.7 Typing

EzyTyping Unification of constraint set which yield a substitution on the variables and error enumeration and minimization as described by Haack & Wells. It furthermore contains the typing functions for structures which are used in the compiler and toplevel.

EzyEnv The `EzyEnv.t` is the typing environment for EasyOCaml. Information on declared types and types of local and global variables is hold. It is build up while constraint generation (`EzyGenerate`) in combination with the type variable substitution resulting from `EzyTyping.solve`.

8.8 Camlp4

OcamlSpecificErrors

9 Typing Rules for EasyOCaml

This section describes the rules for type inference used in EasyOCaml. See section 2.2 for some introducing text. The rules have the following form.

- for expressions $\Delta; \text{lexp} \Downarrow_e \langle ty, C, u \rangle$
- for structure items $\Delta; \text{strit} \Downarrow_s \langle \Delta, C, u \rangle$
- for rules $\Delta; \text{pat} \rightarrow \text{lexp} \mid \text{rules} \Downarrow_r \langle ty_p, ty_e, C, u \rangle$ (just an auxiliary)
- for patterns $\Delta; \text{pat} \Downarrow_p \langle ty, C, b \rangle$ where b maps identifiers to $\langle ty \rangle^l$.

We use the following notations, to keep the rules short: C denotes a set of constraints, a a type variable, ty a type, u a set of identifiers and Δ a general environment. A general environment Δ encapsulates environments for lookup of the

- type of a variable:

$$\Delta|_{\text{id}}(lid) = \langle ty, \varpi, C \rangle^l$$

where $\varpi \in \{\text{mono}, \text{poly}\}$ and lid has been bound accordingly.

- types of record fields:

$$\Delta|_{\text{rec}}(f) = \langle ty_r, ty_f, \mu \rangle$$

where ty'_f is the type of field f in record type ty'_r and ty_f, ty_r are fresh variants of ty'_f, ty'_r . $\mu \in \{\text{mutable}, \text{immutable}\}$

- types of variants

$$\Delta|_{\text{var}}(K) = \langle ty_r, [ty_1, \dots, ty_n] \rangle$$

where ty'_1, \dots, ty'_n are the arguments for variant k of type ty'_r and ty_1, \dots, ty_n, ty_r are fresh variants of $ty'_1, \dots, ty'_n, ty'_r$.

$\Delta|_X[x \mapsto y]$ designates the general environment Δ where x is substituted by y in the encapsulated environment X .

$\Delta|_{\text{id}}[b, C, \varpi]$ is a shorthand for $\Delta|_{\text{id}}[id \mapsto \langle ty, \varpi, C \rangle^l \mid id \mapsto \langle ty \rangle^l \in b]$, i.e. the substitution of all bindings of b in Δ with constraints C where b maps identifiers to $\langle ty \rangle^l$.

9.1 Structure items

$$\frac{\text{EVAL} \quad \Delta; \text{lexp} \Downarrow_e \langle ty, C, u \rangle}{\Delta; \text{lexp} \Downarrow_s \langle \Delta, C, u \rangle}$$

VALUE DECL

$$\begin{array}{c}
\Delta; \text{pat}_i \Downarrow_p \langle \text{ty}_{p,i}, C_{p,i}, b_i \rangle \quad \Delta; \text{exp}_i \Downarrow_e \langle \text{ty}_{e,i}, C_{e,i}, u_i \rangle \\
\varpi_i := \text{poly if value lexp}_i \text{ else mono} \quad C_{x,i} := C_{p,i} \cup C_{e,i} \cup \{ \text{ty}_{p,i} \stackrel{l}{=} \text{ty}_{e,i} \} \\
\Delta' := \Delta|_{\text{id}}[b_i, C_{x,i}, \varpi_i \mid i = 1, \dots, n] \quad \text{dom}(b_i) \cap \text{dom}(b_j) = \emptyset \text{ for all } i \neq j \\
\hline
\Delta; (\text{let pat}_1 = \text{lexp}_n \text{ and } \dots \text{ and pat}_n = \text{lexp}_n)^l \Downarrow_s \langle \Delta', \bigcup_{i=1}^n C_{x,i}, \bigcup_{i=1}^n u_i \rangle
\end{array}$$

REC VALUE DECL

$$\begin{array}{c}
\Delta|_{\text{var}}[x_j \mapsto \langle a_j, \text{mono}, \emptyset \rangle^l \mid j = 1, \dots, n]; \text{lexp}_i \Downarrow_e \langle \text{ty}_i, C_i, u_i \rangle \\
\varpi_i := \text{poly if value lexp}_i \text{ else mono} \\
\text{for } i=1, \dots, n \quad \Delta' := \Delta|_{\text{var}}[x_i \mapsto \langle \text{ty}_i, \varpi_i, C_i \cup \{ \text{ty}_i \stackrel{l}{=} a_i \} \rangle^l \mid \text{for } i = 1, \dots, n] \\
a_1, \dots, a_n \text{ fresh} \quad x_i = x_j \text{ iff } i = j \\
\hline
\Delta; (\text{let rec } x_1 = \text{lexp}_n \text{ and } \dots \text{ and } x_n = \text{lexp}_n)^l \Downarrow_s \langle \Delta', \bigcup_{i=1}^n C_{x,i}, \bigcup_{i=1}^n u_i \rangle
\end{array}$$

RECORD DECL

$$\begin{array}{c}
\Delta' = \Delta|_{\text{rec}}[t \mapsto \{ \langle f_1, \text{ty}_1 \rangle^{l_1}, \dots, \langle f_n, \text{ty}_n \rangle^{l_n} \}^l] \\
\hline
\Delta; (\text{type } t = \{ f_1 :^{l_1} \text{ty}_1; \dots; f_n :^{l_n} \text{ty}_n \})^l \Downarrow_s \langle \Delta', \emptyset, \emptyset \rangle
\end{array}$$

VARIANT DECL

$$\begin{array}{c}
\Delta' = \Delta|_{\text{var}}[t \mapsto \{ \langle K_1, \text{ty}_1 \rangle^{l_1}, \dots, \langle K_n, \text{ty}_n \rangle^{l_n} \}^l] \\
\hline
\Delta; (\text{type } t = K_1 \text{ of}^{l_1} \text{ty}_1 \mid \dots \mid K_n \text{ of}^{l_n} \text{ty}_n)^l \Downarrow_s \langle \Delta', \emptyset, \emptyset \rangle
\end{array}$$

SEQUENCE

$$\begin{array}{c}
\Delta; \text{strit}_1 \Downarrow_s \langle \Delta', C_1, u_1 \rangle \quad \Delta'; \text{strit}_2 \Downarrow_s \langle \Delta'', C_2, u_2 \rangle \\
\hline
\Delta; \text{strit}_1 ;; \text{strit}_2 \Downarrow_s \langle \Delta'', C_1 \cup C_2, u_1 \cup u_2 \rangle
\end{array}$$

9.2 Rules

$$\begin{array}{c}
\Delta; \text{pat} \Downarrow_p \langle \text{ty}_p, C_p, b \rangle \quad \Delta|_{\text{id}}[b, C_p, \text{mono}]; \text{lexp} \Downarrow_e \langle \text{ty}_e, C_e, u \rangle \\
\hline
\Delta; \text{pat} \rightarrow \text{lexp} \Downarrow_r \langle \text{ty}_p, \text{ty}_e, C_p \cup C_e, u \rangle
\end{array}$$

$$\begin{array}{c}
\Delta; \text{pat} \rightarrow \text{lexp} \Downarrow_r \langle \text{ty}_{p,1}, \text{ty}_{e,1}, C_1, u_1 \rangle \quad \Delta; \text{rules} \Downarrow_r \langle \text{ty}_{p,2}, \text{ty}_{e,2}, C_2, u_2 \rangle \\
C = \{ a_p \stackrel{l}{=} \text{ty}_{p,1}, a_p \stackrel{l}{=} \text{ty}_{p,2}, a_e \stackrel{l}{=} \text{ty}_{e,1}, a_e \stackrel{l}{=} \text{ty}_{e,2} \} \cup C_1 \cup C_2 \quad a_p, a_e \text{ fresh} \\
\hline
\Delta; (\text{pat} \rightarrow \text{lexp})^l \mid \text{rules} \Downarrow_r \langle a_p, a_e, C, u_1 \cup u_2 \rangle
\end{array}$$

9.3 Expressions

VAR-MONO

$$\frac{\Delta(x) = \langle ty, \text{mono}, C \rangle^{l'} \quad a, a_x \text{ fresh}}{\Delta; x^l \Downarrow_e \langle a, C \cup \{a_x \stackrel{l}{=} a, ty \stackrel{l'}{=} a_x\}, \emptyset \rangle}$$

VAR-POLY

$$\frac{\Delta(x) = \langle ty, \text{poly}, C \rangle^{l'} \quad a, a_x \text{ fresh} \quad \langle ty', C' \rangle \text{ fresh variant of } \langle ty, C \rangle}{\Delta; x^l \Downarrow_e \langle a, \{a_x \stackrel{l}{=} a, ty' \stackrel{l'}{=} a_x\} \cup C', \emptyset \rangle}$$

VAR-UNDEF

$$\frac{x \notin \text{dom}(\Delta) \quad a \text{ fresh}}{\Delta; x^l \Downarrow_e \langle a, \emptyset, \{x^l\} \rangle}$$

CONST

$$\frac{C_0 = \{ty \stackrel{l}{=} a\} \quad a \text{ fresh} \quad ty \text{ type of constant } c}{\Delta; c^l \Downarrow_e \langle a, C_0, \emptyset \rangle}$$

ABSTR

$$\frac{\Delta; \text{rules} \Downarrow_r \langle ty_p, ty_e, C_0, u \rangle \quad C_1 = \{a \stackrel{l}{=} ty_p \rightarrow ty_e\}}{\Delta; (\text{function rules})^l \Downarrow_e \langle a, C_0 \cup C_1, u \rangle}$$

APP

$$\frac{\begin{array}{c} \Delta; \text{lexp}_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \text{ for } i = 0, \dots, n \\ C' = \{a'_{i-1} \stackrel{l-l_i}{=} a_i \rightarrow a'_i, ty_i \stackrel{l}{=} a_i \mid i = 1, \dots, n\} \cup \{ty_0 \stackrel{l}{=} a'_0, a \stackrel{l}{=} a'_n\} \\ a, a_1, \dots, a_n, a'_0, \dots, a'_n \text{ fresh} \end{array}}{\Delta; (\text{lexp}_0 \text{lexp}_1^{l_1} \dots \text{lexp}_n^{l_n})^l \Downarrow_e \langle a, C' \cup \bigcup_{i=0}^n C_i, \bigcup_{i=1}^n u_i \rangle}$$

LET

$$\begin{array}{c}
\Delta; pat_i \Downarrow_p \langle ty_{p,i}, C_{p,i}, b_i \rangle \\
\Delta; lexp_i \Downarrow_e \langle ty_{e,i}, C_{e,i}, u_i \rangle \quad \varpi_i := \text{poly if value } lexp_i \text{ else mono} \\
\text{for } i = 1, \dots, n \quad \Delta' = \Delta|_{\text{id}}[b_i, C_{p,i} \cup C_{e,i} \cup \{ty_{p,i} \stackrel{l}{=} ty_{e,i}\}, \varpi_i \mid \text{for } i = 1, \dots, n] \\
\Delta'; lexp_{n+1} \Downarrow_e \langle ty_{n+1}, C_{n+1}, u_{n+1} \rangle \\
C_0 = \{a \stackrel{l}{=} ty_{n+1}\} \cup \{ty_{p,i} \stackrel{l}{=} ty_{e,i} \mid i = 1, \dots, n\} \\
\text{dom}(b_i) \cap \text{dom}(b_j) = \emptyset \text{ for all } i \neq j \quad a \text{ fresh} \\
\hline
\Delta; (\text{let } x_1 = lexp_1 \text{ and } \dots \text{ and } x_n = lexp_n \text{ in } lexp_{n+1})^l \Downarrow_e \langle a, \bigcup_{i=0}^{n+1} C_i, \bigcup_{i=1}^{n+1} u_i \rangle
\end{array}$$

LET REC

$$\begin{array}{c}
\Delta|_{\text{id}} \left[x_j \mapsto \langle a_j, \text{mono}, \emptyset \rangle^l \mid j = 1, \dots, n \right]; lexp_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \\
\varpi_i := \text{poly if value } lexp_i \text{ else mono} \\
\text{for } i = 1, \dots, n \quad \Delta' := \Delta|_{\text{id}}[x_j \mapsto \langle ty_j, \varpi_j, C_j \cup \{a_j \stackrel{t}{=} y_j\} \rangle^l \mid j = 1, \dots, n] \\
\Delta'; lexp_{n+1} \Downarrow_e \langle ty_{n+1}, C_{n+1}, u_{n+1} \rangle \\
C_0 = \{a \stackrel{l}{=} ty_{n+1}\} \quad x_i = x_j \text{ iff } i = j \quad a, a_1, \dots, a_n \text{ fresh} \\
\hline
\Delta; (\text{let rec } x_1 = lexp_1 \text{ and } \dots \text{ and } x_n = lexp_n \text{ in } lexp_{n+1})^l \Downarrow_e \langle a, \bigcup_{i=0}^{n+1} C_i, \bigcup_{i=1}^{n+1} u_i \rangle
\end{array}$$

TUPLE

$$\begin{array}{c}
\Delta; lexp_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \text{ for } i = 1, \dots, n \quad C_0 = \{a \stackrel{l}{=} (ty_1, \dots, ty_n)\} \quad a \text{ fresh} \\
\hline
\Delta; (lexp_1, \dots, lexp_n)^l \Downarrow_e \langle a, \bigcup_{i=0}^n C_i, \bigcup_{i=1}^n u_i \rangle
\end{array}$$

RECORD CONSTRUCTION

$$\begin{array}{c}
\Delta; lexp_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \quad \Delta|_{\text{rec}}(f_i) = \langle ty_r, ty_{f,i}, \cdot \rangle \\
\text{for } i = 1, \dots, n \quad C_0 = \{a \stackrel{l}{=} ty_r\} \cup \{ty_i \stackrel{l}{=} ty_{f,i} \mid i = 1, \dots, n\} \\
a \text{ fresh} \quad \{f_i \mid i = 1, \dots, n\} \text{ are the fields of record } ty_r \\
\hline
\Delta; \{f_1 = lexp_1; \dots; f_n = lexp_n\}^l \Downarrow_e \langle a, \bigcup_{i=0}^n C_i, \bigcup_{i=1}^n u_i \rangle \\
\hline
\Delta; lexp_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \text{ for } i = 0, \dots, n \quad \Delta|_{\text{rec}}(f_i) = \langle ty_r, ty_{f,i}, \cdot \rangle \text{ for } i = 1, \dots, n \\
C_0 = \{a \stackrel{l}{=} ty_r, ty_0 \stackrel{l}{=} ty_r\} \cup \{ty_{f,i} \stackrel{l}{=} ty_i \mid i = 1, \dots, n\} \quad a \text{ fresh} \\
\hline
\Delta; \{lexp_0 \text{ with } f_1 = lexp_1; \dots; f_n = lexp_n\}^l \Downarrow_e \langle a, \bigcup_{i=0}^n C_i, \bigcup_{i=1}^n u_i \rangle
\end{array}$$

RECORD ACCESS

$$\frac{\Delta; \text{lexp} \Downarrow_e \langle ty, C, u \rangle \quad \Delta|_{\text{rec}}(f) = \langle ty_f, ty, \cdot \rangle \quad C_0 = \{a \stackrel{l}{=} ty_f, ty \stackrel{l}{=} ty_r\} \quad a \text{ fresh}}{\Delta; (\text{lexp}.f)^l \Downarrow_e \langle a, C_0 \cup C, u \rangle}$$

RECORD FIELD ASSIGNMENT

$$\frac{\Delta; \text{lexp}_1 \Downarrow_e \langle ty_1, C_1, u_1 \rangle \quad \Delta; \text{lexp}_2 \Downarrow_e \langle ty_2, C_2, u_2 \rangle \quad \Delta|_{\text{rec}}(f) = \langle ty_r, ty_f, \text{mutable} \rangle \quad C_0 = \{a \stackrel{l}{=} \underline{\text{unit}}, ty_r \stackrel{l}{=} ty_1, ty_f \stackrel{l}{=} ty_2\}}{\Delta; (\text{lexp}_1.f <- \text{lexp}_2)^l \Downarrow_e \langle a, C_0 \cup C_1 \cup C_2, u_1 \cup u_2 \rangle}$$

VARIANT

$$\frac{\Delta|_{\text{var}}(K) = \langle ty_r, [ty_{a,1}, \dots, ty_{a,n}] \rangle \quad \Delta; \text{lexp}_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \text{ for } i = 1, \dots, n \quad C_0 = \{a \stackrel{l}{=} ty_r\} \cup \{ty_i \stackrel{l}{=} ty_{a,i} \mid i = 1, \dots, n\} \quad a \text{ fresh}}{\Delta; (K \text{ lexp}_1 \dots \text{lexp}_n)^l \Downarrow_e \langle a, \bigcup_{i=0}^n C_i, \bigcup_{i=1}^n u_i \rangle}$$

NB The distinction between $K \text{ lexp}_1 \dots \text{lexp}_n$ (n arguments) and $K (\text{lexp}_1, \dots, \text{lexp}_n)$ (an n -tuple as the single argument) is actually made by an `explicit_arity` flag in the AST.

IF-THEN-ELSE

$$\frac{\Delta; \text{lexp}_1 \Downarrow_e \langle ty_1, C_1, u_1 \rangle \quad \Delta; \text{lexp}_2 \Downarrow_e \langle ty_2, C_2, u_2 \rangle \quad \Delta; \text{lexp}_3 \Downarrow_e \langle ty_3, C_3, u_3 \rangle \quad C = \{ty_1 \stackrel{l}{=} \underline{\text{bool}}, a \stackrel{l}{=} ty_3, a \stackrel{l}{=} ty_2\} \cup C_1 \cup C_2 \cup C_3 \quad a \text{ fresh}}{\Delta; (\text{if } \text{lexp}_1 \text{ then } \text{lexp}_2 \text{ else } \text{lexp}_3)^l \Downarrow_e \langle a, C, u_1 \cup u_2 \cup u_3 \rangle}$$

IF-THEN

$$\frac{\Delta; \text{lexp}_1 \Downarrow_e \langle ty_1, C_1, u_1 \rangle \quad \Delta; \text{lexp}_2 \Downarrow_e \langle ty_2, C_2, u_2 \rangle \quad C_0 = \{ty_1 \stackrel{l}{=} \underline{\text{bool}}, ty_2 \stackrel{l}{=} \underline{\text{unit}}, a \stackrel{l}{=} \underline{\text{unit}}\} \quad a \text{ fresh}}{\Delta; (\text{if } \text{lexp}_1 \text{ then } \text{lexp}_2)^l \Downarrow_e \langle a, C, u \rangle}$$

MATCHING

$$\frac{\Delta; \text{lexp} \Downarrow_e \langle ty_0, C_0, u_0 \rangle \quad \Delta; \text{rules} \Downarrow_r \langle ty_p, ty_e, C_1, u_1 \rangle \quad C = \{ty_0 \stackrel{l}{=} ty_p, a \stackrel{l}{=} ty_e\} \cup C_1 \cup C_2 \quad u = u_0 \cup u_1 \quad a \text{ fresh}}{\Delta; (\text{match } \text{lexp} \text{ with } \text{rules})^l \Downarrow_e \langle a, C, u \rangle}$$

ARRAY CONSTRUCTION

$$\frac{\Delta; \text{lexp}_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \quad C_0 = \{a \stackrel{l}{=} b \text{ array}\} \cup \{ty_i \stackrel{l}{=} b \mid i = 1, \dots, n\} \quad a, b \text{ fresh}}{\Delta; ([\text{lexp}_1; \dots; \text{lexp}_n])^l \Downarrow_e \langle a, \bigcup_{i=0}^n C_i, \bigcup_{i=1}^n u_i \rangle}$$

ARRAY ACCESS

$$\frac{\Delta; \text{lexp}_1 \Downarrow_e \langle ty_1, C_1, u_1 \rangle \quad \Delta; \text{lexp}_2 \Downarrow_e \langle ty_2, C_2, u_2 \rangle \quad C_0 = \{ty_1 \stackrel{l}{=} a \text{ array}, ty_2 \stackrel{l}{=} \text{int}\} \quad a \text{ fresh}}{\Delta; (\text{lexp}_1.(\text{lexp}_2))^l \Downarrow_e \langle a, C_0 \cup C_1 \cup C_2, u_1 \cup u_2 \rangle}$$

WHILE

$$\frac{\Delta; \text{lexp}_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \text{ for } i = 1, 2 \quad C_0 = \{ty_1 \stackrel{l}{=} \text{bool}, ty_2 \stackrel{l}{\leftrightarrow} \text{unit}, a \stackrel{l}{=} \text{unit}\} \quad a \text{ fresh}}{\Delta; (\text{while } \text{lexp}_1 \text{ do } \text{lexp}_2 \text{ done})^l \Downarrow_e \langle a, C_0 \cup C_1 \cup C_2, u_1 \cup u_2 \rangle}$$

FOR

$$\frac{\Delta; \text{lexp}_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \text{ for } i = 1, 2 \quad \Delta' = \Delta|_{\text{id}} \left[\text{var} \mapsto \langle a_{\text{var}}, \text{mono}, \{a_{\text{var}} \stackrel{l}{=} \text{int}\} \right]^l \quad \Delta'; \text{lexp}_3 \Downarrow_e \langle ty_3, C_3, u_3 \rangle \quad C_0 = \{a \stackrel{l}{=} \text{unit}, ty_1 \stackrel{l}{=} \text{int}, ty_2 \stackrel{l}{=} \text{int}, ty_3 \stackrel{l}{\leftrightarrow} \text{unit}\} \quad a, a_{\text{var}} \text{ fresh}}{\Delta; (\text{for } \text{var} = \text{lexp}_1 \text{ to/downto } \text{lexp}_2 \text{ do } \text{lexp}_3 \text{ done})^l \Downarrow_e \langle a, C_0 \cup C_1 \cup C_2, u_1 \cup u_2 \rangle}$$

SEQUENCE

$$\frac{\Delta; \text{lexp}_i \Downarrow_e \langle ty_i, C_i, u_i \rangle \text{ for } i = 1, 2 \quad C_0 = \{a \stackrel{l}{=} ty_2, ty_1 \stackrel{l}{\leftrightarrow} \text{unit}\}}{\Delta; (\text{lexp}_1; \text{lexp}_2)^l \Downarrow_e \langle a, C_0 \cup C_1 \cup C_2, u_1 \cup u_2 \rangle}$$

RAISE

$$\frac{\Delta; \text{lexp} \Downarrow_e \langle ty, C, u \rangle \quad a \text{ fresh}}{\Delta; (\text{raise } \text{lexp})^l \Downarrow_e \langle a, C \cup \{ty \stackrel{l}{=} \text{exc}\}, u \rangle}$$

TRY

$$\frac{\Delta; \text{lexp} \Downarrow_e \langle ty, C_1, u_1 \rangle \quad \Delta; \text{rules} \Downarrow_r \langle ty_p, ty_e, C_2, u_2 \rangle \quad C_0 = \{ty_p \stackrel{l}{=} \text{exc}, a \stackrel{l}{=} ty, a \stackrel{l}{=} ty_e\} \quad a \text{ fresh}}{\Delta; (\text{try } \text{lexp} \text{ with } \text{rules})^l \Downarrow_e \langle a, C_0 \cup C_1 \cup C_2, u_1 \cup u_2 \rangle}$$

ASSERT

$$\frac{\Delta; \text{lexp} \Downarrow_e \langle ty, C_1, u \rangle \quad C_2 = \{ty \stackrel{l}{=} \underline{bool}, a \stackrel{l}{=} \underline{unit}\} \quad a \text{ fresh}}{\Delta; (\text{assert lexp})^l \Downarrow_e \langle a, \emptyset, \emptyset \rangle}$$

$$\overline{\Delta; (\text{assert false})^l \Downarrow_e \langle a, \emptyset, \emptyset \rangle}$$

TYPE-ANNOT

$$\frac{\Delta; \text{lexp} \Downarrow_e \langle ty, C_0, u \rangle \quad C_1 = \{a \stackrel{l}{=} b, b \stackrel{l'}{=} ty', ty \stackrel{l}{=} c, c \stackrel{l'}{=} ty', a \succ^l ct\} \quad a, b, c \text{ fresh} \quad ty' \text{ is a fresh instance of } ct}{\Delta; (\text{lexp} : ct^{l'})^l \Downarrow_e \langle a, C_0 \cup C_1, u \rangle}$$

9.4 Patterns

WILDCARD

$$\frac{a \text{ fresh}}{\Delta; - \Downarrow_p \langle a, \emptyset, \emptyset \rangle}$$

VARIABLE

$$\frac{a \text{ fresh}}{\Delta; x^l \Downarrow_p \langle a, \emptyset, \{x \mapsto \langle a \rangle^l\} \rangle}$$

INT

$$\frac{C_0 = \{int \stackrel{l}{=} a\} \quad a \text{ fresh}}{\Delta; n^l \Downarrow_p \langle a, C_0, \emptyset \rangle}$$

TUPLE

$$\frac{\Delta; pat_i \Downarrow_p \langle ty_i, C_i, b_i \rangle \text{ for } i = 1, \dots, n \quad C_0 = \{a \stackrel{l}{=} (ty_1, \dots, ty_n)\} \quad \text{dom}(b_i) \cap \text{dom}(b_j) = \emptyset \text{ for } i \neq j \quad a \text{ fresh}}{\Delta; (pat_1, \dots, pat_n)^l \Downarrow_p \langle a, \bigcup_{i=0}^n C_i, \bigcup_{i=1}^n b_i \rangle}$$

VARIANT

$$\frac{\begin{array}{l} \Delta|_{\text{var}}(K) = \langle ty_r, [ty_{a,1}, \dots, ty_{a,n}] \quad \Delta; pat_i \Downarrow_p \langle ty_i, C_i, b_i \rangle \text{ for } i = 1, \dots, n \\ C_0 = \{a \stackrel{l}{=} ty_r\} \cup \{ty_i \stackrel{l}{=} ty_{a,i} \mid i = 1, \dots, n\} \quad \text{dom}(b_i) \cap \text{dom}(b_j) = \emptyset \text{ for } i \neq j \end{array}}{\Delta; (K \text{ pat}_1 \dots \text{pat}_n)^l \Downarrow_p \langle a, \bigcup_{i=0}^n C_i, \bigcup_{i=1}^n b_i \rangle}$$

RECORD

$$\frac{\begin{array}{l} \Delta|_{\text{rec}}(f_i) = \langle ty_{r,i}, ty_{f,i} \rangle \quad \Delta; pat_i \Downarrow_p \langle ty_i, C_i, b_i \rangle \\ \text{for } i = 1, \dots, n \quad C_0 = \{a \stackrel{l}{=} ty_{r,i}, ty_i \stackrel{l}{=} ty_{f,i} \mid \text{for } i = 1, \dots, n\} \\ \text{dom}(b_i) \cap \text{dom}(b_j) = \emptyset \text{ for } i \neq j \quad a \text{ fresh} \end{array}}{\Delta; \{f_1=pat_1; \dots; f_n=pat_n\}^l \Downarrow_p \langle a, \bigcup_{i=0}^n C_i, \bigcup_{i=1}^n b_i \rangle}$$

OR

$$\frac{\begin{array}{l} \Delta; pat_i \Downarrow_p \langle ty_i, C_i, b_i \rangle \text{ for } i = 1, 2 \\ \text{dom}(b_1) = \text{dom}(b_2) \quad b = \{id \mapsto \langle a_{id} \rangle^l \mid id \in \text{dom}(b_1)\} \quad C_0 = \{a \stackrel{l}{=} ty_1, a \stackrel{l}{=} ty_2\} \\ C'_i = \{a_{id} \stackrel{l'}{=} ty \mid id \mapsto \langle ty \rangle^{l'} \in b_i\} \cup C_i \text{ for } i = 1, 2 \quad a, a_{id} \text{ fresh for } id \in \text{dom}(b_1) \end{array}}{\Delta; (pat_1 \mid pat_2)^l \Downarrow_p \langle a, C_0 \cup C'_1 \cup C'_2, b \rangle}$$

ALIAS

$$\frac{\Delta; pat \Downarrow_p \langle ty, C, b \rangle \quad a \text{ fresh}}{\Delta; (pat \text{ as } x)^l \Downarrow_p \langle a, \{a \stackrel{l}{=} ty\} \cup C, b[x \mapsto \langle ty \rangle] \rangle}$$

TYPE-ANNOT

$$\frac{\begin{array}{l} \Delta; pat \Downarrow_p \langle ty, C_0, b \rangle \quad C_1 = \{a \stackrel{l}{=} b, b \stackrel{l'}{=} ty', ty \stackrel{l}{=} c, c \stackrel{l'}{=} ty', a \succ^l ct\} \\ a, b, c \text{ fresh} \quad ty' \text{ fresh instance of } ct \end{array}}{\Delta; (pat : ct^{l'})^l \Downarrow_p \langle a, C_0 \cup C_1, b \rangle}$$

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