

## Phase Simplex Report

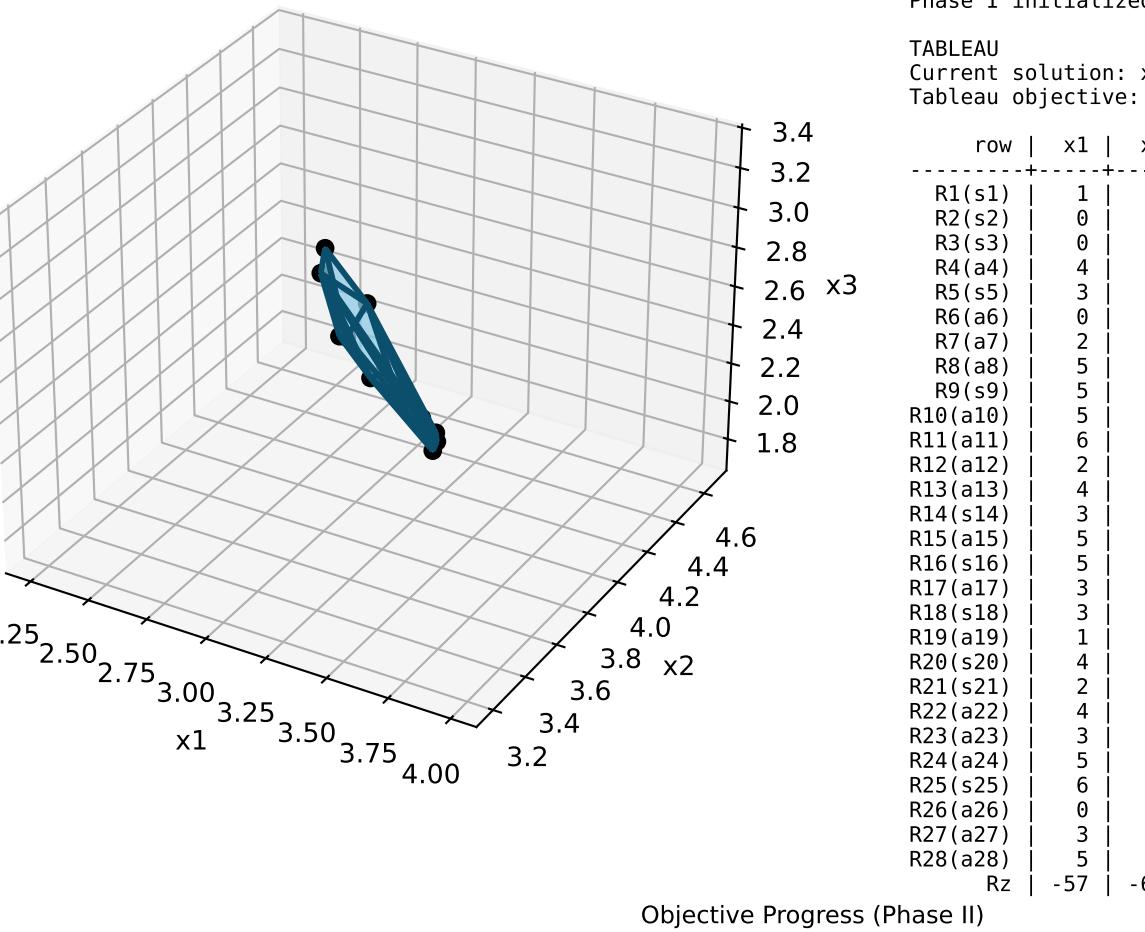
Feasible polytope + extreme points + simplex path State 1/31

ep 0

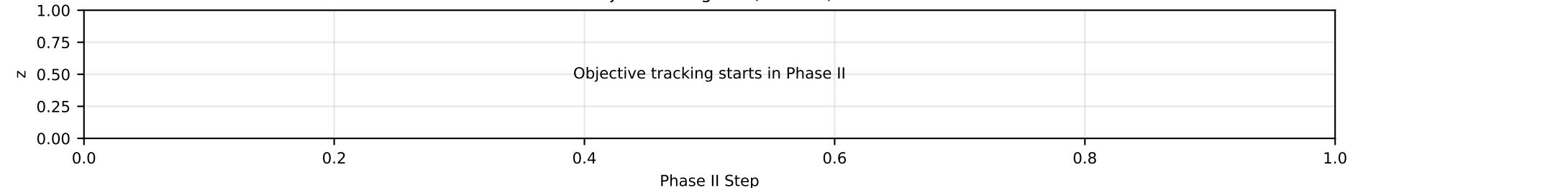
an artificial objective.

$$x_2=0 \quad x_3=0$$

633

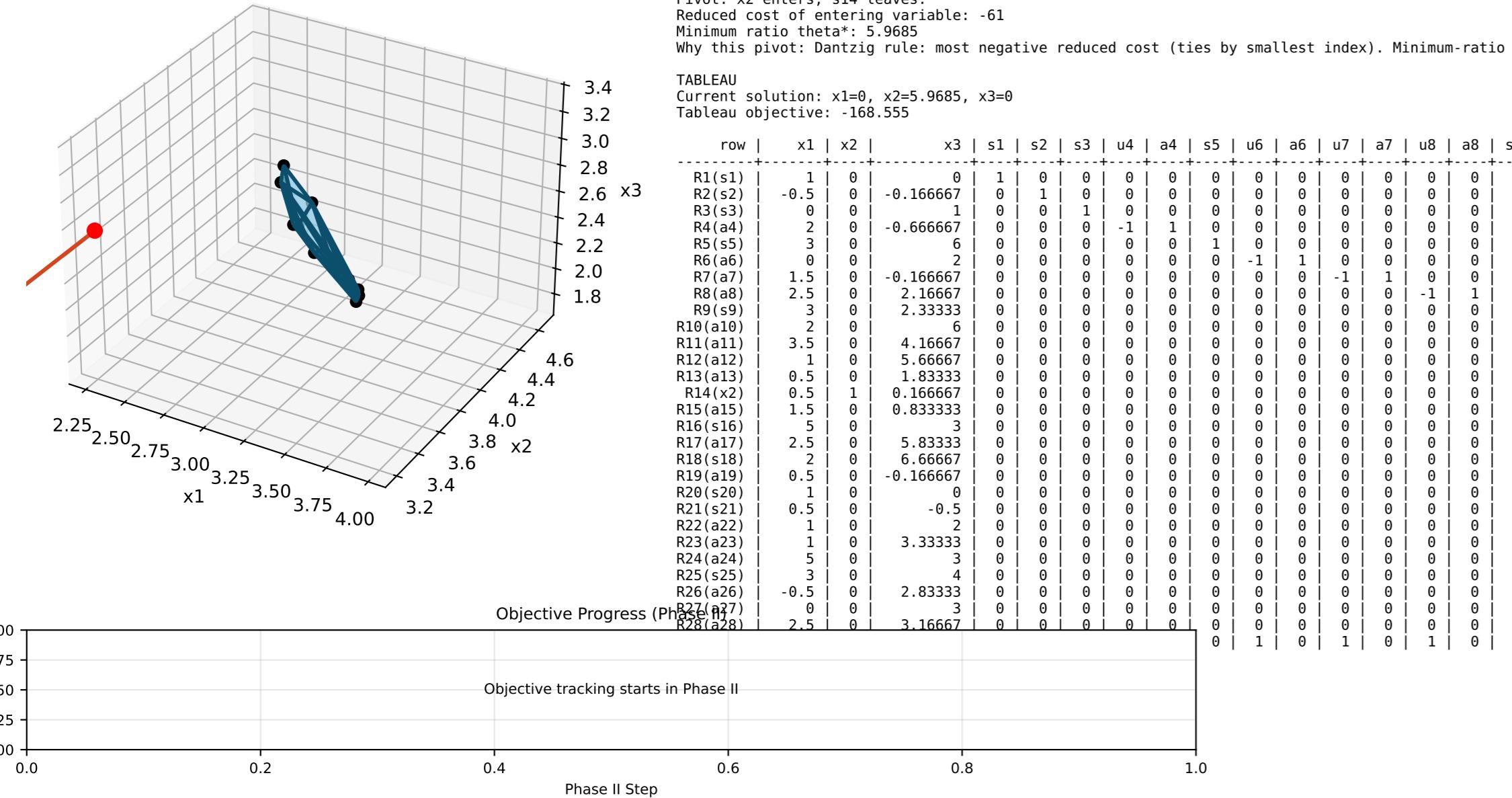


x2=0, x3=0 633	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	u21	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf				
0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf					
1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf					
0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	27.3806	inf						
6	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	25.3127	inf						
2	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.84349	inf						
0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.77031	inf						
3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	41.7099	inf						
3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	39.3197	inf						
7	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	55.9447	inf						
5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	50.3659	inf						
6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	27.994	inf						
3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	47.0236	inf						
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	35.811	inf						
2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	46.5579	inf						
3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	26.2458	inf						
6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	26.1909	inf						
7	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	37.4848	inf						
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.90233	inf						
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	41.59	inf						
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	20.4599	inf						
3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	42.7001	inf						
4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	33.5008	inf						
3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	20.5719	inf						
5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	58.3069	inf						
3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.62938	inf						
4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	41.001	inf						
4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	43.5467	inf						
55	0	0	0	1	0	0	1	0	1	0	1	0	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	-532.633	-						



## **-Phase Simplex Report**

Feasible polytope + extreme points + simplex path State 2/3



step 1 | ENTER: x2 | LEAVE: s14

: DANTZIG  
4 leaves.  
ring variable: -61

zig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

=0, x2=5.9685, x3=0  
168 555

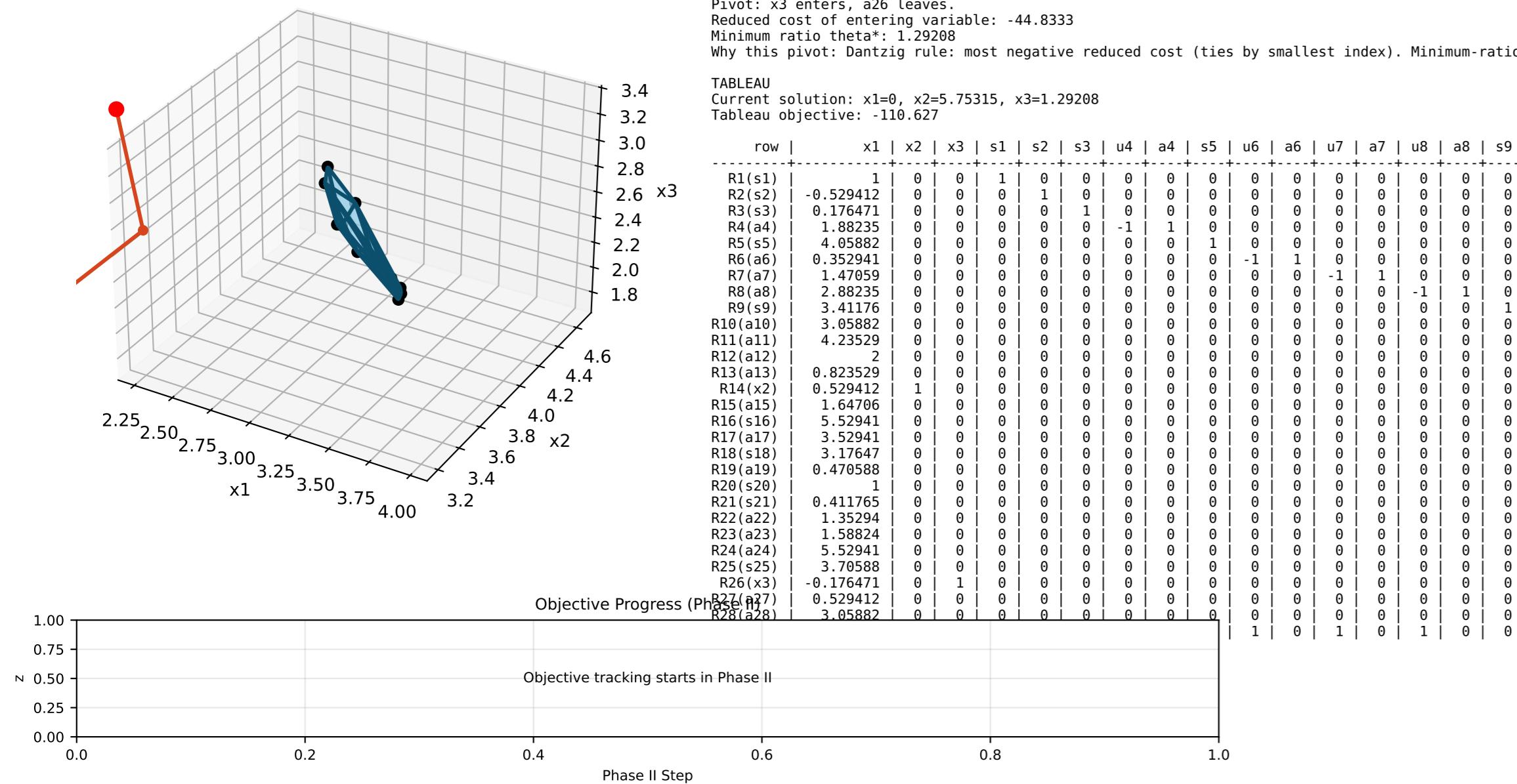
## Phase Simplex Report

feasible polytope + extreme points + simplex path State 3/31

Step 2 | ENTER: x3 | LEAVE: a26

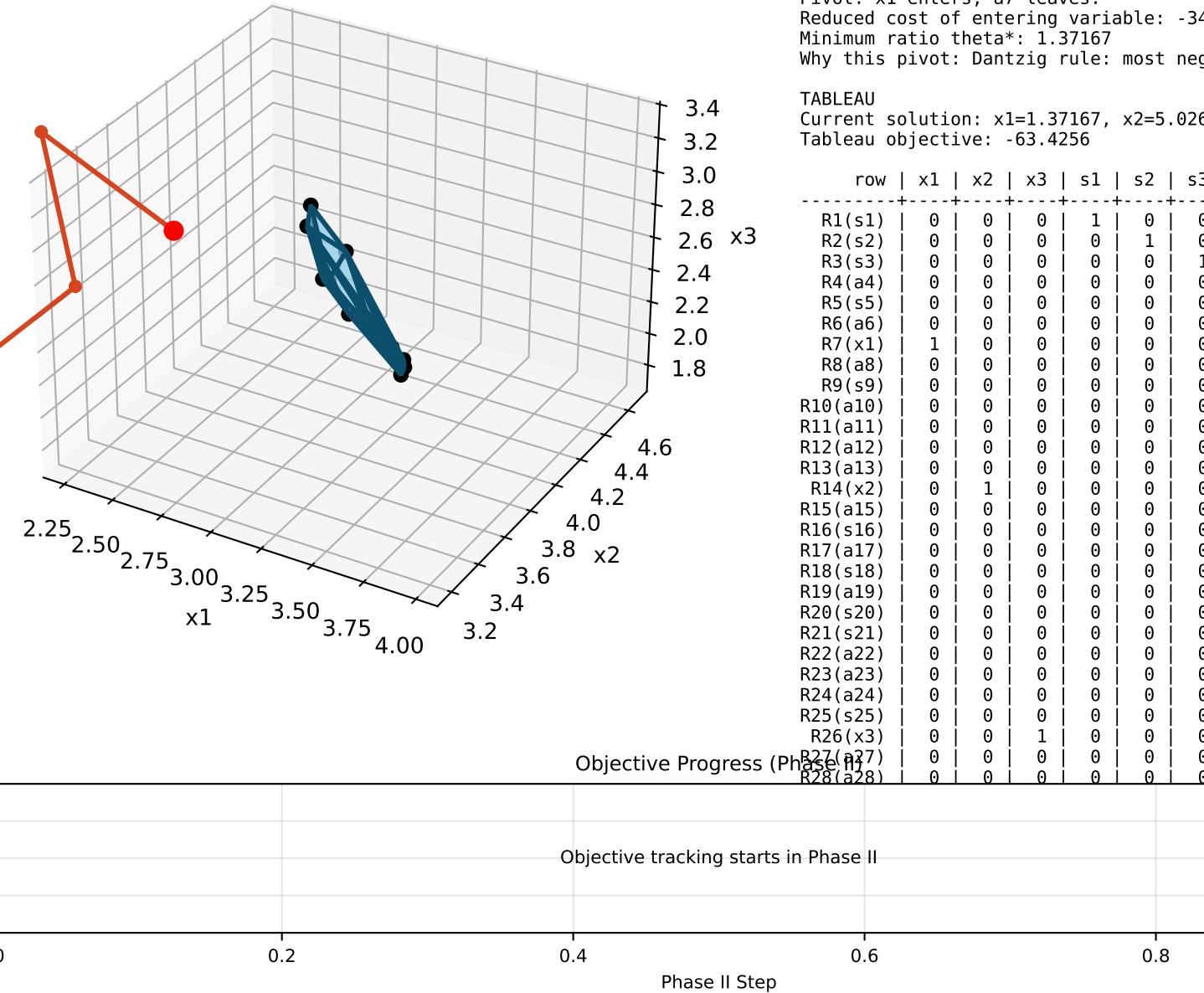
DANTZIG  
leaves.  
ng variable: -44.8333  
.29208  
g rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf				
0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.24685	inf				
0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.352941	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	10.7079	12				
0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.705882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.36797	inf				
0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.352941	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	17.5602	4.21878				
0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0.117647	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25934	1.92175				
0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	-0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.01716	inf				
0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	-0.705882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.06791	5.47726				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	-0.529412	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12.4309	6.61959				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	-0.647059	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12.3813	3.35562				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	-0.588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	15.1398	4.92562				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.73524	2.83359			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.05882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.87532	2.86043				
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.75315	35.811				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.11765	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.7017	5.73411				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	22.3695	8.74858				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12.6853	3.4667				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0588235	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	16.934	3.83218				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14918	inf				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.529412	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.77906	inf				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.882353	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.30495	3.44455				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.470588	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.31986	2.88803				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	16.6956	6.85729				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.764706	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	17.3276	5.62398				
0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.29208	1.29208			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.823529	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.31375	1.72999				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.647059	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.61261	4.32764				
1	0	0	1	0	1	0	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	7.52941	1	0	0	1	0	0	1	0	0	1	0	0	1	0	0	1	0	0	1	0	-110.627	inf				



# Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 4/31 | PHASE I step 3 | ENTER: x1 | LEAVE: a7

## COMMENTS

Teaching Mode | Rule: DANTZIG  
Pivot: x1 enters, a7 leaves.  
Reduced cost of entering variable: -34.4118  
Minimum ratio theta\*: 1.37167

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

## TABLEAU

Current solution: x1=1.37167, x2=5.02697, x3=1.53413  
Tableau objective: -63.4256

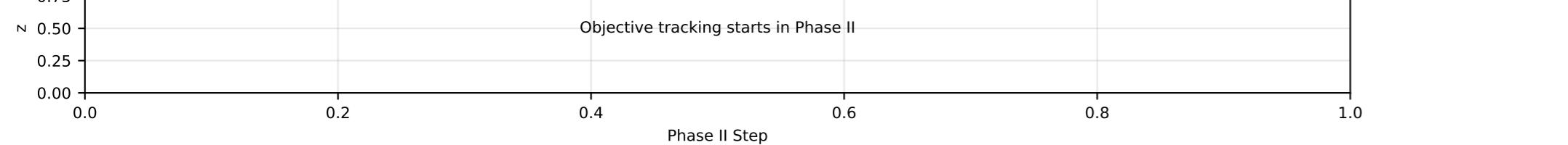
row	x1	x2	x3	s1	s2	s3	s4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	a15	s16	u17	a17	s18	a19	s20	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0.68	-0.68	0	0	0	0	0	0	0	0	0	0	0	0.12	0	0	0	0	0	0.04	-0.04	0	0	0	0	10.6283	12									
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	-0.36	0.36	0	0	0	0	0	0	0	0	0	0	0	-0.24	0	0	0	0	0	-0.08	0.08	0	0	0	0	6.97303	inf									
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0.12	-0.12	0	0	0	0	0	0	0	0	0	0	0	0.08	0	0	0	0	0	0.36	-0.36	0	0	0	0	10.4659	60.6782									
R4(a4)	0	0	0	0	0	0	1	1	0	0	0	1.28	-1.28	0	0	0	0	0	0	0	0	0	0	0	-0.48	0	0	0	0	0	-0.16	0.16	0	0	0	0	1.78602	2.32049									
R5(s5)	0	0	0	0	0	0	0	0	0	0	1	0.24	-0.24	0	0	0	0	0	0	0	0	0	0	0	0.84	0	0	0	0	0	2.28	-2.28	0	0	0	0	11.9929	4.32643									
R6(a6)	0	0	0	0	0	0	0	0	0	0	-1	1	0.68	-0.68	0	0	0	0	0	0	0	0	0	0	0.16	0	0	0	0	0	0.72	-0.72	0	0	0	0	0.775222	3.56813									
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	-0.68	0.68	0	0	0	0	0	0	0	0	0	0	0	-0.12	0	0	0	0	0	-0.04	0.04	0	0	0	0	1.37167	1.37167									
R8(a8)	0	0	0	0	0	0	0	0	0	0	0	1.96	-1.96	-1	1	0	0	0	0	0	0	0	0	0	-0.36	0	0	0	0	0	0.88	-0.88	0	0	0	0	5.11428	3.14601									
R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	2.32	-2.32	0	0	0	0	0	0	0	0	0	0	-0.12	0	0	0	0	0	0.96	-0.96	0	0	0	0	7.75106	3.64353									
R10(a10)	0	0	0	0	0	0	0	0	0	0	0	0	2.08	-2.08	0	0	0	0	0	0	0	0	0	0	-0.28	0	0	0	0	0	2.24	-2.24	0	0	0	0	8.18559	4.04772									
R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	2.88	-2.88	0	0	0	0	0	0	0	0	0	0	-0.08	0	0	0	0	0	1.64	-1.64	0	0	0	0	9.33037	3.57467									
R12(a12)	0	0	0	0	0	0	0	0	0	0	0	0	1.36	-1.36	0	0	0	0	0	0	0	0	0	0	0.24	0	0	0	0	0	2.08	-2.08	0	0	0	0	5.99191	4.36762									
R13(a13)	0	0	0	0	0	0	0	0	0	0	0	0	0.56	-0.56	0	0	0	0	0	0	0	0	0	0	-1	1	-0.96	0	0	0	0	0	0.68	-0.68	0	0	0	0	1.74572	3.49146							
R14(x2)	1	0	0	0	0	0	0	0	0	0	0	0	0.36	-0.36	0	0	0	0	0	0	0	0	0	0	0.24	0	0	0	0	0	0.08	-0.08	0	0	0	0	5.02697	10.8671									
R15(a15)	0	0	0	0	0	0	0	0	0	0	0	0	1.12	-1.12	0	0	0	0	0	0	0	0	0	0	-0.92	-1	1	0	0	0	0.36	-0.36	0	0	0	0	1.44248	2.24746									
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	3.76	-3.76	0	0	0	0	0	0	0	0	0	0	0.84	0	0	0	0	0	1.28	-1.28	0	0	0	0	14.785	4.04555									
R17(a17)	0	0	0	0	0	0	0	0	0	0	0	0	2.4	-2.4	0	0	0	0	0	0	0	0	0	0	0.6	0	0	0	0	0	2.2	-2.2	0	0	0	0	7.84414	3.59417									
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	2.16	-2.16	0	0	0	0	0	0	0	0	0	0	0.44	0	0	0	0	0	2.48	-2.48	0	0	0	0	12.5769	5.33107									
R19(a19)	0	0	0	0	0	0	0	0	0	0	0	0	0.32	-0.32	0	0	0	0	0	0	0	0	0	0	-0.12	0	0	0	0	0	0.04	-0.04	0	0	0	0	0.503686	2.442									
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0.68	-0.68	0	0	0	0	0	0	0	0	0	0	-0.88	0	0	0	0	0	0.04	-0.04	0	0	0	0	4.40739	5.77906									
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0.28	-0.28	0	0	0	0	0	0	0	0	0	0	-0.48	0	0	0	0	0	0.16	-0.16	0	0	0	0	2.63566	7.77255									
R22(a22)	0	0	0	0	0	0	0	0	0	0	0	0	0.92	-0.92	0	0	0	0	0	0	0	0	0	0	-0.72	0	0	0	0	0	0.76	-0.76															

# **base Simplex Report**

feasible polytope + extreme points + simplex path State 5/31

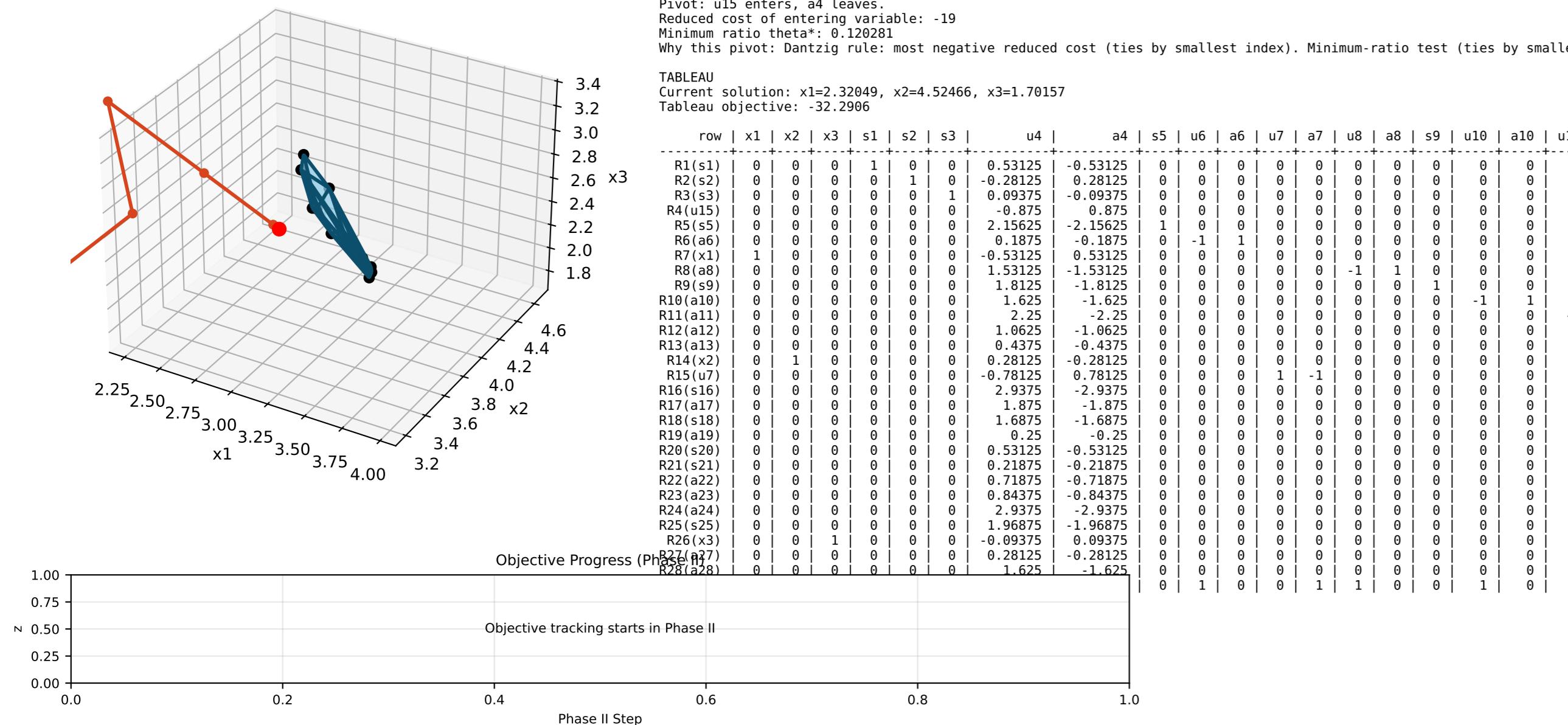
**COMMENTS**  
Teaching Mode | Rule: DAM  
Pivot: u7 enters, a15 leaves  
Reduced cost of entering  
Minimum ratio theta\*: 1.2  
Why this pivot: Dantzig rule

**TABLEAU**  
Current solution:  $x_1=2.24746$ ,  $x_2=4.56332$ ,  $x_3=1.68869$   
Tableau objective: -34.5759



## **Phase Simplex Report**

Feasible polytope + extreme points + simplex path State 6/31



step 5 | ENTER: u15 | LEAVE: a4

#### DANTZIG

## DANTZIG leaves

ing variable: -19

ing variable: -19  
0.130381

ig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

2 32049 x2-4 52466 x3-1 70157

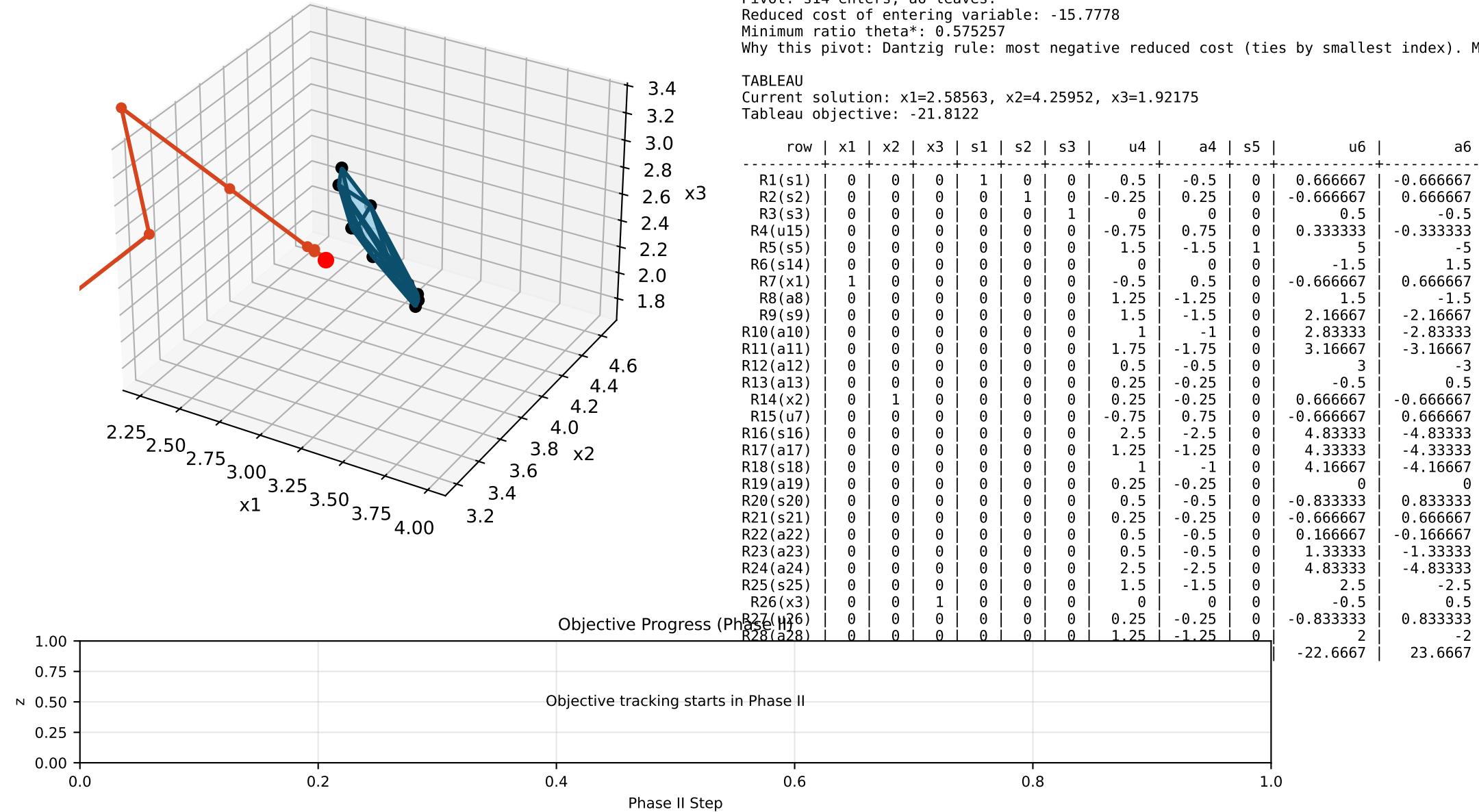
2.32049, x2=4

x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	u21	a22	s23	u24	a24	s25	u26	a26	s27	u27	a27	s28	rhs	ratio
0	1	0	0	0.53125	-0.53125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	9.67951	16.063						
0	0	1	0	-0.28125	0.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	7.47534	inf							
0	0	0	1	0.09375	-0.09375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	0	0	0	0	0	0	0	0	0	0	0.375	-0.375	0	0	0	10.2984	96.2389							
0	0	0	0	-0.875	0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.5	1	-1	0	0	0	0	0	0	0	0	0	-0.5	0.5	0	0	0	0.120281	0.120281						
0	0	0	0	2.15625	-2.15625	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.875	0	0	0	0	0	0	0	0	0	0	0	2.625	-2.625	0	0	0	8.14176	3.42418					
0	0	0	0	0.1875	-0.1875	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0.440344	2.17522						
0	0	0	0	-0.53125	0.53125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	2.32049	int						
0	0	0	0	1.53125	-1.53125	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0	1.125	-1.125	0	0	0	2.37945	1.47997					
0	0	0	0	1.8125	-1.8125	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0.75	0	0	0	0	0	0	0	0	0	0	0	1.25	-1.25	0	0	0	4.51391	2.29941						
0	0	0	0	1.625	-1.625	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	2.5	-2.5	0	0	0	5.28331	2.96514					
0	0	0	0	2.25	-2.25	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	0	5.31183	2.18599				
0	0	0	0	1.0625	-1.0625	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	2.25	-2.25	0	0	0	4.09427	3.49203				
0	0	0	0	0.4375	-0.4375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	-0.75	0	0	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0.964335	2.04895					
0	0	0	0	0.28125	-0.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	4.52466	14.197					
0	0	0	0	-0.78125	0.78125	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	1.39532	int					
0	0	0	0	2.9375	-2.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25	0	0	1	0	0	0	0	0	0	0	0	0	1.75	-1.75	0	0	0	9.5386	2.96157					
0	0	0	0	1.875	-1.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	2.5	-2.5	0	0	0	4.49536	2.21812			
0	0	0	0	1.6875	-1.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	2.75	-2.75	0	0	0	9.56304	5.0789					
0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	0.320417		
0	0	0	0	0.53125	-0.53125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	3.45857	5.81675				
0	0	0	0	0.21875	-0.21875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	2.24497	9.10015				
0	0	0	0	0.71875	-0.71875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0.875	-0.875	0	0	0	1.16547	1.53912				
0	0	0	0	0.84375	-0.84375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	1.375	-1.375	0	0	0	1.63438	1.8152				
0	0	0	0	2.9375	-2.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.86471	1.27147					
0	0	0	0	1.96875	-1.96875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.75	-1.75	0	0	0	8.72816	3.99947			
1	0	0	0	-0.09375	0.09375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0.375	0	0	0	1.70157	int				
0	0	0	0	0.28125	-0.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	-1.25	-1	1	0	0.08526	0.385534			
0	0	0	0	1.625	-1.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	-1.5	0	0	-1	2.51465	1.47432				



# Phase Simplex Report

feasible polytope + extreme points + simplex path State 8/3



p 7 | ENTER: s14 | LEAVE: a6

NT7TG

aves

variable: -15.7778

variable: 15.7778  
575257

rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

8563 x2=4 25952

8383, x2=4.23932, x3=1.92173  
122

122

s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	u21	a22	u22	a23	u23	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
1	0	0	0.5	-0.5	0	0.666667	-0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.41437	21.7576						
0	1	0	-0.25	0.25	0	-0.666667	0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.74048	inf							
0	0	1	0	0.25	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	10.0783	30.81						
0	0	0	-0.75	0.75	0	0.333333	-0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0303394	0.711784							
0	0	0	1.5	-1.5	1	5	-5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.02529	2.38284							
0	0	0	0	0	0	-1.5	1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.575257	0.575257								
0	0	0	-0.5	0.5	0	-0.666667	0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.58563	inf								
0	0	0	1.25	-1.25	0	1.5	-1.5	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.71893	2.29419							
0	0	0	1.5	-1.5	0	2.16667	-2.16667	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.58825	3.05943								
0	0	0	1	-1	0	2.83333	-2.83333	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.00725	2.69674							
0	0	0	1.75	-1.75	0	3.16667	-3.16667	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.94583	2.44433							
0	0	0	0.5	-0.5	0	3	-3	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.77324	1.96187							
0	0	0	0.25	-0.25	0	-0.5	0.5	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.09925	inf						
0	0	0	0.25	-0.25	0	0.666667	-0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.25952	10.1592								
0	0	0	-0.75	0.75	0	-0.666667	0.666667	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.66047	inf								
0	0	0	2.5	-2.5	0	4.83333	-4.83333	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.55237	2.9191								
0	0	0	1.25	-1.25	0	4.33333	-4.33333	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.64405	1.4905							
0	0	0	1	-1	0	4.16667	-4.16667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.7567	3.36767							
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf					
0	0	0	0.5	-0.5	0	-0.833333	0.833333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.76869	inf					
0	0	0	0.25	-0.25	0	-0.666667	0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.51011	inf					
0	0	0	0.5	-0.5	0	0.166667	-0.166667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.03524	9.89243					
0	0	0	0.5	-0.5	0	1.33333	-1.33333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.01884	1.72145					
0	0	0	2.5	-2.5	0	4.83333	-4.83333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.87848	1.15823						
0	0	0	1.5	-1.5	0	2.5	-2.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.6273	5.15164		
0	0	0	0	0	0	-0.5	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.92175	inf		
0	0	0	0.25	-0.25	0	-0.833333	0.833333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.395374	inf			
0	0	0	1.25	-1.25	0	2	-2	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.63396	1.80073			

## Phase Simplex Report

Feasible polytope + extreme points + simplex path State 9/

Step 8 | ENTER: u6 | LEAVE: u15

ANTZTG

leaves

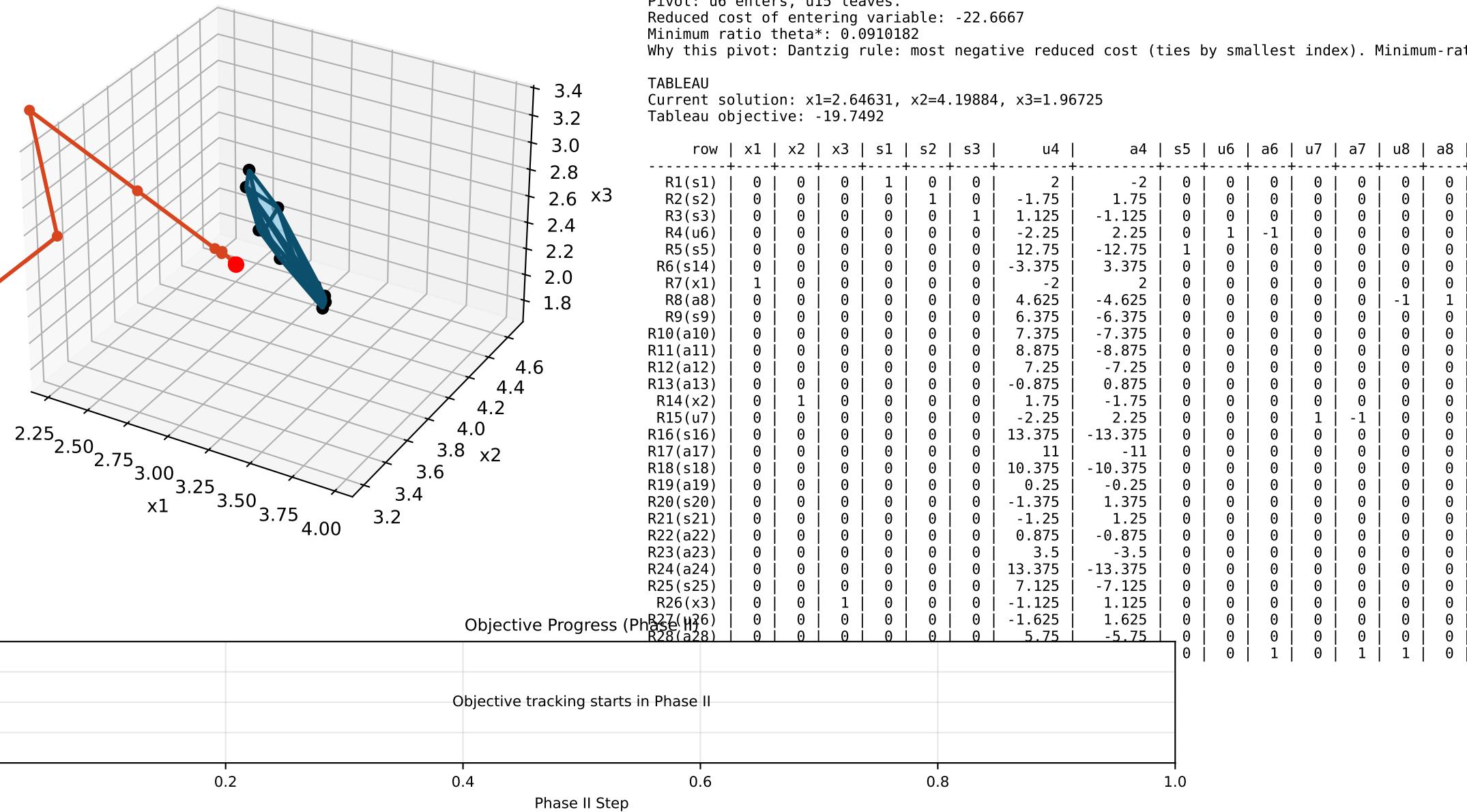
variable: -22.6667

Variable. -22.000/  
0010182

rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

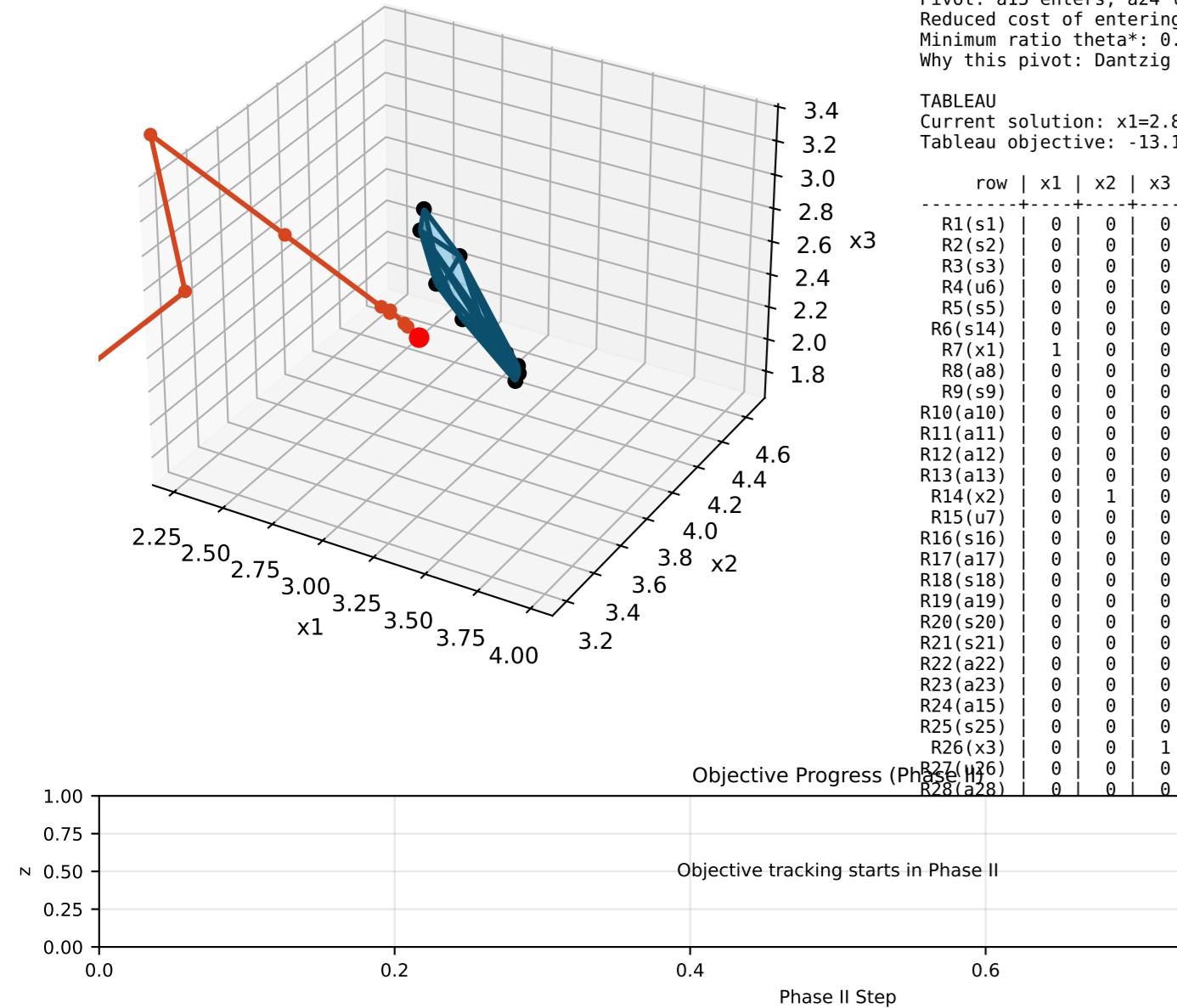
$$64631 \times 2 = 129262 \\ 19884 \times 3 = 59652 \\ 96725 \times 1 = 96725$$

4031, x2=4.19884, x3=1.907492



## Phase Simplex Report

feasible polytope + extreme points + simplex path State 10/3



Step 9 | ENTER: a15 | LEAVE: a24

ANTZIG

-leaves.

g variable: -67

0992111

rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

34473  $\times 2 = 4$  00041  $\times 3 =$

102

102

s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	u21	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio	
1	0	0	0.155172	-0.155172	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.15527	4.67685		
0	1	0	0.0948276	-0.0948276	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.99959	inf			
0	0	1	-0.258621	0.258621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.6885	inf		
0	0	0	0.517241	-0.517241	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.371347	inf		
0	0	0	-1.08621	1.08621	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.08204	inf		
0	0	0	0.775862	-0.775862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.15823	inf		
0	0	0	-0.155172	0.155172	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.84473	inf		
0	0	0	0.474138	-0.474138	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.351645	0.351645		
0	0	0	0.37931	-0.37931	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.74617	0.521699		
0	0	0	-0.465517	0.465517	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.441102	0.441102		
0	0	0	0.112069	-0.112069	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.90607	0.385011		
0	0	0	-1.05172	1.05172	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.7151	0.277798		
0	0	0	0.508621	-0.508621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.29357	inf		
0	0	0	-0.0948276	0.0948276	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.09942	0.09942		
0	0	0	-0.405172	0.405172	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.91957	inf		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	0.490514	
0	0	0	-0.991379	0.991379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.959889	0.173049	
0	0	0	-1.15517	1.15517	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.13732	0.590196		
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf		
0	0	0	0.931034	-0.931034	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.09256	inf		
0	0	0	0.594828	-0.594828	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.76921	inf		
0	0	0	0.413793	-0.413793	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.970466	2.04014		
0	0	0	-0.189655	0.189655	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.22437	0.22437		
0	0	0	0.922414	-0.922414	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0992111	0.0992111		
0	0	0	0.206897	-0.206897	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.65568	0.986634		
0	0	0	0.258621	-0.258621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.11607	inf
0	0	0	0.681034	-0.681034	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.71925	inf
0	0	0	0.215517	-0.215517	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.856656	0.241987	

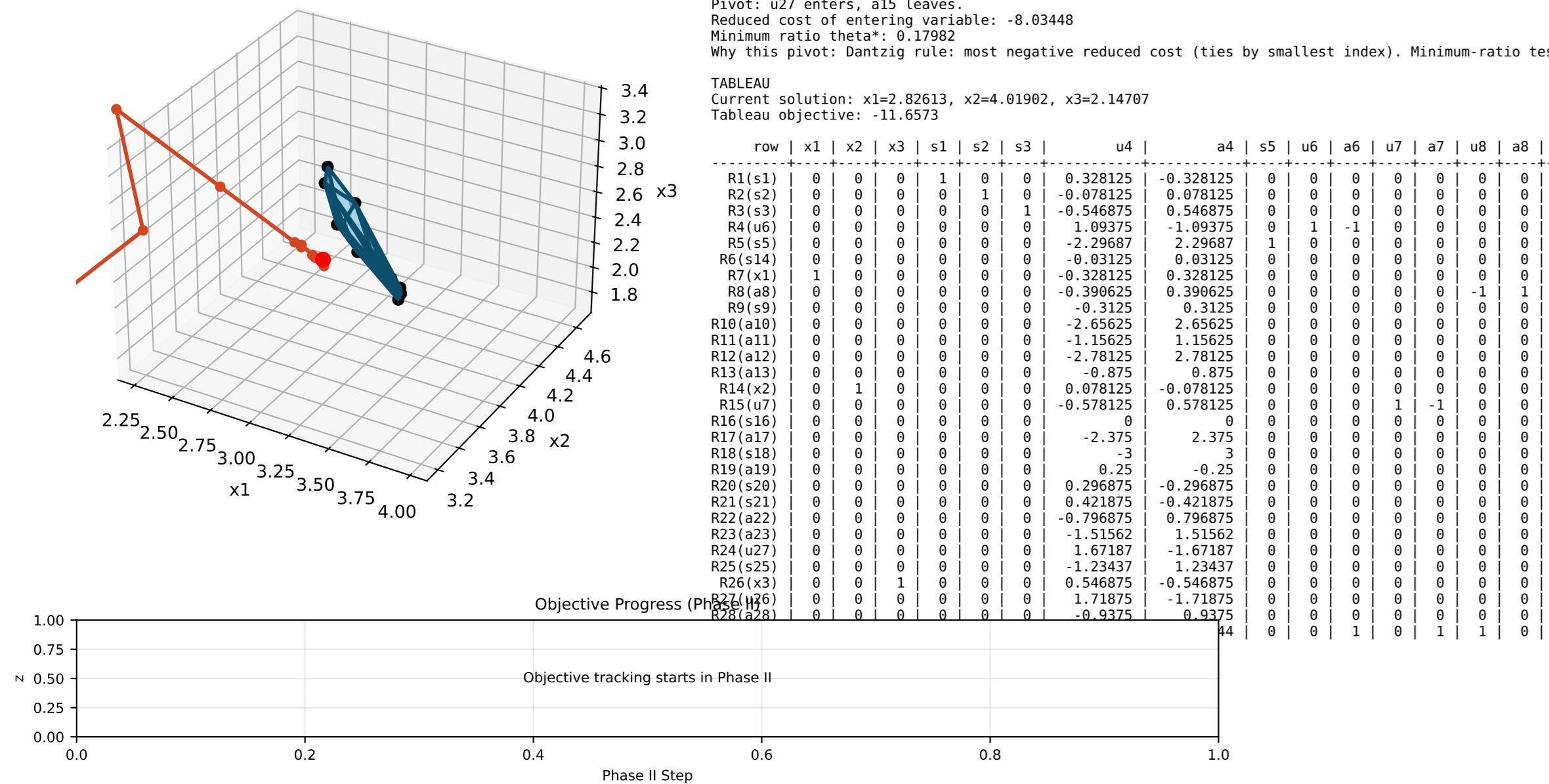
## **Phase Simplex Report**

feasible polytope + extreme points + simplex path State 11/31

I step 10 | ENTER: u27 | LEAVE: a15

```
: DANTZIG
15 leaves.
ring variable: -8.03448
: 0.17982
zig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).
```

x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
0	1	0	0	0.328125	-0.328125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.1875	0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.17387	inf			
0	0	1	0	-0.078125	0.078125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.98098	77.3293			
0	0	0	1	-0.546875	0.546875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.3125	-0.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.85293	57.3268			
0	0	0	0	1.09375	-1.09375	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.450659	inf			
0	0	0	0	-2.29687	2.29687	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.3125	-1.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.95182	5.6371		
0	0	0	0	-0.03125	0.03125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.875	-0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.07142	2.3992		
0	0	0	0	-0.328125	0.328125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.82613	27.4991		
0	0	0	0	-0.390625	0.390625	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0.9375	-0.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.04294	2.19618		
0	0	0	0	-0.3125	0.3125	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.67176	6.63658		
0	0	0	0	-2.65625	2.65625	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	2.375	-2.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.67045	2.21779		
0	0	0	0	-1.15625	1.15625	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	1.375	-1.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.57868	3.579		
0	0	0	0	-2.78125	2.78125	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	1.875	-1.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.42126	1.55371	
0	0	0	0	-0.875	0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14476	1.56307			
0	0	0	0	0.078125	-0.078125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.1875	0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.01902	inf			
0	0	0	0	-0.578125	0.578125	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.90097	18.5558			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf		
0	0	0	0	-2.375	2.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	-1.5	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.811072	1.15987		
0	0	0	0	-3	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.93889	5.56194		
0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf		
0	0	0	0	0.296875	-0.296875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.6875	-0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.02435	10.7895			
0	0	0	0	0.421875	-0.421875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.75061	26.7691			
0	0	0	0	-0.796875	0.796875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.3125	-1.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.840251	1.34017			
0	0	0	0	-1.51562	1.51562	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.4375	-1.4375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.358018	0.631234			
0	0	0	0	1.67187	-1.67187	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.8125	1.8125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.17982	0.17982			
0	0	0	0	-1.23437	1.23437	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5625	-1.5625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.50066	7.72058			
1	0	0	0	0.546875	-0.546875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.3125	0.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.14707	inf			
0	0	0	0	1.71875	-1.71875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.125	1.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.830862	inf			
0	0	0	0	-0.9375	0.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	-1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0.732642	1.24215		



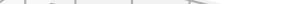




## -Phase Simplex Report

Feasible polytope + extreme points + simplex path State 1

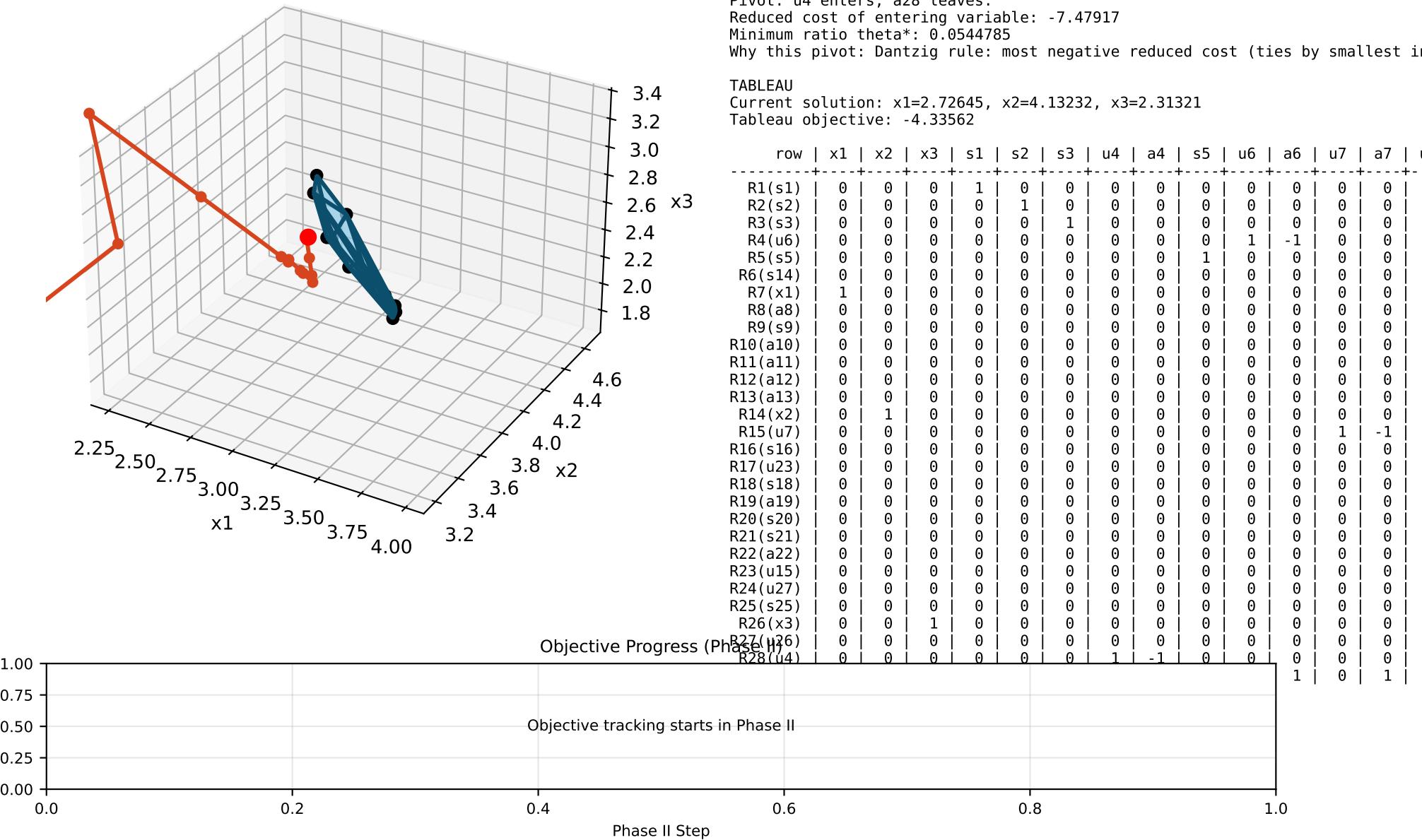
COMMENTS  
Teaching Made Easier

 Teaching Mode | Rule: DANIZIG  
Pivot: u4 enters, a28 leaves.  
Reduced cost of entering variable: -7.47917  
Minimum ratio theta\*: 0.0544785

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

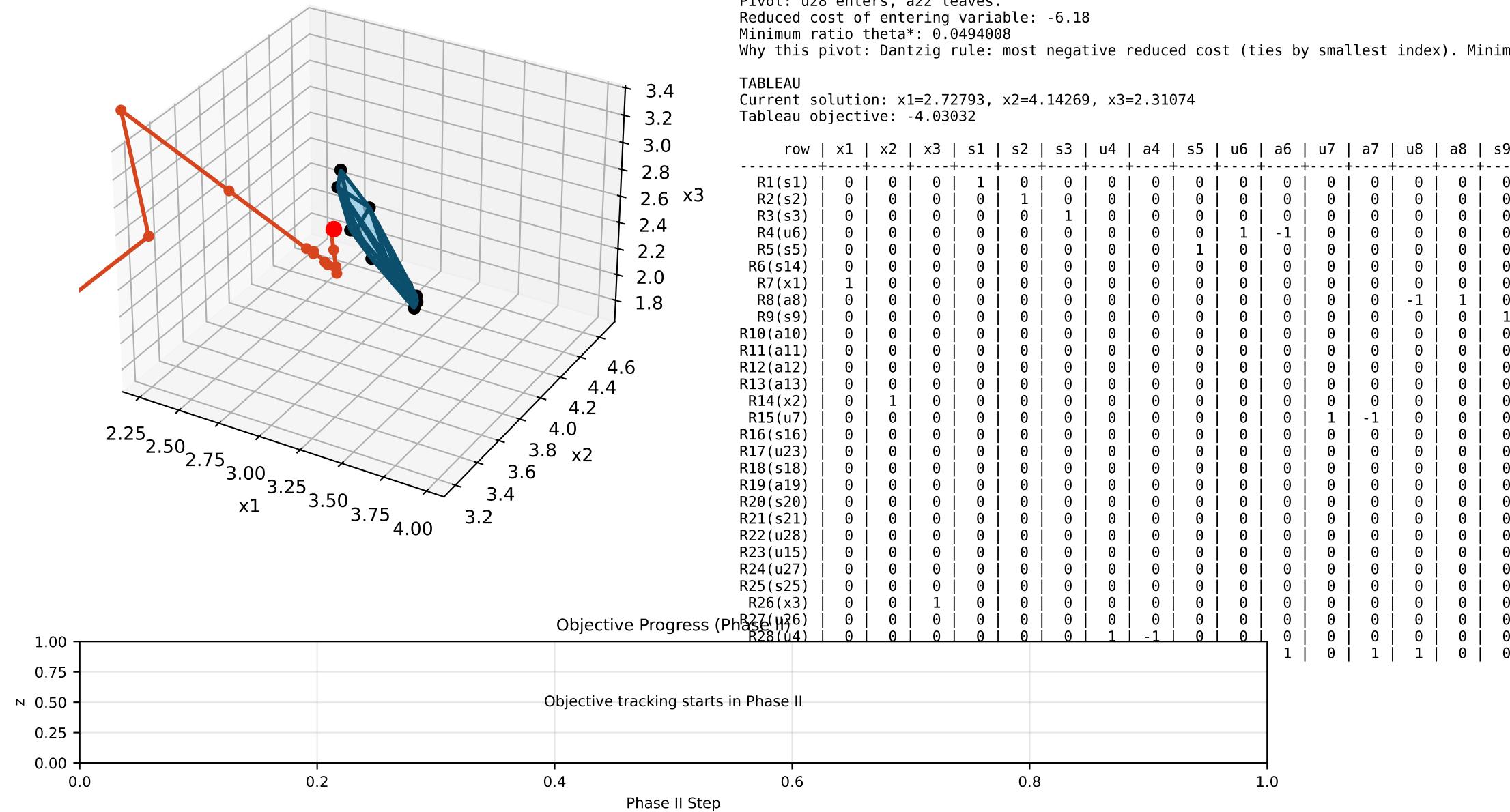
TABLEAU

**3.4** Current solution  
**3.2** Tableau objectiv



# **Phase Simplex Report**

feasible polytope + extreme points + simplex path State 15/3



tep 14 | ENTER: u28 | LEAVE: a22

| Rule: DANTZIG  
ers, a22 leaves.  
f entering variable: -6.18  
theta\*: 0.0494008  
| Dantzig rule: most negative reduced cost (ties by

on:  $x_1=2.72793$ ,  $x_2=4.14269$ ,  $x_3=2.37500$

## **Phase Simplex Report**

feasible polytope + extreme points + simplex path State 16/3

**COMMENTS**  
Teaching Mode | Rule: DANTZIG  
Pivot: u22 enters, a13 leaves.  
Reduced cost of entering variable: -4.02439  
Minimum ratio theta\*: 0.154459  
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index)

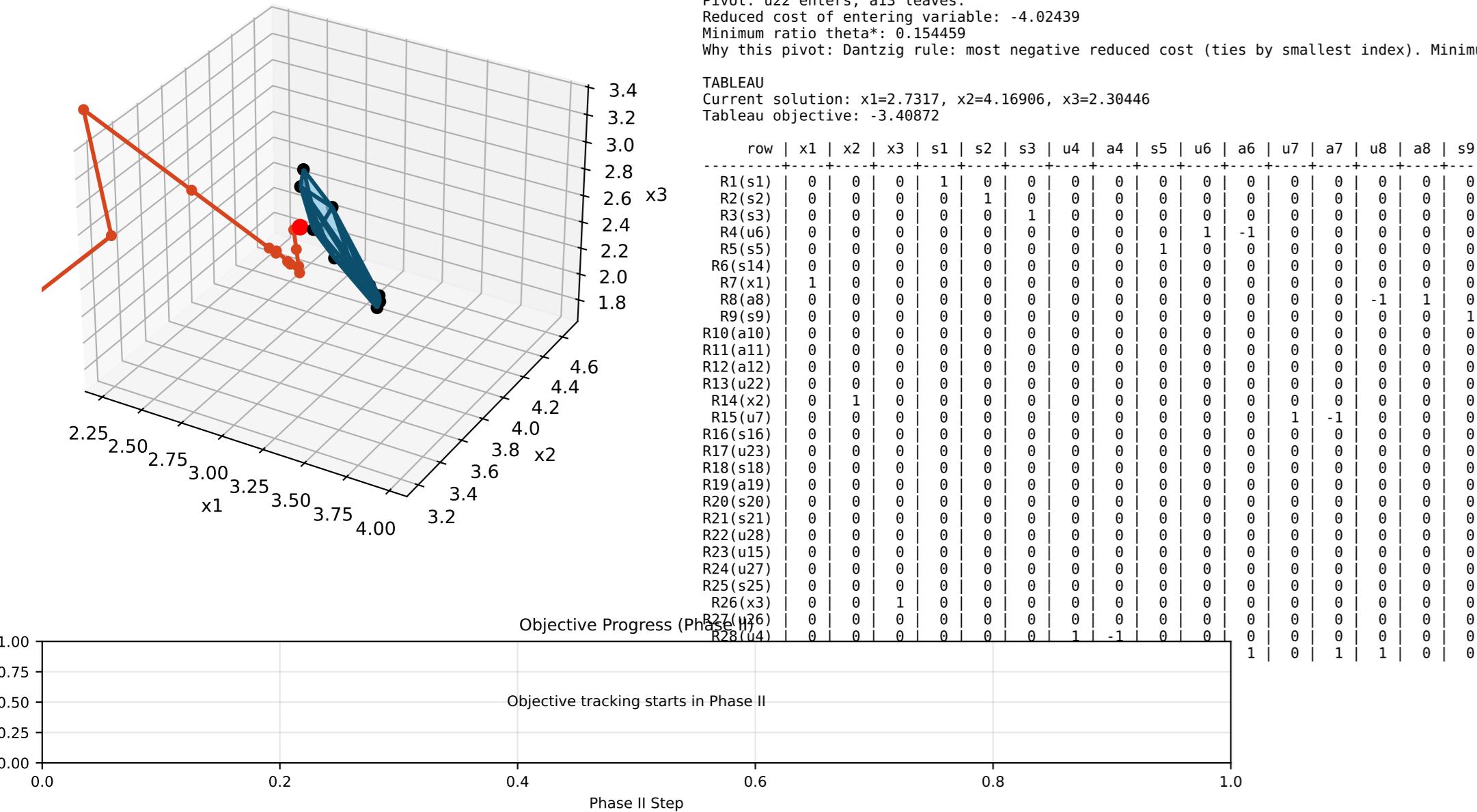
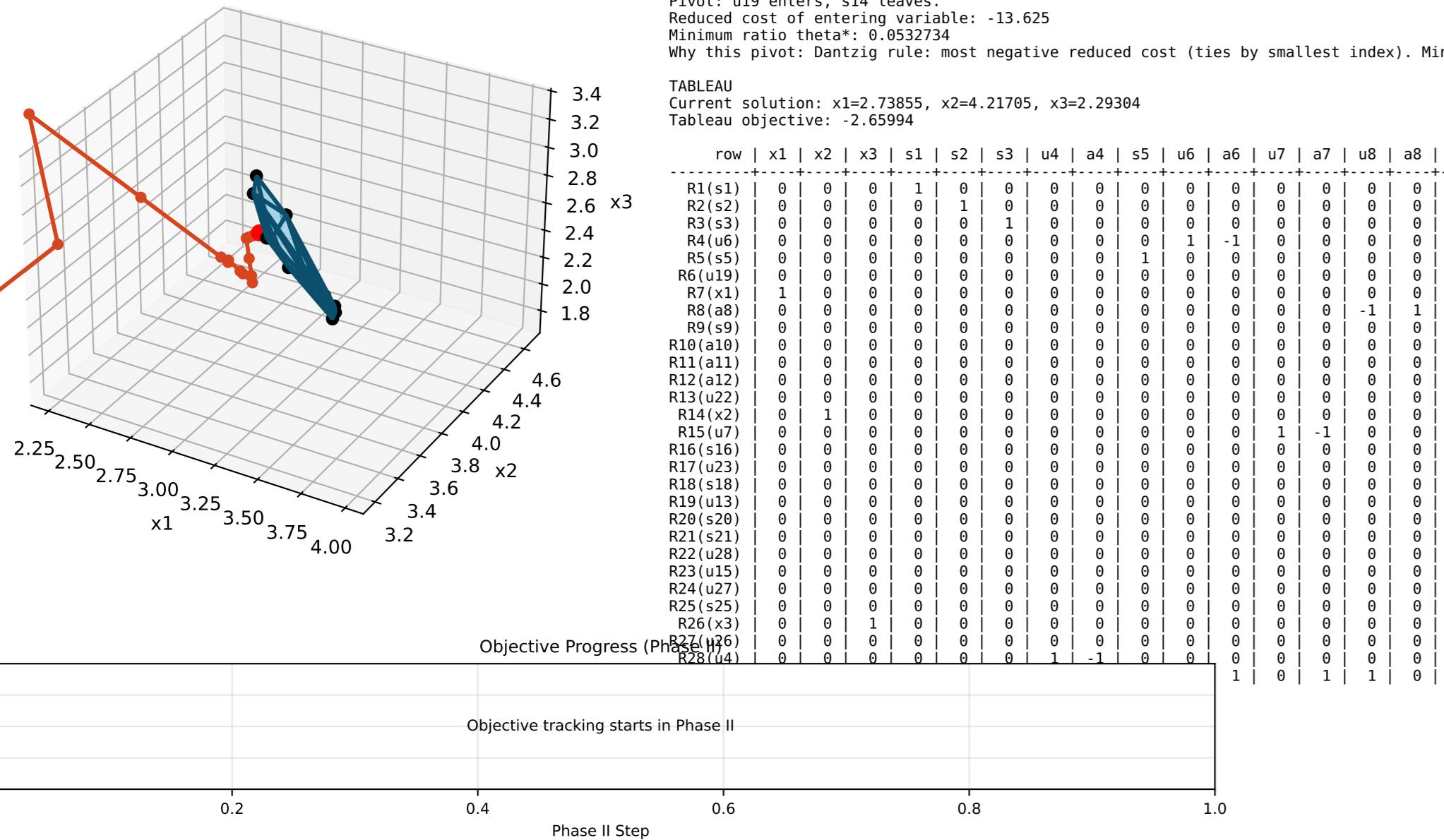


TABLEAU  
Current solution:  $x_1=2.7317$ ,  $x_2=4.16906$ ,  $x_3=2.30446$   
Tableau objective: -3.40872



# Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



# Phase Simplex Report

feasible polytope + extreme points + simplex path State 19/3

p 18 | ENTER: u17 | LEAVE: a12

TZIG

aves.

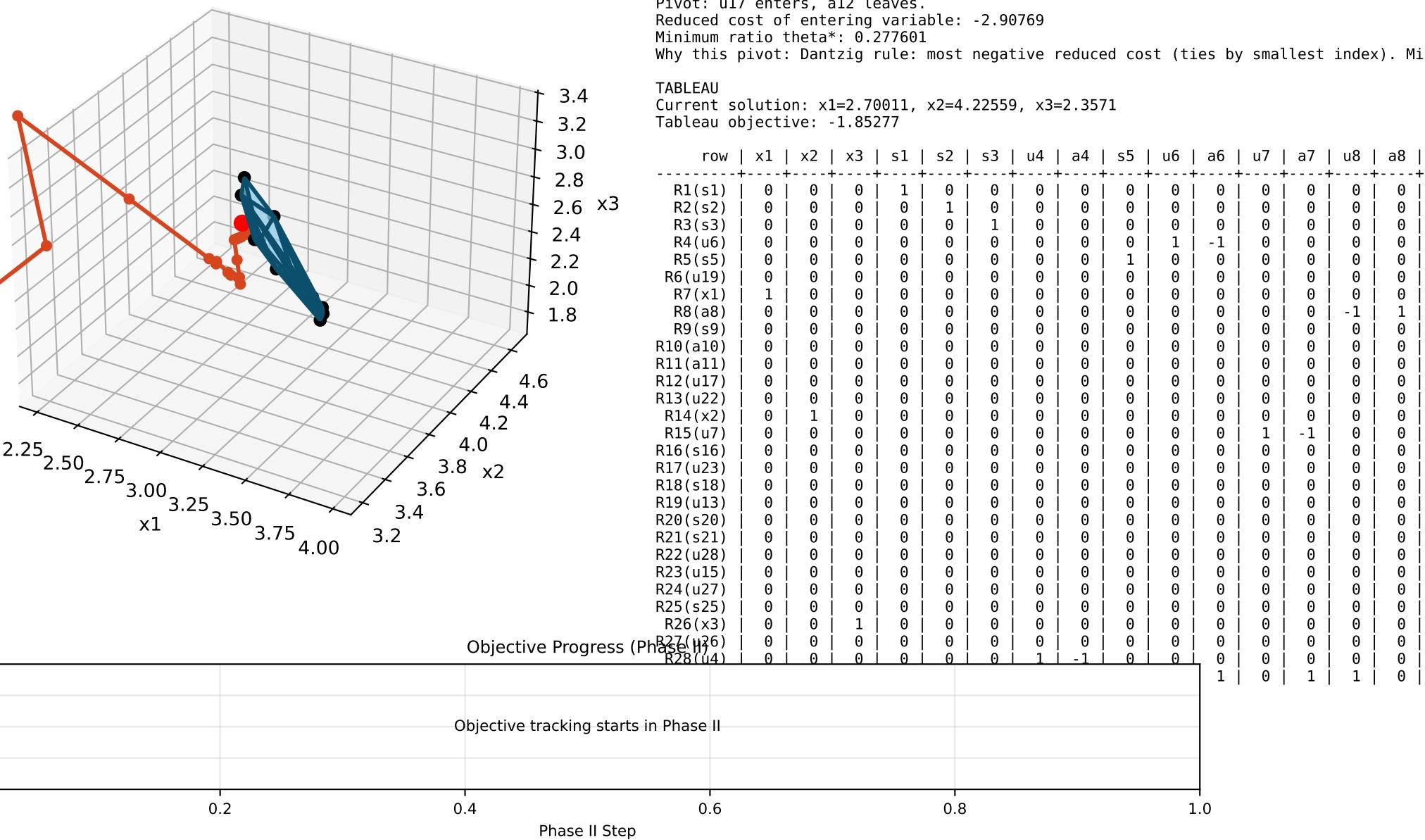
variable: -2.90769

variable 2190765  
77601

rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

011. x2=4.22559. x3=2.3571

811, X2 112255

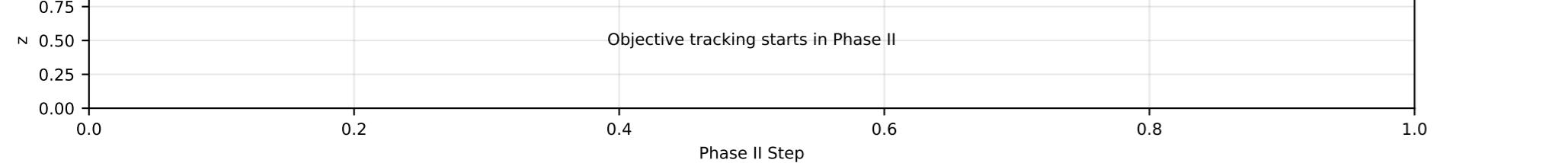


## **-Phase Simplex Report**

Feasible polytope + extreme points + simplex path State 20

**COMMENTS**  
Teaching Mode |  
Pivot: u12 enter  
Reduced cost of  
Minimum ratio th:  
Why this pivot:

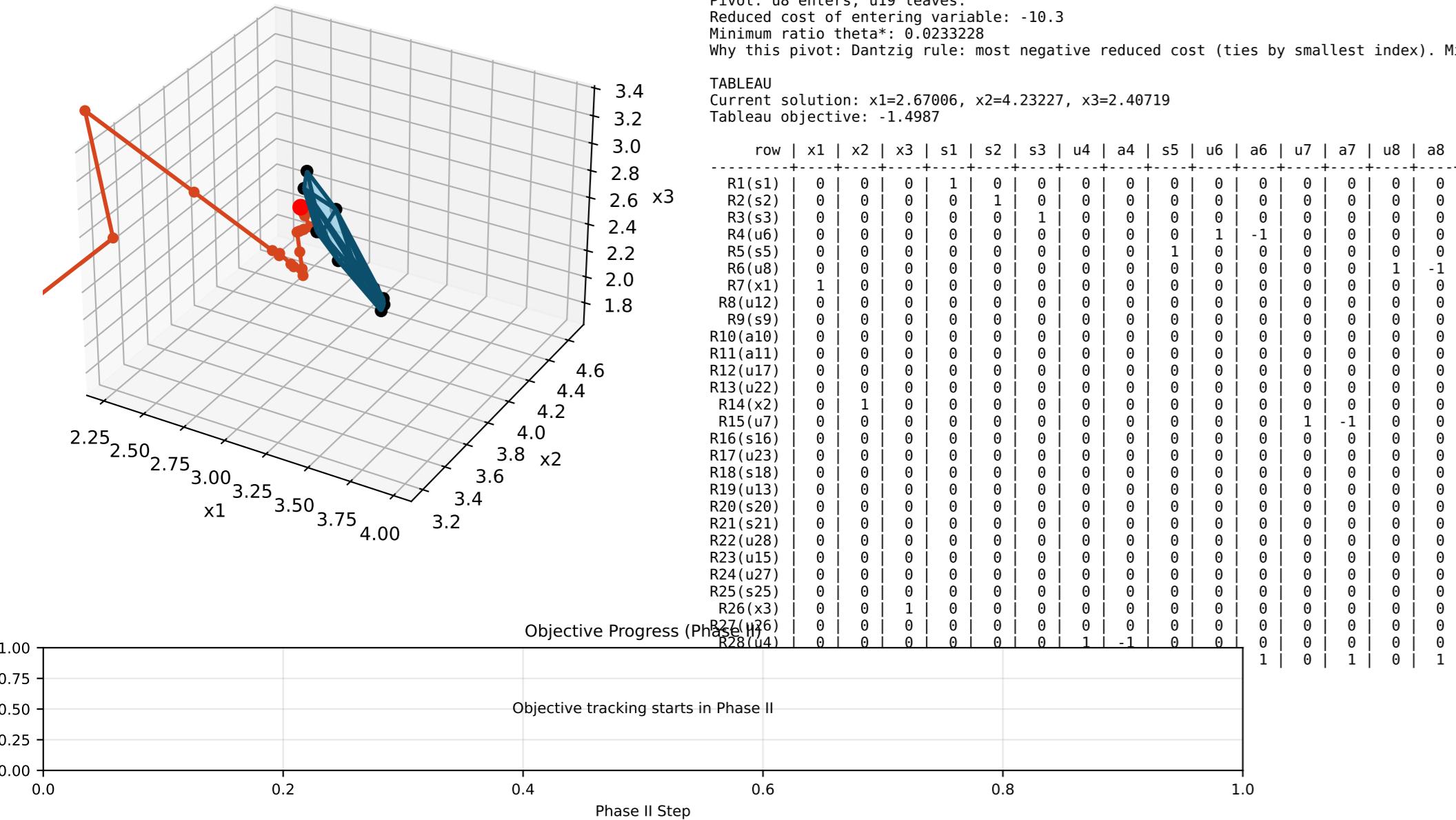
**TABLEAU**  
Current solution:  $x_1=2.69105$ ,  $x_2=4.2276$ ,  $x_3=2.37221$   
Tableau objective: -1.73893



# **Phase Simplex Report**

Feasible polytope + extreme points + simplex path State 21

**COMMENTS**  
Teaching Mode | Rule:  
Pivot: u8 enters, u19  
Reduced cost of enter  
Minimum ratio theta\*: 0.000000  
Why this pivot: Dantz



step 20 | ENTER: u8 | LEAVE: u19

## DANTZIG

## DANTZIG leaves

ing variable: -10

0.0233228

ig rule: most negativ

ing rate: most negative reduced cost (ties by smallest index). Minimum ratio test (ties by smallest row index).

$$x_1=2.67006, \quad x_2=4.23227,$$

.4987

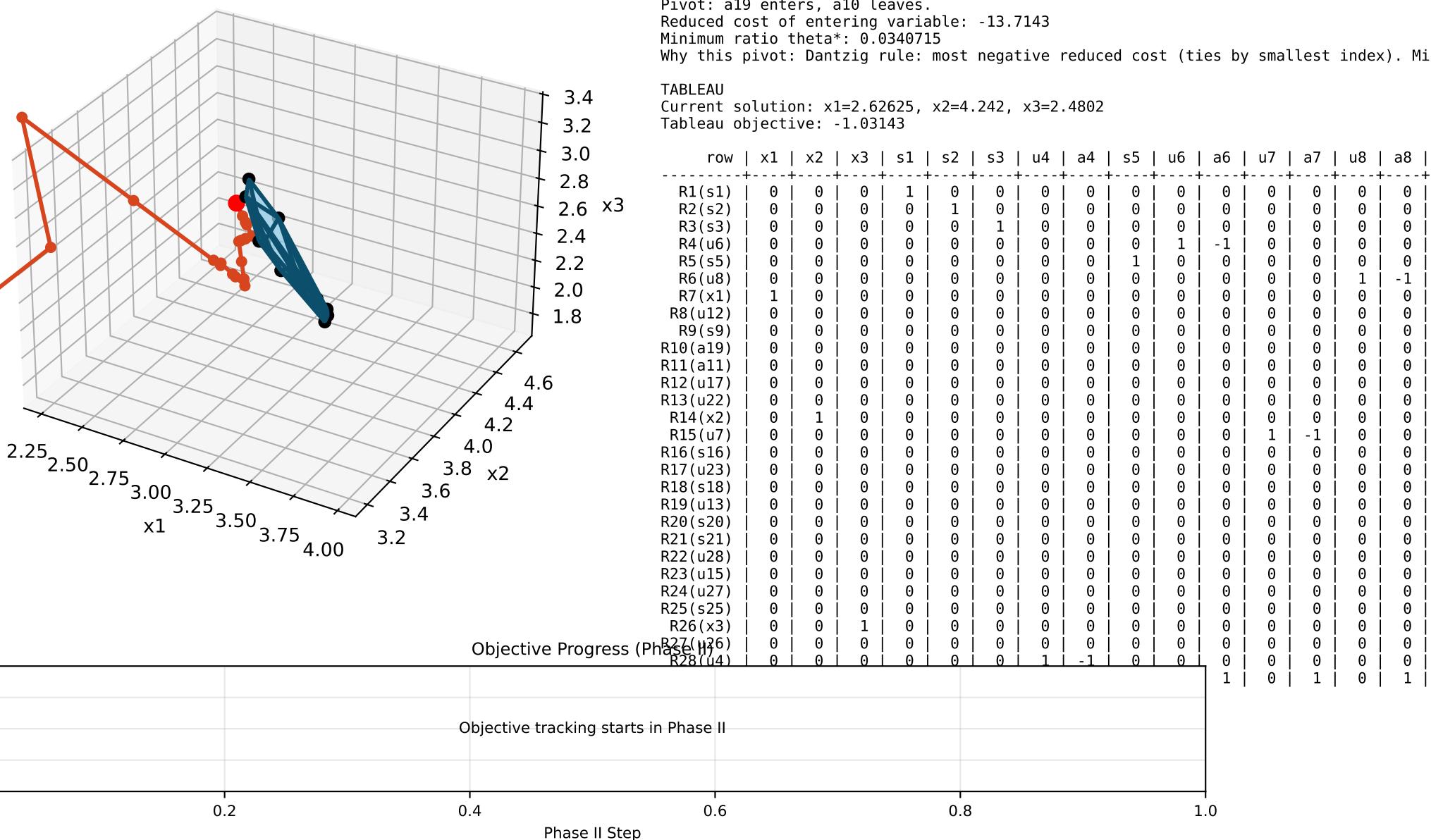
x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.214286	0	0	0	0	0	0	0	0.0714286	-0.0714286	0	0	0	0	0	0	0	0	0	9.32994	inf						
0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.214286	0	0.285714	0	0.0714286	0	0	0	-0.0714286	0.0714286	0	0	0	0	0	0	0	0	0	7.76773	38.862						
0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.357143	0	0	0	0	0	0	0	0.214286	-0.214286	0	0	0	0	0	0	0	0	0	6.41853	inf						
0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0.714286	0	0	0	0	0	0	0	0.428571	-0.428571	0	0	0	0	0	0	0	0	0	0.970897	2.85932						
0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.477183	0.0233228			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.07143	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0233228	2.99005			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.214286	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.67006	1.81875			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.857143	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.29676	0.0719964			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-2.71429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.393727	1.14286			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.57143	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14825	0.42857		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.71429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.494682	inf			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.595339	inf		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.214286	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.23227	inf		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.214286	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14962	1.80208		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.28571	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.06726	inf	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.28571	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.15977	0.530611	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-2.28571	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.504088	inf	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.71429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.109	inf	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.785714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.42299	inf	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.214286	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.593744	inf	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.42857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.23265	12.3499	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14286	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.0316	inf	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.07143	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.85697	1.49513	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.78571	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.82447	inf	
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.357143	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.40719	inf	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.28571	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.05011	0.228727	

# Phase Simplex Report

feasible polytope + extreme points + simplex path State 22/22

p 21 | ENTER: a19 | LEAVE: a10

```
TZIG  
aves.  
variable: -13.7143  
340715  
ule: most negative reduced cost (ties by smallest index).
```



## **Phase Simplex Report**

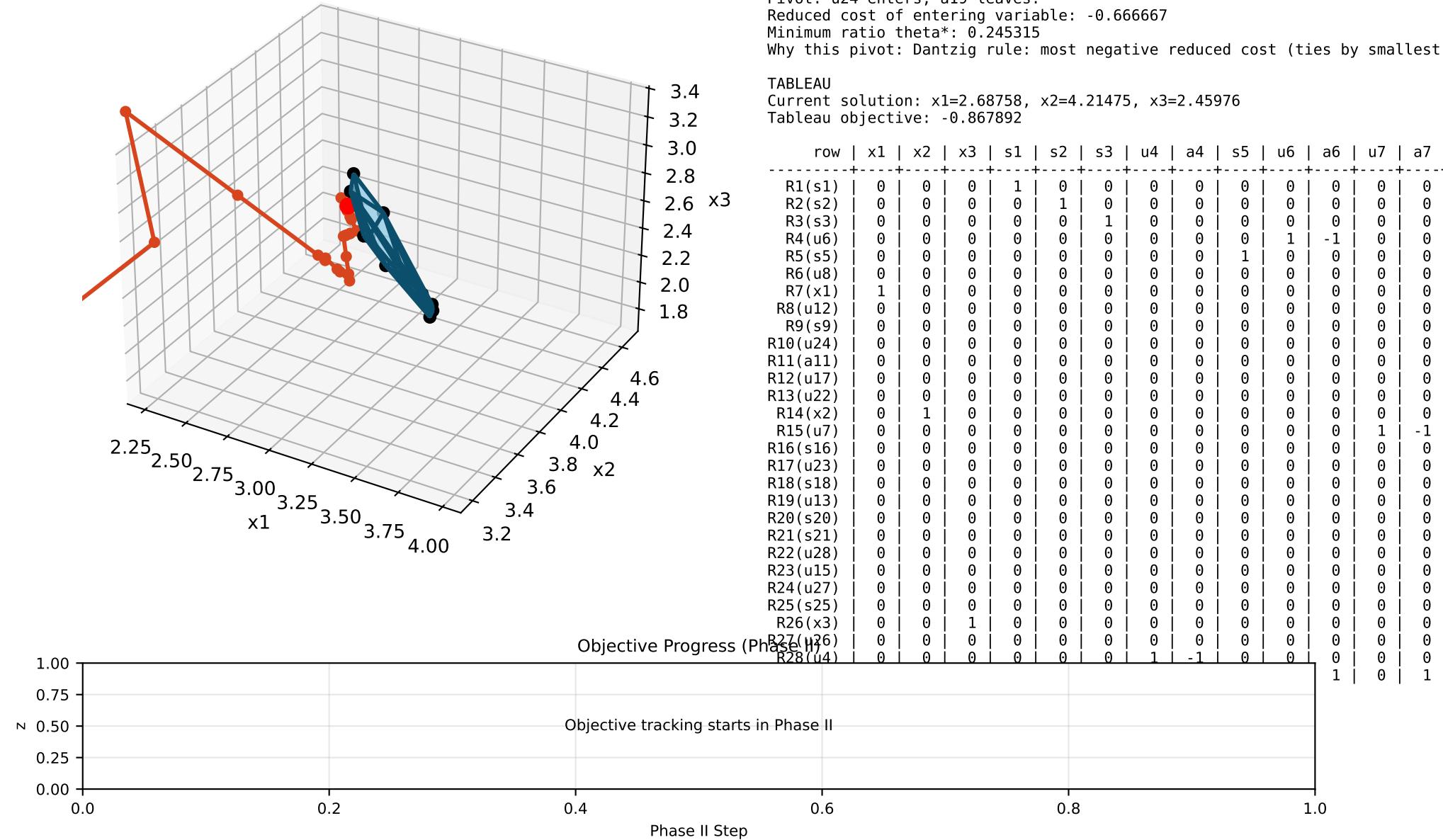
Feasible polytope + extreme points + simplex path State 23/33

#### COMMENTS

Teaching Mode | Rule: DANTZIG  
Pivot: u24 enters, a19 leaves.  
Reduced cost of entering variable: -0.666667

Reduced cost of entering variable: -0.00000  
 Minimum ratio theta\*: 0.245315  
 Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

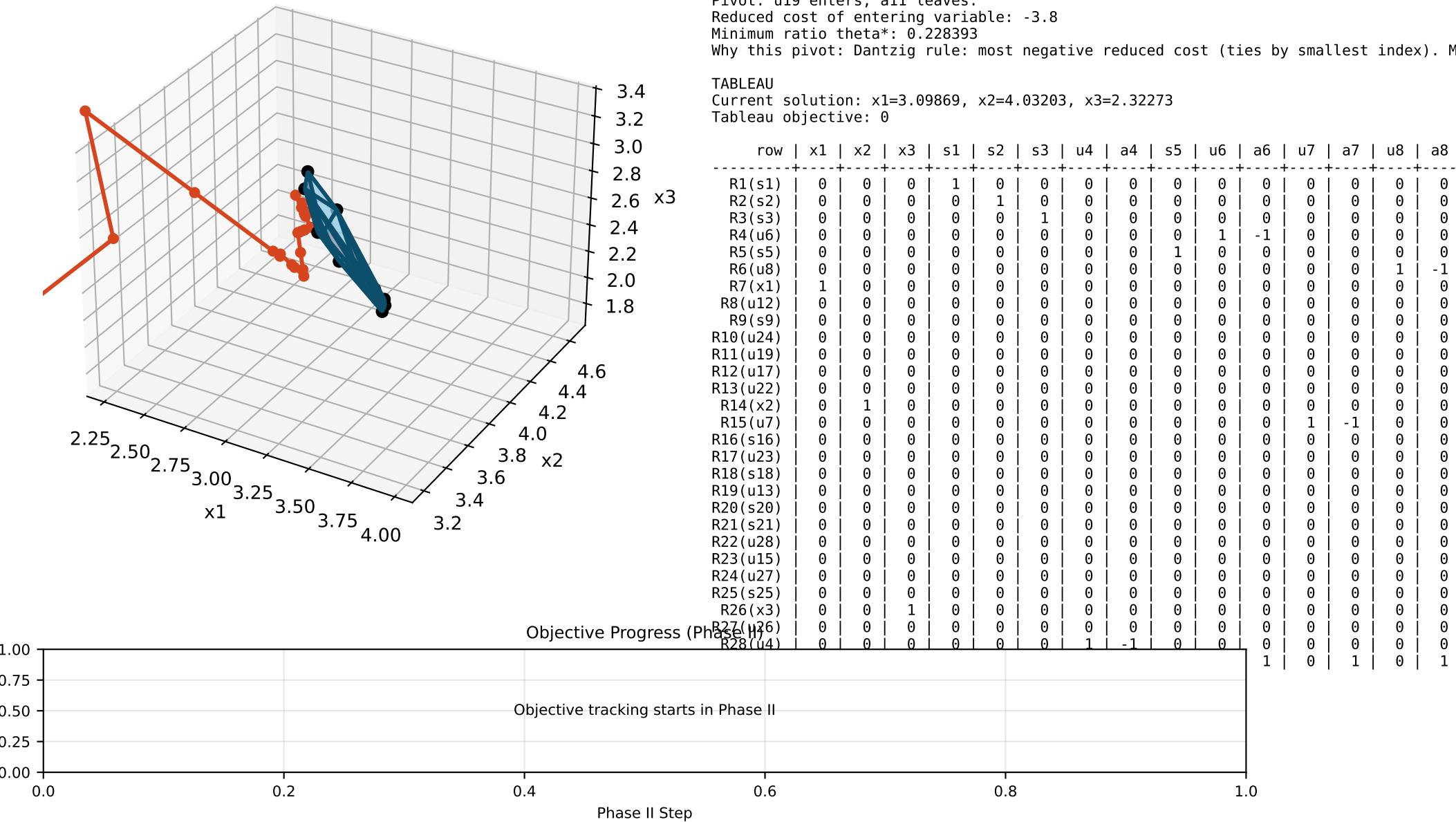
TABLEAU  
Current solution:  $x_1=2.68758$ ,  $x_2=4.21475$ ,  $x_3=2.45976$



# **Phase Simplex Report**

## Feasible polytope + extreme points + simplex path

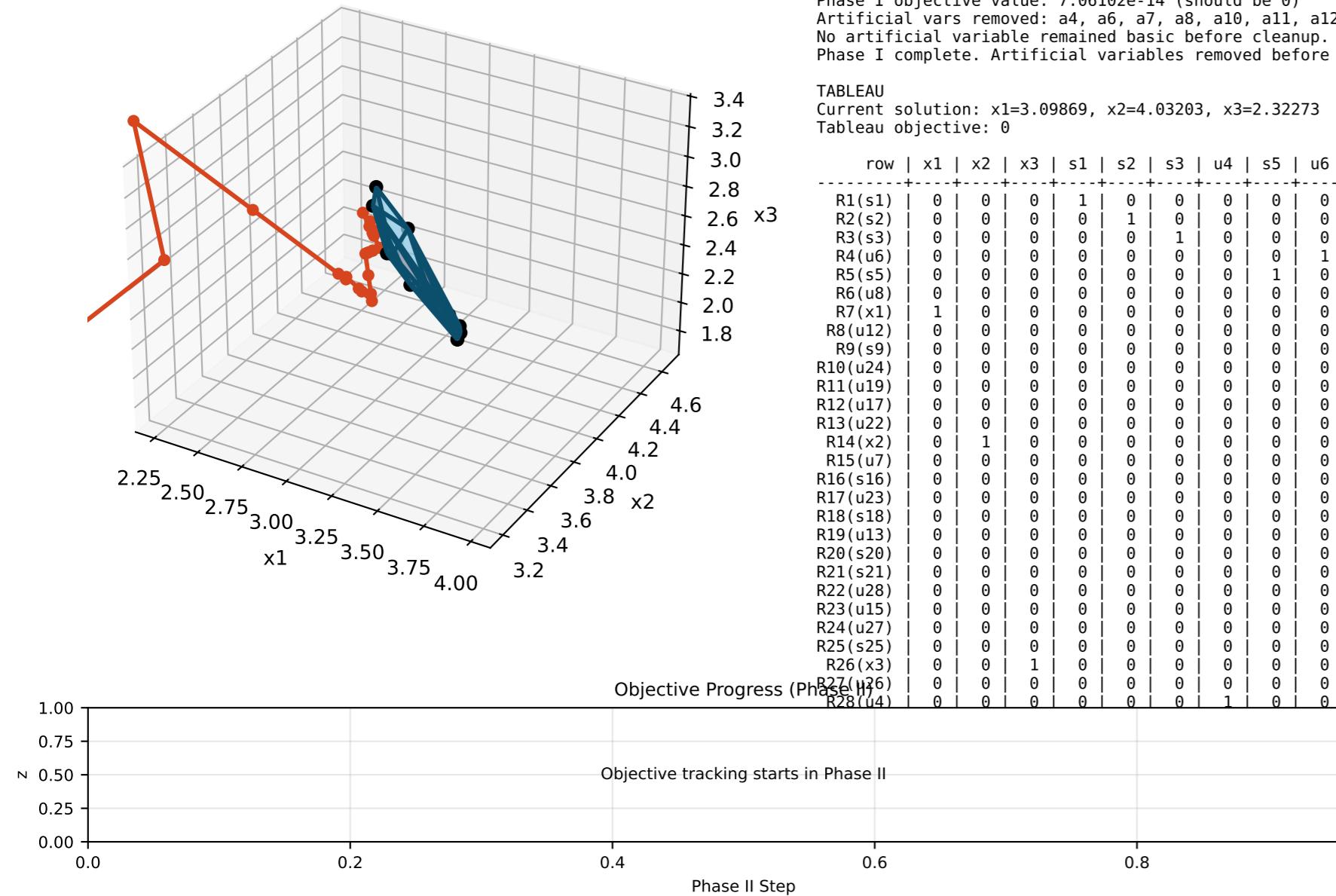
**COMMENTS**  
Teaching Mode | Rule: DANTZIG  
Pivot: u19 enters, a11 leaves.  
Reduced cost of entering variable: -3.8  
Minimum ratio theta\*: 0.228393  
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smalles



**TABLEAU**  
Current solution:  $x_1=3.09869$ ,  $x_2=4.03203$ ,  $x_3=2.32273$   
Tableau objective: 0

# **Phase Simplex Report**

Feasible polytope + extreme points + simplex path



25/31 | PHASE I -> PHASE II step 0

ENTS

ing Mode | Phase Transition

I objective value: 7.06102e-14 (should be 0)

Initial vars removed: a4, a6, a7, a8, a10, a11, a

Artificial variable remained basic

I complete. Artificial variables removed before restoring original

AU

nt solution:  $x_1=3.09869$ ,  $x_2=4.03203$ ,  $x_3=2.32273$

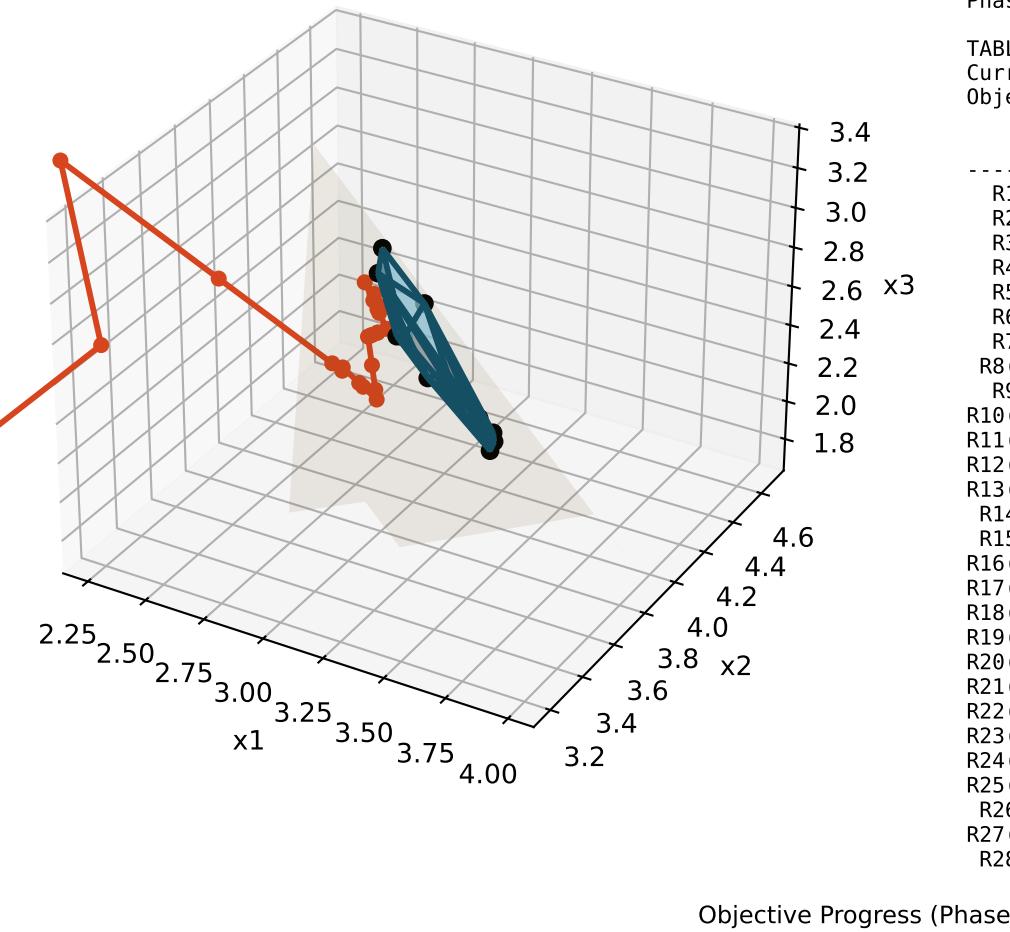
Final objective: 0

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio				
s1)	0	0	0	1	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.90131	inf				
s2)	0	0	0	0	1	0	0	0	0	0	0	0	0.118421	-0.210526	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.96797	inf				
s3)	0	0	0	0	0	1	0	0	0	0	0	0	0.276316	-0.157895	0	0	0.144737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.67727	inf				
u6)	0	0	0	0	0	0	0	0	0	1	0	0	-0.552632	0.315789	0	0	-0.289474	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.801961	inf				
s5)	0	0	0	0	0	0	0	1	0	0	0	0	0.671053	0.473684	0	0	1.06579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.08024	inf				
u8)	0	0	0	0	0	0	0	0	0	0	1	0	0.223684	-0.842105	0	0	0.355263	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.911881	inf				
x1)	1	0	0	0	0	0	0	0	0	0	0	0	0.328947	-0.473684	0	0	-0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.09869	inf				
x12)	0	0	0	0	0	0	0	0	0	0	0	0	-1.23684	0.421053	1	0	-0.552632	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.203795	inf			
s9)	0	0	0	0	0	0	0	0	0	0	0	0	1	-0.342105	1.05263	0	0	-0.131579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.729953	inf			
x24)	0	0	0	0	0	0	0	0	0	0	0	0	0	0.815789	-1.89474	0	0	-0.763158	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.88974	inf			
x19)	0	0	0	0	0	0	0	0	0	0	0	0	0	0.210526	-0.263158	0	0	0.157895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.228393	inf			
x17)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.789474	-0.263158	0	0	-0.842105	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1.07352	inf		
x22)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.223684	-0.157895	0	0	0.644737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.855033	inf		
x2x2)	0	1	0	0	0	0	0	0	0	0	0	0	-0.118421	0.210526	0	0	0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.03203	inf		
u7)	0	0	0	0	0	0	0	0	0	0	1	0	0	0.539474	-0.736842	0	0	0.0921053	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.4591	inf		
x16)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.815789	1.89474	0	0	0.763158	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.78415	inf	
x23)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.592105	0.0526316	0	0	0.118421	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.21433	inf	
x18)	0	0	0	0	0	0	0	0	0	0	0	0	0	1.18421	-0.105263	0	0	0.763158	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	3.86563	inf	
x13)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.342105	0.0526316	0	1	0.868421	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.563544	inf		
x20)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	-0.934211	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.68037	inf	
x21)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.302632	0.315789	0	0	-0.539474	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.16645	inf	
x28)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0526316	-0.684211	0	0	0.210526	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.39783	inf
x15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0.263158	-0.578947	0	0	0.947368	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.80521	inf	
x27)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.828947	0.473684	0	0	0.565789	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.7782	inf	
x25)	0	0	0	0	0	0	0	0	0	0	0	0	0	0.118421	0.789474	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.90896	inf	
x3x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	-0.276316	0.157895	0	0	-0.144737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.32273	inf	
x86)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.947368	0.684211	0	0	-0.210526	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.37083	inf	
x44)	0	0	0	0	0	0	0	1	0	0	0	0	0	0.842105	-1.05263	0	0	0.631579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.1423	inf	

## **o-Phase Simplex Report**

Feasible polytope + extreme points + simplex path

$$15 \times 1 + 10 \times 2 + 12 \times 3 = 115$$



te 26/31 | PHASE II step 0 | Z=114.673

## MENTS

atching Mode | PHASE II

use II objective restored and made basis-consistent.

LEAU

current solution:  $x_1=3.09869$ ,  $x_2=4.03203$ ,  $x_3=2.32273$

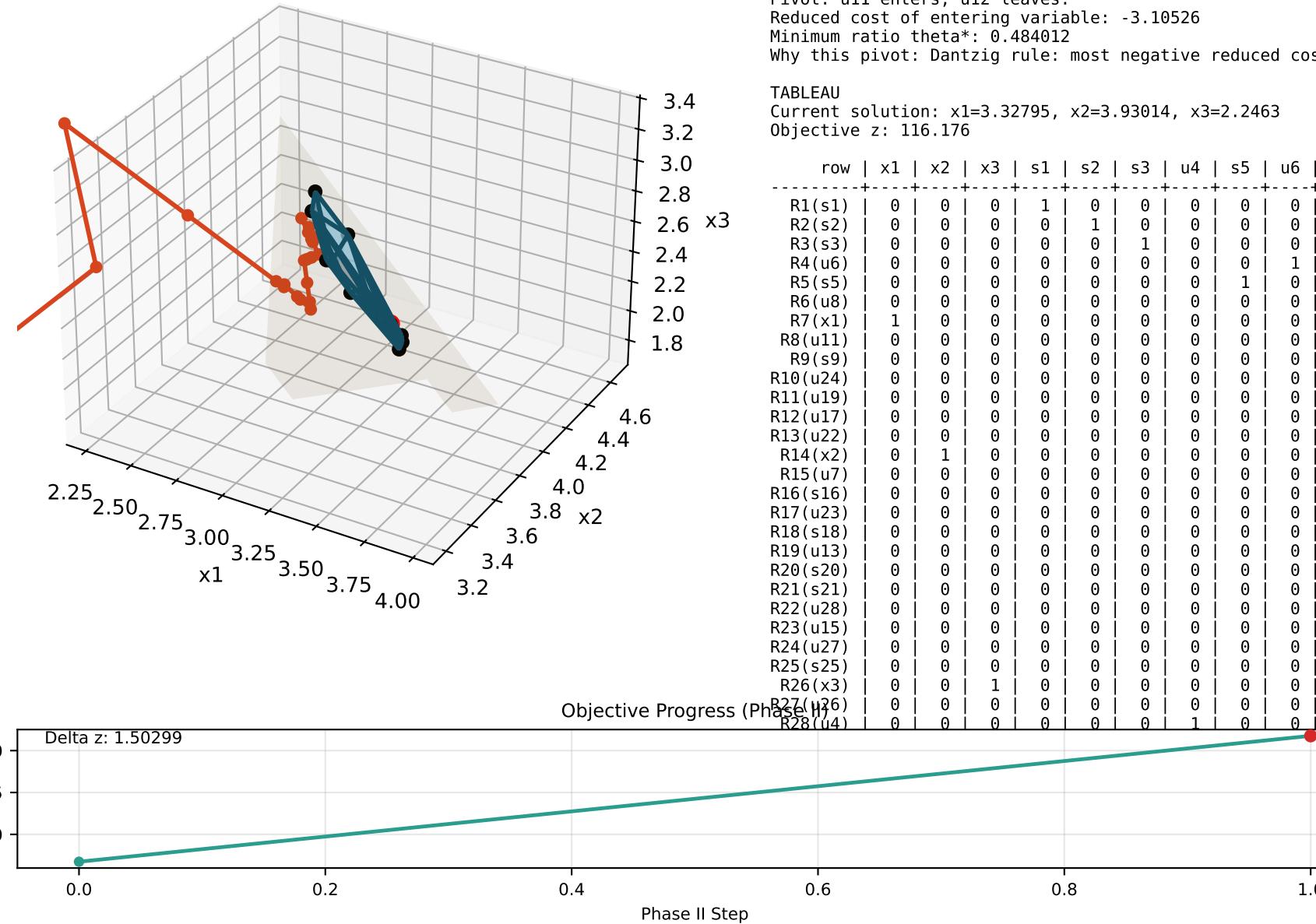
negative z: 114.673

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio			
1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.90131	inf		
2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0.118421	-0.210526	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.96797	inf		
3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0.276316	-0.157895	0	0	0.144737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.67727	inf		
4(u6)	0	0	0	0	0	0	0	0	0	1	0	0	-0.552632	0.315789	0	0	-0.289474	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.801961	inf		
5(s5)	0	0	0	0	0	0	0	0	1	0	0	0	0.671053	0.473684	0	0	1.06579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.08024	inf		
5(u8)	0	0	0	0	0	0	0	0	0	0	1	0	0.223684	-0.842105	0	0	0.355263	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.911881	inf		
7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0.328947	-0.473684	0	0	-0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.09869	inf		
(u12)	0	0	0	0	0	0	0	0	0	0	0	0	-1.23684	0.421053	1	0	-0.552632	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.203795	inf	
9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	1	-0.342105	1.05263	0	0	-0.131579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.729953	inf	
(u24)	0	0	0	0	0	0	0	0	0	0	0	0	0.815789	-1.89474	0	0	-0.763158	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.88974	inf	
(u19)	0	0	0	0	0	0	0	0	0	0	0	0	0.210526	-0.263158	0	0	0.157895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.228393	inf		
(u17)	0	0	0	0	0	0	0	0	0	0	0	0	-0.789474	-0.263158	0	0	-0.842105	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	1.07352	inf	
(u22)	0	0	0	0	0	0	0	0	0	0	0	0	-0.223684	-0.157895	0	0	0.644737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.855033	inf	
4(x2)	0	1	0	0	0	0	0	0	0	0	0	0	-0.118421	0.210526	0	0	0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.03203	inf	
5(u7)	0	0	0	0	0	0	0	0	0	1	0	0	0.539474	-0.736842	0	0	0.0921053	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.4591	inf	
(s16)	0	0	0	0	0	0	0	0	0	0	0	0	-0.815789	1.89474	0	0	0.763158	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.78415	inf
(u23)	0	0	0	0	0	0	0	0	0	0	0	0	-0.592105	0.0526316	0	0	0.118421	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.21433	inf	
(s18)	0	0	0	0	0	0	0	0	0	0	0	0	1.18421	-0.105263	0	0	0.763158	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	3.86563	inf	
(u13)	0	0	0	0	0	0	0	0	0	0	0	0	-0.342105	0.0526316	0	1	0.868421	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.563544	inf	
(s20)	0	0	0	0	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	-0.934211	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	2.68037	inf	
(s21)	0	0	0	0	0	0	0	0	0	0	0	0	-0.302632	0.315789	0	0	-0.539474	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	2.16645	inf	
(u28)	0	0	0	0	0	0	0	0	0	0	0	0	-0.0526316	-0.684211	0	0	0.210526	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.39783	inf
(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0.263158	-0.578947	0	0	0.947368	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.80521	inf	
(u27)	0	0	0	0	0	0	0	0	0	0	0	0	-0.828947	0.473684	0	0	0.565789	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.7782	inf	
(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0.118421	0.789474	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.90896	inf	
(x3)	0	0	1	0	0	0	0	0	0	0	0	0	-0.276316	0.157895	0	0	-0.144737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.32273	inf	
(u26)	0	0	0	0	0	0	1	0	0	0	0	0	-0.947368	0.684211	0	0	-0.210526	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.37083	inf	
(s4)	0	0	0	0	0	0	1	0	0	0	0	0	0.842105	-1.05263	0	0	0.631579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.1423	inf	
Rz	0	0	0	0	0	0	0	0	0	0	0	0	0.434211	-3.10526	0	0	-0.486842	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	114.673	-

## **Phase Simplex Report**

## Feasible polytope + extreme points + simplex path

$$15 \times 1 + 10 \times 2 + 12 \times 3 = 116$$



27/31 | PHASE II step 1 | ENTER: u11 | LEAVE: u12 | Z=116.

ENTS

ing Mode | Rule: DANTZIG

: u11 enters, u12 leaves.

ed cost of entering variable: -3.10526

um ratio theta\*: 0.484

this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

AU

nt solution: x1=3.32795, x2=3.93014, x3=2.2463

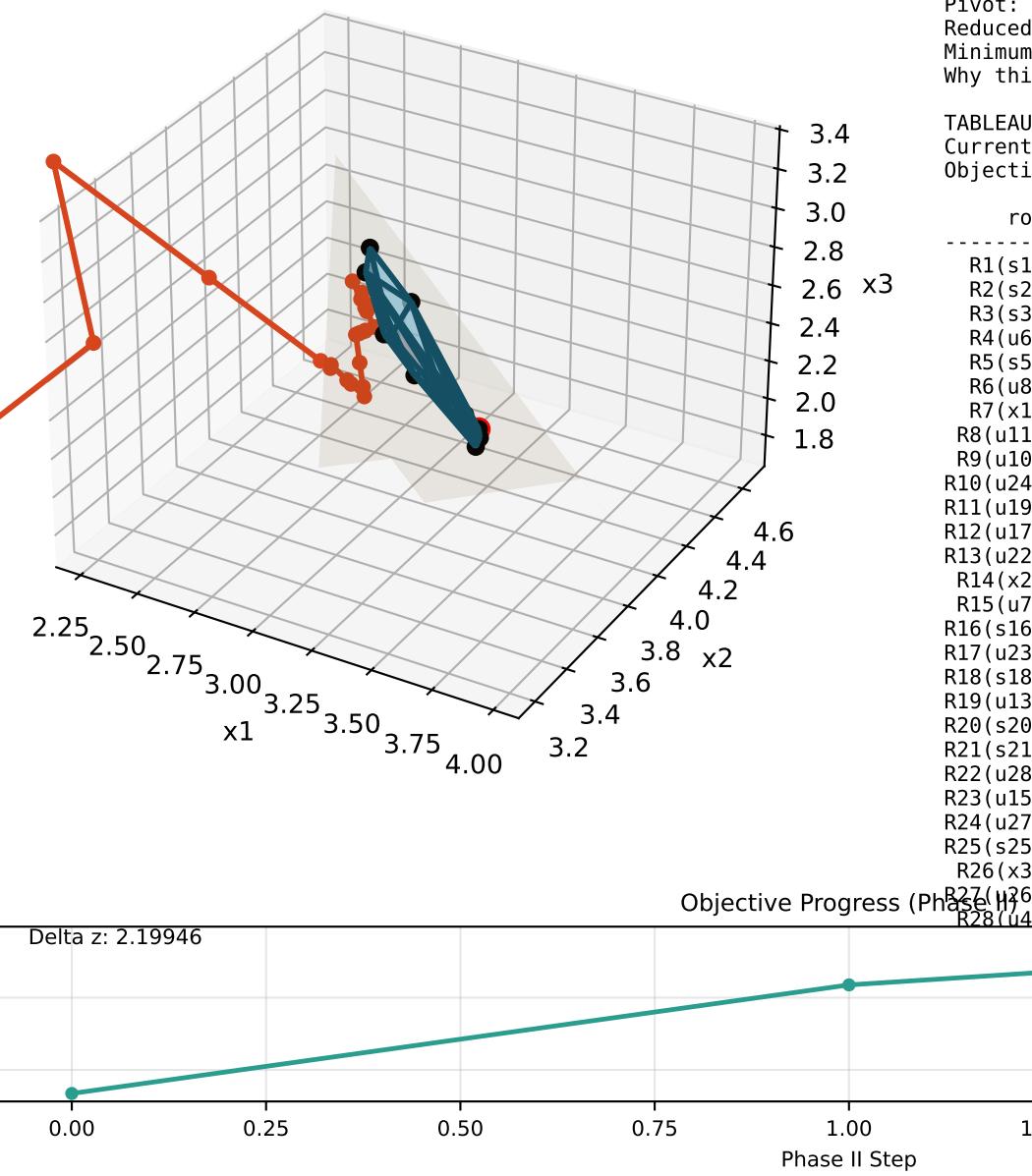
tive z: 116.176

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio	
s1)	0	0	0	1	0	0	0	0	0	0	0	0	1.0625	0	-1.125	0	0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	8.67205	18.7917		
s2)	0	0	0	0	1	0	0	0	0	0	0	0	-0.5	0	0.5	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	8.06986	inf			
s3)	0	0	0	0	0	1	0	0	0	0	0	0	-0.1875	0	0.375	0	-0.0625	0	0	0	0	0	0	0	0	0	0	0	0	9.7537	inf			
u6)	0	0	0	0	0	0	0	0	0	1	0	0	0.375	0	-0.75	0	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0.649115	2.53954			
s5)	0	0	0	0	0	0	0	0	1	0	0	0	2.0625	0	-1.125	0	1.6875	0	0	0	0	0	0	0	0	0	0	0	0	1.85097	4.39162			
u8)	0	0	0	0	0	0	0	0	0	0	1	0	-2.25	0	2	0	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	1.31947	inf		
x1)	1	0	0	0	0	0	0	0	0	0	0	0	-1.0625	0	1.125	0	-0.6875	0	0	0	0	0	0	0	0	0	0	0	0	3.32795	inf			
u11)	0	0	0	0	0	0	0	0	0	0	0	0	-2.9375	1	2.375	0	-1.3125	0	0	0	0	0	0	0	0	0	0	0	0	0.484012	0.484012			
s9)	0	0	0	0	0	0	0	0	0	0	0	1	2.75	0	-2.5	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0.220467	0.693456			
u24)	0	0	0	0	0	0	0	0	0	0	0	0	-4.75	0	4.5	0	-3.25	0	0	0	0	0	0	0	0	0	0	0	0	2.80682	inf			
u19)	0	0	0	0	0	0	0	0	0	0	0	0	-0.5625	0	0.625	0	-0.1875	0	0	0	0	1	0	0	0	0	0	0	0	0.355764	inf			
u17)	0	0	0	0	0	0	0	0	0	0	0	0	-1.5625	0	0.625	0	-1.1875	0	0	0	1	0	0	0	0	0	0	0	0	1.2009	inf			
u22)	0	0	0	0	0	0	0	0	0	0	0	0	-0.6875	0	0.375	0	0.4375	0	0	0	0	0	0	0	0	0	0	0	0	0.931456	inf			
x2)	0	1	0	0	0	0	0	0	0	0	0	0	0.5	0	-0.5	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	3.93014	19.1522		
u7)	0	0	0	0	0	0	0	0	0	1	0	0	-1.625	0	1.75	0	-0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	2.81574	inf		
u16)	0	0	0	0	0	0	0	0	0	0	0	0	4.75	0	-4.5	0	3.25	0	1	0	0	0	0	0	0	0	0	0	0	0	2.86707	1.99719		
u23)	0	0	0	0	0	0	0	0	0	0	0	0	-0.4375	0	-0.125	0	0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	1.18885	23.0722		
u18)	0	0	0	0	0	0	0	0	0	0	0	0	0.875	0	0.25	0	0.625	0	0	0	1	0	0	0	0	0	0	0	0	3.91658	inf			
u13)	0	0	0	0	0	0	0	0	0	0	0	0	-0.1875	0	-0.125	1	0.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0.53807	10.7073		
u20)	0	0	0	0	0	0	0	0	0	0	0	0	1.0625	0	-1.125	0	-0.3125	0	0	0	0	0	1	0	0	0	0	0	0	0	2.4511	5.65856		
u21)	0	1	0	0	0	0	0	0	0	0	0	0	0.625	0	-0.75	0	-0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	2.0136	6.86041		
u28)	0	0	0	0	0	0	0	0	0	0	0	0	-2.0625	0	1.625	0	-0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.729	inf	
u15)	0	0	0	0	0	0	0	0	0	0	0	0	-1.4375	0	1.375	0	0.1875	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.08542	inf
u27)	0	0	0	0	0	0	0	0	0	0	0	0	0.5625	0	-1.125	0	1.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.54893	3.75397	
u25)	0	0	0	0	0	0	0	0	0	0	0	0	2.4375	0	-1.875	0	0.8125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.52684	4.95134	
x3)	0	0	1	0	0	0	0	0	0	0	0	0	0.1875	0	-0.375	0	0.0625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.2463	14.7106	
u26)	0	0	0	0	0	0	0	0	0	0	0	0	1.0625	0	-1.625	0	0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.03967	2.00352	
u4)	0	0	0	0	0	0	0	1	0	0	0	0	-2.25	0	2.5	0	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.65178	inf	
													0	0	-8.6875	0	7.375	0	-4.5625	0	0	0	0	0	0	0	0	0	0	0	0	0	116.176	-

# Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 117$$



State 28/31 | PHASE II step 2 | ENTER: u10 | LEAVE: s9 | Z=116.873

## COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u10 enters, s9 leaves.

Reduced cost of entering variable: -8.6875

Minimum ratio theta\*: 0.0801697

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

## TABLEAU

Current solution:  $x_1=3.41314$ ,  $x_2=3.89005$ ,  $x_3=2.23127$

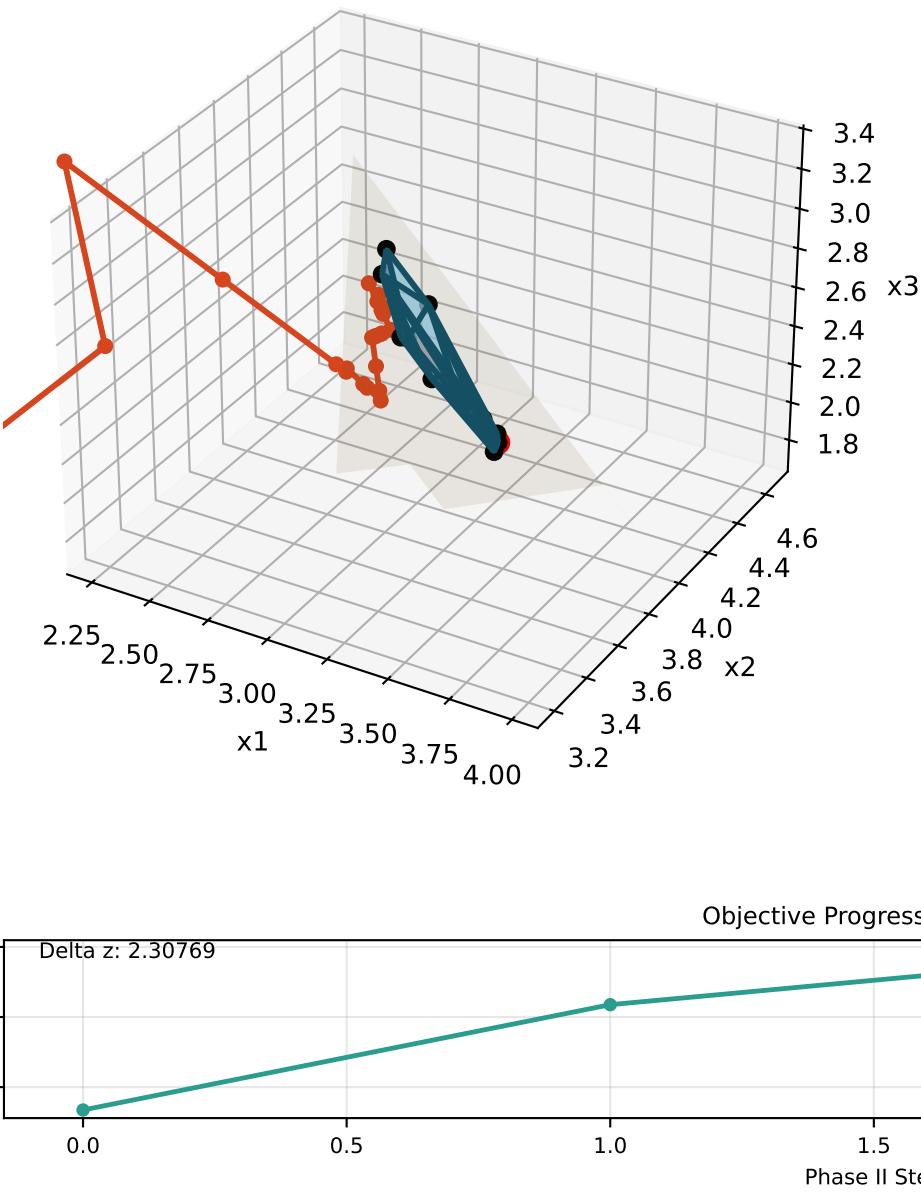
Objective z: 116.873

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio			
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	-0.386364	0	0	-0.159091	0	0.204545	0	0	0	0	0	0	0	0	0	0	0	0	0	8.58686	8.16193				
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0.181818	0	0	0.0454545	0	-0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	8.10995	inf				
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0.0681818	0	0	0.204545	0	0.0227273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.76873	inf			
R4(u6)	0	0	0	0	0	0	0	0	0	1	0	-0.136364	0	0	-0.409091	0	-0.0454545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.619051	1.73097			
R5(s5)	0	0	0	0	0	0	0	0	1	0	0	-0.75	0	0	0.75	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.68562	0.897442		
R6(u8)	0	0	0	0	0	0	0	0	0	0	1	0.818182	0	0	-0.0454545	0	0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.49985	inf		
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0.386364	0	0	0.159091	0	-0.204545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.41314	inf		
R8(u11)	0	0	0	0	0	0	0	0	0	0	0	1.06818	0	1	-0.295455	0	0.0227273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.719511	inf		
R9(u10)	0	0	0	0	0	0	0	0	0	0	0	0.363636	1	0	-0.909091	0	0.454545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0801697	0.0801697		
R10(u24)	0	0	0	0	0	0	0	0	0	0	0	1.72727	0	0	0.181818	0	-1.09091	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.18762	inf		
R11(u19)	0	0	0	0	0	0	0	0	0	0	0	0.204545	0	0	0.113636	0	0.0681818	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0.40086	inf		
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0.568182	0	0	-0.795455	0	-0.477273	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	1.32616	inf		
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0.25	0	0	-0.25	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.986572	inf
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	-0.181818	0	0	-0.0454545	0	0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.89005	7.86027		
R15(u7)	0	0	0	0	0	0	0	0	0	0	1	0	0.590909	0	0	0.272727	0	-0.136364	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.94601	inf	
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	-1.72727	0	0	-0.181818	0	1.09091	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.48626	0.603594	
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0.159091	0	0	-0.522727	0	0.386364	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.22393	inf	
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	-0.318182	0	0	1.04545	0	0.227273	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	3.84643	4.47609	
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0.0681818	0	0	-0.295455	1	1.02273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.553102	inf	
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	-0.386364	0	0	-0.159091	0	-0.795455	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.36592	2.30692	
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	-0.227273	0	0	-0.181818	0	-0.409091	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.96349	3.22176	
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0.75	0	0	-0.25	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.89435	inf
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0.522727	0	0	0.0681818	0	0.840909	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.20067	inf	
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	-0.204545	0	0	-0.613636	0	0.931818	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.50383	2.75365		
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	-0.886364	0	0	0.340909	0	-0.295455	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.33143	1.44691	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	-0.0681818	0	0	-0.204545	0	-0.0227273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.23127	11.9803		
R27(u36)	0	0	0	0	0																															

# Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 117$$



State 29/31 | PHASE II step 3 | ENTER: s14 | LEAVE: u10 | Z=116.981

## COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: s14 enters, u10 leaves.

Reduced cost of entering variable: -0.613636

Minimum ratio theta\*: 0.176373

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

## TABLEAU

Current solution:  $x_1=3.44921$ ,  $x_2=3.84195$ ,  $x_3=2.23528$

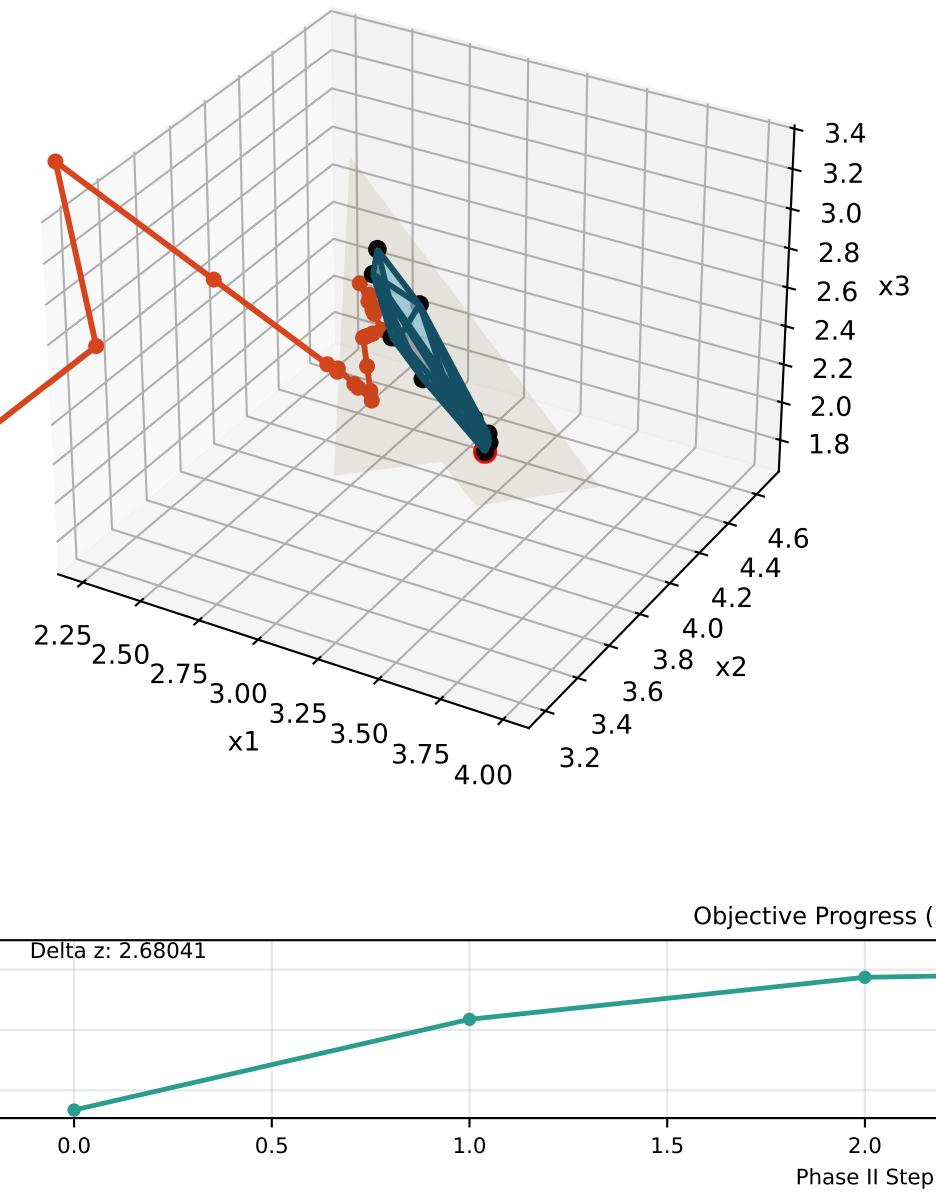
Objective z: 116.981

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio			
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	-0.55	-0.45	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.55079	41.9802					
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0.4	0.6	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.15805	inf					
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0.05	-0.05	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.76472	429.824					
R4(u6)	0	0	0	0	0	0	0	0	0	1	0	0	-0.1	0.1	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.627068	inf				
R5(s5)	0	0	0	0	0	0	0	0	1	0	0	-1.35	-1.65	0	2.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.55334	2.2475				
R6(u8)	0	0	0	0	0	0	0	0	0	0	1	0.6	-0.6	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.45175	5.49946				
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0.55	0.45	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.44921	inf				
R8(u11)	0	0	0	0	0	0	0	0	0	0	0	1.05	-0.05	1	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.715502	31.6585				
R9(s14)	0	0	0	0	0	0	0	0	0	0	0	0.8	2.2	0	-2	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176373	0.176373			
R10(u24)	0	0	0	0	0	0	0	0	0	0	0	2.6	2.4	0	-2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.38003	inf			
R11(u19)	0	0	0	0	0	0	0	0	0	0	0	0.15	-0.15	0	0.25	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0.388834	5.87927				
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0.95	1.05	0	-1.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.41034	inf				
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	-0.35	-1.65	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.854292	1.31543				
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	-0.4	-0.6	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.84195	14.2635			
R15(u7)	0	0	0	0	0	0	0	0	0	0	1	0	0.7	0.3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.97007	inf			
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	-2.6	-2.4	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.29386	2.27908			
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	-0.15	-0.85	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.15578	3.16781			
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	-0.5	-0.5	0	1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.80634	16.9243		
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	-0.75	-2.25	0	1.75	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.37272	0.540811		
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0.25	1.75	0	-1.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.50622	inf		
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0.1	0.9	0	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.03565	inf	
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0.55	-0.55	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.85026	7.5774		
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	-0.15	-1.85	0	1.75	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.205235	2.61701	
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	-0.95	-2.05	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.33949	1.61387	
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	-0.65	0.65	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.38354	inf	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	-0.05	0.05	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.23528	inf	
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	-0.55	-0.45	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.91841	4.66638
R28(u4)	0	0	0	0	0	0	0	0	0	1	0	0	0.6	-0.6	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.78406	6.71794

# Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 117$$



State 30/31 | PHASE II step 4 | ENTER: u12 | LEAVE: u13 | Z=117.354

## COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u12 enters, u13 leaves.

Reduced cost of entering variable: -1.75

Minimum ratio theta\*: 0.212983

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

## TABLEAU

Current solution:  $x_1=3.50246, x_2=3.73546, x_3=2.28853$

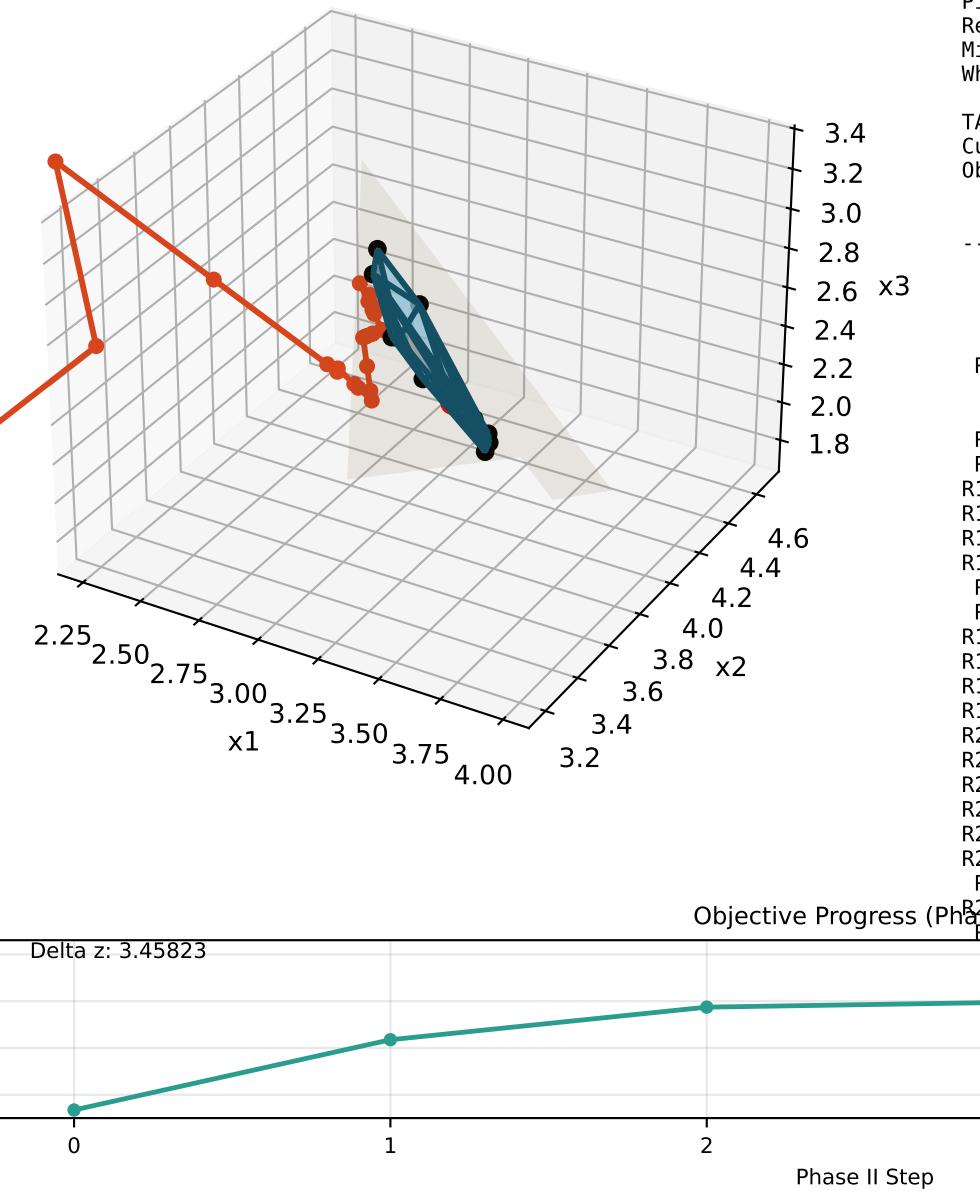
Objective z: 117.354

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	-0.442857	-0.128571	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.49754	34.2032	
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0.185714	-0.0428571	0	0	0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.26454	inf	
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0.157143	0.271429	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.71147	39.0589	
R4(u6)	0	0	0	0	0	0	0	0	0	1	0	-0.314286	-0.542857	0	0	0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.73356	inf	
R5(s5)	0	0	0	0	0	0	0	0	1	0	0	-0.385714	1.24286	0	0	-1.28571	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.07413	0.690375	
R6(u8)	0	0	0	0	0	0	0	0	0	0	1	0.814286	0.0428571	0	0	-0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.34526	2.9035	
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0.442857	0.128571	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.50246	inf	
R8(u11)	0	0	0	0	0	0	0	0	0	0	0	0.942857	-0.371429	1	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.768748	inf	
R9(s14)	0	0	0	0	0	0	0	0	0	0	0	-0.0571429	-0.371429	0	0	1.14286	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.602339	inf	
R10(u24)	0	0	0	0	0	0	0	0	0	0	0	1.74286	-0.171429	0	0	1.14286	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.806	inf	
R11(u19)	0	0	0	0	0	0	0	0	0	0	0	0.257143	0.171429	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.335588	1.55534	
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0.2	-1.2	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.78306	inf
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0.185714	-0.0428571	0	0	-0.714286	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.588064	0.683434	
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	-0.185714	0.0428571	0	0	-0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.73546	7.6839	
R15(u7)	0	0	0	0	0	0	0	0	0	0	1	0	0.7	0.3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.97007	inf
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	-1.74286	0.171429	0	0	-1.14286	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1.86789	1.14693	
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	-0.0428571	-0.528571	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	1.10254	4.62313		
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0.142857	1.42857	0	0	-0.857143	0	0	0	1	0	0	0	0	0	0	0	0	0	0	3.48687	2.53756	
R19(u12)	0	0	0	0	0	0	0	0	0	0	0	-0.428571	-1.28571	0	1	0.571429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.212983	0.212983	
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	-0.5	-0.5	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.87894	inf
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	-0.328571	-0.385714	0	0	0.571429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.24863	inf	
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0.657143	-0.228571	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.79701	7.40103	
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0.6	0.4	0	0	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.67963	1.17277
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	-0.414286	-0.442857	0	0	-0.714286	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.07326	1.07159	
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	-0.757143	0.328571	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	1	3.43678	inf	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	-0.157143	-0.271429	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.28853	inf	
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	-0.657143	-0.771429	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.971655	inf	
R28(u4)	0	0	0	0	0	0	0	0	0	1	0	1.02857	0.685714	0	0	-0.571429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.57108	1.78406	

# Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 118$$



State 31/31 | PHASE II step 5 | ENTER:  $u_{10}$  | LEAVE:  $s_5$  |  $Z=118.132$

## COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot:  $u_{10}$  enters,  $s_5$  leaves.

Reduced cost of entering variable: -0.9

Minimum ratio theta\*: 0.864244

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

## TABLEAU

Current solution:  $x_1=3.39134$ ,  $x_2=3.69842$ ,  $x_3=2.52311$

Objective z: 118.132

row	$x_1$	$x_2$	$x_3$	$s_1$	$s_2$	$s_3$	$s_4$	$s_5$	$u_6$	$u_7$	$u_8$	$s_9$	$u_{10}$	$u_{11}$	$u_{12}$	$u_{13}$	$s_{14}$	$u_{15}$	$s_{16}$	$u_{17}$	$s_{18}$	$u_{19}$	$s_{20}$	$s_{21}$	$u_{22}$	$u_{23}$	$u_{24}$	$s_{25}$	$u_{26}$	$u_{27}$	$u_{28}$	rhs	ratio
R1( $s_1$ )	0	0	0	1	0	0	0	0.103448	0	0	0	-0.482759	0	0	0	-0.275862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.60866	inf	
R2( $s_2$ )	0	0	0	0	1	0	0	0.0344828	0	0	0	0.172414	0	0	0	0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.30158	inf	
R3( $s_3$ )	0	0	0	0	0	1	0	-0.218391	0	0	0	0.241379	0	0	0	0.137931	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.47689	35.7791	
R4( $u_6$ )	0	0	0	0	0	0	0	0.436782	1	0	0	-0.482759	0	0	0	-0.275862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.20272	inf	
R5( $u_{10}$ )	0	0	0	0	0	0	0	0.804598	0	0	0	-0.310345	1	0	0	-1.03448	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.864244	0.864244	
R6( $u_8$ )	0	0	0	0	0	0	0	-0.0344828	0	0	1	0.827586	0	0	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.30822	31.3894	
R7( $x_1$ )	1	0	0	0	0	0	0	-0.103448	0	0	0	0.482759	0	0	0	0.275862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.39134	27.2413	
R8( $u_{11}$ )	0	0	0	0	0	0	0	0.298851	0	0	0	0.827586	0	1	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.08975	inf	
R9( $s_{14}$ )	0	0	0	0	0	0	0	0.298851	0	0	0	-0.172414	0	0	0	0.758621	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.923344	inf	
R10( $u_{24}$ )	0	0	0	0	0	0	0	0.137931	0	0	0	1.68966	0	0	0	0.965517	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.95415	inf	
R11( $u_{19}$ )	0	0	0	0	0	0	0	-0.137931	0	0	0	0.310345	0	0	0	0.0344828	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.187432	1.9576	
R12( $u_{17}$ )	0	0	0	0	0	0	0	0.965517	0	0	0	-0.172414	0	0	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.82015	inf
R13( $u_{22}$ )	0	0	0	0	0	0	0	0.0344828	0	0	0	0.172414	0	0	0	-0.758621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.625103	inf
R14( $x_2$ )	0	1	0	0	0	0	0	-0.0344828	0	0	0	-0.172414	0	0	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.69842	87.1607
R15( $u_7$ )	0	0	0	0	0	0	0	-0.241379	0	1	0	0.793103	0	0	0	0.310345	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.71079	9.9022
R16( $s_{16}$ )	0	0	0	0	0	0	0	-0.137931	0	0	0	-1.68966	0	0	0	-0.965517	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1.71974	10.896
R17( $u_{23}$ )	0	0	0	0	0	0	0	0.425287	0	0	0	-0.206897	0	0	0	-0.689655	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.55935	inf
R18( $s_{18}$ )	0	0	0	0	0	0	0	-1.14943	0	0	0	0.586207	0	0	0	0.62069	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25224	2.44081
R19( $u_{12}$ )	0	0	0	0	0	0	0	1.03448	0	0	0	-0.827586	0	0	0	-0.758621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.32415	inf
R20( $s_{20}$ )	0	0	0	0	0	0	0	0.402299	0	0	0	-0.655172	0	0	0	0.482759	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.31106	inf
R21( $s_{21}$ )	0	0	0	0	0	0	0	0.310345	0	0	0	-0.448276	0	0	0	0.172414	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.58198	inf
R22( $u_{28}$ )	0	0	0	0	0	0	0	0.183908	0	0	0	0.586207	0	0	0	-0.37931	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.99455	inf
R23( $s_{15}$ )	0	0	0	0	0	0	0	0.321839	0	0	0	0.724138	0	0	0	-0.586207	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1.33394	4.19909
R24( $u_{27}$ )	0	0	0	0	0	0	0	0.356322	0	0	0	-0.551724	0	0	0	-1.17241	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.45599	inf
R25( $s_{25}$ )	0	0	0	0	0	0	0	-0.264368	0																								