

Phase Simplex Report

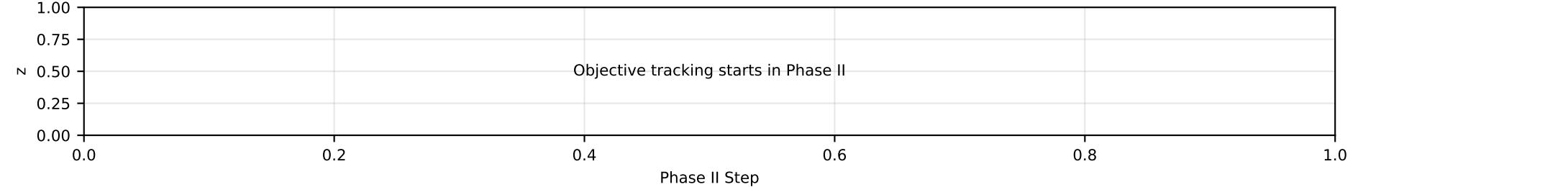
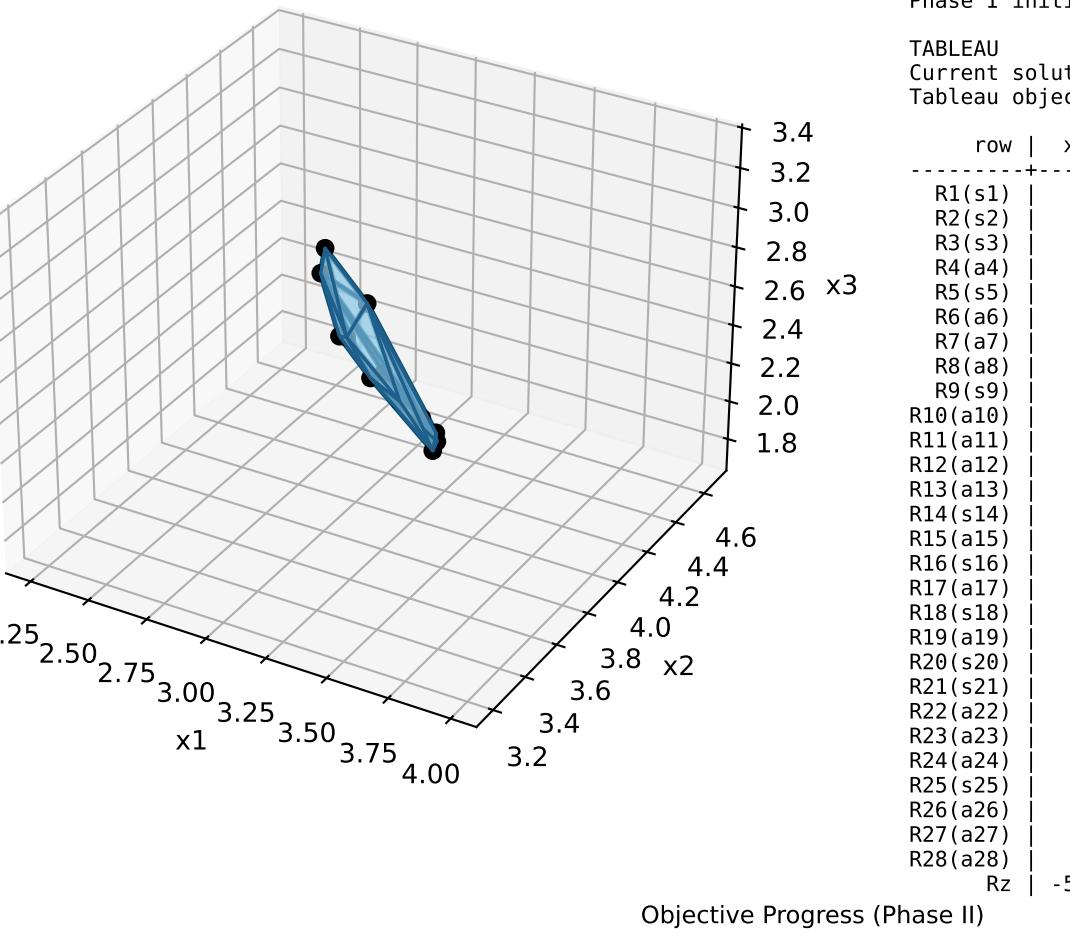
Feasible polytope + extreme points + simplex path State 1/31

ep 0

an artificial objective.

$x_2=0$ $x_3=0$

$\lambda_2=0$, $\lambda_3=0$
633

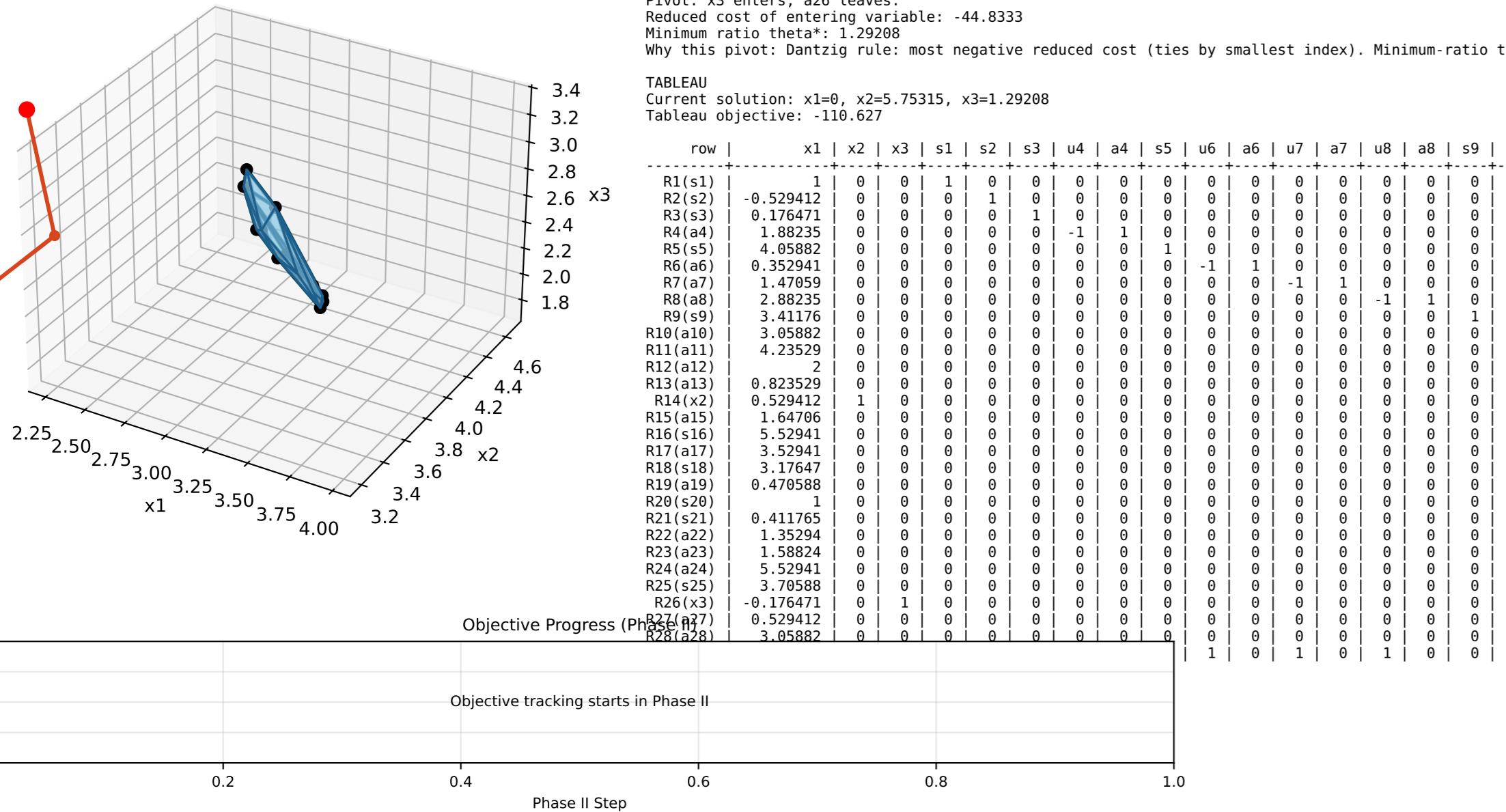


Phase Simplex Report

feasible polytope + extreme points + simplex path State 3/31

COMMENTS
Teaching Mode, L Rules; D

Teaching Mode | Rule: DANTZIG
Pivot: x3 enters, a26 leaves.
Reduced cost of entering variable: -44.8333
Minimum ratio theta*: 1.29208
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index)



Step 2 | ENTER: x3 | LEAVE: a26

ANTZIG

eaves.

variable: -44.8333

29208

rule: most negat

rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

$$x_2=5.75315, x_3=1.29208$$

.627

x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	u21	a22	u23	a23	u24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf							
0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.24685	inf		
0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	10.7079	12		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.705882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.36797	inf		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.352941	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	17.5602	4.21878		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.117647	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25934	1.92175		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.01716	inf		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.705882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.06791	5.47726		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.529412	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12.4309	6.61959		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.647059	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12.3813	3.35562		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	15.1398	4.92562		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.73524	2.83359	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.05882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.87532	2.86043		
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.73411	35.811		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.11765	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.7017	5.73411		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	22.3695	8.74858		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12.6853	3.4667		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	16.934	3.83218		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14918	inf		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.77906	inf	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.529412	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.20046	inf		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.882353	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.30495	3.44455		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.470588	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.31986	2.88803		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	16.6956	6.85729		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.764706	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	17.3276	5.62398		
0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.29208	1.29208		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.823529	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.72999	1.72999		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.647059	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.31375	1.31375		
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.61261	4.32764

-Phase Simplex Report

Feasible polytope + extreme points + simplex path State 4/

COMMENTS

Teaching Mode | Rule: DANIZIG

Pivot. XI enters. Reduced cost of

Minimum ratio of the number of nodes to the number of edges

Why this pivot:

TABLEAU

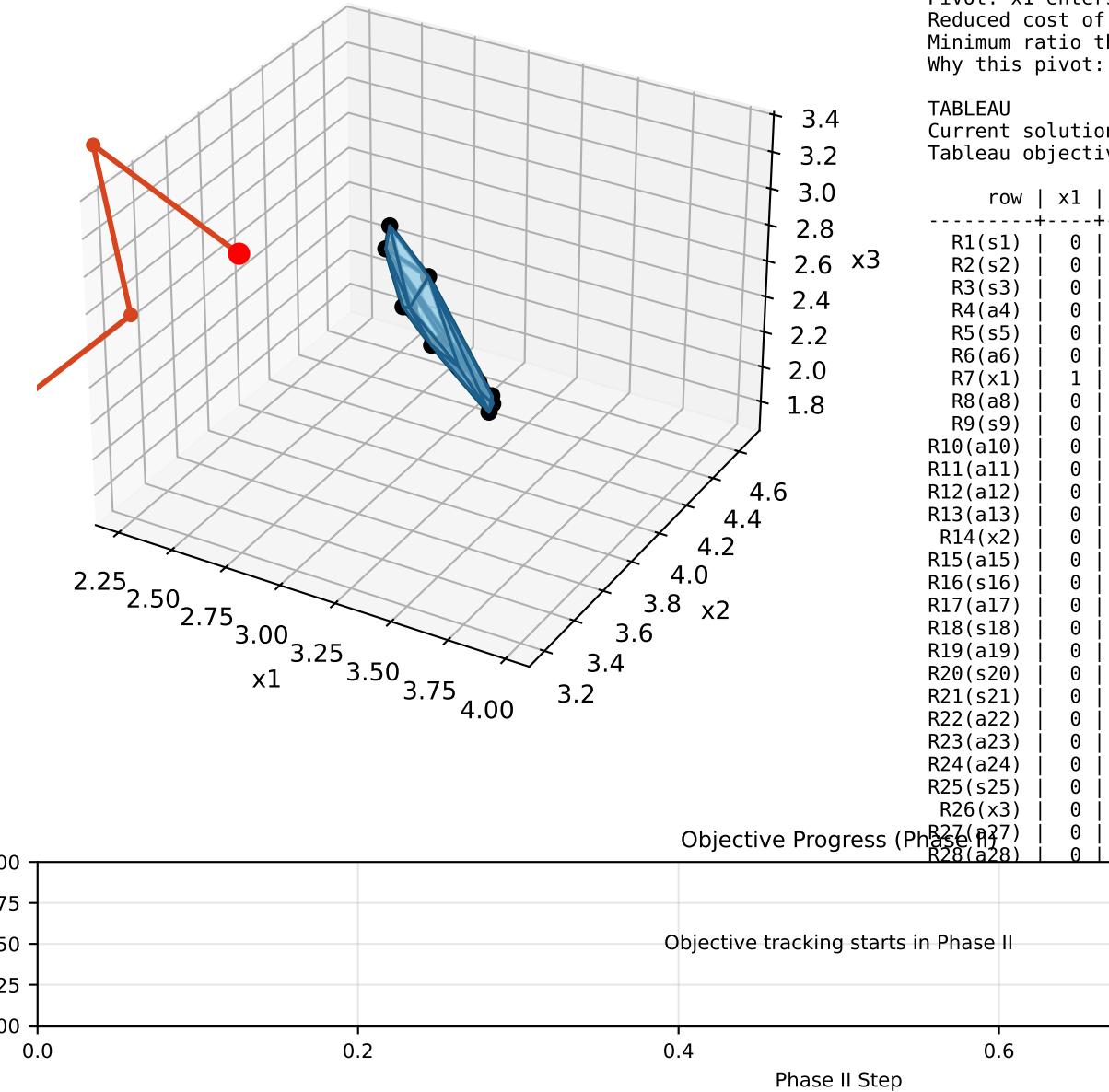
TABLEAU Current solution

Current solution
Tableau objective
32

3.2 Vast majority of objects

row | x1 |

2.8 D1(-1) + 2.8 D2(1)



ASE I step 3 | ENTER: x1 | LEAVE: a7

Rule: DANTZIG

s, a7 leaves.

entering variable:

Dantzig rule: most

Dantzig rule: most r

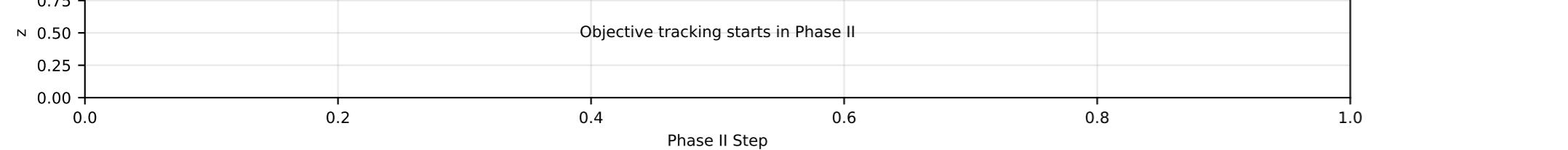
x2		x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
0	0	1	0	0	0	0	0	0	0	0.68	-0.68	0	0	0	0	0	0	0	0	0	0	0	0.12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.04	-0.04	0	0	0	10.6283	12					
0	0	0	1	0	0	0	0	0	0	-0.36	0.36	0	0	0	0	0	0	0	0	0	0	0	-0.24	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.08	0.08	0	0	0	6.97303	inf					
0	0	0	0	1	0	0	0	0	0	0.12	-0.12	0	0	0	0	0	0	0	0	0	0	0	0.08	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.36	-0.36	0	0	0	10.4659	60.6782					
0	0	0	0	0	-1	1	0	0	0	0.28	-1.28	0	0	0	0	0	0	0	0	0	0	0	-0.48	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.16	0.16	0	0	0	1.78602	2.32049					
0	0	0	0	0	0	1	0	0	0	0.276	-2.76	0	0	0	0	0	0	0	0	0	0	0	0.84	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.28	-2.28	0	0	0	11.9929	4.32643				
0	0	0	0	0	0	0	0	0	0	-0.68	0.68	0	0	0	0	0	0	0	0	0	0	0	0.16	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.72	-0.72	0	0	0	0.775222	3.56813				
0	0	0	0	0	0	0	0	0	0	-1	1	0.24	-0.24	0	0	0	0	0	0	0	0	0	-0.12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.04	0.04	0	0	0	1.37167	1.37167					
0	0	0	0	0	0	0	0	0	0	-0.68	0.68	0	0	0	0	0	0	0	0	0	0	0	-0.36	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.88	-0.88	0	0	0	5.11428	3.14601				
0	0	0	0	0	0	0	0	0	0	1.96	-1.96	-1	1	0	0	0	0	0	0	0	0	0	-0.36	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.96	-0.96	0	0	0	7.75106	3.64353				
0	0	0	0	0	0	0	0	0	0	2.32	-2.32	0	0	0	1	0	0	0	0	0	0	0	-0.12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.24	-2.24	0	0	0	8.18559	4.04772				
0	0	0	0	0	0	0	0	0	0	2.08	-2.08	0	0	0	-1	1	0	0	0	0	0	0	-0.28	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.64	-1.64	0	0	0	9.33037	3.57467			
0	0	0	0	0	0	0	0	0	0	2.88	-2.88	0	0	0	0	-1	1	0	0	0	0	0	-0.08	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.08	-2.08	0	0	0	5.99191	4.36762			
0	0	0	0	0	0	0	0	0	0	1.36	-1.36	0	0	0	0	-1	1	0	0	0	0	0	0.24	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.68	-0.68	0	0	0	1.74572	3.49146			
1	0	0	0	0	0	0	0	0	0	0.56	-0.56	0	0	0	0	0	0	0	0	0	0	-1	1	-0.96	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.08	-0.08	0	0	0	5.02697	10.8671			
0	0	0	0	0	0	0	0	0	0	0.36	-0.36	0	0	0	0	0	0	0	0	0	0	0	0.24	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.36	-0.36	0	0	0	1.44248	2.24746			
0	0	0	0	0	0	0	0	0	0	1.12	-1.12	0	0	0	0	0	0	0	0	0	0	0	-0.92	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.28	-1.28	0	0	0	14.785	4.04555		
0	0	0	0	0	0	0	0	0	0	3.76	-3.76	0	0	0	0	0	0	0	0	0	0	0	0.84	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1.22	-2.22	0	0	0	7.84414	3.59417		
0	0	0	0	0	0	0	0	0	0	2.4	-2.4	0	0	0	0	0	0	0	0	0	0	0	0.6	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	2.48	-2.48	0	0	0	12.5769	5.33107		
0	0	0	0	0	0	0	0	0	0	2.16	-2.16	0	0	0	0	0	0	0	0	0	0	0	0.44	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.04	0.04	0	0	0	0.503686	2.442		
0	0	0	0	0	0	0	0	0	0	0.32	-0.32	0	0	0	0	0	0	0	0	0	0	0	-0.12	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.04	-0.04	0	0	0	4.40739	5.77906		
0	0	0	0	0	0	0	0	0	0	0.68	-0.68	0	0	0	0	0	0	0	0	0	0	0	0.88	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.16	0.16	0	0	0	2.63566	7.77255		
0	0	0	0	0	0	0	0	0	0	0.28	-0.28	0	0	0	0	0	0	0	0	0	0	0	-0.48	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.76	0.76	0	0	0	2.44917	3.18192	
0	0	0	0	0	0	0	0	0	0	0.92	-0.92	0	0	0	0	0	0	0	0	0	0	0	-0.72	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.24	-1.24	0	0	0	3.14133	3.34954	
0	0	0	0	0	0	0	0	0	0	1.08	-1.08	0	0	0	0	0	0	0	0	0	0	0	-0.28	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.28	-1.28	0	0	0	9.11113	3.01942	
0	0	0	0	0	0	0	0	0	0	3.76	-3.76	0	0	0	0	0	0	0	0	0	0	0	0.84	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.56	-1.56	0	0	0	12.2444	4.67571	
0	1	0	0	0	0	0	0	0	0	0	2.52	-2.52	0	0	0	0	0	0	0	0	0	0	-0.32	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.36	0.36	0	0	0	1.53413	inf
0	0	0	0	0	0	0	0	0	0	-0.12	0.12	0	0	0	0	0	0	0	0	0	0	-0.08	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.58757	2.48153					
0	0	0	0	0	0	0	0	0	0	0.36	-0.36	0	0	0	0	0	0	0	0	0	0	-0.76	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.41692	3.14258	
0	0	0	0	0	0	0	0	0	0	2.08	-2.08	0	0	0	0	0	0	0	0	0	0	-0.28	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-16.2	17.2	0	0	0	-63.4256	-

Phase Simplex Report

feasible polytope + extreme points + simplex path State 5/31

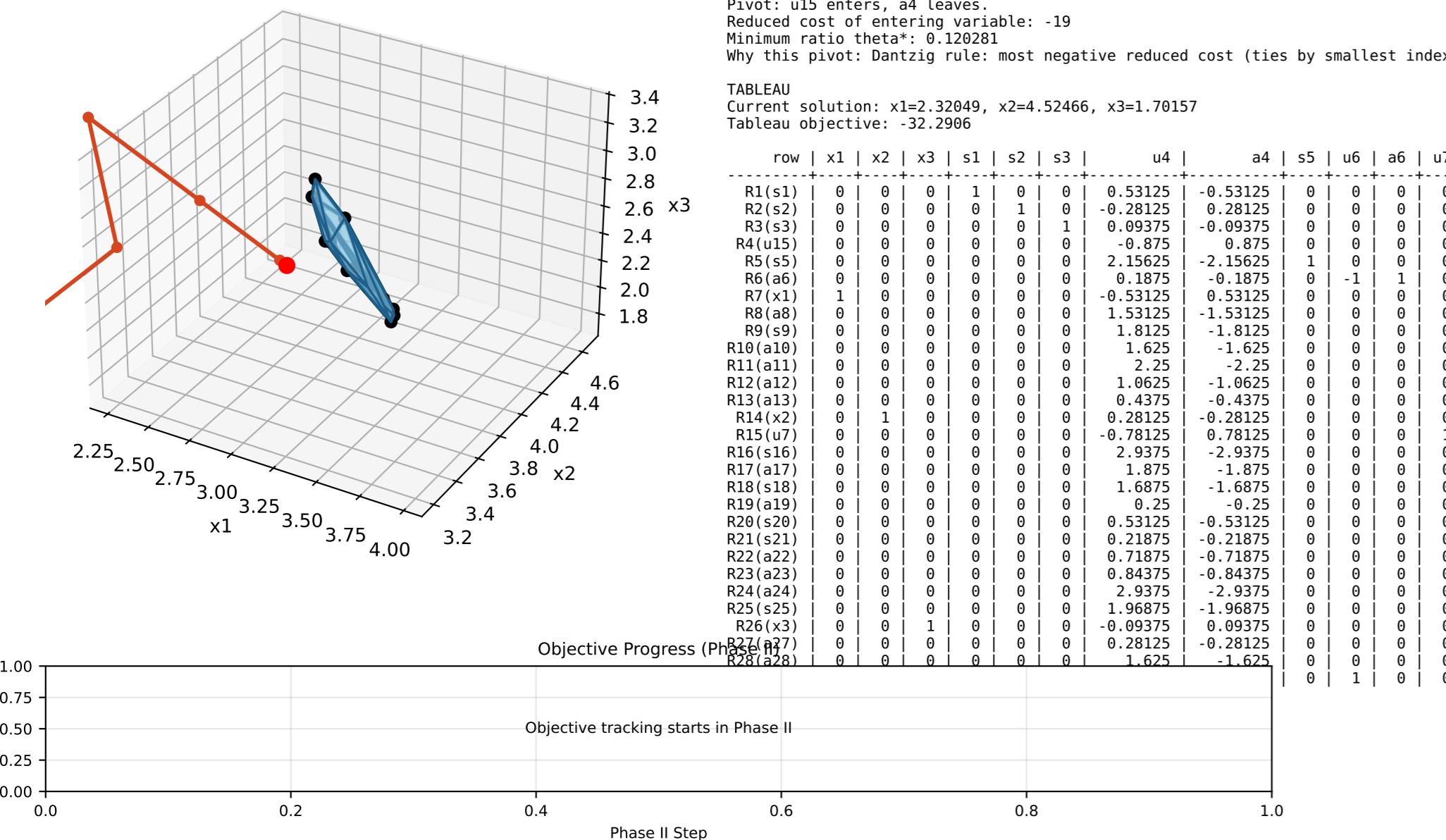
COMMENTS
Teaching Mode | Rule: DAM
Pivot: u7 enters, a15 leaves
Reduced cost of entering
Minimum ratio theta*: 1.2
Why this pivot: Dantzig rule

TABLEAU
Current solution: $x_1=2.24746$, $x_2=4.56332$, $x_3=1.68869$
Tableau objective: -34.5759



Phase Simplex Report

Feasible polytope + extreme points + simplex path State 6/3



step 5 | ENTER: u15 | LEAVE: a4

DANTZIG

DANTZIG leaves

ing variable: -19

Using variable: -19
0.130281

ig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

$x_2 = 32049$, $x_2 - 4 = 52466$, $x_3 - 1 = 70157$

2.32049, x2=4
2.3006

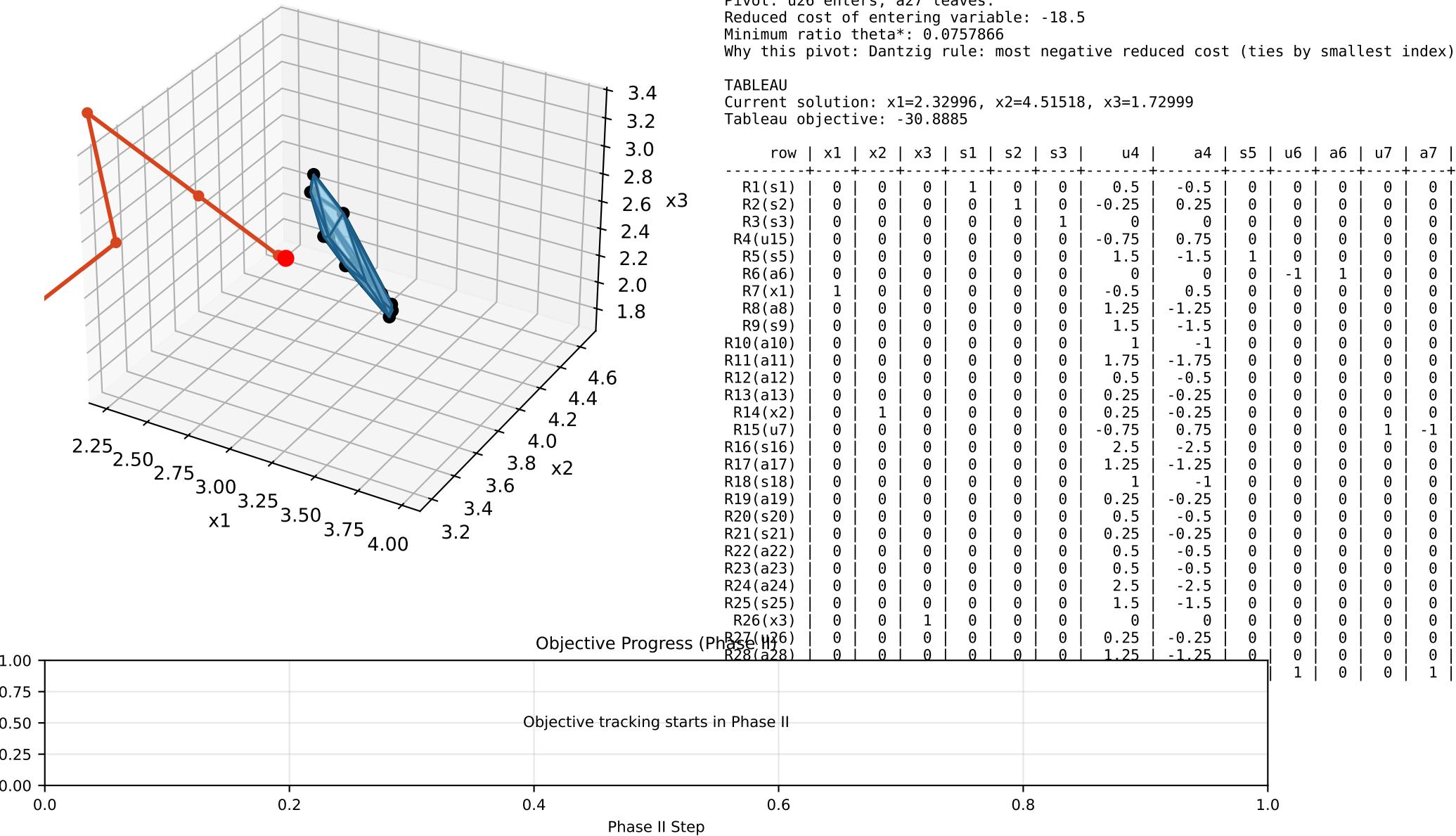
x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	u21	s22	u23	a23	u24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
0	1	0	0	0.53125	-0.53125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	9.67951	16.063					
0	0	1	0	-0.28125	0.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	7.47534	int					
0	0	0	1	0.09375	-0.09375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0.375	-0.375	0	0	0	10.2984	96.2389					
0	0	0	0	-0.875	0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.5	1	-1	0	0	0	0	0	0	0	0	0	0	-0.5	0.5	0	0	0	0.120281	0.120281					
0	0	0	0	2.15625	-2.15625	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.875	0	0	0	0	0	0	0	0	0	0	0	0	0	2.625	-2.625	0	0	0	8.14176	3.42418				
0	0	0	0	0.1875	-0.1875	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0.440344	2.17522				
0	0	0	0	-0.53125	0.53125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	2.32049	int				
0	0	0	0	1.53125	-1.53125	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	1.125	-1.125	0	0	0	2.37945	1.47997				
0	0	0	0	1.8125	-1.8125	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	-1.25	0	0	0	4.51391	2.29941				
0	0	0	0	1.625	-1.625	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	2.5	-2.5	0	0	0	5.28331	2.96514				
0	0	0	0	2.25	-2.25	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	0	5.31183	2.18599				
0	0	0	0	1.0625	-1.0625	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	2.25	-2.25	0	0	0	4.09427	3.49203				
0	0	0	0	0.4375	-0.4375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0.964335	2.04895				
0	0	0	0	0.28125	-0.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	4.52466	14.197				
0	0	0	0	-0.78125	0.78125	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	1.39532	int				
0	0	0	0	2.9375	-2.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25	0	0	1	0	0	0	0	0	0	0	0	0	0	1.75	-1.75	0	0	0	9.5386	2.96157				
0	0	0	0	1.875	-1.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	2.5	-2.5	0	0	0	4.49536	2.21812			
0	0	0	0	1.6875	-1.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	2.75	-2.75	0	0	0	0.956304	5.0789					
0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	0.320417			
0	0	0	0	0.53125	-0.53125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	3.45857	5.81675				
0	0	0	0	0.21875	-0.21875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	2.24497	9.10015				
0	0	0	0	0.71875	-0.71875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0.875	-0.875	0	0	0	1.16547	1.53912				
0	0	0	0	0.84375	-0.84375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	1.375	-1.375	0	0	0	1.63438	1.8152					
0	0	0	0	2.9375	-2.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25	0	0	0	0	0	0	0	0	0	0	0	0	0	1.75	-1.75	0	0	0	3.86471	1.27147					
0	0	0	0	1.96875	-1.96875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	1.875	-1.875	0	0	0	8.72816	3.99947					
1	0	0	0	-0.09375	0.09375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0.375	0	0	0	1.70157	int					
0	0	0	0	0.28125	-0.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	-1.25	-1	1	0	0.08526	0.385534					
0	0	0	0	1.625	-1.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	1.5	-1.5	0	0	-1	2.51465	1.47432							

Phase Simplex Report

Feasible polytope + extreme points + simplex path State 7/31

p 6 | ENTER: u26 | LEAVE: a27

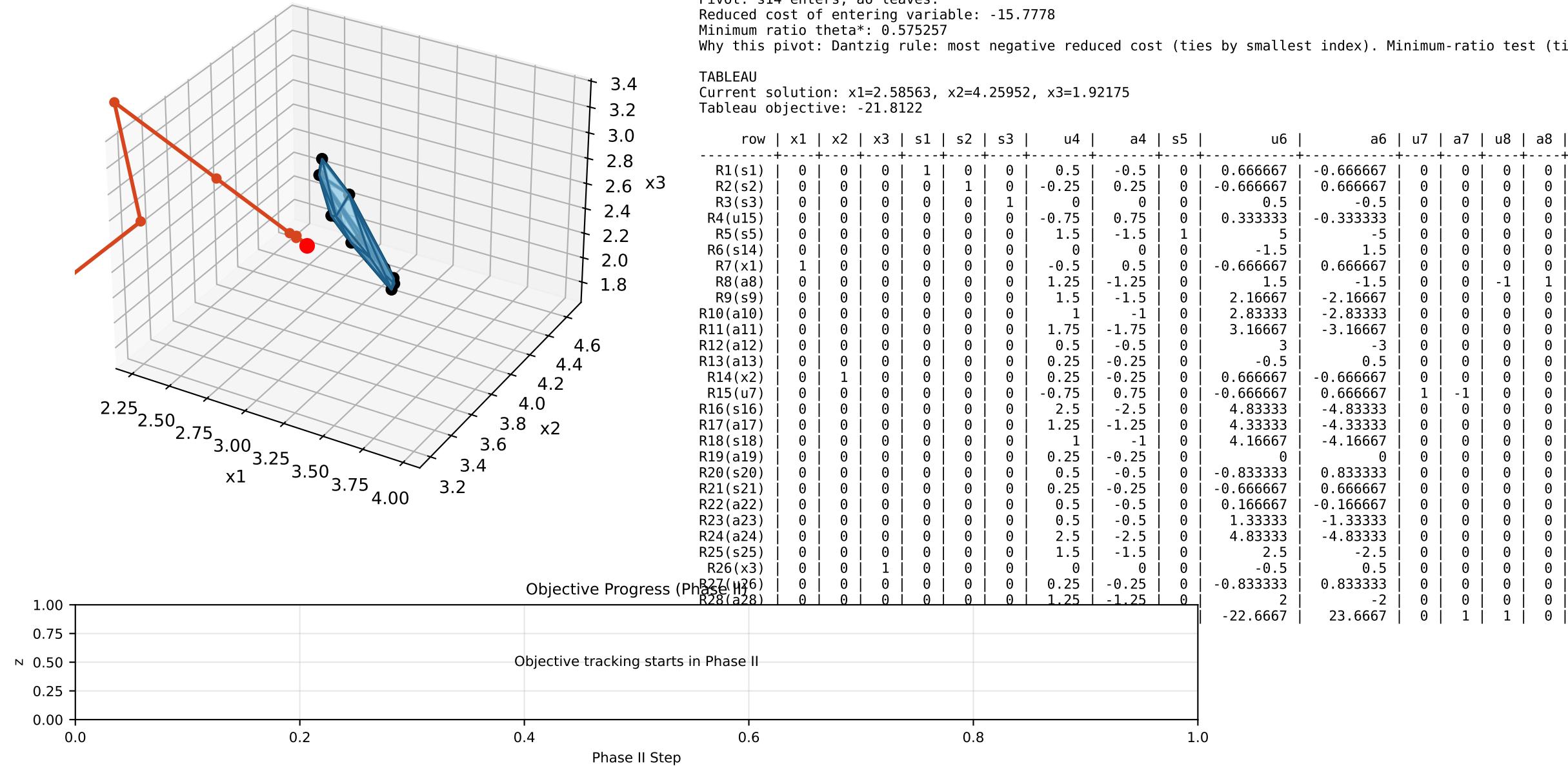
```
NTZIG  
eaves.  
  variable: -18.5  
0757866  
rule: most negative reduced cost (ties by smallest index)
```



2996, x2=4.51518, x3=1.72999																																														
885																																														
s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
1	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.4444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1111111	-0.1111111	-0.1111111	0	0	9.67004	77.4361						
0	1	0	-0.25	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.4444444	0	0	0	0	0	0	0	0	0	0	0	0	-0.1111111	0.1111111	0.3333333	0	0	7.48482	inf							
0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.3333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.3333333	-0.3333333	0	0	0	10.27	27.4625					
0	0	0	-0.75	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.2222222	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.158174	inf				
0	0	0	1.5	-1.5	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.94282	3.10162				
0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.383504	0.587126					
0	0	0	-0.5	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.4444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.32996	inf				
0	0	0	1.25	-1.25	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.29419	2.11506				
0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	1.444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.49197	3.61113				
0	0	0	1	-1	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	1.88889	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.09385	2.11333				
0	0	0	1.75	-1.75	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	2.111111	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.16026	2.65592				
0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.92375	1.81968				
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	-0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.907495	1.28578					
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.4444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.51518	36.1973					
0	0	0	-0.75	0.75	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	-0.4444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.4048	inf					
0	0	0	2.5	-2.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.222222	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.40597	5.45063				
0	0	0	1.25	-1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.88889	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.3059	1.79815				
0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.777778	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.35463	3.47747				
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf			
0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.555556	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.4491	27.6686				
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.4444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25444	inf				
0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1111111	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.09916	1.33197				
0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.888889	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.53018	1.18864				
0	0	0	2.5	-2.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.222222	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.73209	2.20841				
0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.58606	4.65502			
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	inf				
0	0	0	1.25	-1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	1.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.72999	1.67643			

Phase Simplex Report

feasible polytope + extreme points + simplex path State 8/31



7 | ENTER: s14 | LEAVE: a6

ZIG

res.

variable: -15.7778

5257

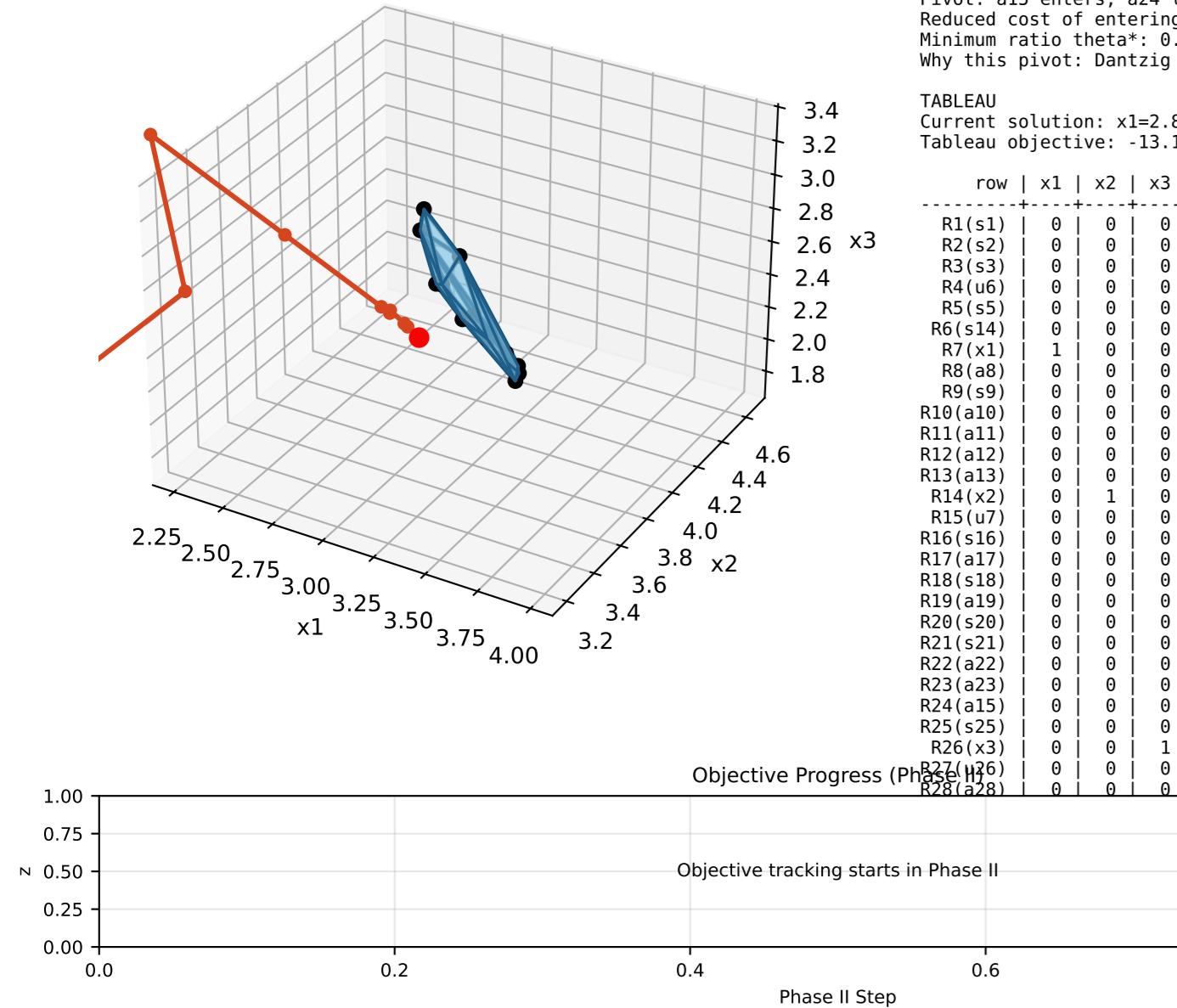
le: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

63. $x_2=4.25952$, x

2

Phase Simplex Report

feasible polytope + extreme points + simplex path State 10/3



Step 9 | ENTER: a15 | LEAVE: a24

ANTZIG

-leaves.

g variable: -67

0992111

rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

34473 $\times 2 = 4$ 00041 $\times 3 =$

$\text{b4}=3$, $\text{x2}=4.00041$, $\text{x3}=2.1188$
102

102

s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	u21	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
1	0	0	0.155172	-0.155172	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.15527	4.67685								
0	1	0	0.0948276	-0.0948276	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.99959	inf									
0	0	1	-0.258621	0.258621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.6885	inf								
0	0	0	0.517241	-0.517241	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.388652	0.371347								
0	0	0	-1.08621	1.08621	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.08204	inf								
0	0	0	0.775862	-0.775862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.15823	inf								
0	0	0	-0.155172	0.155172	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.84473	inf								
0	0	0	0.474138	-0.474138	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.13595	0.351645								
0	0	0	0.37931	-0.37931	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.74617	0.521699								
0	0	0	-0.465517	0.465517	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.90607	0.441102								
0	0	0	0.112069	-0.112069	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.7151	0.385011								
0	0	0	-1.05172	1.05172	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.60728	0.277798								
0	0	0	0.508621	-0.508621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.29357	inf							
0	0	0	-0.0948276	0.0948276	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.00041	2.09942								
0	0	0	-0.405172	0.405172	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.91957	inf								
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	0.490514								
0	0	0	-0.991379	0.991379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.959889	0.173049								
0	0	0	-1.15517	1.15517	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.13732	0.590196								
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf							
0	0	0	0.931034	-0.931034	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.09256	inf								
0	0	0	0.594828	-0.594828	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.76921	inf								
0	0	0	0.413793	-0.413793	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.970466	2.04014							
0	0	0	-0.189655	0.189655	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.500634	0.22437								
0	0	0	0.922414	-0.922414	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0992111	0.0992111								
0	0	0	0.206897	-0.206897	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.65568	0.986634								
0	0	0	0.258621	-0.258621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.11607	inf								
0	0	0	0.681034	-0.681034	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.71925	inf								
0	0	0	0.215517	-0.215517	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.856656	0.241987							

Phase Simplex Report

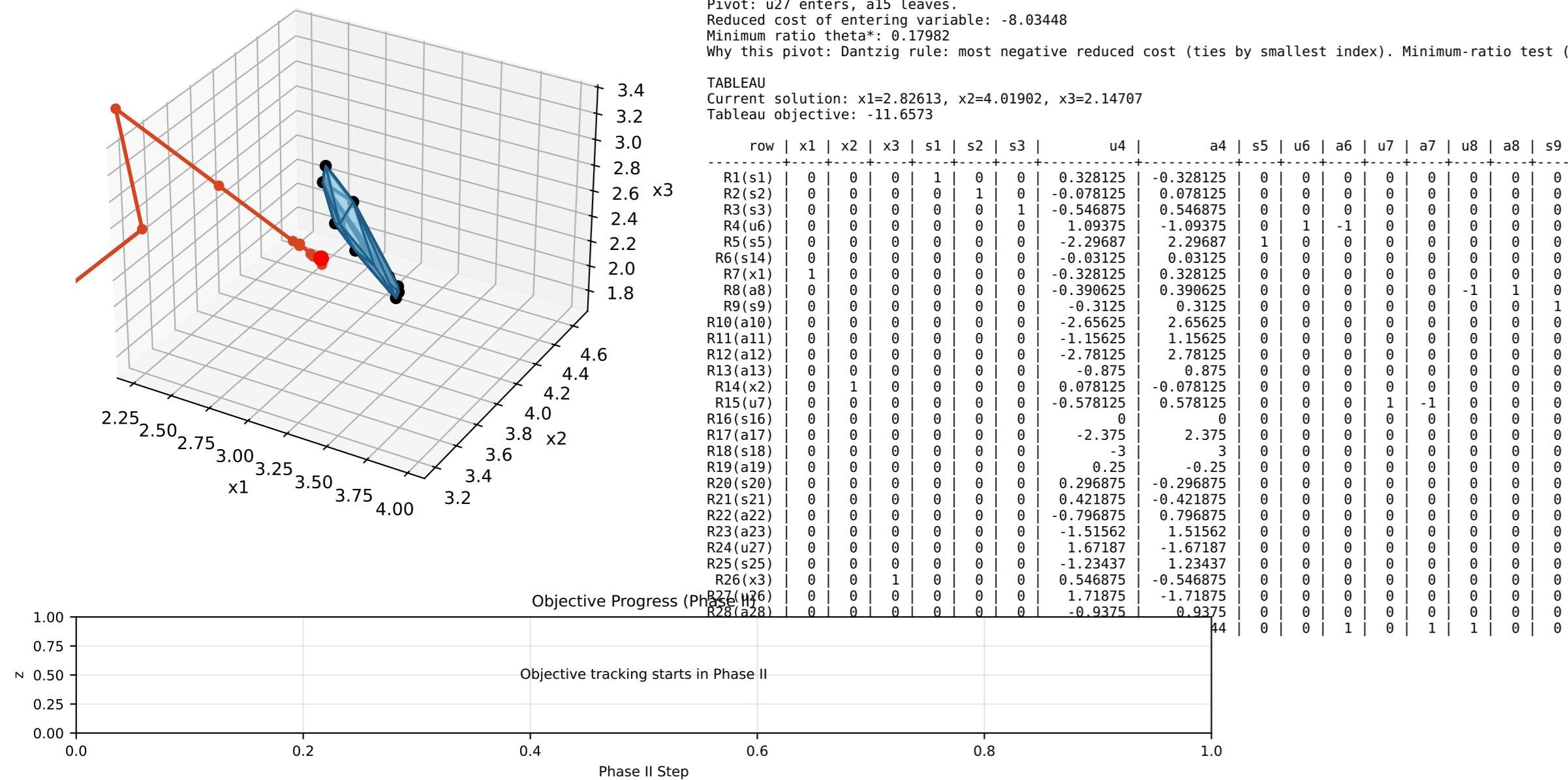
feasible polytope + extreme points + simplex path State 11/31

Step 10 | ENTER: u27 | LEAVE: a15

ANTZIG
leaves.
g variable: -8.03448
.17982
rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

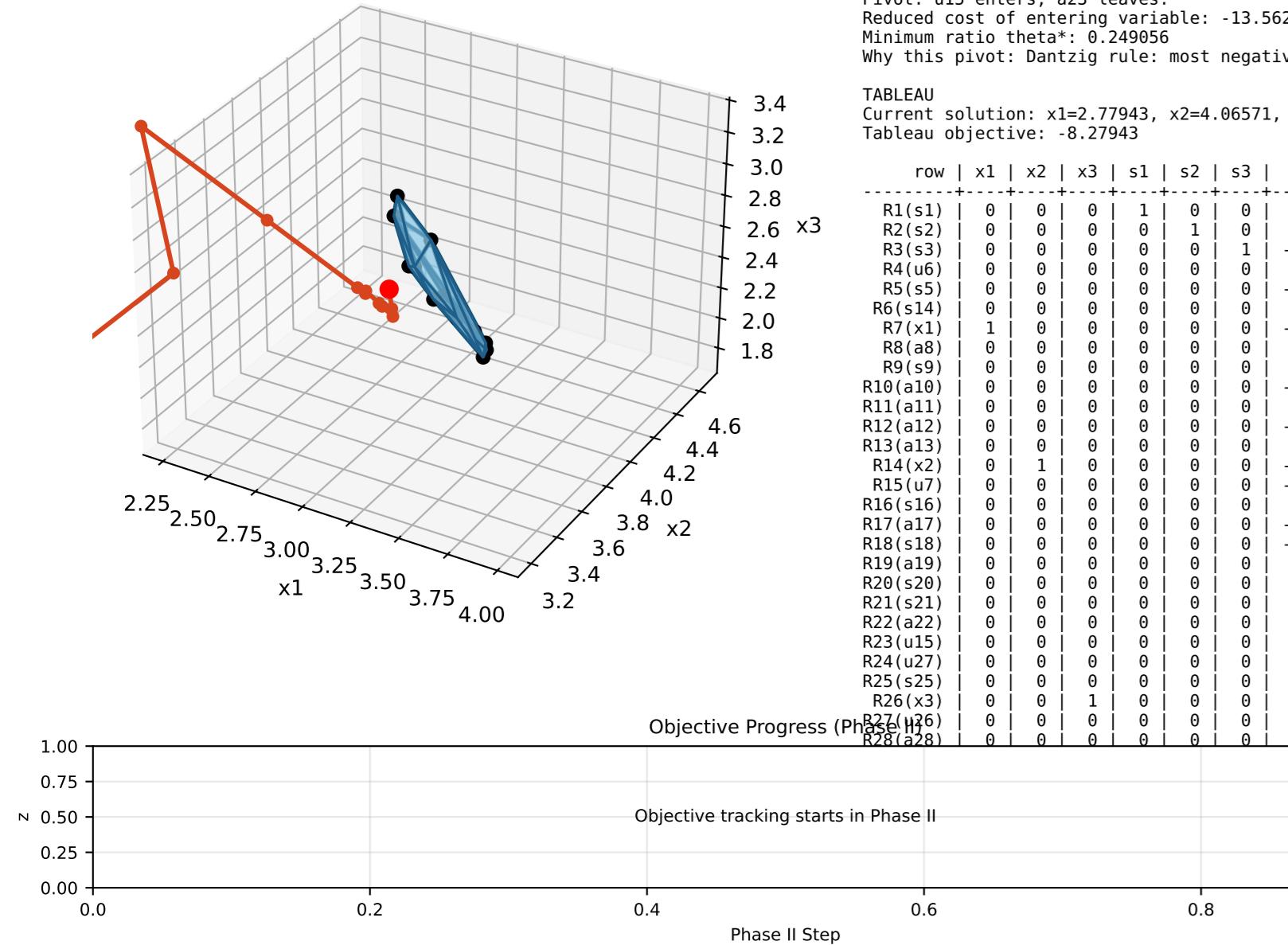
82613, $x_2=4.01902$, $x_3=2.14707$
5573

s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
1	0	0	0.328125	-0.328125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.1875	0.1875	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	0	0	0	0	9.17387	inf					
0	1	0	-0.078125	0.078125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	7.98098	77.3293					
0	0	1	-0.546875	0.546875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.3125	-0.3125	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	0	0	0	0	9.85293	57.3268				
0	0	0	1.09375	-1.09375	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0.625	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	0.450659	inf				
0	0	0	-2.29687	2.29687	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.3125	-1.3125	0	0	0	0	0	0	0	0	0	0.125	-1.125	0	0	0	0	0	0	0	0	3.95182	5.6371			
0	0	0	-0.03125	0.03125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.875	-0.875	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	1.07142	2.3992				
0	0	0	-0.328125	0.328125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	2.82613	27.4991				
0	0	0	-0.390625	0.390625	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0.9375	-0.9375	0	0	0	0	0	0	0	0	0	0.375	-0.375	0	0	0	0	0	0	0	0	1.04294	2.19618			
0	0	0	-0.3125	0.3125	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0	0	0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	2.67176	6.63658			
0	0	0	-2.65625	2.65625	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	2.375	-2.375	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0	0	0	0	2.67045	2.21779			
0	0	0	-1.15625	1.15625	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	1.375	-1.375	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0	0	0	0	2.57868	3.579			
0	0	0	-2.78125	2.78125	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	1.875	-1.875	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0	0	0	0	1.42126	1.55371		
0	0	0	-0.875	0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14476	1.56307		
0	0	0	0.078125	-0.078125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.1875	0.1875	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	0	0	0	0	4.01902	inf				
0	0	0	-0.578125	0.578125	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	1.90097	18.5558				
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf	
0	0	0	-2.375	2.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	-1.5	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.811072	1.15987	
0	0	0	-3	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.93889	5.56194
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf
0	0	0	0.296875	-0.296875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.6875	-0.6875	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	4.02435	10.7895			
0	0	0	0.421875	-0.421875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	2.75061	26.7691		
0	0	0	-0.796875	0.796875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.3125	-1.3125	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0.840251	1.34017			
0	0	0	-1.51562	1.51562	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.4375	-1.4375	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0.358018	0.631234			
0	0	0	1.67187	-1.67187	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.8125	1.8125	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	0	0.17982	0.17982	
0	0	0	-1.23437	1.23437	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5625	-1.5625	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	1	0	0	0	0	0	0	0	0	0	6.50066	7.72058
0	0	0	0.546875	-0.546875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.3125	0.3125	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	0	2.14707	inf		
0	0	0	1.71875	-1.71875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.125	1.125	0	0	0	0	0	0	0	0	0	0	-0.25	0.25	0	1	-1	0	0	0	0	0	0	0	0	0.830862	inf
0	0	0	-0.9375	0.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	-1.25	0	0	0	0	0	0	0	0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	-1	1	0.732642	1.24215	



Phase Simplex Report

Feasible polytope + extreme points + simplex path State 12/3



Step 11 | ENTER: u15 | LEAVE: a23

Table: -13 5625

table: -13.5625
6

⁶ most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

$\times 2-4 .06571 \quad \times 3-2 .2249$

$$x_2=4.065/1, \quad x_3=2.2249$$

s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	u21	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio
1	0	0	0.130435	-0.130435	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.22057	inf								
0	1	0	0.119565	-0.119565	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.93429	42.5652									
0	0	1	-0.217391	0.217391	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.7751	31.5294								
0	0	0	0.434783	-0.434783	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.606319	inf									
0	0	0	-0.913043	0.913043	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.62494	3.01091									
0	0	0	0.891304	-0.891304	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.8535	1.22448									
0	0	0	-0.130435	0.130435	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.77943	15.0727									
0	0	0	0.597826	-0.597826	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.809453	1.11247									
0	0	0	0.478261	-0.478261	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.48497	3.56235									
0	0	0	-0.152174	0.152174	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.07894	1.1244									
0	0	0	0.293478	-0.293478	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	2.23623	1.87541								
0	0	0	-0.804348	0.804348	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.954281	0.758006									
0	0	0	0.706522	-0.706522	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.771172	0.763171								
0	0	0	-0.119565	0.119565	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.06571	inf								
0	0	0	-0.380435	0.380435	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.85427	10.1385									
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf									
0	0	0	-0.793478	0.793478	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.437488	0.540715									
0	0	0	-0.891304	0.891304	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.44078	2.96945								
0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf									
0	0	0	1.02174	-1.02174	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.85313	5.85361									
0	0	0	0.619565	-0.619565	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.70391	14.6699								
0	0	0	0.586957	-0.586957	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.513365	0.640192									
0	0	0	-1.05435	1.05435	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.249056	0.249056									
0	0	0	-0.23913	0.23913	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.631234	inf								
0	0	0	0.413043	-0.413043	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.11151	4.16042								
0	0	0	0.217391	-0.217391	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.2249	inf						
0	0	0	0.532609	-0.532609	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.11105	inf								
0	0	0	0.380435	-0.380435	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.421322	0.586113								

Phase Simplex Report

feasible polytope + extreme points + simplex path State 13/3

COMMENTS
Teaching Mode | Rule: D
Pivot: u23 enters, a17
Reduced cost of entering
Minimum ratio theta*: 0
Why this pivot: Dantzig

3.4 TABLEAU
Current solution: $x_1=2.72474$, $x_2=4.1204$, $x_3=2$
Tableau objective: -4.74307



-Phase Simplex Report

Feasible polytope + extreme points + simplex path State 1

COMMENTS
D. L. M. J.

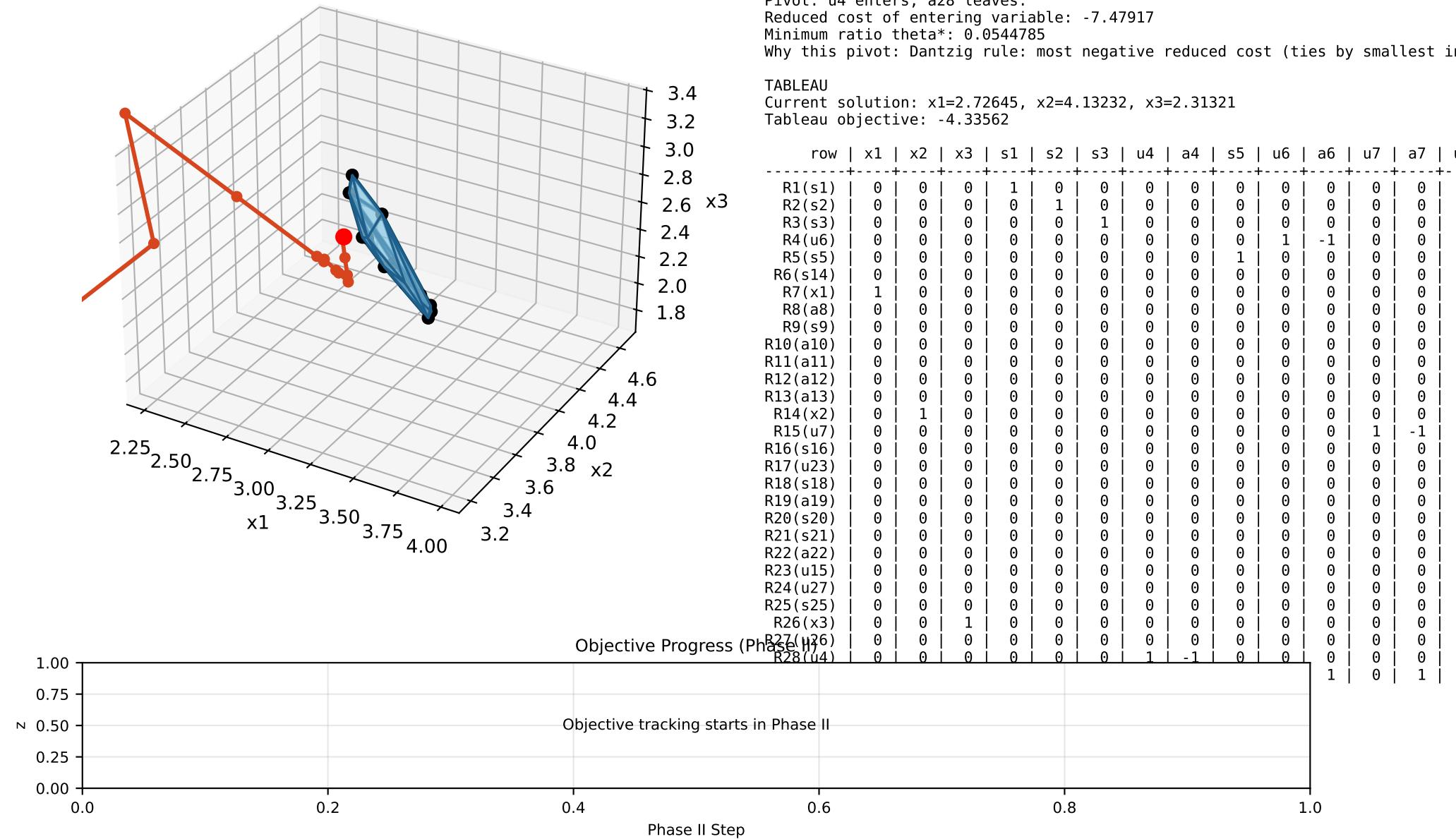
Teaching Mode | Rule: DANIZIG
Pivot: u4 enters, a28 leaves.
Reduced cost of entering variable: -
Minimum ratio theta*: 0.0544785

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

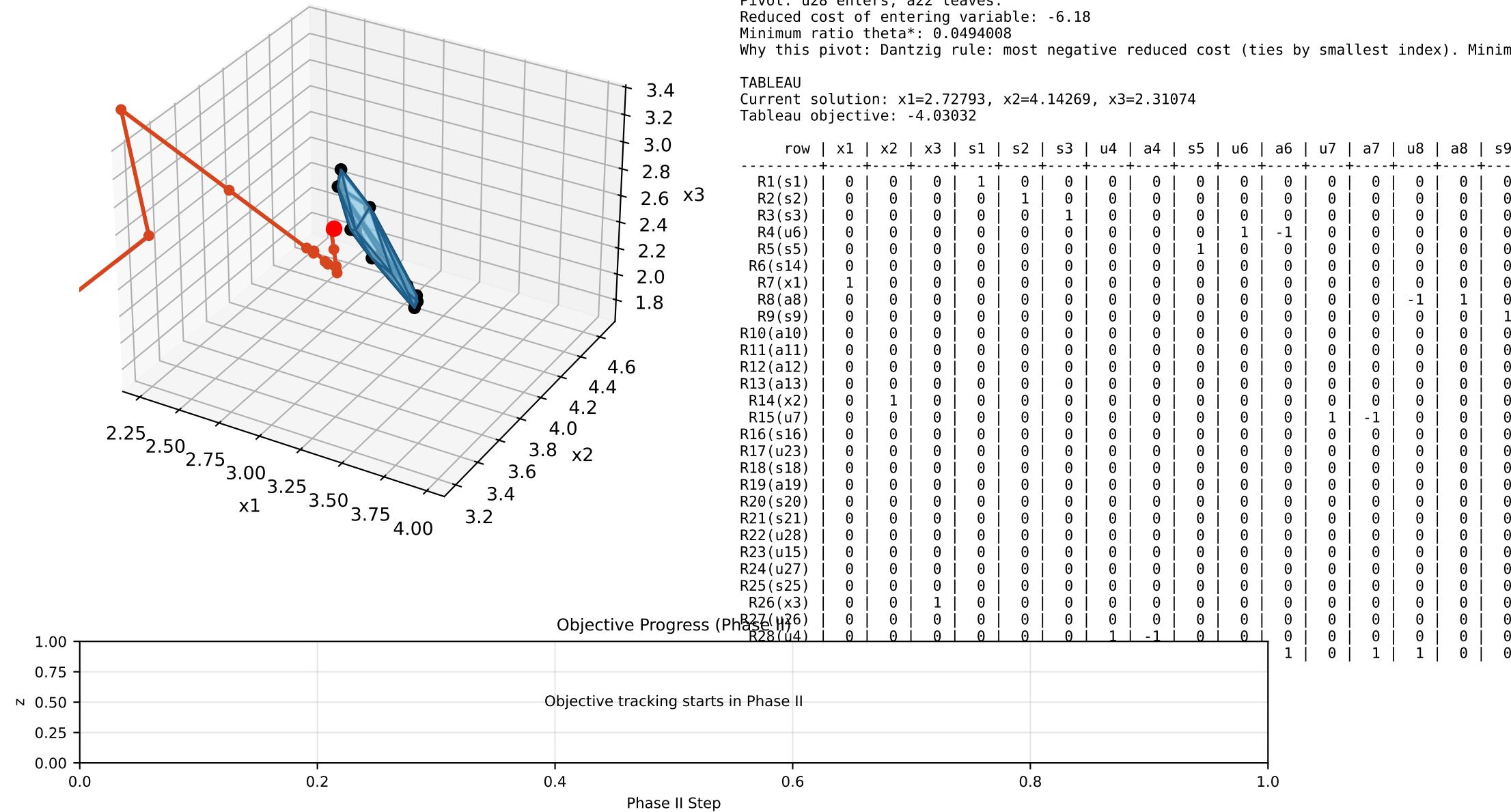
Current solution: $x_1=2.72645$, $x_2=4.13232$, $x_3=2.31321$
Tableau objective: -4.33562

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	a18	u19	a19	s20	u21	a21	s22	u23	a23	u24	a24	s25	u26	a26	s27	u27	a27	u28	a28	rhs	ratio
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.15	0.15	0	0	0	0.26	-0.26	0	0	0	0	0	0	0.03	-0.03	9.27355	296.808										
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.05	0.05	0	0	0	-0.18	0.18	0	0	0	0	0	0	0.21	-0.21	7.86768	36.021										
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.25	-0.25	0	0	0	-0.1	0.1	0	0	0	0	0	0	0.05	0.05	9.68679	inf										
R4(u6)	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.5	0.5	0	0	0	-0.2	0.2	0	0	0	0	0	0	0.1	-0.1	0.78293	7.57061									
R5(s5)	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1.05	-1.05	0	0	0	0.18	-0.18	0	0	0	0	0	0	-0.21	0.21	3.25405	inf									
R6(s14)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.5	0.5	0	0	0	-0.4	0.4	0	0	0	0	0	0	0.524526	0.441821											
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.15	-0.15	0	0	0	-0.26	0.26	0	0	0	0	0	-0.03	0.03	2.72645	inf										
R8(a8)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0.1	-0.1	0	0	0	0	0	0	0.476438	0.490079											
R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.2	0.2	0	0	0	0.28	-0.28	0	0	0	0	0	0	0.84	-0.84	2.21856	2.58997									
R10(a10)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.7	-0.7	0	0	0	0.48	-0.48	0	0	0	0	0	0	1.06	-1.06	1.3261	1.25547								
R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1	-0.1	0	0	0	0.16	-0.16	0	0	0	0	0	0	0.98	-0.98	1.77959	1.79775								
R12(a12)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0.18	-0.18	0.397206	2.17291								
R13(a13)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.144	-0.144	0.251967	0.222456								
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.21	0.21	4.13232	inf								
R15(u7)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.8149	inf										
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.567389	inf										
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.460686	inf										
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.16	-0.16	4.84838	29.1448								
R19(a19)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0435621	0.228727										
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.35714	2.63647										
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.69	-0.69	2.61007	3.68588								
R22(a22)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.060763	0.101903										
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.626972	inf										
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.123	-0.123	1.22513	inf								
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.558826	4.56266										
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0544785	44.4681										
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.06	-0.06	1.44257	inf								
R28(u44)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.096	0.96	0.0544785	0.0544785								



Phase Simplex Report

feasible polytope + extreme points + simplex path State 15/3



tep 14 | ENTER: u28 | LEAVE: a22

| Rule: DANTZIG

vers. a?? leaves.

of entering variable: -6.18

theta*: 0.0491008

: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

exp: x1=3.73793 x2=4.14269 x3=3.31974

on: $x_1=2.72793$, $x_2=4.14269$, $x_3=2.31483$

Phase Simplex Report

feasible polytope + extreme points + simplex path State 16/3

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u22 enters, a13 leaves.
Reduced cost of entering variable: -4.02439
Minimum ratio theta*: 0.154459
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index)

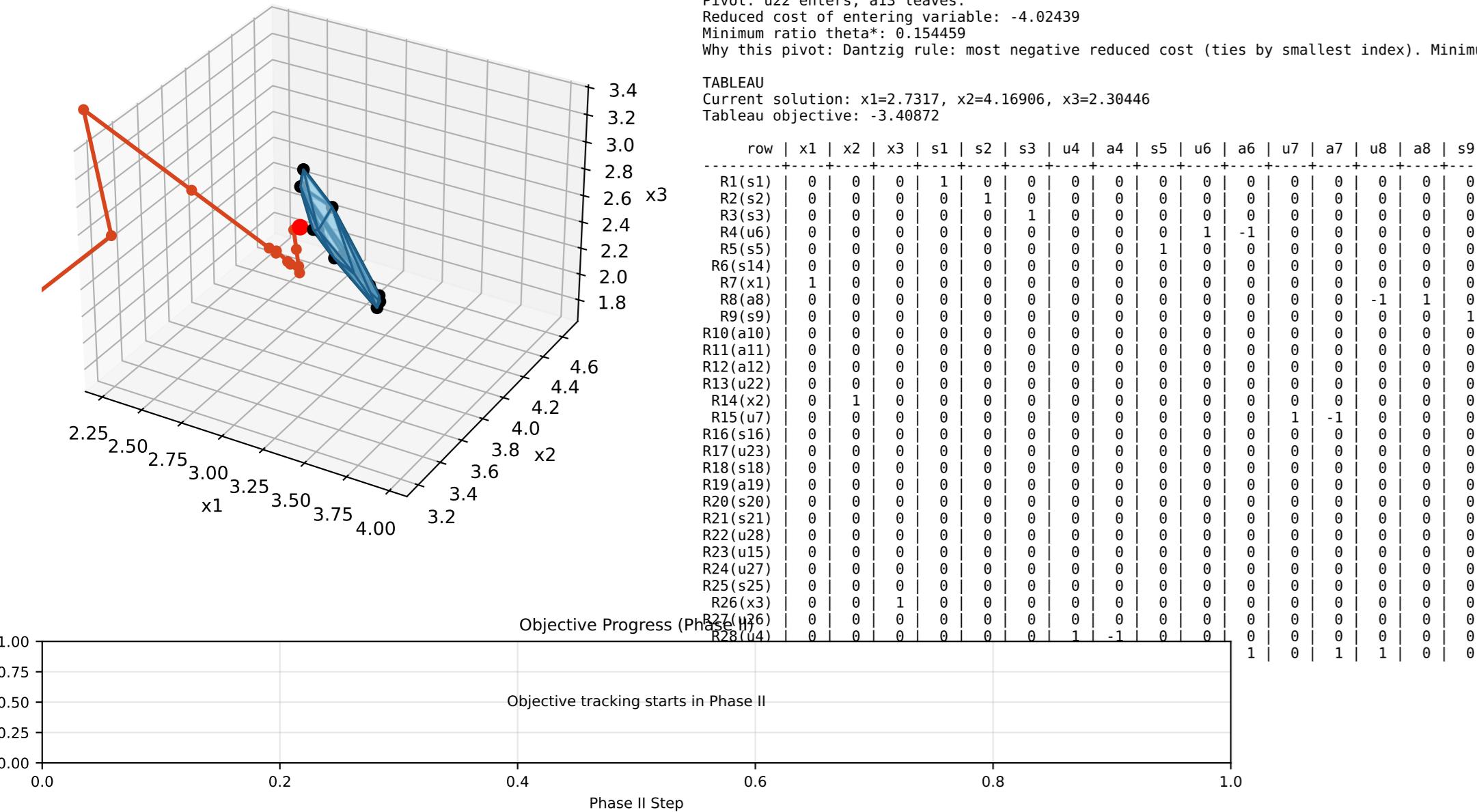


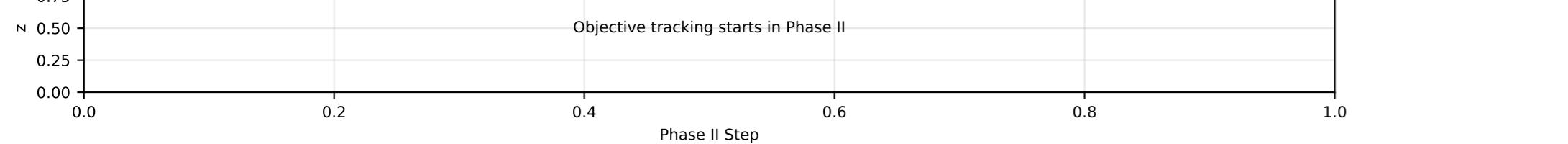
TABLEAU
Current solution: $x_1=2.7317$, $x_2=4.16906$, $x_3=2.30446$
Tableau objective: -3.40872

Phase Simplex Report

Feasible polytope + extreme points + simplex path State 18/

COMMENTS
Teaching Mode | Rule:
Pivot: u19 enters, s14
Reduced cost of entering
Minimum ratio theta*: 0.000000
Why this pivot: Dantzig

TABLEAU
Current solution: $x_1=2.73855$, $x_2=4.21705$, $x_3=2.29304$
Tableau objective: -2.65994



Phase Simplex Report

feasible polytope + extreme points + simplex path State 19/3

Step 18 | ENTER: u17 | LEAVE: a12

ENTZIG

eaves.

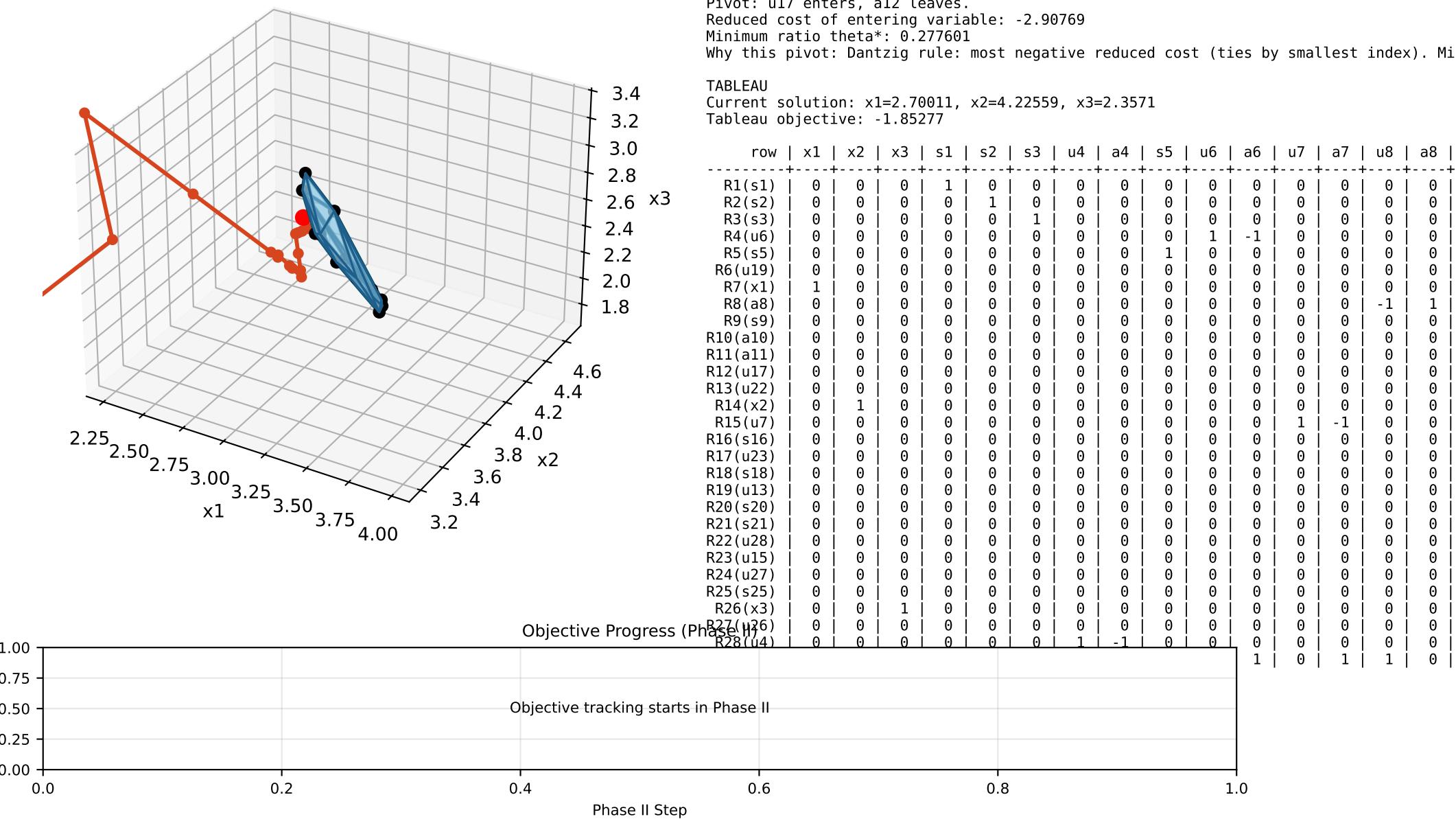
variable: -2.90769

277601

rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

0011. x2=4.22559. x3=2.3571

277

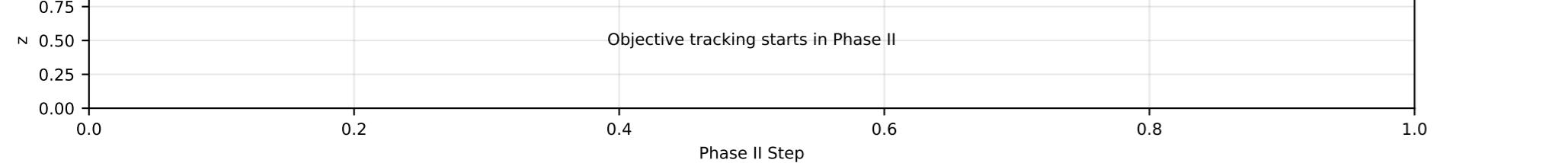


-Phase Simplex Report

Feasible polytope + extreme points + simplex path State 20

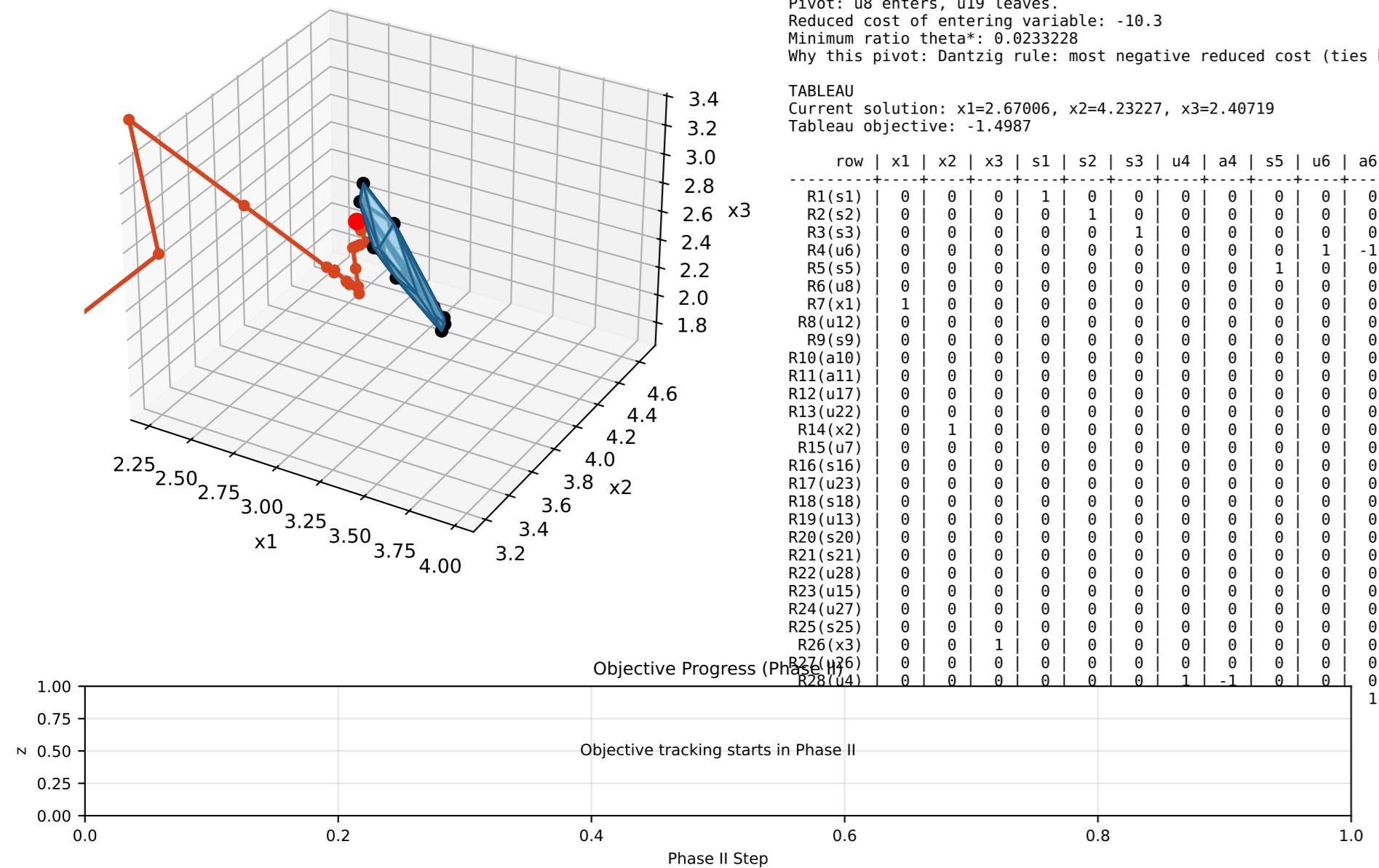
COMMENTS
Teaching Mode |
Pivot: u12 enter
Reduced cost of
Minimum ratio th
Why this pivot:

TABLEAU
Current solution: $x_1=2.69105$, $x_2=4.2276$, $x_3=2.37221$
Tableau objective: -1.73893



Phase Simplex Report

Feasible polytope + extreme points + simplex path State 21



step 20 | ENTER: u8 | LEAVE: u19

DANTZIG

BANBEE

ing variable: -10.3

0.0233228

ig rule: most negative

¹³ Value most negative reduced cost (less by smallest LHS), ¹⁴ Maximum value less (less by smallest RHS).

3-67000

$x_2=4.23221$, $x_3=1.083$

.4987

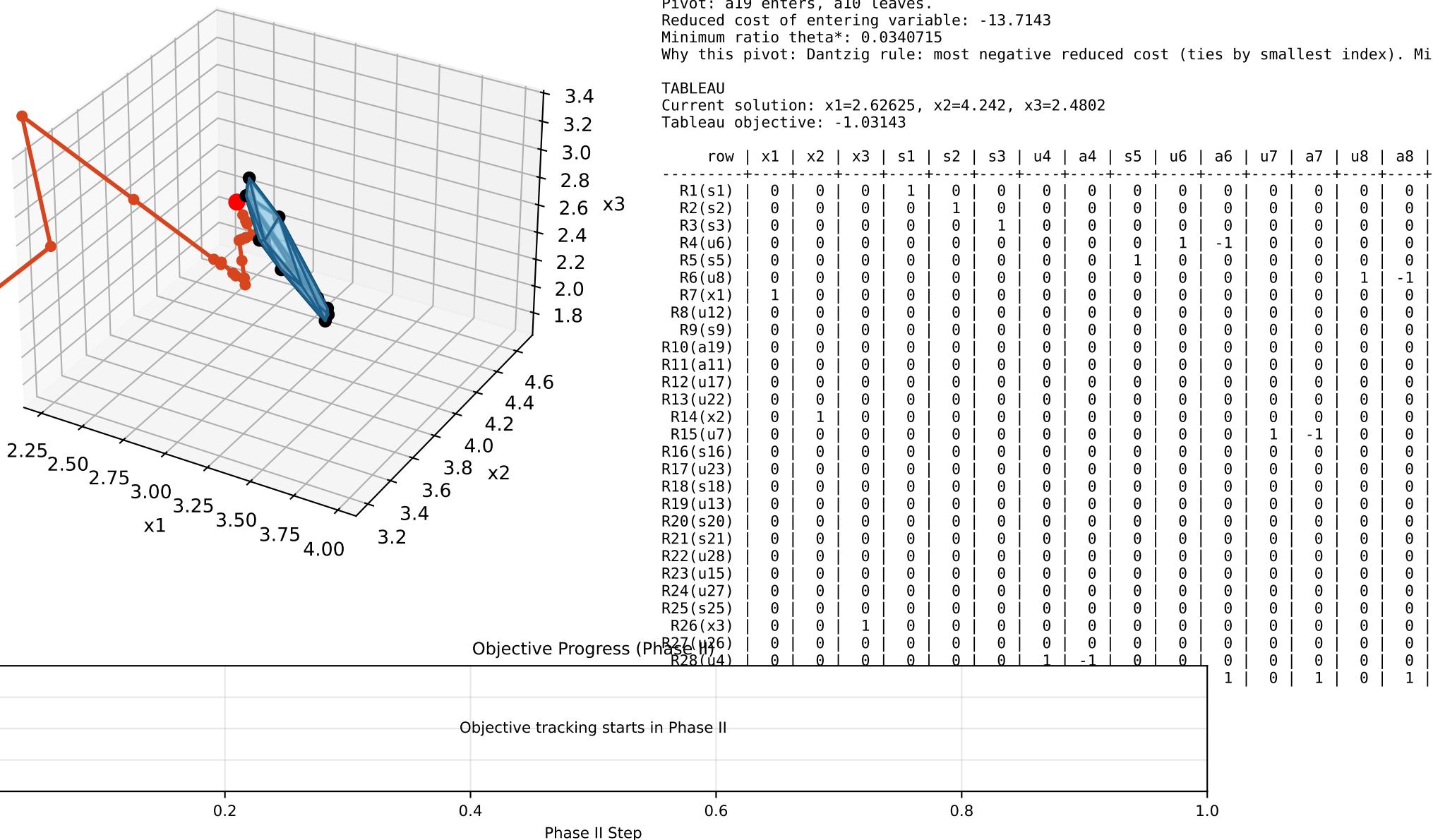
-2- | -1- | -2- | -3- |

Phase Simplex Report

feasible polytope + extreme points + simplex path State 22

o 21 | ENTER: a19 | LEAVE: a10

```
TZIG
aves.
variable: -13.7143
340715
ule: most negative reduced cost (ties by smallest index).
```



Phase Simplex Report

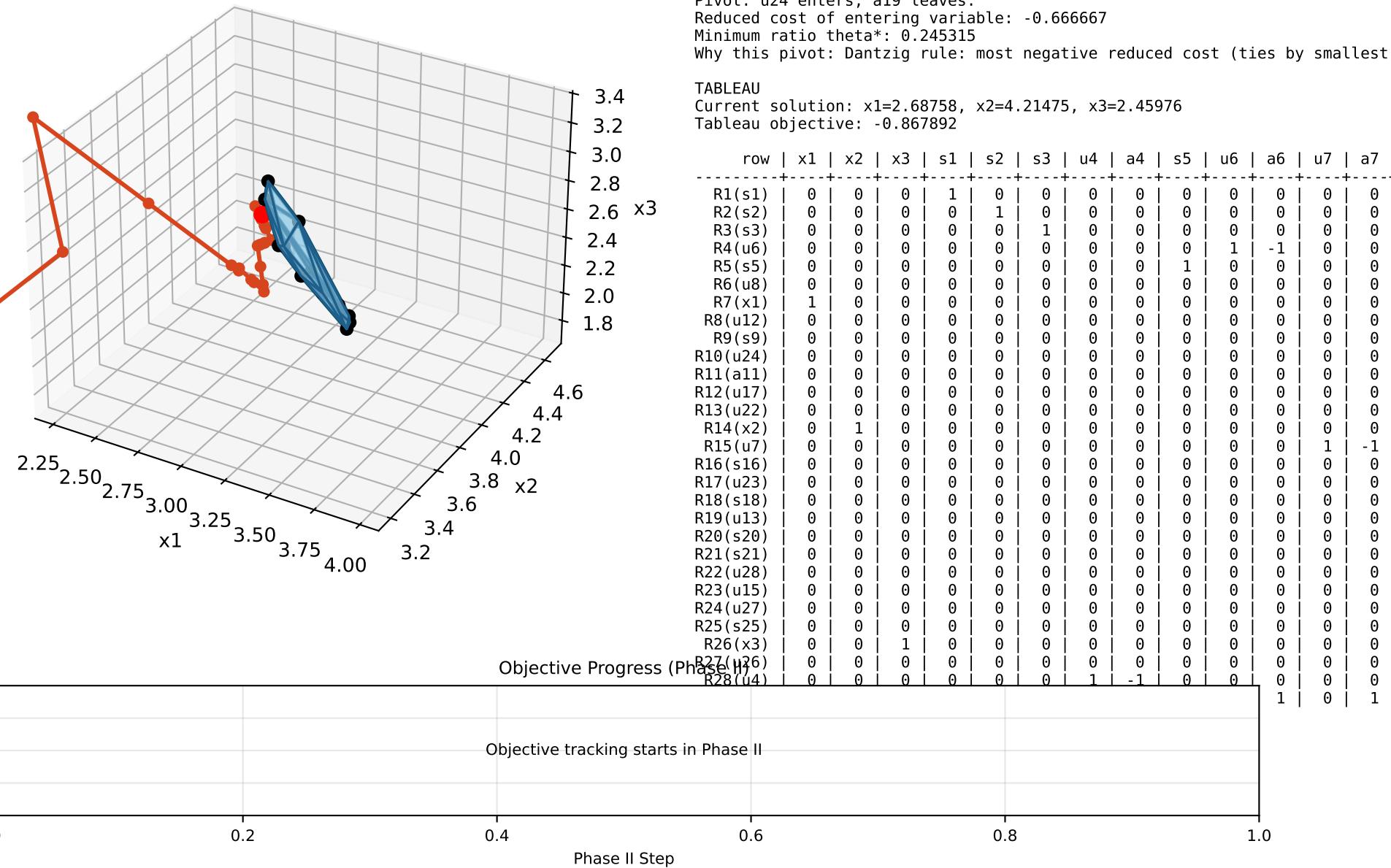
Feasible polytope + extreme points + simplex path State 23/33

COMMENTS

Teaching Mode | Rule: DANTZIG
Pivot: u24 enters, a19 leaves.
Reduced cost of entering variable: -0.666667

Reduced cost of entering variable: -0.00000
 Minimum ratio theta*: 0.245315
 Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

why this pivot. Banting rate: most negative reduced cost (ties by Smallest)



Phase Simplex Report

Feasible polytope + extreme points + simplex path

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u19 enters, a11 leaves.
Reduced cost of entering variable: -3.8
Minimum ratio theta*: 0.228393
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smalles

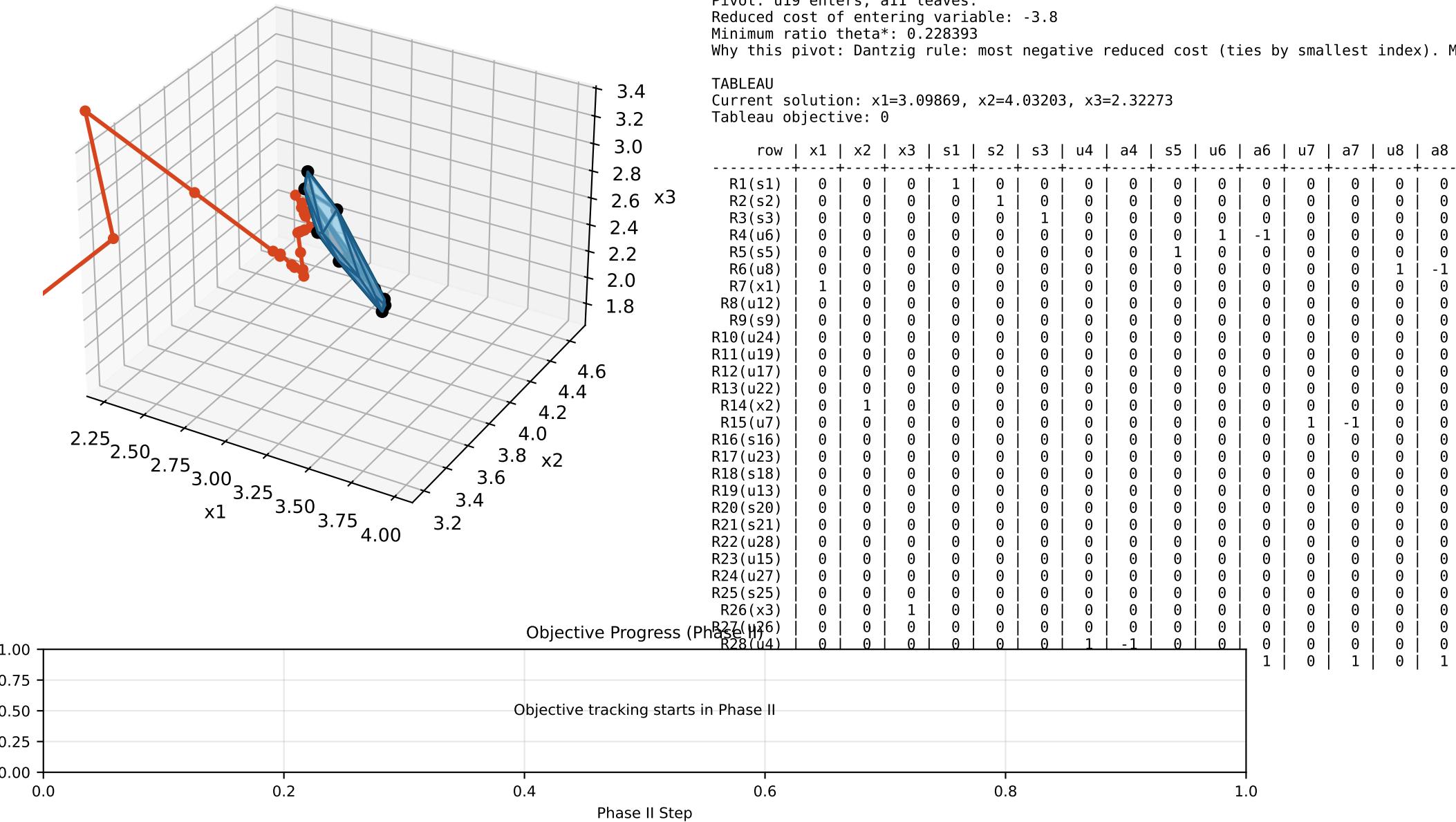
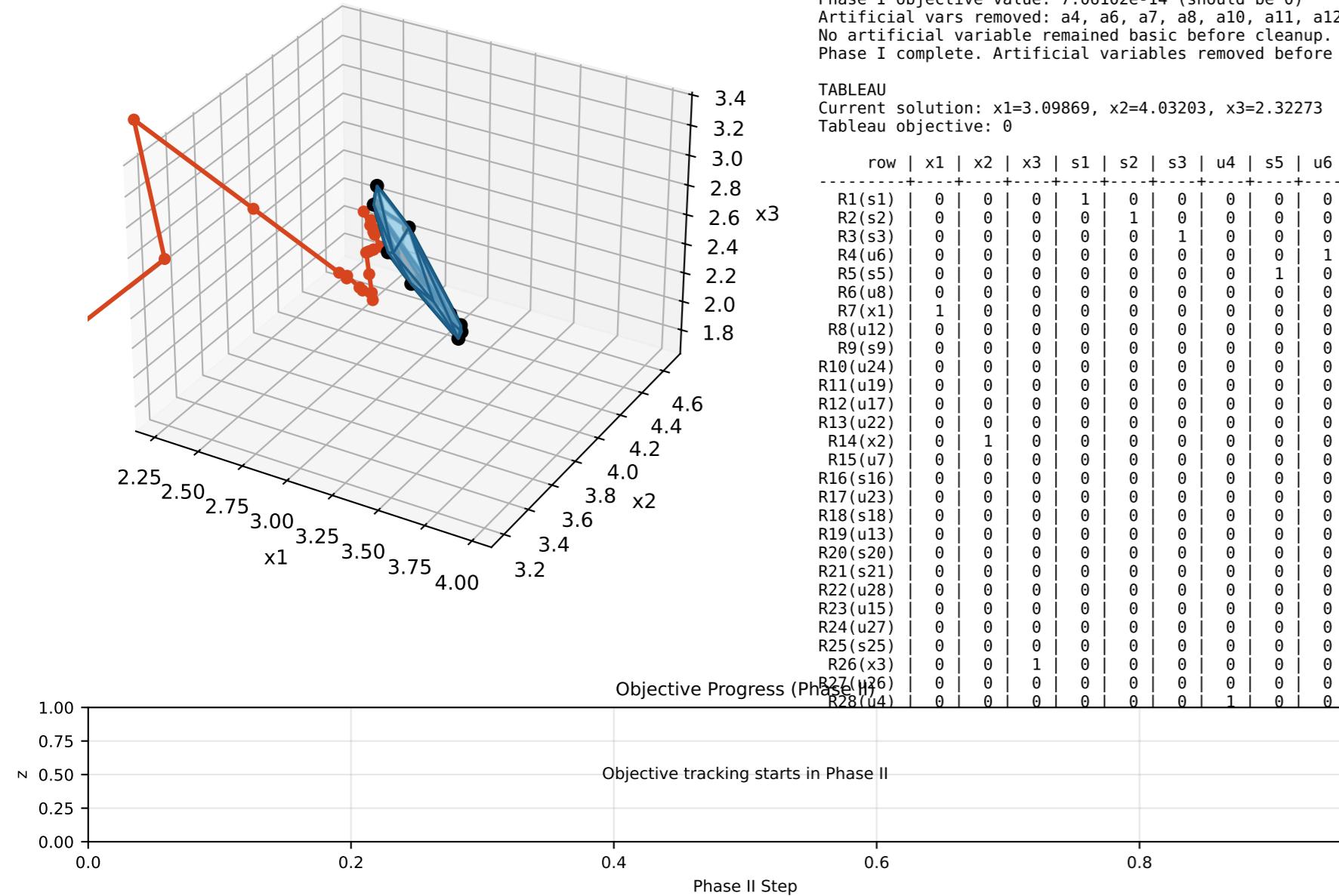


TABLEAU
Current solution: $x_1=3.09869$, $x_2=4.03203$, $x_3=2.32273$
Tableau objective: 0

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 25/31 | PHASE I -> PHASE II step 0

COMMENTS

Teaching Mode | Phase Transition

Phase I objective value: 7.06102e-14 (should be 0)

Artificial vars removed: a4, a6, a7, a8, a10, a11, a12, a13, a15, a17, a19, a22, a23, a24, a26, a27, a28

No artificial variable remained basic before cleanup.

Phase I complete. Artificial variables removed before restoring original objective.

TABLEAU

Current solution: $x_1=3.09869$, $x_2=4.03203$, $x_3=2.32273$

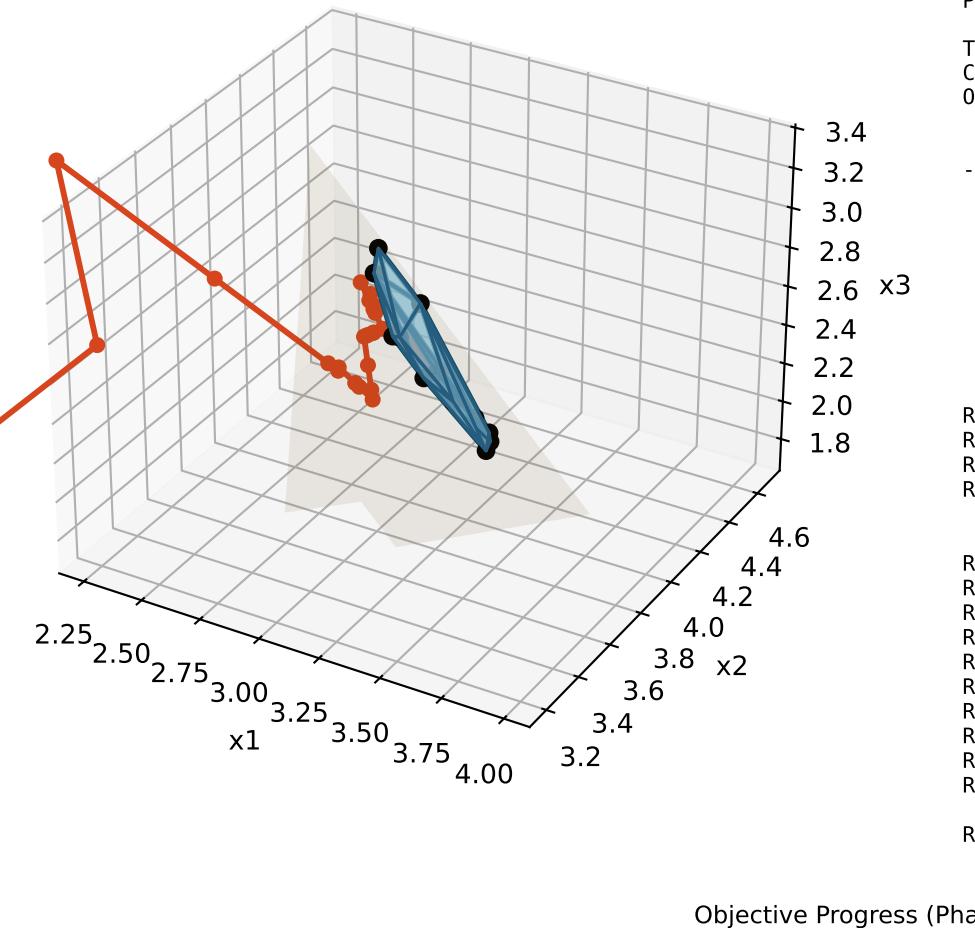
Tableau objective: 0

row	x_1	x_2	x_3	s_1	s_2	s_3	u_4	s_5	u_6	u_7	u_8	s_9	u_{10}	u_{11}	u_{12}	u_{13}	s_{14}	u_{15}	s_{16}	u_{17}	s_{18}	u_{19}	s_{20}	s_{21}	u_{22}	u_{23}	u_{24}	s_{25}	u_{26}	u_{27}	u_{28}	rhs	ratio			
R1(s_1)	0	0	0	1	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.90131	inf		
R2(s_2)	0	0	0	0	1	0	0	0	0	0	0	0	0.118421	-0.210526	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.96797	inf		
R3(s_3)	0	0	0	0	0	1	0	0	0	0	0	0	0.276316	-0.157895	0	0	0.144737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.67727	inf		
R4(u_6)	0	0	0	0	0	0	0	0	0	1	0	0	-0.552632	0.315789	0	0	-0.289474	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.801961	inf		
R5(s_5)	0	0	0	0	0	0	0	0	0	1	0	0	0.671053	0.473684	0	0	1.06579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.08024	inf	
R6(u_8)	0	0	0	0	0	0	0	0	0	0	1	0	0.223684	-0.842105	0	0	0.355263	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.911881	inf	
R7(x_1)	1	0	0	0	0	0	0	0	0	0	0	0	0.328947	-0.473684	0	0	-0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.09869	inf		
R8(u_{12})	0	0	0	0	0	0	0	0	0	0	0	0	-1.23684	0.421053	1	0	-0.552632	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.203795	inf	
R9(s_9)	0	0	0	0	0	0	0	0	0	0	0	1	-0.342105	1.05263	0	0	-0.131579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.729953	inf	
R10(u_{24})	0	0	0	0	0	0	0	0	0	0	0	0	0.815789	-1.89474	0	0	-0.763158	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.88974	inf	
R11(u_{19})	0	0	0	0	0	0	0	0	0	0	0	0	0.210526	-0.263158	0	0	0.157895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.228393	inf	
R12(u_{17})	0	0	0	0	0	0	0	0	0	0	0	0	-0.789474	-0.263158	0	0	-0.842105	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	1.07352	inf	
R13(u_{22})	0	0	0	0	0	0	0	0	0	0	0	0	-0.223684	-0.157895	0	0	0.644737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.855033	inf	
R14(x_2)	0	1	0	0	0	0	0	0	0	0	0	0	-0.118421	0.210526	0	0	0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.03203	inf	
R15(u_7)	0	0	0	0	0	0	0	0	0	0	1	0	0.539474	-0.736842	0	0	0.0921053	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.4591	inf	
R16(s_{16})	0	0	0	0	0	0	0	0	0	0	0	0	-0.815789	1.89474	0	0	0.763158	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.78415	inf
R17(u_{23})	0	0	0	0	0	0	0	0	0	0	0	0	-0.592105	0.0526316	0	0	0.118421	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.21433	inf	
R18(s_{18})	0	0	0	0	0	0	0	0	0	0	0	0	0	1.18421	-0.105263	0	0	0.763158	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	3.86563	inf
R19(u_{13})	0	0	0	0	0	0	0	0	0	0	0	0	-0.342105	0.0526316	0	1	0.868421	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.563544	inf	
R20(s_{20})	0	0	0	0	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	-0.934211	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.68037	inf
R21(s_{21})	0	0	0	0	0	0	0	0	0	0	0	0	-0.3026316	0.315789	0	0	-0.539474	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.16645	inf	
R22(u_{28})	0	0	0	0	0	0	0	0	0	0	0	0	-0.0526316	-0.684211	0	0	0.210526	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.39783	inf	
R23(u_{15})	0	0	0	0	0	0	0	0	0	0	0	0	0.263158	-0.578947	0	0	0.947368	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.80521	inf	
R24(u_{27})	0	0	0	0	0	0	0	0	0	0	0	0	-0.828947	0.473684	0	0	0.565789	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.7782	inf	
R25(s_{25})	0	0	0	0	0	0	0	0	0	0	0	0	0.118421	0.789474	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.90896	inf	
R26(x_3)	0	0	1	0	0																															

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 115$$



State 26/31 | PHASE II step 0 | Z=114.673

COMMENTS

Teaching Mode | PHASE II

Phase II objective restored and made basis-consistent.

TABLEAU

Current solution: $x_1=3.09869$, $x_2=4.03203$, $x_3=2.32273$

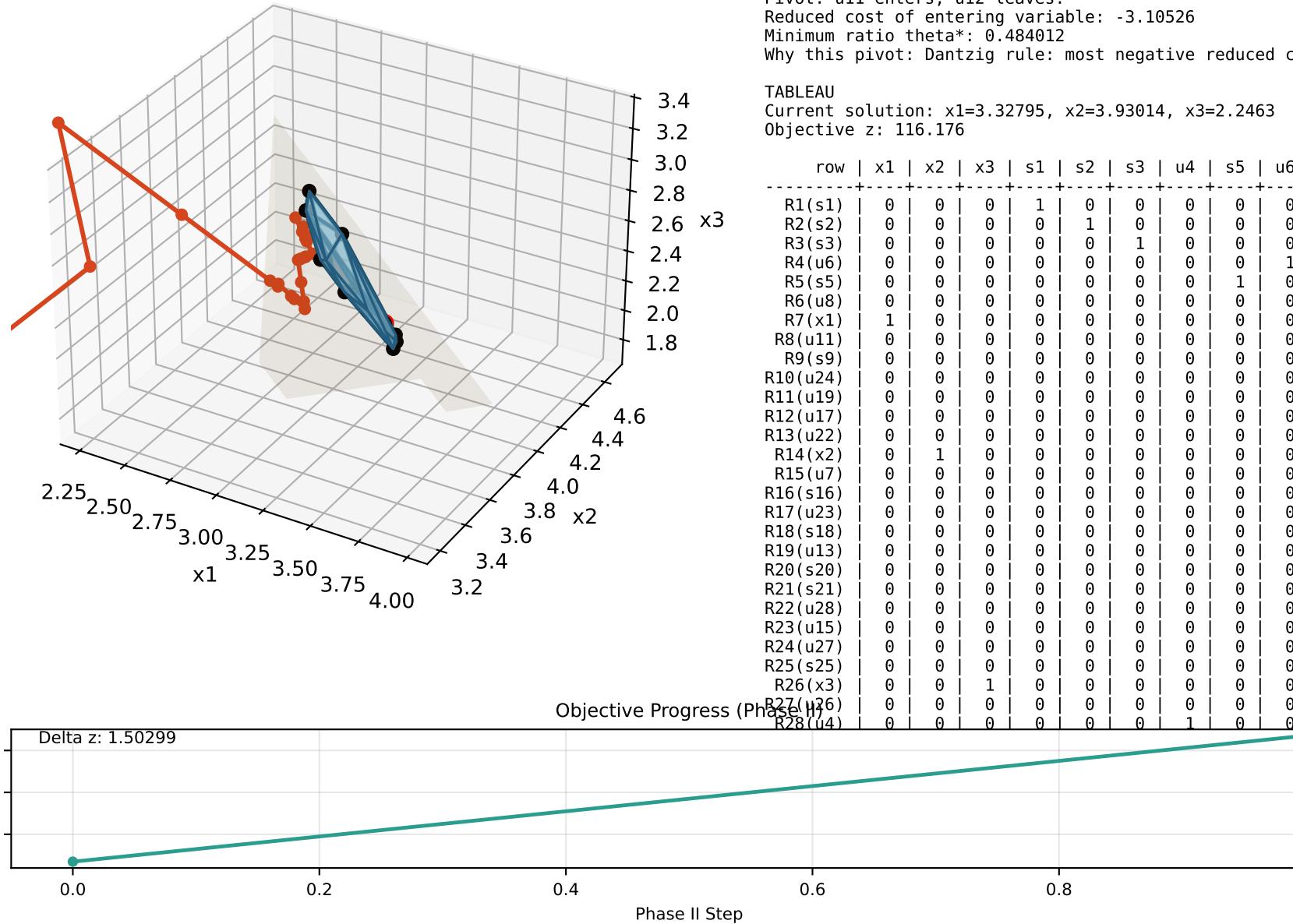
Objective z: 114.673

row	x_1	x_2	x_3	s_1	s_2	s_3	u_4	s_5	u_6	u_7	u_8	s_9	u_{10}	u_{11}	u_{12}	u_{13}	s_{14}	u_{15}	s_{16}	u_{17}	s_{18}	u_{19}	s_{20}	s_{21}	u_{22}	u_{23}	s_{25}	u_{26}	u_{27}	u_{28}	rhs	ratio			
R1(s_1)	0	0	0	1	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.90131	inf		
R2(s_2)	0	0	0	0	0	1	0	0	0	0	0	0	0.118421	-0.210526	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.96797	inf		
R3(s_3)	0	0	0	0	0	0	1	0	0	0	0	0	0.276316	-0.157895	0	0	0.144737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.67727	inf		
R4(u_6)	0	0	0	0	0	0	0	0	0	1	0	0	-0.552632	0.315789	0	0	-0.289474	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.801961	inf	
R5(s_5)	0	0	0	0	0	0	0	0	1	0	0	0	0.671053	0.473684	0	0	1.06579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.08024	inf	
R6(u_8)	0	0	0	0	0	0	0	0	0	0	0	1	0	0.223684	-0.842105	0	0	0.355263	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.911881	inf	
R7(x_1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0.328947	-0.473684	0	0	-0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.09869	inf	
R8(u_{12})	0	0	0	0	0	0	0	0	0	0	0	0	-1.23684	0.421053	1	0	-0.552632	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.203795	inf	
R9(s_9)	0	0	0	0	0	0	0	0	0	0	0	0	1	-0.342105	1.05263	0	0	-0.131579	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.729953	inf	
R10(u_{24})	0	0	0	0	0	0	0	0	0	0	0	0	0	0.815789	-1.89474	0	0	-0.763158	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.88974	inf	
R11(u_{19})	0	0	0	0	0	0	0	0	0	0	0	0	0	0.210526	-0.263158	0	0	0.157895	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.228393	inf	
R12(u_{17})	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.789474	-0.263158	0	0	-0.842105	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.07352	inf	
R13(u_{22})	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.223684	-0.157895	0	0	0.644737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.855033	inf	
R14(x_2)	0	1	0	0	0	0	0	0	0	0	0	0	0	-0.118421	0.210526	0	0	0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.03203	inf	
R15(u_7)	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0.539474	-0.736842	0	0	0.0921053	0	0	0	0	0	0	0	0	0	0	0	0	0	2.4591	inf	
R16(s_{16})	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.815789	1.89474	0	0	0.763158	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	3.78415	inf
R17(u_{23})	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.592105	0.0526316	0	0	0.118421	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.21433	inf	
R18(s_{18})	0	0	0	0	0	0	0	0	0	0	0	0	0	1.18421	-0.105263	0	0	0.763158	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.86563	inf
R19(u_{13})	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.342105	0.0526316	0	1	0.868421	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.563544	inf	
R20(s_{20})	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	-0.934211	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.68037	inf	
R21(s_{21})	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.302632	0.315789	0	0	-0.539474	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.16645	inf	
R22(u_{28})	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0526316	-0.684211	0	0	0.210526	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.39783	inf	
R23(u_{15})	0	0	0	0	0	0	0	0	0	0	0	0	0	0.263158	-0.578947	0	0	0.947368	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1.80521	inf	
R24(u_{27})	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.828947	0.473684	0	0	0.565789	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.7782	inf	
R25(s_{25})	0	0	0	0	0	0	0	0	0	0	0	0	0	0.118421	0.789474	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.90896	inf	
R26(x_3)	0	0	1	0	0	0	0	0	0	0	0	0	0	-0.276316	0.157895	0	0	-0.144737	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.32273	inf	
R27(u_{26})	0	0																																	

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 116$$



State 27/31 | PHASE II step 1 | ENTER: u_{11} | LEAVE: u_{12} | $Z=116.176$

COMMENTS

Teaching Mode | Rule: DANTZIG
 Pivot: u_{11} enters, u_{12} leaves.
 Reduced cost of entering variable: -3.10526
 Minimum ratio theta*: 0.484012

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

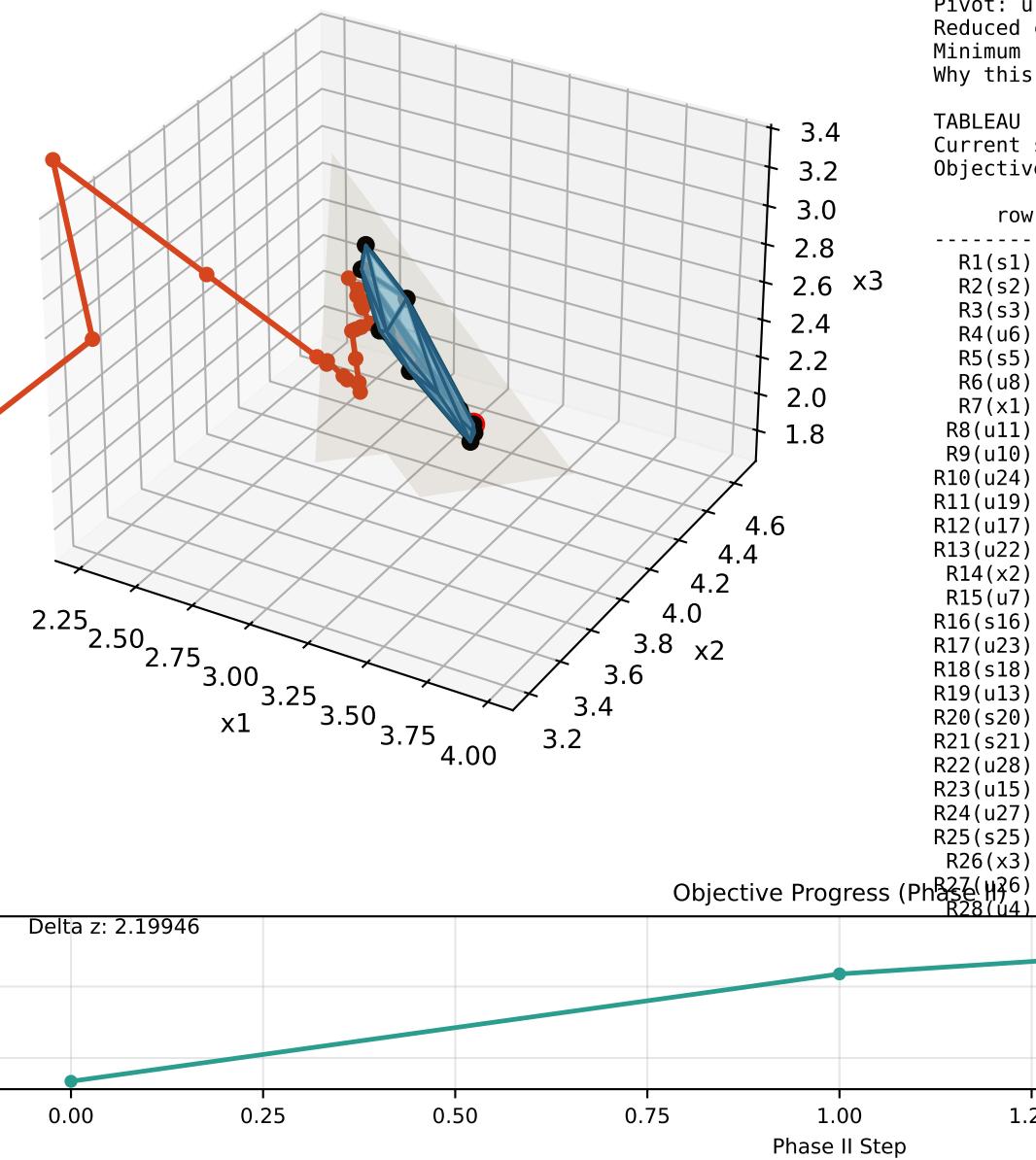
Current solution: $x_1=3.32795$, $x_2=3.93014$, $x_3=2.2463$
 Objective z: 116.176

row	x_1	x_2	x_3	s_1	s_2	s_3	u_4	s_5	u_6	u_7	u_8	s_9	u_{10}	u_{11}	u_{12}	u_{13}	s_{14}	u_{15}	s_{16}	u_{17}	s_{18}	u_{19}	s_{20}	s_{21}	u_{22}	u_{23}	u_{24}	s_{25}	u_{26}	u_{27}	u_{28}	rhs	ratio	
R1(s_1)	0	0	0	1	0	0	0	0	0	0	0	0	1.0625	0	-1.125	0	0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	8.67205	18.7917		
R2(s_2)	0	0	0	0	1	0	0	0	0	0	0	0	-0.5	0	0.5	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	8.06986	inf		
R3(s_3)	0	0	0	0	0	1	0	0	0	0	0	0	-0.1875	0	0.375	0	-0.0625	0	0	0	0	0	0	0	0	0	0	0	0	0	9.7537	inf		
R4(u_6)	0	0	0	0	0	0	0	0	0	1	0	0	0.375	0	-0.75	0	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0.649115	2.53954		
R5(s_5)	0	0	0	0	0	0	0	0	0	0	0	1	2.0625	0	-1.125	0	1.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	1.85097	4.39162		
R6(u_8)	0	0	0	0	0	0	0	0	0	0	0	0	-2.25	0	2	0	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.31947	inf	
R7(x_1)	1	0	0	0	0	0	0	0	0	0	0	0	-1.0625	0	1.125	0	-0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	3.32795	inf		
R8(u_{11})	0	0	0	0	0	0	0	0	0	0	0	0	-2.9375	1	2.375	0	-1.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0.484012	0.484012		
R9(s_9)	0	0	0	0	0	0	0	0	0	0	0	1	2.75	0	-2.5	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0.220467	0.693456		
R10(u_{24})	0	0	0	0	0	0	0	0	0	0	0	0	-4.75	0	4.5	0	-3.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.80682	inf	
R11(u_{19})	0	0	0	0	0	0	0	0	0	0	0	0	-0.5625	0	0.625	0	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0.355764	inf		
R12(u_{17})	0	0	0	0	0	0	0	0	0	0	0	0	-1.5625	0	0.625	0	-1.1875	0	0	1	0	0	0	0	0	0	0	0	0	0	1.2009	inf		
R13(u_{22})	0	0	0	0	0	0	0	0	0	0	0	0	-0.6875	0	0.375	0	0.4375	0	0	0	0	0	0	0	0	0	0	0	0	0	0.931456	inf		
R14(x_2)	0	1	0	0	0	0	0	0	0	0	0	0	0.5	0	-0.5	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.93014	19.1522	
R15(u_7)	0	0	0	0	0	0	0	0	0	0	0	1	0	-1.625	0	1.75	0	-0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	2.81574	inf	
R16(s_{16})	0	0	0	0	0	0	0	0	0	0	0	0	4.75	0	-4.5	0	3.25	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	2.86707	1.99719
R17(u_{23})	0	0	0	0	0	0	0	0	0	0	0	0	-0.4375	0	-0.125	0	0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.18885	23.0722	
R18(s_{18})	0	0	0	0	0	0	0	0	0	0	0	0	0.875	0	0.25	0	0.625	0	0	0	1	0	0	0	0	0	0	0	0	0	0	3.91658	inf	
R19(u_{13})	0	0	0	0	0	0	0	0	0	0	0	0	-0.1875	0	-0.125	1	0.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.53807	10.7073
R20(s_{20})	0	0	0	0	0	0	0	0	0	0	0	0	1.0625	0	-1.125	0	-0.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.4511	5.65856
R21(s_{21})	0	0	0	0	0	0	0	0	0	0	0	0	0.625	0	-0.75	0	-0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.0136	6.86041
R22(u_{28})	0	0	0	0	0	0	0	0	0	0	0	0	-2.0625	0	1.625	0	-0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.729	inf
R23(u_{15})	0	0	0	0	0	0	0	0	0	0	0	0	-1.4375	0	1.375	0	0.1875	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.08542	inf
R24(u_{27})	0	0	0	0	0	0	0	0	0	0	0	0	0.5625	0	-1.125	0	1.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.54893	3.75397
R25(s_{25})	0	0	0	0	0	0	0	0	0	0	0	0	2.4375	0	-1.875	0	0.8125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.52684	4.95134
R26(x_3)	0	0	1	0	0	0	0	0	0	0	0	0	0.1875	0	-0.375	0	0.0625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.2463	14.7106
R27(s_{26})	0	0	0	0	0	0	0	0	0	0	0	0	0	1.0625	0	-1.625	0	0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.03967	2.00352
R28(u_{14})	0</td																																	

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 117$$



State 28/31 | PHASE II step 2 | ENTER: u10 | LEAVE: s9 | Z=116.873

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u10 enters, s9 leaves.

Reduced cost of entering variable: -8.6875

Minimum ratio theta*: 0.0801697

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

Current solution: $x_1=3.41314$, $x_2=3.89005$, $x_3=2.23127$

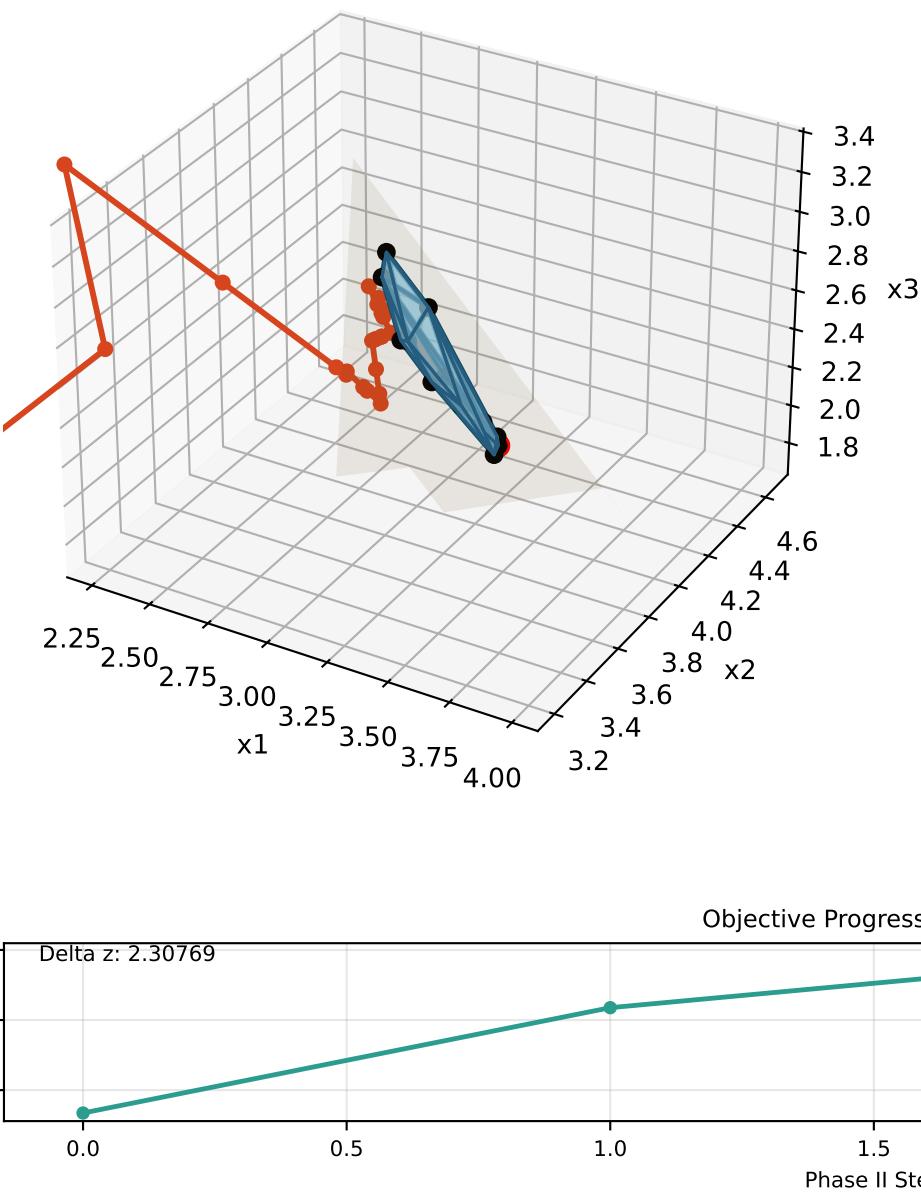
Objective z: 116.873

row	x_1	x_2	x_3	s_1	s_2	s_3	u_4	s_5	u_6	u_7	u_8	s_9	u_{10}	u_{11}	u_{12}	u_{13}	s_{14}	u_{15}	s_{16}	u_{17}	s_{18}	u_{19}	s_{20}	s_{21}	u_{22}	u_{23}	u_{24}	s_{25}	u_{26}	u_{27}	u_{28}	rhs	ratio		
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	-0.386364	0	0	-0.159091	0	0.204545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.58686	8.16193		
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0.181818	0	0	0.0454545	0	-0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.10995	inf		
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0.0681818	0	0	0.204545	0	0.0227273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.76873	inf		
R4(u6)	0	0	0	0	0	0	0	0	0	1	0	-0.136364	0	0	-0.409091	0	-0.0454545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.619051	1.73097		
R5(s5)	0	0	0	0	0	0	0	0	1	0	0	-0.75	0	0	0.75	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.68562	0.897442		
R6(u8)	0	0	0	0	0	0	0	0	0	0	1	0.818182	0	0	-0.0454545	0	0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.49985	inf		
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0.386364	0	0	0.159091	0	-0.204545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.41314	inf		
R8(u11)	0	0	0	0	0	0	0	0	0	0	0	1.06818	0	1	-0.295455	0	0.0227273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.719511	inf		
R9(u10)	0	0	0	0	0	0	0	0	0	0	0	0.363636	1	0	-0.909091	0	0.454545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0801697	0.0801697		
R10(u24)	0	0	0	0	0	0	0	0	0	0	0	1.72727	0	0	0.181818	0	-1.09091	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.18762	inf	
R11(u19)	0	0	0	0	0	0	0	0	0	0	0	0.204545	0	0	0.113636	0	0.0681818	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0.40086	inf		
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0.568182	0	0	-0.795455	0	-0.477273	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1.32616	inf		
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0.25	0	0	-0.25	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.986572	inf
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	-0.181818	0	0	-0.0454545	0	0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.89005	7.86027	
R15(u7)	0	0	0	0	0	0	0	0	0	0	1	0	0.590909	0	0	0.272727	0	-0.136364	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.94601	inf	
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	-1.72727	0	0	-0.181818	0	1.09091	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	2.48626	0.603594	
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0.159091	0	0	-0.522727	0	0.386364	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.22393	inf	
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	-0.318182	0	0	1.04545	0	0.227273	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	3.84643	4.47609	
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0.0681818	0	0	-0.295455	1	1.02273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.553102	inf	
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	-0.386364	0	0	-0.159091	0	-0.795455	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	2.36592	2.30692	
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	-0.227273	0	0	-0.181818	0	-0.409091	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	1.96349	3.22176	
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0.75	0	0	-0.25	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.89435	inf
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0.522727	0	0	0.0681818	0	0.840909	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.20067	inf	
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	-0.204545	0	0	-0.613636	0	0.931818	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.50383	2.75365	
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	-0.886364	0	0	0.340909	0	-0.295455	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.33143	1.44691	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	-0.0681818	0	0	-0.204545																				

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 117$$



State 29/31 | PHASE II step 3 | ENTER: s14 | LEAVE: u10 | Z=116.981

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: s14 enters, u10 leaves.

Reduced cost of entering variable: -0.613636

Minimum ratio theta*: 0.176373

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

Current solution: $x_1=3.44921$, $x_2=3.84195$, $x_3=2.23528$

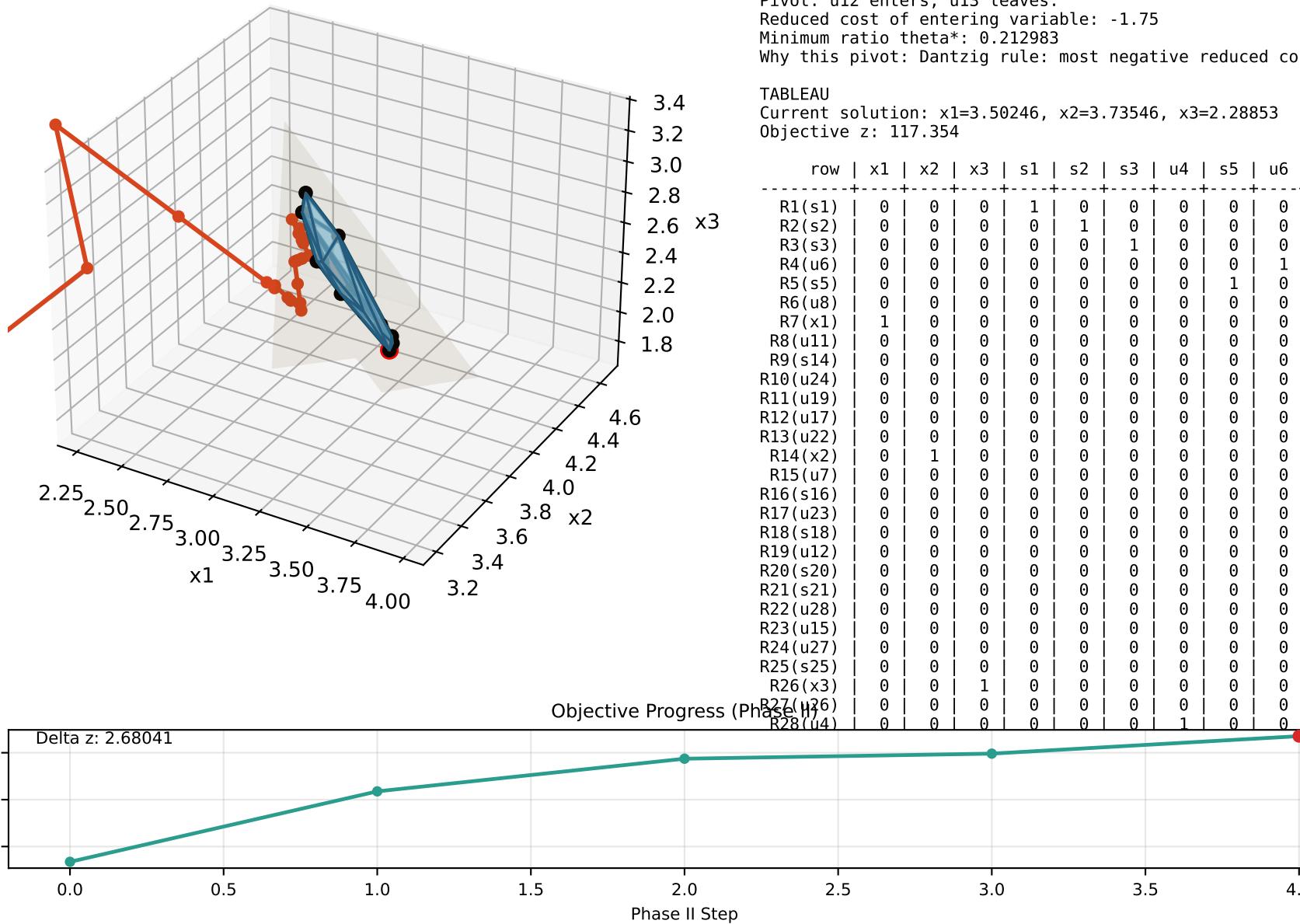
Objective z: 116.981

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio			
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	-0.55	-0.45	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.55079	41.9802					
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0.4	0.6	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.15805	inf					
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0.05	-0.05	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.76472	429.824					
R4(u6)	0	0	0	0	0	0	0	0	0	1	0	0	-0.1	0.1	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.627068	inf				
R5(s5)	0	0	0	0	0	0	0	0	1	0	0	-1.35	-1.65	0	2.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.55334	2.2475				
R6(u8)	0	0	0	0	0	0	0	0	0	0	1	0.6	-0.6	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.45175	5.49946				
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0.55	0.45	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.44921	inf				
R8(u11)	0	0	0	0	0	0	0	0	0	0	0	1.05	-0.05	1	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.715502	31.6585				
R9(s14)	0	0	0	0	0	0	0	0	0	0	0	0.8	2.2	0	-2	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176373	0.176373			
R10(u24)	0	0	0	0	0	0	0	0	0	0	0	2.6	2.4	0	-2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.38003	inf			
R11(u19)	0	0	0	0	0	0	0	0	0	0	0	0.15	-0.15	0	0.25	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0.388834	5.87927				
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0.95	1.05	0	-1.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.41034	inf				
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	-0.35	-1.65	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.854292	1.31543				
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	-0.4	-0.6	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.84195	14.2635			
R15(u7)	0	0	0	0	0	0	0	0	0	0	1	0	0.7	0.3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.97007	inf			
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	-2.6	-2.4	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.29386	2.27908			
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	-0.15	-0.85	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.15578	3.16781			
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	-0.5	-0.5	0	1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.80634	16.9243		
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	-0.75	-2.25	0	1.75	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.37272	0.540811		
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0.25	1.75	0	-1.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.50622	inf		
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0.1	0.9	0	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.03565	inf	
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0.55	-0.55	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.85026	7.5774		
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	-0.15	-1.85	0	1.75	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.205235	2.61701	
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	-0.95	-2.05	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.33949	1.61387	
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	-0.65	0.65	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.38354	inf	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	-0.05	0.05	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.23528	inf	
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	-0.55	-0.45	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.91841	4.66638
R28(u4)	0	0	0	0	0	0	0	0	0	1	0	0	0.6	-0.6	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.78406	6.71794

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15 \times 1 + 10 \times 2 + 12 \times 3 = 117$$



30/31 | PHASE II step 4 | ENTER: u12 | LEAVE: u13 | Z=117.3

ENTS

ing Mode | Rule: DANTZIG

: u12 enters, u13 leaves

ed cost of entering v

sum ratio theta*: 0.21

this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

AU

nt solution: $x_1=3.50246$, $x_2=3.73546$, $x_3=2.28853$

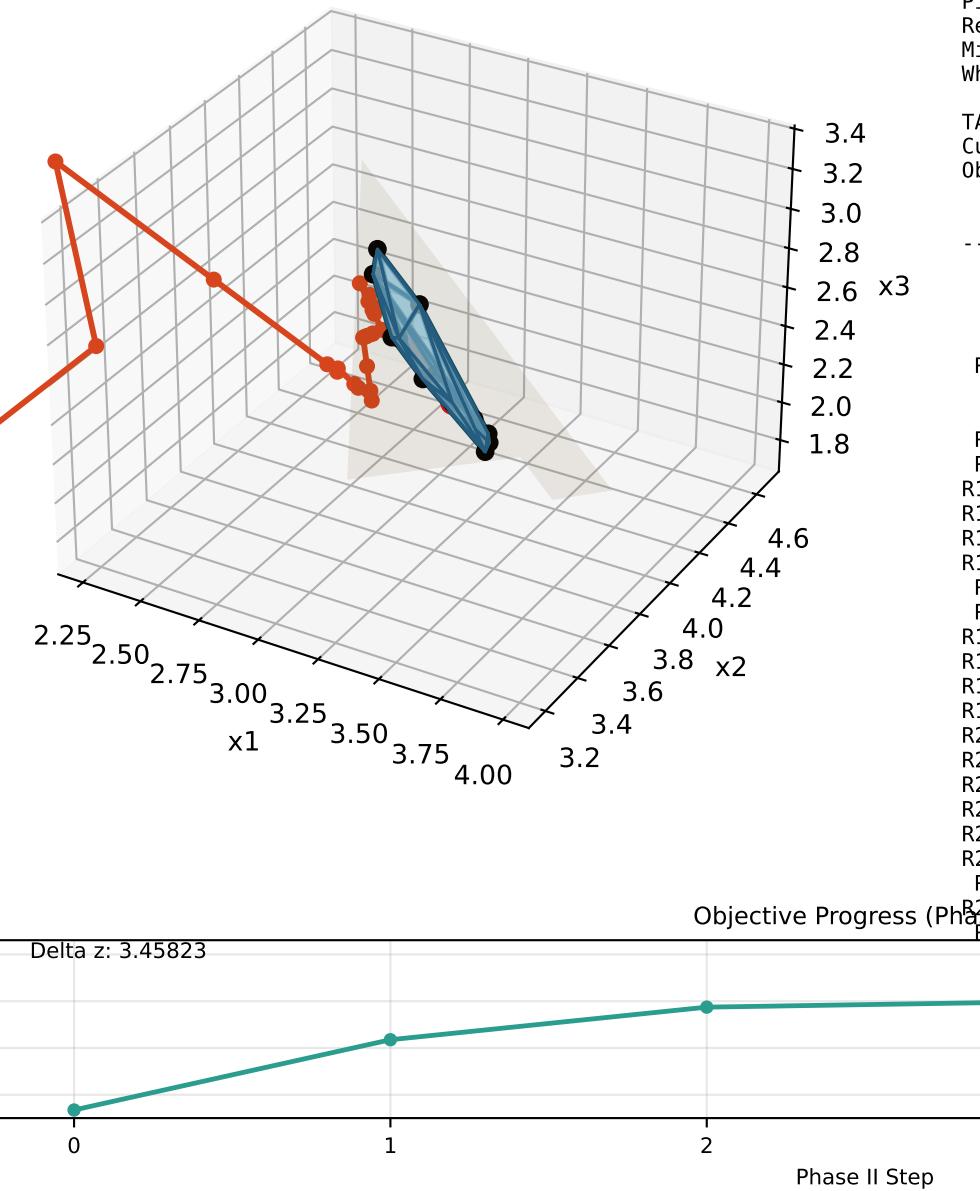
tive z: 117.354

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio		
s1)	0	0	0	1	0	0	0	0	0	0	0	-0.442857	-0.128571	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.49754	34.2032			
s2)	0	0	0	0	1	0	0	0	0	0	0	0.185714	-0.0428571	0	0	0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.26454	inf			
s3)	0	0	0	0	0	1	0	0	0	0	0	0.157143	0.271429	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.71147	39.0589			
u6)	0	0	0	0	0	0	0	0	1	0	0	-0.314286	-0.542857	0	0	0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.73356	inf			
s5)	0	0	0	0	0	0	0	1	0	0	0	-0.385714	1.24286	0	0	-1.28571	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.07413	0.690375			
u8)	0	0	0	0	0	0	0	0	0	0	1	0.814286	0.0428571	0	0	-0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.34526	2.9035			
x1)	1	0	0	0	0	0	0	0	0	0	0	0.442857	0.128571	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.50246	inf			
11)	0	0	0	0	0	0	0	0	0	0	0	0.942857	-0.371429	1	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.768748	inf			
14)	0	0	0	0	0	0	0	0	0	0	0	-0.0571429	-0.371429	0	0	1.14286	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.602339	inf			
24)	0	0	0	0	0	0	0	0	0	0	0	1.74286	-0.171429	0	0	1.14286	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.806	inf			
19)	0	0	0	0	0	0	0	0	0	0	0	0.257143	0.171429	0	0	-0.142857	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0.335588	1.55534			
17)	0	0	0	0	0	0	0	0	0	0	0	0.2	-1.2	0	0	1	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	1.78306	inf		
22)	0	0	0	0	0	0	0	0	0	0	0	0.185714	-0.0428571	0	0	-0.714286	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0.588064	0.683434			
x2)	0	1	0	0	0	0	0	0	0	0	0	-0.185714	0.0428571	0	0	-0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.73546	7.6839			
u7)	0	0	0	0	0	0	0	0	0	1	0	0.7	0.3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.97007	inf		
16)	0	0	0	0	0	0	0	0	0	0	0	-1.74286	0.171429	0	0	-1.14286	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	1.86789	1.14693		
23)	0	0	0	0	0	0	0	0	0	0	0	-0.0428571	-0.528571	0	0	-0.142857	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	1.10254	4.62313		
18)	0	0	0	0	0	0	0	0	0	0	0	0.142857	1.42857	0	0	-0.857143	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	3.48687	2.53756		
12)	0	0	0	0	0	0	0	0	0	0	0	-0.428571	-1.28571	0	1	0.571429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.212983	0.212983		
20)	0	0	0	0	0	0	0	0	0	0	0	-0.5	-0.5	0	0	1	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	2.87894	inf	
21)	0	0	0	0	0	0	0	0	0	0	0	-0.328571	-0.385714	0	0	0.571429	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	2.24863	inf	
28)	0	0	0	0	0	0	0	0	0	0	0	0.657143	-0.228571	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.79701	7.40103	
15)	0	0	0	0	0	0	0	0	0	0	0	0.6	0.4	0	0	-1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.67963	1.17277
27)	0	0	0	0	0	0	0	0	0	0	0	-0.414286	-0.442857	0	0	-0.714286	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.07326	1.07159		
25)	0	0	0	0	0	0	0	0	0	0	0	-0.757143	0.328571	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	3.43678	inf		
x3)	0	0	1	0	0	0	0	0	0	0	0	-0.157143	-0.271429	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.28853	inf		
26)	0	0	0	0	0	0	0	0	0	0	0	-0.657143	-0.771429	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0.971655	inf		
4)	0	0	0	0	0	0	0	1	0	0	0	0	1.02857	0.685714	0	0	-0.571429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.57108	1.78406	
												2.9	-0.9	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	117.354	-

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 118$$



State 31/31 | PHASE II step 5 | ENTER: u_{10} | LEAVE: s_5 | $Z=118.132$

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u_{10} enters, s_5 leaves.

Reduced cost of entering variable: -0.9

Minimum ratio theta*: 0.864244

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

Current solution: $x_1=3.39134$, $x_2=3.69842$, $x_3=2.52311$

Objective z: 118.132

row	x_1	x_2	x_3	s_1	s_2	s_3	s_4	s_5	u_6	u_7	u_8	s_9	u_{10}	u_{11}	u_{12}	u_{13}	s_{14}	u_{15}	s_{16}	u_{17}	s_{18}	u_{19}	s_{20}	s_{21}	u_{22}	u_{23}	u_{24}	s_{25}	u_{26}	u_{27}	u_{28}	rhs	ratio
R1(s_1)	0	0	0	1	0	0	0	0.103448	0	0	0	-0.482759	0	0	0	-0.275862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.60866	inf	
R2(s_2)	0	0	0	0	1	0	0	0.0344828	0	0	0	0.172414	0	0	0	0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.30158	inf	
R3(s_3)	0	0	0	0	0	1	0	-0.218391	0	0	0	0.241379	0	0	0	0.137931	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.47689	35.7791	
R4(u_6)	0	0	0	0	0	0	0	0.436782	1	0	0	-0.482759	0	0	0	-0.275862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.20272	inf	
R5(u_{10})	0	0	0	0	0	0	0	0.804598	0	0	0	-0.310345	1	0	0	-1.03448	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.864244	0.864244	
R6(u_8)	0	0	0	0	0	0	0	-0.0344828	0	0	1	0.827586	0	0	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.30822	31.3894	
R7(x_1)	1	0	0	0	0	0	0	-0.103448	0	0	0	0.482759	0	0	0	0.275862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.39134	27.2413	
R8(u_{11})	0	0	0	0	0	0	0	0.298851	0	0	0	0.827586	0	1	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.08975	inf	
R9(s_{14})	0	0	0	0	0	0	0	0.298851	0	0	0	-0.172414	0	0	0	0.758621	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.923344	inf	
R10(u_{24})	0	0	0	0	0	0	0	0.137931	0	0	0	1.68966	0	0	0	0.965517	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.95415	inf	
R11(u_{19})	0	0	0	0	0	0	0	-0.137931	0	0	0	0.310345	0	0	0	0.0344828	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.187432	1.9576	
R12(u_{17})	0	0	0	0	0	0	0	0.965517	0	0	0	-0.172414	0	0	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.82015	inf	
R13(u_{22})	0	0	0	0	0	0	0	0.0344828	0	0	0	0.172414	0	0	0	-0.758621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.625103	inf
R14(x_2)	0	1	0	0	0	0	0	-0.0344828	0	0	0	-0.172414	0	0	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.69842	87.1607
R15(u_7)	0	0	0	0	0	0	0	-0.241379	0	1	0	0.793103	0	0	0	0.310345	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.71079	9.9022
R16(s_{16})	0	0	0	0	0	0	0	-0.137931	0	0	0	-1.68966	0	0	0	-0.965517	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1.71974	10.896
R17(u_{23})	0	0	0	0	0	0	0	0.425287	0	0	0	-0.206897	0	0	0	-0.689655	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.55935	inf
R18(s_{18})	0	0	0	0	0	0	0	-1.14943	0	0	0	0.586207	0	0	0	0.62069	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25224	2.44081
R19(u_{12})	0	0	0	0	0	0	0	1.03448	0	0	0	-0.827586	0	0	0	-0.758621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.32415	inf
R20(s_{20})	0	0	0	0	0	0	0	0.402299	0	0	0	-0.655172	0	0	0	0.482759	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.31106	inf
R21(s_{21})	0	0	0	0	0	0	0	0.310345	0	0	0	-0.448276	0	0	0	0.172414	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.58198	inf
R22(u_{28})	0	0	0	0	0	0	0	0.183908	0	0	0	0.586207	0	0	0	-0.37931	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.99455	inf
R23(u_{15})	0	0	0	0	0	0	0	0.321839	0	0	0	0.724138	0	0	0	-0.586207	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1.33394	4.19909
R24(u_{27})	0	0	0	0	0	0	0	0.356322	0	0	0	-0.551724	0	0	0	-1.17241	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.45599	inf
R25(s_{25})	0	0	0	0	0																												