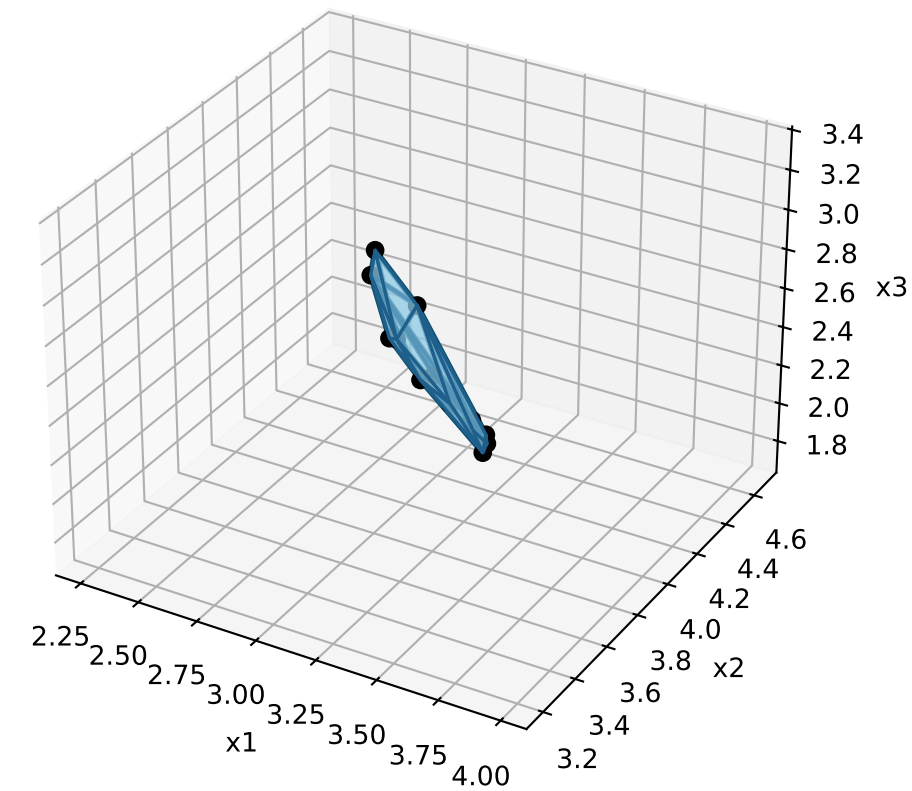


Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



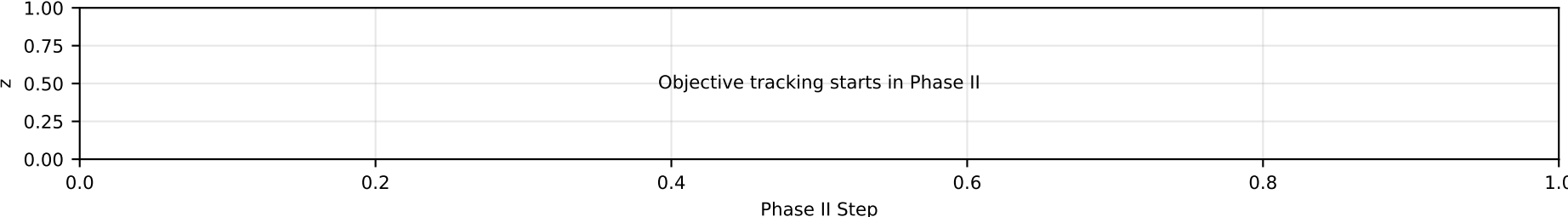
State 1/31 | PHASE I step 0

COMMENTS
Teaching Mode | PHASE I
Phase I initialized with artificial objective.

TABLEAU
Current solution: x1=0, x2=0, x3=0
Tableau objective: -532.633

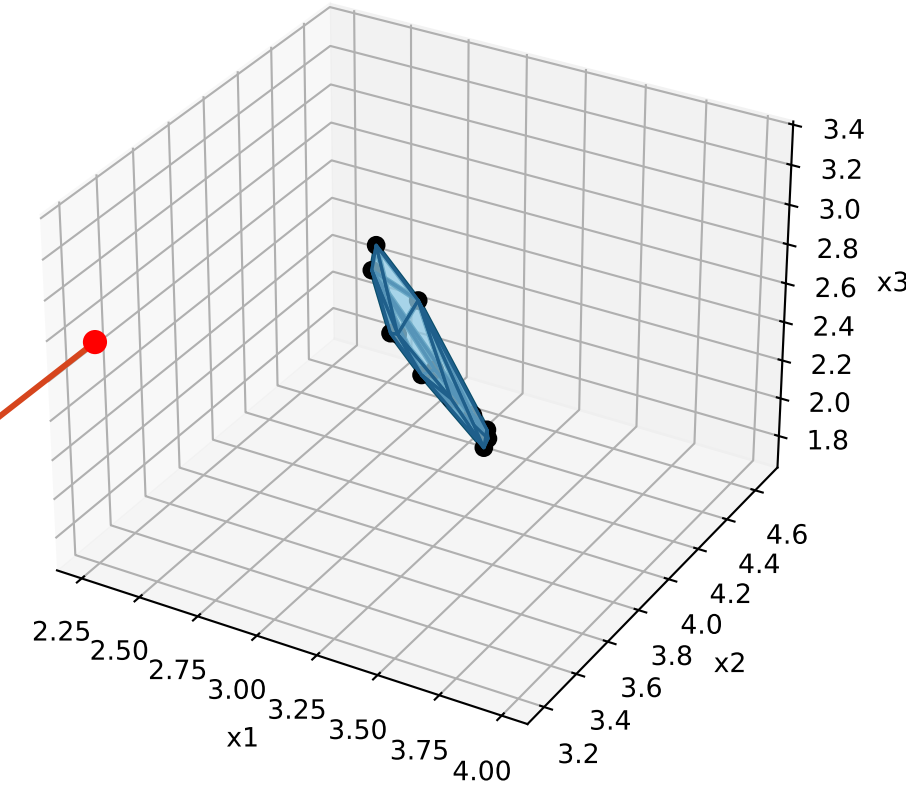
row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio	
R1(s1)	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf			
R2(s2)	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf			
R3(s3)	0	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf			
R4(a4)	4	4	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	27.3806	inf			
R5(s5)	3	0	6	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	25.3127	inf			
R6(a6)	0	0	2	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.84349	inf			
R7(a7)	2	1	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.77031	inf			
R8(a8)	5	5	3	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	41.7099	inf			
R9(s9)	5	4	3	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	39.3197	inf			
R10(a10)	5	6	7	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	55.9447	inf			
R11(a11)	6	5	5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	50.3659	inf			
R12(a12)	2	2	6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	27.994	inf			
R13(a13)	4	7	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	47.0236	inf			
R14(s14)	3	6	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	35.811	inf			
R15(a15)	5	7	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	46.5579	inf		
R16(s16)	5	0	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	26.2458	inf		
R17(a17)	3	1	6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	26.1909	inf		
R18(s18)	3	2	7	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	37.4848	inf		
R19(a19)	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	6.90233	inf			
R20(s20)	4	6	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	41.59	inf			
R21(s21)	2	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	20.4599	inf				
R22(a22)	4	6	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	42.7001	inf				
R23(a23)	3	4	4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	33.5008	inf			
R24(a24)	5	0	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	20.5719	inf			
R25(s25)	6	6	5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	58.3069	inf			
R26(a26)	0	1	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	9.62938	inf			
R27(a27)	3	6	4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	41.001	inf		
R28(a28)	5	5	4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	43.5467	inf
Rz	-57	-61	-55	0	0	0	1	0	0	1	0	1	0	1	0	0	1	0	1	0	1	0	1	0	0	1	0	1	0	0	1	0	0	1	0	0	1	0	1	0	1	0	1	0	1	0	0	-532.633			

Objective Progress (Phase II)



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

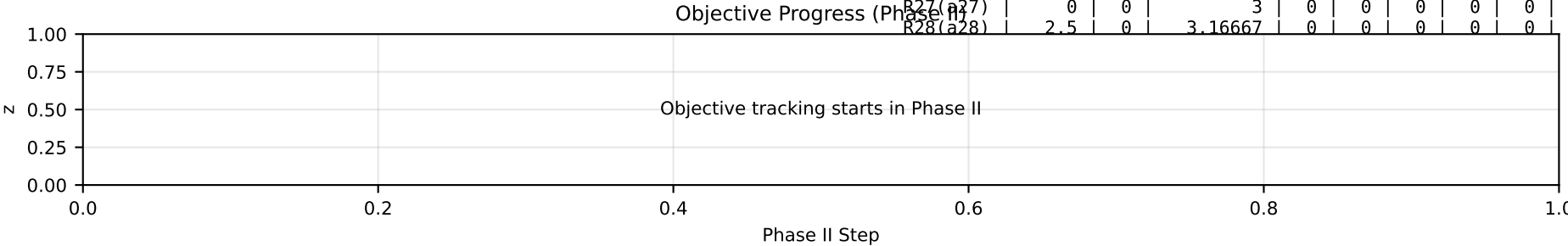


State 2/31 | PHASE I step 1 | ENTER: x2 | LEAVE: s14

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: x2 enters, s14 leaves.
Reduced cost of entering variable: -61
Minimum ratio theta*: 5.9685
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

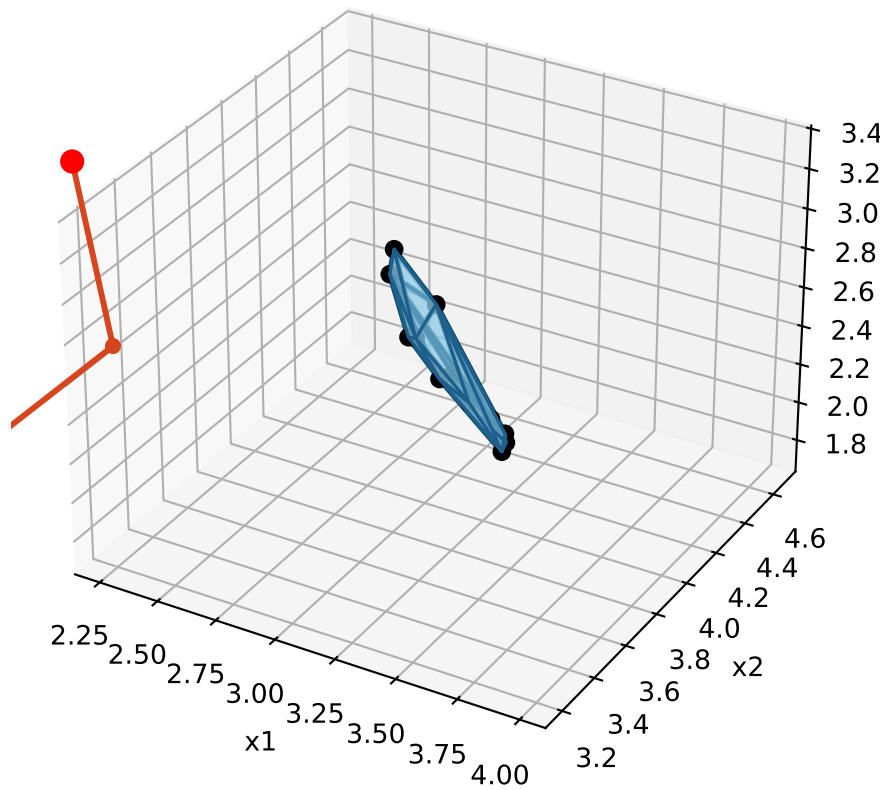
TABLEAU
Current solution: x1=0, x2=5.9685, x3=0
Tableau objective: -168.555

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio	
R1(s1)	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf			
R2(s2)	-0.5	0	-0.166667	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.166667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.0315	12		
R3(s3)	0	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf			
R4(a4)	2	0	-0.666667	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.50659	6.84514		
R5(s5)	3	0	6	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	25.3127	inf			
R6(a6)	0	0	2	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.84349	inf			
R7(a7)	1.5	0	-0.166667	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	-0.166667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.80181	7.77031		
R8(a8)	2.5	0	2.16667	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	-0.833333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	11.8674	8.34198		
R9(s9)	3	0	2.33333	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	-0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	15.4457	9.82992		
R10(a10)	2	0	6	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	20.1337	9.32412			
R11(a11)	3.5	0	4.16667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	-0.833333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	20.5234	10.0732		
R12(a12)	1	0	5.66667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	-0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	16.057	13.997		
R13(a13)	0.5	0	1.83333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	-1.16667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.24413	6.71766			
R14(x2)	0.5	1	0.166667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.166667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.9685	5.9685			
R15(a15)	1.5	0	0.833333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.16667	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.77843	6.65113		
R16(s16)	5	0	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	26.2458	inf			
R17(a17)	2.5	0	5.83333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.166667	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	20.2224	26.1909		
R18(s18)	2	0	6.66667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.333333	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	25.5478	18.7424		
R19(a19)	0.5	0	-0.166667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.166667	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.933829	6.90233			
R20(s20)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	5.77906	6.93167			
R21(s21)	0.5	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	2.55442	6.81997				
R22(a22)	1	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	6.88911	7.11668				
R23(a23)	1	0	3.33333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	9.62678	8.37519			
R24(a24)	5	0	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	20.5719	inf			
R25(s25)	3	0	4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	22.4959	9.71782			
R26(a26)	-0.5	0	2.83333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.166667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	3.66088	9.62938		
R27(a27)	0	0	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	5.18998	6.83349		
R28(a28)	2.5	0	3.16667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.833333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	13.7042	8.70933	
										0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	10.1667	1	0	0	0	1	0	0	1	0	0	1	0	0	1	0	1	0	1	0	0	1	0	1	0	-168.555	



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 3/31 | PHASE I step 2 | ENTER: x3 | LEAVE: a26

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: x3 enters, a26 leaves.

Reduced cost of entering variable: -44.8333

Minimum ratio theta*: 1.29208

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

Current solution: x1=0, x2=5.75315, x3=1.29208

Tableau objective: -110.627

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio			
R1(s1)	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12	inf	
R2(s2)	-0.529412	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.24685	inf	
R3(s3)	0.176471	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	10.7079	12
R4(a4)	1.88235	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.705882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.36797	inf	
R5(s5)	4.05882	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.352941	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	17.5602	4.21878	
R6(a6)	0.352941	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.117647	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25934	1.92175	
R7(a7)	1.47059	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	-0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.01716	inf	
R8(a8)	2.88235	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	-0.705882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.06791	5.47726	
R9(s9)	3.41176	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	-0.529412	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12.4309	6.61959	
R10(a10)	3.05882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	-0.647059	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12.3813	3.35562	
R11(a11)	4.23529	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	-0.588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	15.1398	4.92562	
R12(a12)	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.73524	2.83359			
R13(a13)	0.823529	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	-1.05882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.73524	2.83359	
R14(x2)	0.529412	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.75315	35.811		
R15(a15)	1.64706	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.11765	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.7017	5.73411		
R16(s16)	5.52941	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	22.3695	8.74858		
R17(a17)	3.52941	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12.6853	3.4667	
R18(s18)	3.17647	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0588235	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	16.934	3.83218	
R19(a19)	0.470588	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.176471	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14918	inf		
R20(s20)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.77906	inf			
R21(s21)	0.411765	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.529412	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	3.20046	inf		
R22(a22)	1.35294	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.882353	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	4.30495	3.44455		
R23(a23)	1.58824	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.470588	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	5.31986	2.88803		
R24(a24)	5.52941	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176471	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	16.6956	6.85729		
R25(s25)	3.70588	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.764706	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	17.3276	5.62398		
R26(x3)	-0.176471	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0588235	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.29208	1.29208		
R27(a27)	0.529412	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.823529	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.31375	1.72999	
R28(a28)	3.05882	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.647059	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.61261	4.32764	
										1	0	1	0	1	0	0	1	0	1	0	1	0	1	0	7.52941	1	0	0	1	0	0	1	0	0	0	0	1	0	0	1	0	1	0	0	0	-14.8235	15.8235	1	0	1	0	-110.627	-

Objective Progress (Phase I)

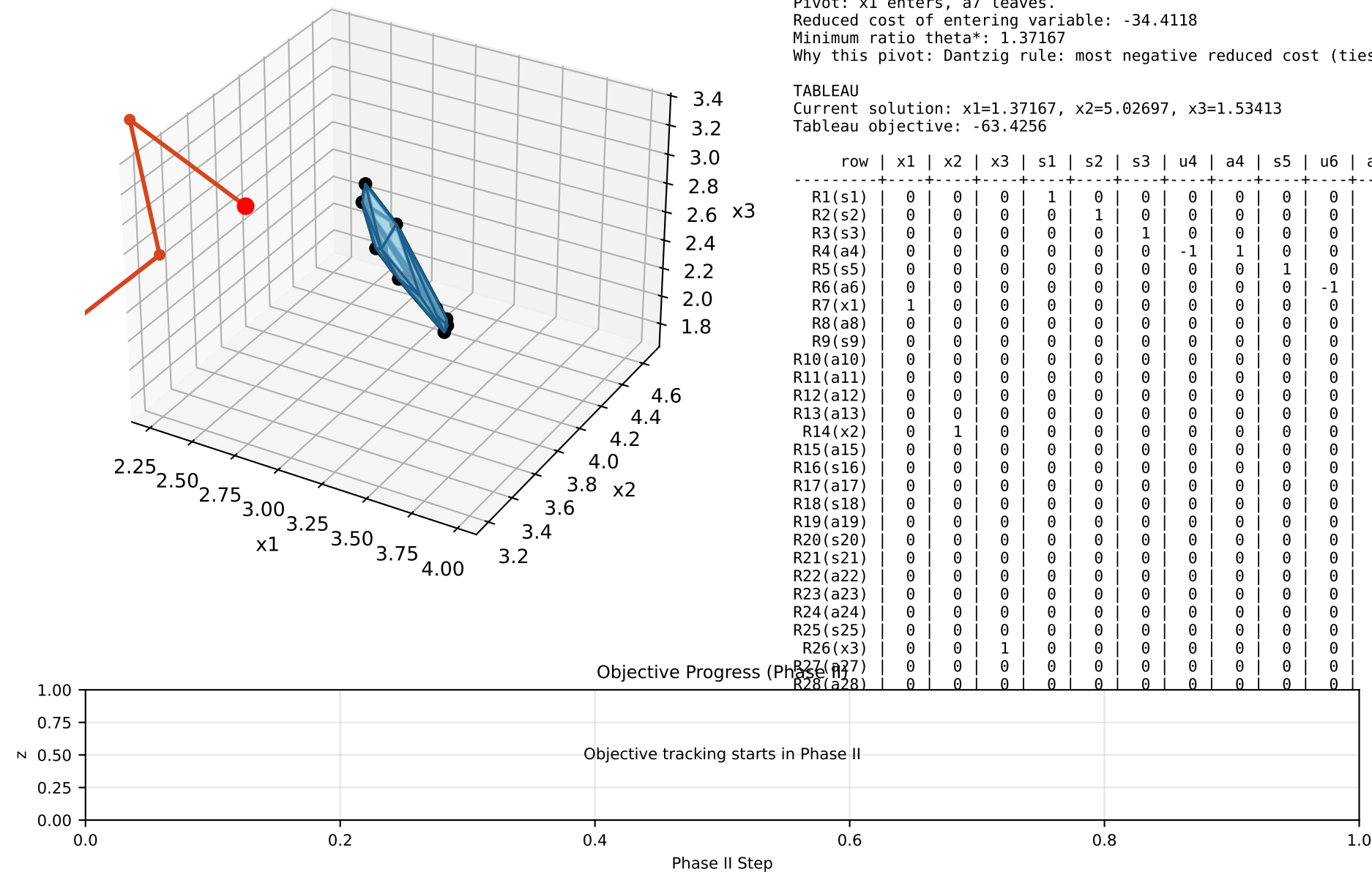
Objective tracking starts in Phase II

Phase II Step

State 4/31 | PHASE I step 3 | ENTER: x1 | LEAVE: a7

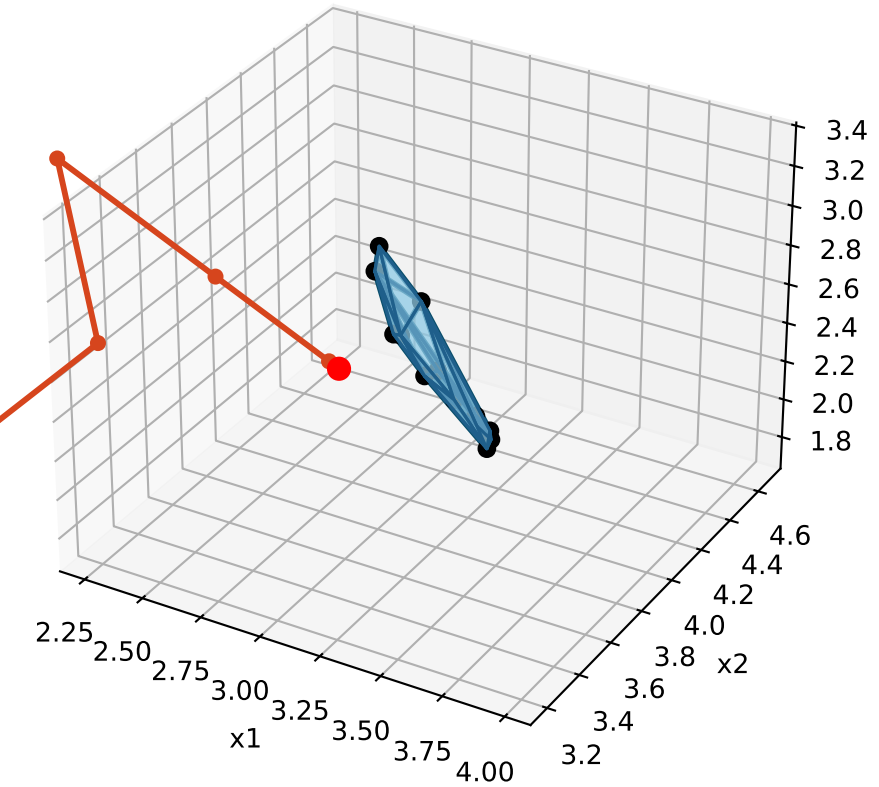
COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: x1 enters, a7 leaves.
Reduced cost of entering variable: -34.4118
Minimum ratio theta*: 1.37167
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU
Current solution: $x_1=1.37167$, $x_2=5.02697$, $x_3=1.53413$
Tableau objective: -63.4256



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

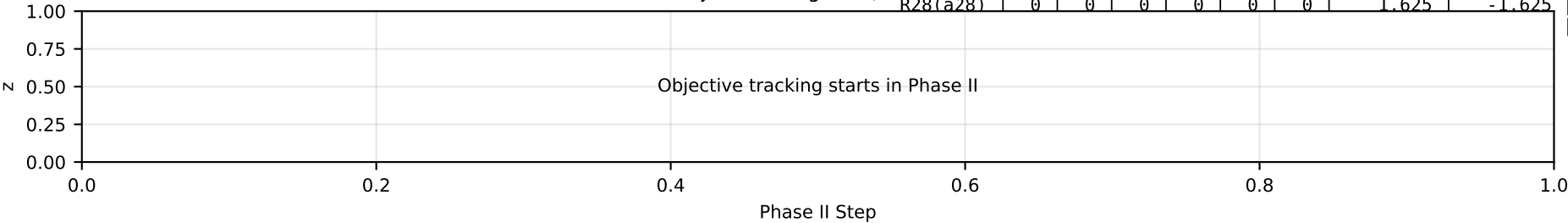


State 6/31 | PHASE I step 5 | ENTER: u15 | LEAVE: a4

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u15 enters, a4 leaves.
Reduced cost of entering variable: -19
Minimum ratio theta*: 0.120281
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

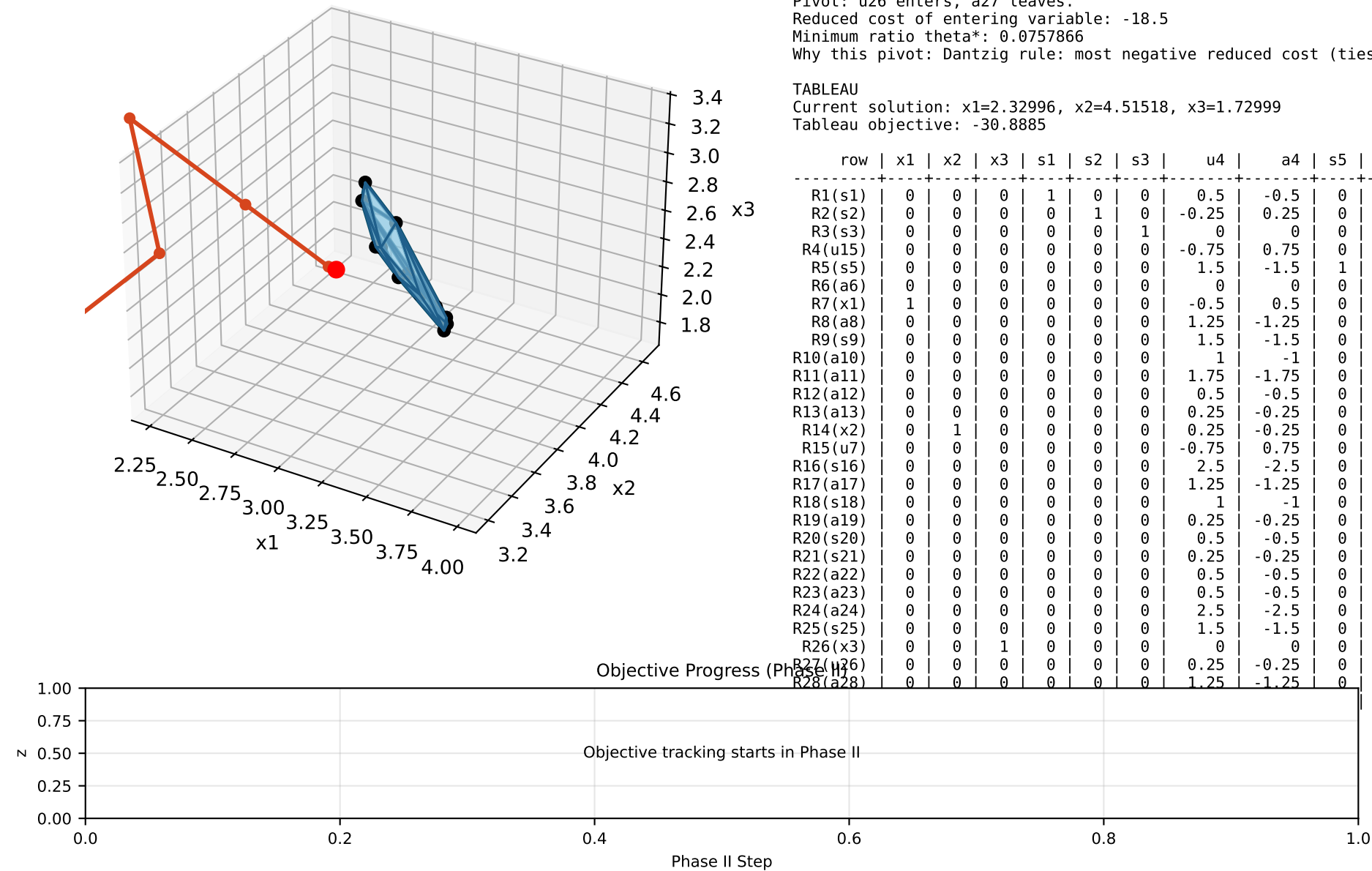
TABLEAU
Current solution: x1=2.32049, x2=4.52466, x3=1.70157
Tableau objective: -32.2906

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio									
R1(s1)	0	0	0	1	0	0	0.53125	-0.53125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	9.67951	16.063								
R2(s2)	0	0	0	0	1	0	-0.28125	0.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	7.47534	inf									
R3(s3)	0	0	0	0	0	1	0.09375	-0.09375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	10.2984	96.2389									
R4(u15)	0	0	0	0	0	0	-0.875	0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.5	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.120281	0.120281									
R5(s5)	0	0	0	0	0	0	2.15625	-2.15625	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.625	-2.625	0	0	0	0	8.14176	3.42418								
R6(a6)	0	0	0	0	0	0	0.1875	-0.1875	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.440344	2.17522									
R7(x1)	1	0	0	0	0	0	-0.53125	0.53125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	2.32049	inf							
R8(a8)	0	0	0	0	0	0	1.53125	-1.53125	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.37945	1.47997							
R9(s9)	0	0	0	0	0	0	1.8125	-1.8125	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	-1.25	0	0	0	0	4.51391	2.29941							
R10(a10)	0	0	0	0	0	0	1.625	-1.625	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.5	-2.5	0	0	0	0	5.28331	2.96514							
R11(a11)	0	0	0	0	0	0	2.25	-2.25	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	0	0	5.31183	2.18599							
R12(a12)	0	0	0	0	0	0	1.0625	-1.0625	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25	-2.25	0	0	0	0	4.09427	3.49203						
R13(a13)	0	0	0	0	0	0	0.4375	-0.4375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0.964335	2.04895							
R14(x2)	0	1	0	0	0	0	0.28125	-0.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.52466	14.197							
R15(u7)	0	0	0	0	0	0	-0.78125	0.78125	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.39532	inf							
R16(s16)	0	0	0	0	0	0	2.9375	-2.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.5386	2.96157						
R17(a17)	0	0	0	0	0	0	1.875	-1.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.5	-2.5	0	0	0	0	4.49536	2.21812							
R18(s18)	0	0	0	0	0	0	1.6875	-1.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.75	-2.75	0	0	0	0	9.56304	5.0789						
R19(a19)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	0.320417								
R20(s20)	0	0	0	0	0	0	0.53125	-0.53125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	3.45857	5.81675								
R21(s21)	0	0	0	0	0	0	0.21875	-0.21875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	2.24497	9.10015							
R22(a22)	0	0	0	0	0	0	0.71875	-0.71875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.375	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0.875	-0.875	0	0	0	0	1.16547	1.53912						
R23(a23)	0	0	0	0	0	0	0.84375	-0.84375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	1.375	-1.375	0	0	0	0	1.63438	1.8152				
R24(a24)	0	0	0	0	0	0	2.9375	-2.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	1.75	-1.75	0	0	0	0	3.86471	1.27147		
R25(s25)	0	0	0	0	0	0	1.96875	-1.96875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.875	-1.875	0	0	0	0	8.72816	3.99947
R26(x3)	0	0	1	0	0	0	-0.09375	0.09375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.70157	inf							
R27(a27)	0	0	0	0	0	0	0.28125	-0.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.125	-1.125	-1	1	0	0	0.08526	0.385534
R28(a28)	0	0	0	0	0	0	1.625	-1.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.51465	1.47432						
									0	1	0	0	1	1	0	0	0	1	0	1	0	1	0	0	-5.5	0	1	0	1	0	0	1	0	0	0	1	0	1	0	1	0	0	-18.5	19.5	1	0	1	0	0	0	-32.2906								



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 7/31 | PHASE I step 6 | ENTER: u26 | LEAVE: a27

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u26 enters, a27 leaves.

Reduced cost of entering variable: -18.5

Minimum ratio theta*: 0.0757866

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

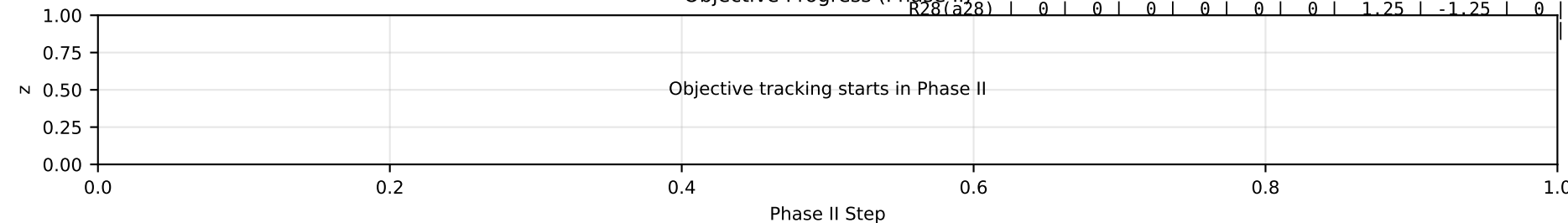
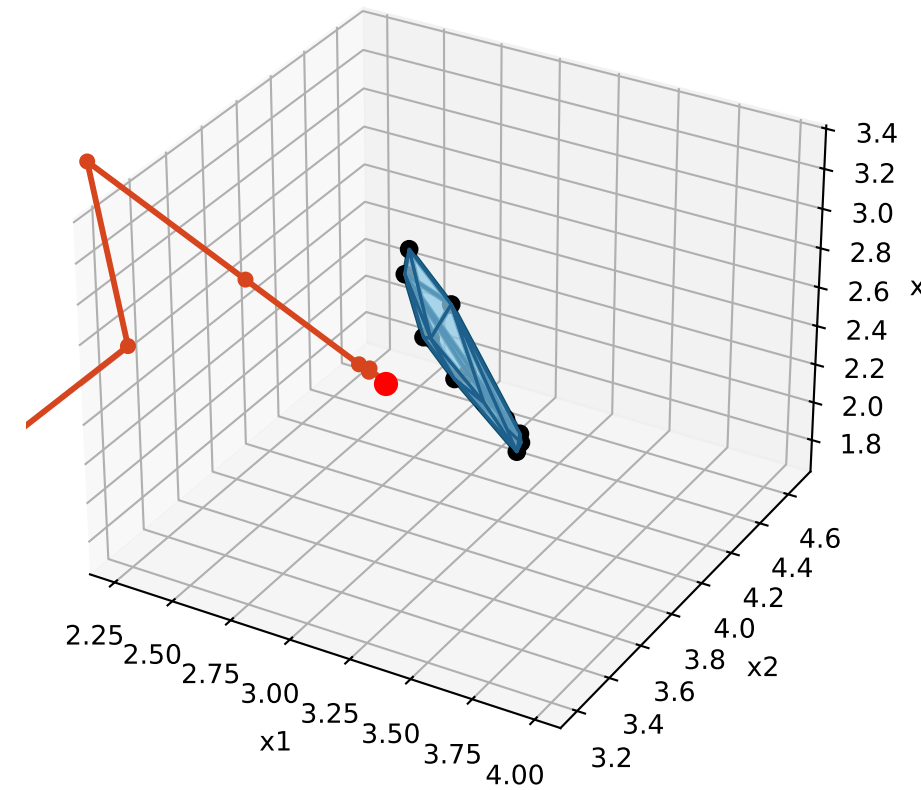
Current solution: x1=2.32996, x2=4.51518, x3=1.72999

Tableau objective: -30.8885

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio																	
R1(s1)	0	0	0	1	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.111111	-0.111111	0	0	9.67004	77.4361															
R2(s2)	0	0	0	0	1	0	-0.25	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.111111	0.111111	0	0	7.48482	inf													
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.333333	-0.333333	0	0	10.27	27.4625											
R4(u15)	0	0	0	0	0	0	-0.75	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.222222	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.444444	0.444444	0	0	0.158174	inf										
R5(s5)	0	0	0	0	0	0	1.5	-1.5	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.33333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.33333	-2.33333	0	0	7.94282	3.10162										
R6(a6)	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.666667	-0.666667	0	0	0.383504	0.587126									
R7(x1)	1	0	0	0	0	0	-0.5	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.111111	0.111111	0	0	2.32996	inf									
R8(a8)	0	0	0	0	0	0	1.25	-1.25	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	2.29419	2.11506									
R9(s9)	0	0	0	0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	1.44444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.11111	-1.11111	0	0	4.41917	3.61113					
R10(a10)	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	1.88889	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.22222	-2.22222	0	0	5.09385	2.11333								
R11(a11)	0	0	0	0	0	0	1.75	-1.75	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	2.11111	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.77778	-1.77778	0	0	5.16026	2.65592					
R12(a12)	0	0	0	0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	3.92375	1.81968									
R13(a13)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	-0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.666667	-0.666667	0	0	0.907495	1.28578									
R14(x2)	0	1	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.111111	-0.111111	0	0	4.51518	36.1973					
R15(u7)	0	0	0	0	0	0	-0.75	0.75	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	-0.444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.111111	0.111111	0	0	1.4048	inf							
R16(s16)	0	0	0	0	0	0	2.5	-2.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.22222	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.55556	-1.55556	0	0	9.40597	5.45063					
R17(a17)	0	0	0	0	0	0	1.25	-1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.88889	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.22222	-2.22222	0	0	4.3059	1.79815				
R18(s18)	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.77778	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.44444	-2.44444	0	0	9.35463	3.47747				
R19(a19)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf								
R20(s20)	0	0	0	0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.555556	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.111111	-0.111111	0	0	3.4491	27.6686				
R21(s21)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.444444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.111111	0.111111	0	0	2.25444	inf				
R22(a22)	0	0	0	0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.111111	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.777778	-0.777778	0	0	1.09916	1.33197			
R23(a23)	0	0	0	0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.888889	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.22222	-1.22222	0	0	1.53018	1.18864				
R24(a24)	0	0	0	0	0	0	2.5	-2.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.22222	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.55556	-1.55556	0	0	3.73209	2.20841			
R25(s25)	0	0	0	0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.66667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.66667	-1.66667	0	0	8.58606	4.65502				
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.333333	0.333333	0	0	1.72999	inf			
R27(u27)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.555556	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.888889	0.888889	0	0	0.0757866	0.0757866
R28(a28)	0	0																																																																	

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 8/31 | PHASE I step 7 | ENTER: s14 | LEAVE: a6

COMMENTS:

Teaching Mode | Rule: DANTZIC

Pivot: s14 enters, a6 leaves

Reduced cost of entering variable: -15.7778

Minimum ratio theta*: 0.57525

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

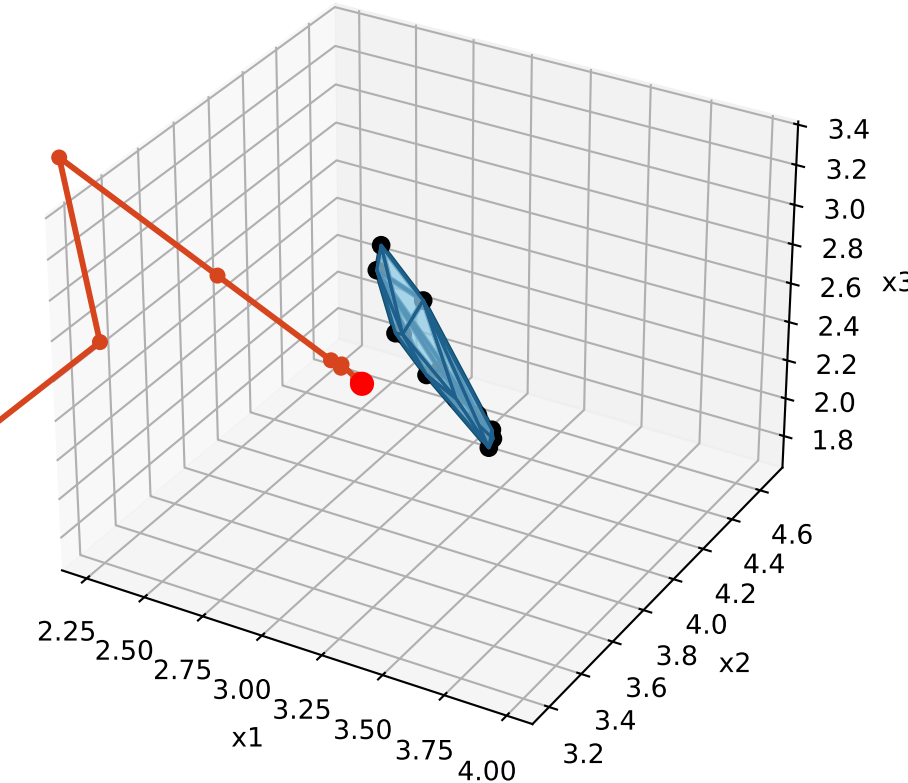
Current solution: $x_1=2.58563$, $x_2=4.25952$, $x_3=1.92175$

Tableau objective: -21.8125

	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																
R1(s1)	0	0	0	1	0	0	0.5	-0.5	0	0.666667	-0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.333333	0.333333	0	0	9.41437	21.7576																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																
R2(s2)	0	0	0	0	1	0	-0.25	0.25	0	-0.666667	0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.333333	-0.333333	0	0	7.74048	inf																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																
R3(s3)	0	0	0	0	0	1	0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	10.0783	30.81																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																															
R4(u15)	0	0	0	0	0	0	-0.75	0.75	0	0.333333	-0.333333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.666667	0.666667	0	0	0.0303394	0.711784																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																											
R5(s5)	0	0	0	0	0	0	1.5	-1.5	1	5	-5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	6.02529	2.38284																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																										
R6(s14)	0	0	0	0	0	0	0	0	0	-1.5	1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0.575257	0.575257																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																			
R7(x1)	1	0	0	0	0	0	-0.5	0.5	0	-0.666667	0.666667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.333333	-0.333333	0	0	2.58563	inf																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																				
R8(a8)	0	0	0	0	0	0	1.25	-1.25	0	1.5	-1.5	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.71893	2.29419																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																																								
R9(s9)	0	0	0	0	0	0	1.5	-1.5	0	2.16667	-2.16667	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

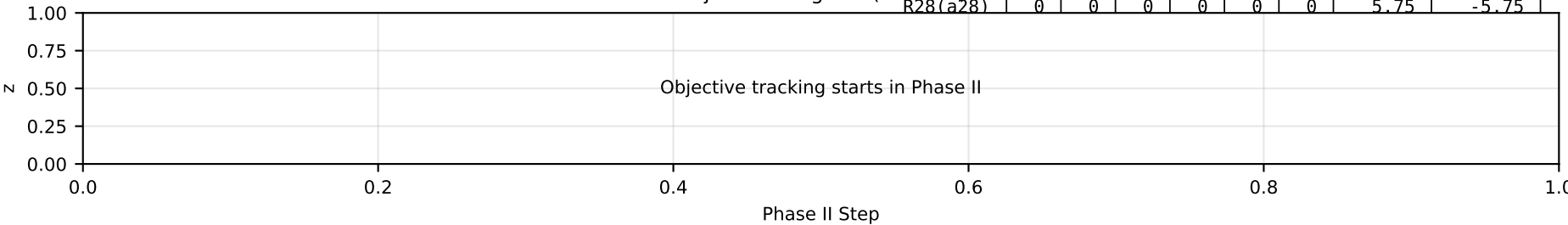


State 9/31 | PHASE I step 8 | ENTER: u6 | LEAVE: u15

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u6 enters, u15 leaves.
Reduced cost of entering variable: -22.6667
Minimum ratio theta*: 0.0910182
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

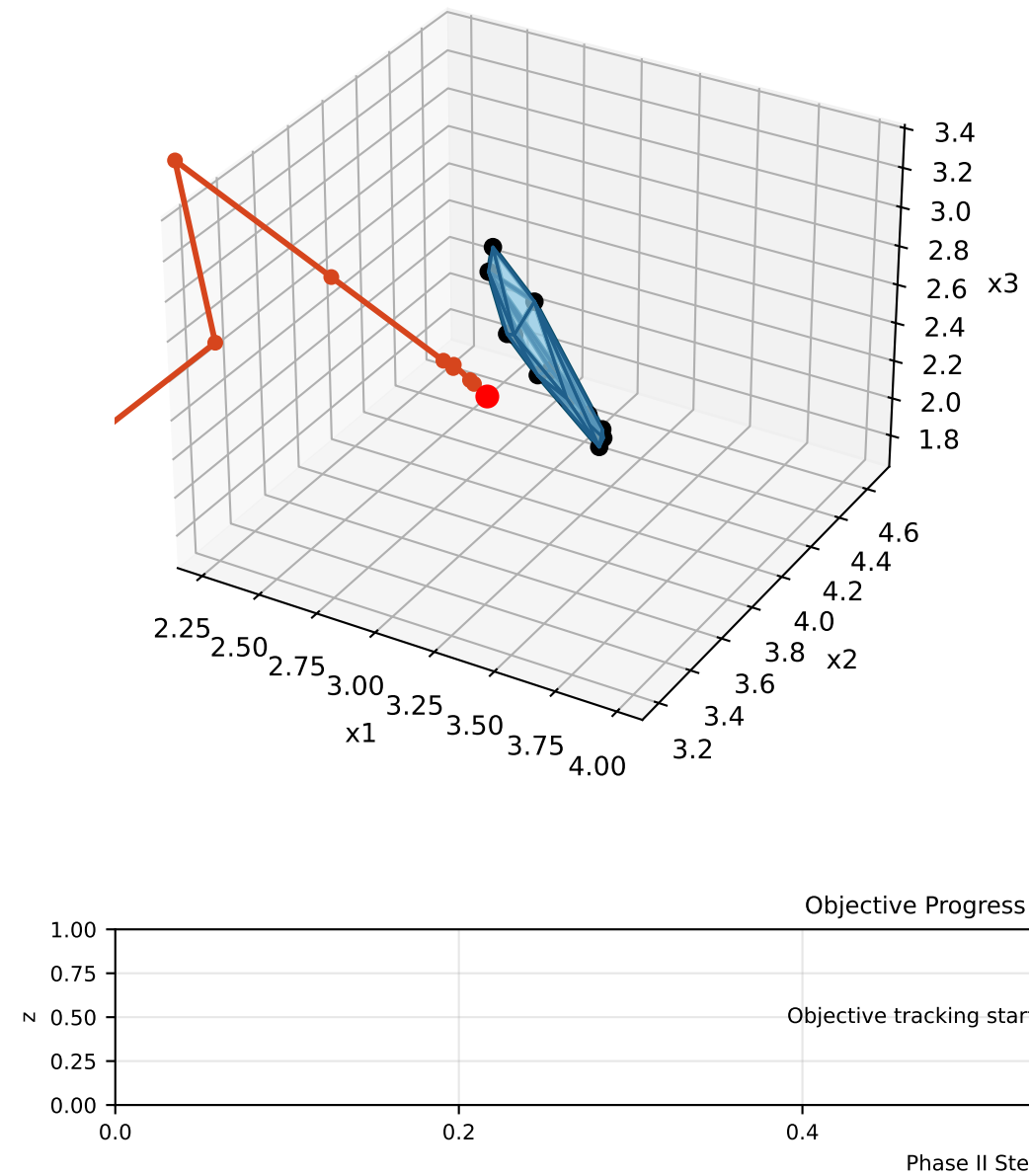
TABLEAU
Current solution: x1=2.64631, x2=4.19884, x3=1.96725
Tableau objective: -19.7492

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio		
R1(s1)	0	0	0	1	0	0	2	-2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-2	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	9.35369	14.1216		
R2(s2)	0	0	0	0	1	0	-1.75	1.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	7.80116	inf		
R3(s3)	0	0	0	0	0	1	1.125	-1.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.5	1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	10.0327	20.1565		
R4(u6)	0	0	0	0	0	0	-2.25	2.25	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3	-3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-2	2	0	0	0.0910182	0.0910182		
R5(s5)	0	0	0	0	0	0	12.75	-12.75	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-15	15	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9	-9	0	0	5.5702	1.20506		
R6(s14)	0	0	0	0	0	0	-3.375	3.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	4.5	-4.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-2	2	0	0	0.711784	inf	
R7(x1)	1	0	0	0	0	0	-2	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	2.64631	inf		
R8(a8)	0	0	0	0	0	0	4.625	-4.625	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	-4.5	4.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3	-3	0	0	1.5824	1.14595		
R9(s9)	0	0	0	0	0	0	6.375	-6.375	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	-6.5	6.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4	-4	0	0	3.39104	1.65611		
R10(a10)	0	0	0	0	0	0	7.375	-7.375	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	-8.5	8.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6	-6	0	0	3.74937	1.41432		
R11(a11)	0	0	0	0	0	0	8.875	-8.875	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	-9.5	9.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6	-6	0	0	3.65761	1.24605			
R12(a12)	0	0	0	0	0	0	7.25	-7.25	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	-9	9	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6	-6	0	0	2.50018	0.924412			
R13(a13)	0	0	0	0	0	0	-0.875	0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14476	inf		
R14(x2)	0	1	0	0	0	0	1.75	-1.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-2	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	4.19884	6.38927		
R15(u7)	0	0	0	0	0	0	-2.25	2.25	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	1.72115	inf		
R16(s16)	0	0	0	0	0	0	13.375	-13.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-14.5	14.5	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8	-8	0	0	7.11245	1.56256	
R17(a17)	0	0	0	0	0	0	11	-11	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-13	13	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	8	-8	0	0	2.24963	0.610164		
R18(s18)	0	0	0	0	0	0	10.375	-10.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-12.5	12.5	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	8	-8	0	0	7.37745	1.86161		
R19(a19)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf			
R20(s20)	0	0	0	0	0	0	-1.375	1.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.5	-2.5	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	-1	1	0	0	3.84453	inf		
R21(s21)	0	0	0	0	0	0	-1.25	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	2.57079	inf		
R22(a22)	0	0	0	0	0	0	0.875	-0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.5	0.5	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	1	-1	0	0	1.02007	6.21145		
R23(a23)	0	0	0	0	0	0	3.5	-3.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-4	4	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	3	-3	0	0	0.897479	0.764127			
R24(a24)	0	0	0	0	0	0	13.375	-13.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-14.5	14.5	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	-1	1	0	0	1.43856	0.388652		
R25(s25)	0	0	0	0	0	0	7.125	-7.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-7.5	7.5	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	5	-5	0	0	7.39976	3.05092	
R26(x3)	0	0	1	0	0	0	-1.125	1.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	1.96725	inf		
R27(u26)	0	0	0	0	0	0	-1.625	1.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.5	-2.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	-2	2	0	0	0.471222	inf	
R28(a28)	0	0	0	0	0	0	5.75	-5.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-6	6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4	-4	-1	1	1.45192	0.816979		
									0	0	1	0	1	1	0	0	0	1	0	1	0	1	0	1	0	0	68	-67	0	1	0	0	0	1	0	0	0	1	0	1	0	1	0	0	0	1	-45	46	1	0	-19.7492	



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 10/31 | PHASE I step 9 | ENTER: a15 | LEAVE: a24

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: a15 enters, a24 leaves.

Reduced cost of entering variable: -67

Minimum ratio theta*: 0.0992111

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

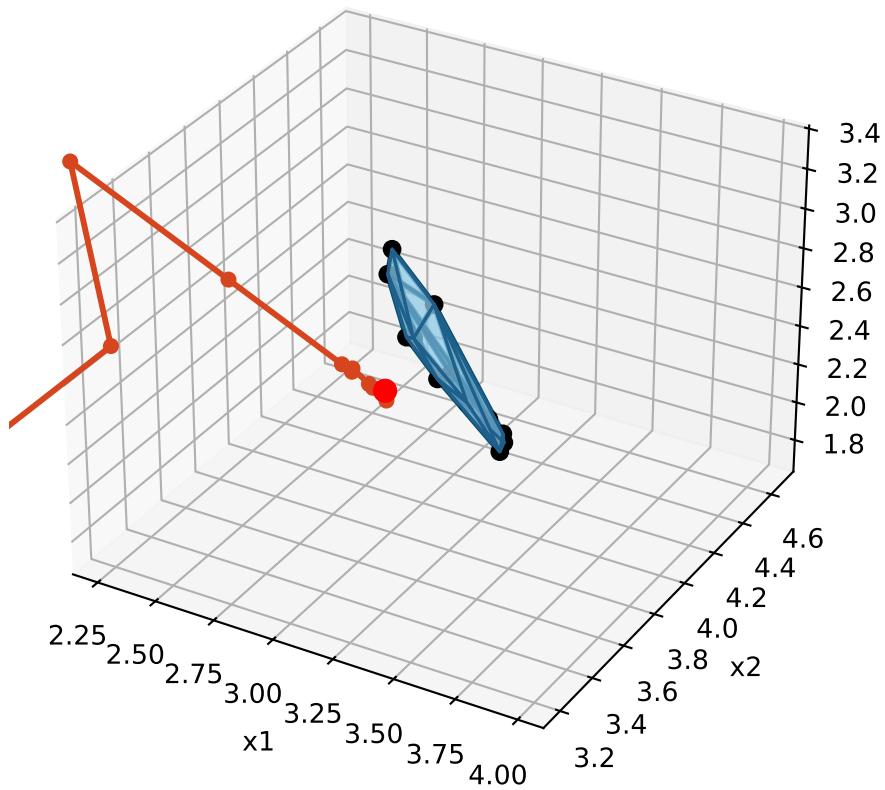
Current solution: $x_1=2.84473$, $x_2=4.00041$, $x_3=2.11607$

Tableau objective: -13.102

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio		
R1(s1)	0	0	0	1	0	0	0.155172	-0.155172	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.137931	-0.137931	0	0	0	-0.103448	0.103448	0	0	9.15527	4.67685			
R2(s2)	0	0	0	0	1	0	0.0948276	-0.0948276	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.99959	inf				
R3(s3)	0	0	0	0	0	1	-0.258621	0.258621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.88393	6.6885				
R4(u6)	0	0	0	0	0	0	0.517241	-0.517241	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.388652	inf				
R5(s5)	0	0	0	0	0	0	-1.08621	1.08621	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.08204	0.371347				
R6(s14)	0	0	0	0	0	0	0.775862	-0.775862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.15823	inf				
R7(x1)	1	0	0	0	0	0	-0.155172	0.155172	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.84473	inf				
R8(a8)	0	0	0	0	0	0	0.474138	-0.474138	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.13595	0.351645				
R9(s9)	0	0	0	0	0	0	0.37931	-0.37931	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.74617	0.521699				
R10(a10)	0	0	0	0	0	0	-0.465517	0.465517	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.90607	0.441102				
R11(a11)	0	0	0	0	0	0	0.112069	-0.112069	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.7151	0.385011				
R12(a12)	0	0	0	0	0	0	-1.05172	1.05172	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.60728	0.277798				
R13(a13)	0	0	0	0	0	0	0.508621	-0.508621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.29357	inf				
R14(x2)	0	1	0	0	0	0	-0.0948276	0.0948276	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.00041	2.09942					
R15(u7)	0	0	0	0	0	0	-0.405172	0.405172	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.91957	inf				
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	0.490514			
R17(a17)	0	0	0	0	0	0	-0.991379	0.991379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.827586	-0.827586	0	0	0.959889	0.173049
R18(s18)	0	0	0	0	0	0	-1.15517	1.15517	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.13732	0.590196				
R19(a19)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf				
R20(s20)	0	0	0	0	0	0	0.931034	-0.931034	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.09256	inf				
R21(s21)	0	0	0	0	0	0	0.594828	-0.594828	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.76921	inf				
R22(a22)	0	0	0	0	0	0	0.413793	-0.413793	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.970466	2.04014				
R23(a23)	0	0	0	0	0	0	-0.189655	0.189655	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.500634	0.22437				
R24(a15)	0	0	0	0	0	0	0.922414	-0.922414	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0992111	0.0992111				
R25(s25)	0	0	0	0	0	0	0.206897	-0.206897	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.65568	0.986634				
R26(x3)	0	0	1	0	0	0	0.258621	-0.258621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.11607	inf				
R27(u26)	0	0	0	0	0	0	0.681034	-0.681034	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.71925	inf				
R28(a28)	0	0	0	0	0	0	0.215517	-0.215517	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.856656	0.241987				
									0	0	1	0	1	1	0	0	1	0	1	0	1	0	1	0	0	1	0	0	1	0	0	0	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	-13.102		

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

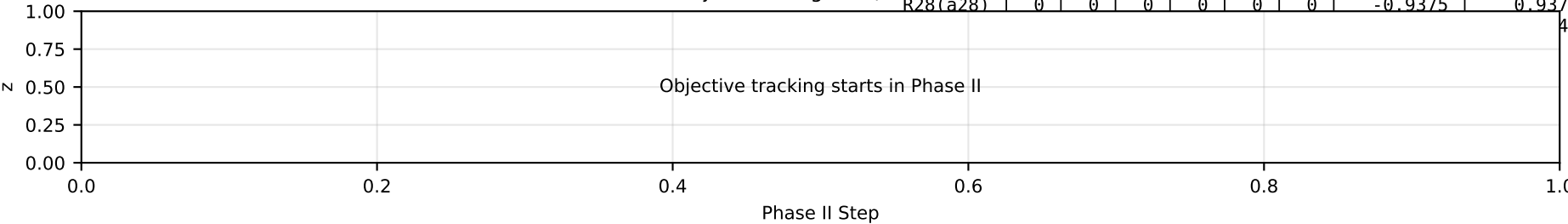


State 11/31 | PHASE I step 10 | ENTER: u27 | LEAVE: a15

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u27 enters, a15 leaves.
Reduced cost of entering variable: -8.03448
Minimum ratio theta*: 0.17982
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

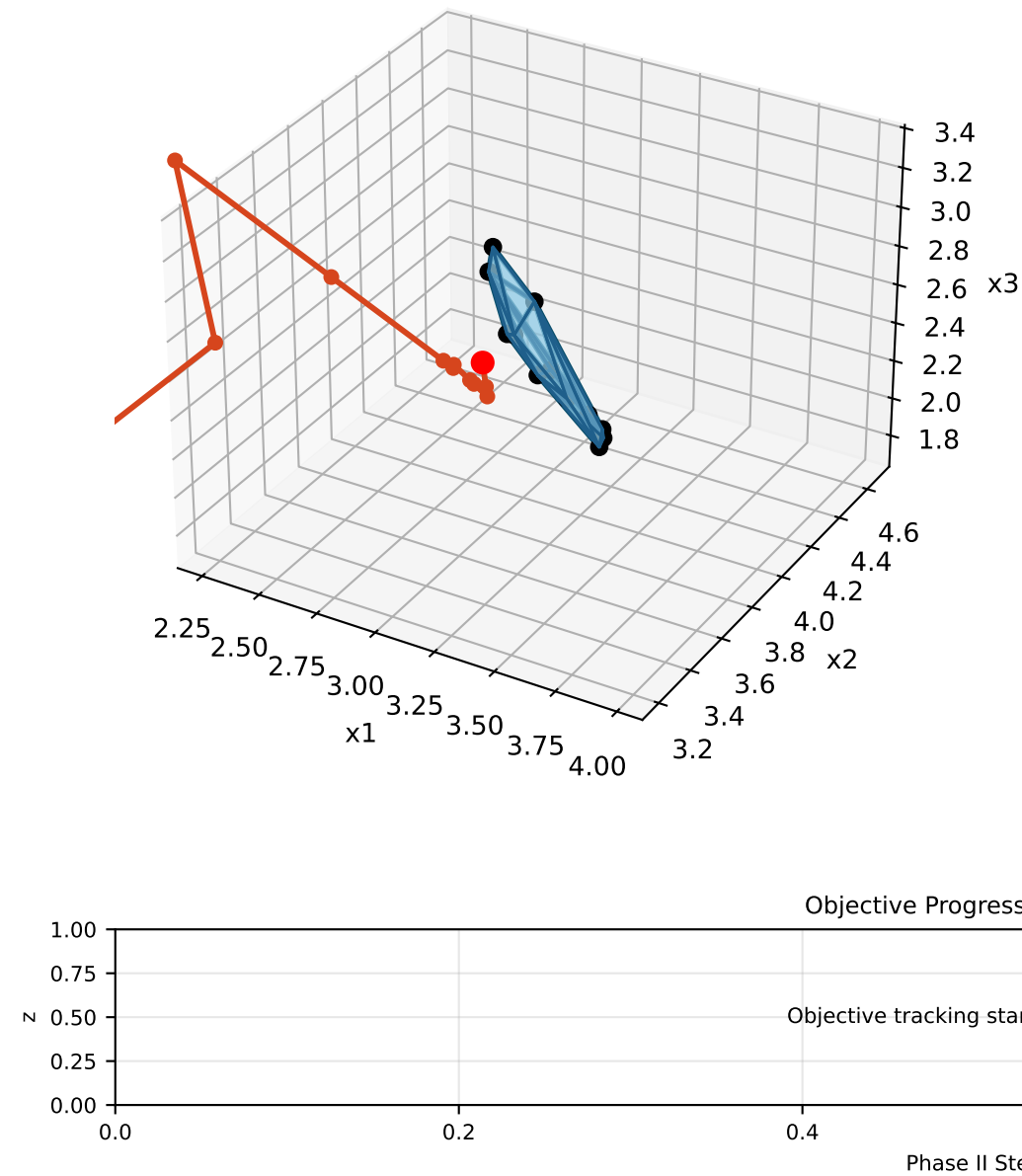
TABLEAU
Current solution: x1=2.82613, x2=4.01902, x3=2.14707
Tableau objective: -11.6573

	row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio							
	R1(s1)	0	0	0	1	0	0	0.328125	-0.328125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.1875	0.1875	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	0	0	0	0	9.17387	inf						
	R2(s2)	0	0	0	0	1	0	-0.078125	0.078125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	7.98098	77.3293					
	R3(s3)	0	0	0	0	0	1	-0.546875	0.546875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.3125	-0.3125	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	0	0	0	0	9.85293	57.3268					
	R4(u6)	0	0	0	0	0	0	1.09375	-1.09375	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0.625	0	0	0	0	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	0.450659	inf					
	R5(s5)	0	0	0	0	0	0	-2.29687	2.29687	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.3125	-1.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.95182	5.6371					
	R6(s14)	0	0	0	0	0	0	-0.03125	0.03125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.875	-0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.07142	2.3992					
	R7(x1)	1	0	0	0	0	0	-0.328125	0.328125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.82613	27.4991					
	R8(a8)	0	0	0	0	0	0	-0.390625	0.390625	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0.9375	-0.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.04294	2.19618				
	R9(s9)	0	0	0	0	0	0	-0.3125	0.3125	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.67176	6.63658				
	R10(a10)	0	0	0	0	0	0	-2.65625	2.65625	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	2.375	-2.375	0	0	0	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0	0	0	0	0	0	2.67045	2.21779			
	R11(a11)	0	0	0	0	0	0	-1.15625	1.15625	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	1.375	-1.375	0	0	0	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0	0	0	0	0	0	2.57868	3.579			
	R12(a12)	0	0	0	0	0	0	-2.78125	2.78125	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	1.875	-1.875	0	0	0	0	0	0	0	0	0	0	0	0	0.75	-0.75	0	0	0	0	0	0	0	0	0	0	1.42126	1.55371			
	R13(a13)	0	0	0	0	0	0	-0.875	0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14476	1.56307				
	R14(x2)	0	1	0	0	0	0	0.078125	-0.078125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.1875	0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.01902	inf				
	R15(u7)	0	0	0	0	0	0	-0.578125	0.578125	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.90097	18.5558			
	R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf					
	R17(a17)	0	0	0	0	0	0	-2.375	2.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	-1.5	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.811072	1.15987			
	R18(s18)	0	0	0	0	0	0	-3	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2	-2	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.93889	5.56194					
	R19(a19)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf						
	R20(s20)	0	0	0	0	0	0	0.296875	-0.296875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.6875	-0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.02435	10.7895				
	R21(s21)	0	0	0	0	0	0	0.421875	-0.421875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.75061	26.7691				
	R22(a22)	0	0	0	0	0	0	-0.796875	0.796875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.3125	-1.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.840251	1.34017				
	R23(a23)	0	0	0	0	0	0	-1.51562	1.51562	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.4375	-1.4375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.358018	0.631234			
	R24(u27)	0	0	0	0	0	0	1.67187	-1.67187	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.8125	1.8125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.17982	0.17982			
	R25(s25)	0	0	0	0	0	0	-1.23437	1.23437	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5625	-1.5625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	6.50066	7.72058			
	R26(x3)	0	0	1	0	0	0	0.546875	-0.546875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.3125	0.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.14707	inf			
	R27(u16)	0	0	0	0	0	0	1.71875	-1.71875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.125	1.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.830862	inf			
	R28(a28)	0	0	0	0	0	0	-0.9375	0.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.25	-1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.732642	1.24215		
		44	0	0	0	0	0	0	0	0	0	1	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	-13.5625	14.5625	0	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-11.6573	



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 12/31 | PHASE I step 11 | ENTER: u15 | LEAVE: a23

COMMENTS

Teaching Mode | Rule: DANTZIG
Pivot: u15 enters, a23 leaves.
Reduced cost of entering variable: -13.5625
Minimum ratio theta*: 0.249056
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

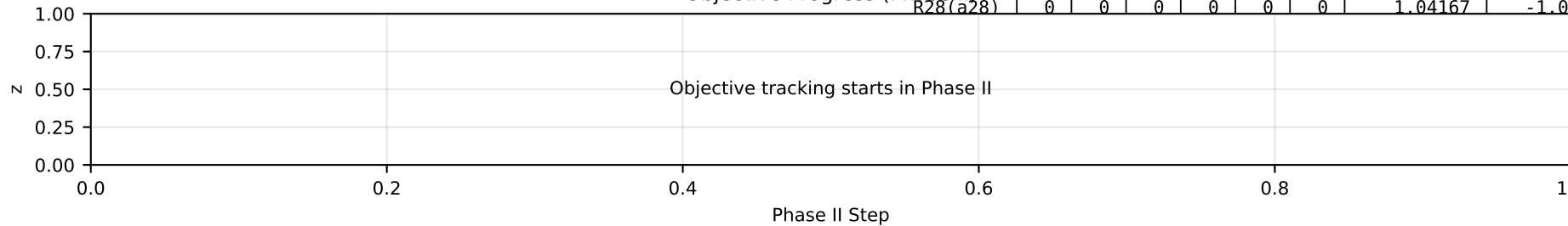
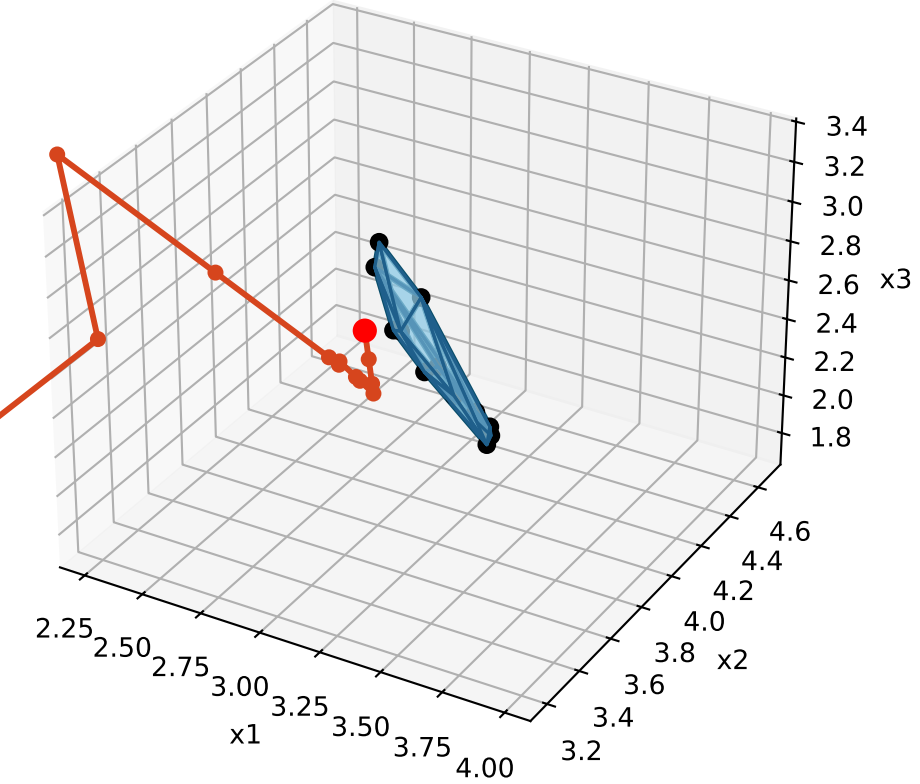
TABLEAU

Current solution: x1=2.77943, x2=4.06571, x3=2.2249
Tableau objective: -8.27943

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio	
R1(s1)	0	0	0	1	0	0	0.130435	-0.130435	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.130435	0.130435	0.173913	-0.173913	0	0	0	0	0	0	0	9.22057	inf	
R2(s2)	0	0	0	0	1	0	0.119565	-0.119565	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.130435	-0.130435	-0.173913	0.173913	0	0	0	0	0	0	0	7.93429	42.5652	
R3(s3)	0	0	0	0	0	1	-0.217391	0.217391	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.217391	-0.217391	0.0434783	-0.0434783	0	0	0	0	0	0	0	9.7751	31.5294	
R4(u6)	0	0	0	0	0	0	0.434783	-0.434783	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.434783	0.434783	-0.0869565	0.0869565	0	0	0	0	0	0	0	0.606319	inf	
R5(s5)	0	0	0	0	0	0	-0.913043	0.913043	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.913043	-0.913043	0.782609	-0.782609	0	0	0	0	0	0	0	3.62494	3.01091		
R6(s14)	0	0	0	0	0	0	0.891304	-0.891304	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0.608696	-0.608696	-0.478261	0.478261	0	0	0	0	0	0	0	0.8535	1.22448		
R7(x1)	1	0	0	0	0	0	-0.130435	0.130435	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.130435	-0.130435	-0.173913	0.173913	0	0	0	0	0	0	0	2.77943	15.0727		
R8(a8)	0	0	0	0	0	0	0.597826	-0.597826	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.652174	-0.652174	0.130435	-0.130435	0	0	0	0	0	0	0	0.809453	1.11247		
R9(s9)	0	0	0	0	0	0	0.478261	-0.478261	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.521739	-0.521739	0.304348	-0.304348	0	0	0	0	0	0	0	2.48497	3.56235		
R10(a10)	0	0	0	0	0	0	-0.152174	0.152174	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.65217	-1.65217	0.130435	-0.130435	0	0	0	0	0	0	0	2.07894	1.1244			
R11(a11)	0	0	0	0	0	0	0.293478	-0.293478	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.956522	-0.956522	0.391304	-0.391304	0	0	0	0	0	0	0	2.23623	1.87541			
R12(a12)	0	0	0	0	0	0	-0.804348	0.804348	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.30435	-1.30435	0.26087	-0.26087	0	0	0	0	0	0	0	0.954281	0.758006		
R13(a13)	0	0	0	0	0	0	0.706522	-0.706522	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1.04348	-1.04348	-0.391304	0.391304	0	0	0	0	0	0	0	0.771172	0.763171		
R14(x2)	0	1	0	0	0	0	-0.119565	0.119565	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.130435	0.130435	0.173913	-0.173913	0	0	0	0	0	0	0	4.06571	inf		
R15(u7)	0	0	0	0	0	0	-0.380435	0.380435	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.130435	-0.130435	-0.173913	0.173913	0	0	0	0	0	0	0	1.85427	10.1385		
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	5.67389	inf			
R17(a17)	0	0	0	0	0	0	-0.793478	0.793478	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	-1.04348	-1.04348	0.608696	-0.608696	0	0	0	0	0	0	0	0.437488	0.540715	
R18(s18)	0	0	0	0	0	0	-0.891304	0.891304	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.44078	2.96945		
R19(a19)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf	
R20(s20)	0	0	0	0	0	0	1.02174	-1.02174	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.478261	-0.478261	-0.304348	0.304348	0	0	0	0	0	0	0	3.85313	5.85361	
R21(s21)	0	0	0	0	0	0	0.619565	-0.619565	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.130435	-0.130435	-0.173913	0.173913	0	0	0	0	0	0	0	2.70391	14.6699	
R22(a22)	0	0	0	0	0	0	0.586957	-0.586957	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.913043	-0.913043	-0.217391	0.217391	0	0	0	0	0	0	0	0.513365	0.640192		
R23(u15)	0	0	0	0	0	0	-1.05435	1.05435	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	-0.695652	0.695652	0.26087	-0.26087	0	0	0	0	0	0	0	0.249056	0.249056		
R24(u27)	0	0	0	0	0	0	-0.23913	0.23913	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.26087	1.26087	0.347826	-0.347826	0	0	0	1	-1	0	0	0.631234	inf		
R25(s25)	0	0	0	0	0	0	0.413043	-0.413043	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.08696	-1.08696	0.217391	-0.217391	1	0	0	0	0	0	0	6.11151	4.16042		
R26(x3)	0	0	1	0	0	0	0.217391	-0.217391	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.217391	0.217391	-0.0434783	0.0434783	0	0	0	0	0	0	0	2.2249	inf		
R27(u26)	0	0	0	0	0	0	0.532609	-0.532609	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.782609	0.782609	0.0434783	-0.0434783	0	1	-1	0	0	0	0	1.11105	inf
R28(a28)	0	0	0	0	0	0	0.380435	-0.380435	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.869565	-0.869565	0.173913	-0.173913	0	0	0	0	-1	1	0	0.421322	0.586113	
z	0	0	0	0	0	0	0	0	0	0	1	0	1	1	0	0	1	0	1	0	1	0	1	0	0	0	1	0	0	0	0	0	0	0	0	-8.43478	9.43478	-1.08696	2.08696	0	0	1	0	1	1	0	-8.27943	-			

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 13/31 | PHASE I step 12 | ENTER: u23 | LEAVE: a17

COMMENTS

Teaching Mode | Rule: DANTZIG
Pivot: u23 enters, a17 leaves.
Reduced cost of entering variable: -8.43478
Minimum ratio theta*: 0.419259
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

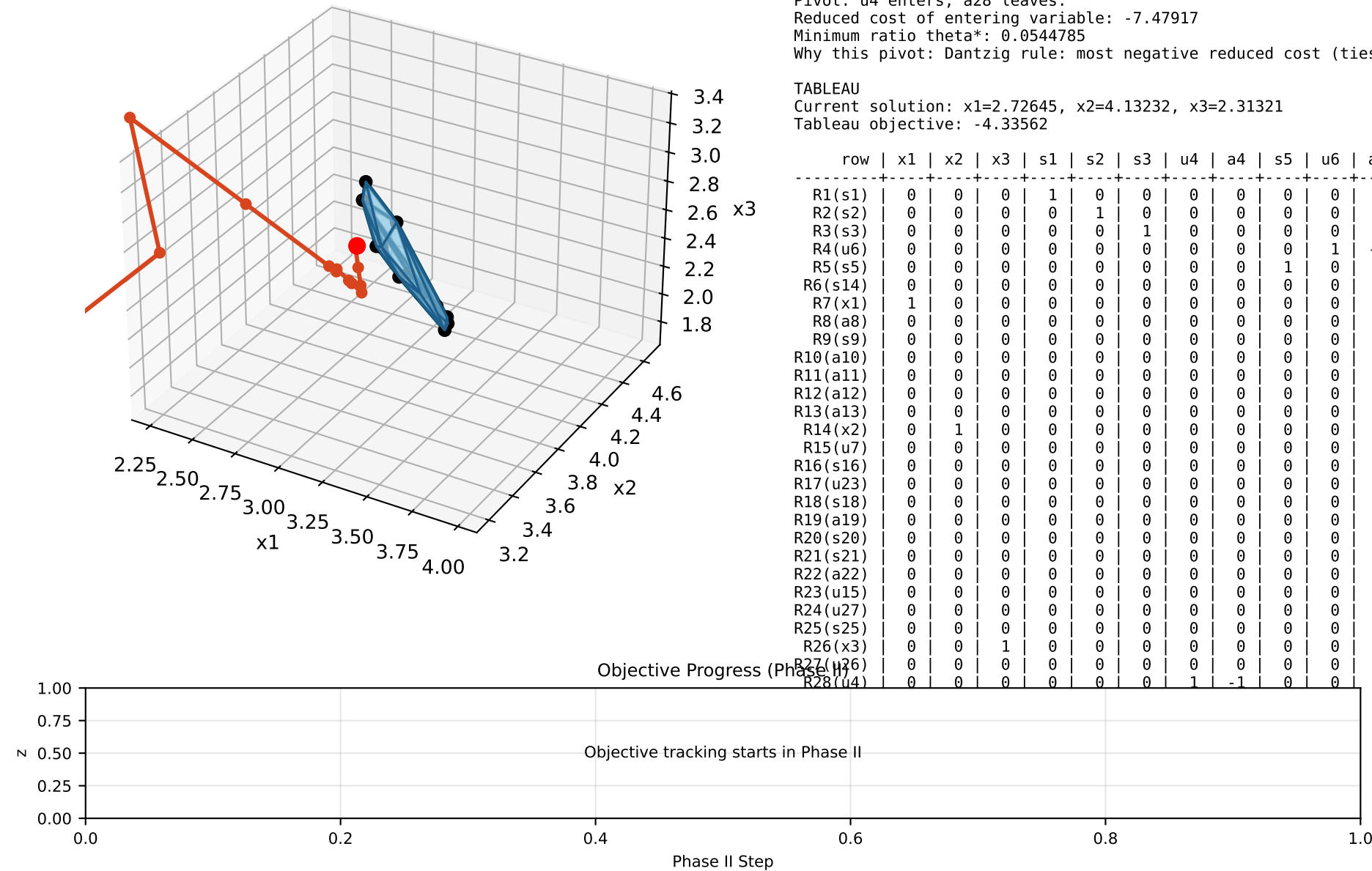
TABLEAU

Current solution: x1=2.72474, x2=4.1204, x3=2.31605
Tableau objective: -4.74307

	row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio		
	R1(s1)	0	0	0	1	0	0	0.03125	-0.03125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	9.27526	inf	
	R2(s2)	0	0	0	0	1	0	0.21875	-0.21875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	7.8796	60.8295	
	R3(s3)	0	0	0	0	0	1	-0.0520833	0.0520833	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.208333	-0.208333	0	0	0	0	0	0	0	0	0	-0.0833333	0.0833333	0	0	0	0	0	0	0	0	9.68395	44.9654	
	R4(u6)	0	0	0	0	0	0	0.104167	-0.104167	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.416667	0.416667	0	0	0	0	0	0	0	0	0	0.166667	-0.166667	0	0	0	0	0	0	0	0	0.788605	inf	
	R5(s5)	0	0	0	0	0	0	-0.21875	0.21875	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.875	-0.875	0	0	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	3.24213	3.97017		
	R6(s14)	0	0	0	0	0	0	1.35417	-1.35417	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0.583333	-0.583333	0	0	0	0	0	0	0	0	0	-0.833333	0.833333	0	0	0	0	0	0	0	0	0.598299	1.40218	
	R7(x1)	1	0	0	0	0	0	-0.03125	0.03125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	2.72474	21.309		
	R8(a8)	0	0	0	0	0	0	1.09375	-1.09375	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0.625	-0.625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.536024	1.24116	
	R9(s9)	0	0	0	0	0	0	0.875	-0.875	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0.5	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.26623	4.76286	
	R10(a10)	0	0	0	0	0	0	1.10417	-1.10417	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	1.58333	-1.58333	0	0	0	0	0	0	0	0	0	-0.833333	0.833333	0	0	0	0	0	0	0	0	1.38625	1.2583	
	R11(a11)	0	0	0	0	0	0	1.02083	-1.02083	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0.916667	-0.916667	0	0	0	0	0	0	0	0	0	-0.166667	0.166667	0	0	0	0	0	0	0	0	1.8352	2.33788	
	R12(a12)	0	0	0	0	0	0	0.1875	-0.1875	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	1.25	-1.25	0	0	0	0	0	0	0	0	-0.5	0.5	0	0	0	0	0	0	0	0	0.407421	0.731615		
	R13(a13)	0	0	0	0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0.333684	0.73904			
	R14(x2)	0	1	0	0	0	0	-0.21875	0.21875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	4.1204	inf		
	R15(u7)	0	0	0	0	0	0	-0.28125	0.28125	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	1.79958	14.2161		
	R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	5.67389	inf				
	R17(u23)	0	0	0	0	0	0	-0.760417	0.760417	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.958333	0.958333	0	0	0	0	0	0	0	0	1	-1	0.583333	-0.583333	0	0	0	0	0	0	0	0	0.419259	0.419259
	R18(s18)	0	0	0	0	0	0	0.166667	-0.166667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.33333	-1.33333	1	0	0	0	0	0	0	0	0	-0.333333	0.333333	0	0	0	0	0	0	0	0	4.85746	3.91056	
	R19(a19)	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0571818	inf				
	R20(s20)	0	0	0	0	0	0	1.38542	-1.38542	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.458333	-0.458333	0	0	0	1	0	0	0	0	0	-0.583333	0.583333	0	0	0	0	0	0	0	0	3.65261	8.05654	
	R21(s21)	0	0	0	0	0	0	0.71875	-0.71875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	1	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	2.64923	20.73		
	R22(a22)	0	0	0	0	0	0	1.28125	-1.28125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.875	-0.875	0	0	0	0	0	0	0	0	-0.75	0.75	0	0	0	0	0	0	0	0	0.130564	0.562257		
	R23(u15)	0	0	0	0	0	0	-1.58333	1.58333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	-0.666667	0.666667	0	0	0	0	0	0	0	0	0	0.666667	-0.666667	0	0	0	0	0	0	0	0	0.540715	inf
	R24(u27)	0	0	0	0	0	0	-1.19792	1.19792	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.20833	1.20833	0	0	0	0	0	0	0	0	0	1.08333	-1.08333	0	0	0	1	-1	0	0	0	1.15987	inf	
	R25(s25)	0	0	0	0	0	0	1.23958	-1.23958	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.04167	-1.04167	0	0	0	0	0	0	0	0	0	-0.416667	0.416667	1	0	0	0	0	0	0	0	5.65579	5.62259	
	R26(x3)	0	0	1	0	0	0	0.0520833	-0.0520833	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.208333	0.208333	0	0	0	0	0	0	0	0	0	0.0833333	-0.0833333	0	0	0	0	0	0	0	0	2.31605	inf	
	R27(u26)	0	0	0	0	0	0	-0.0625	0.0625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.75	0.75	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	1.43917	inf			
	R28(a28)	0	0	0	0	0	0	1.04167	-1.04167	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.833333	-0.833333	0	0	0	0	0	0	0	0	0	-0.333333	0.333333	0	0	0	0	0	-1	1	0.0567485	0.48452		
									7917	0	0	1	0	1	1	0	0	1	0	1	0	1	0	1	0	0	0	0	1	0	-7.08333	8.08333	0	1	0	0	0	1	0	0	0	0	0	1	0	1	0	1	1	0		-4.74307	

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 14/31 | PHASE I step 13 | ENTER: u4 | LEAVE: a28

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u4 enters, a28 leaves.

Reduced cost of entering variable: -7.47917

Minimum ratio theta*: 0.0544785

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

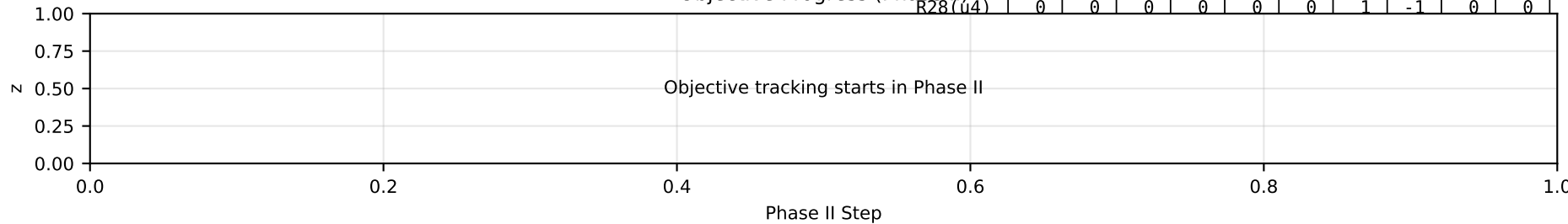
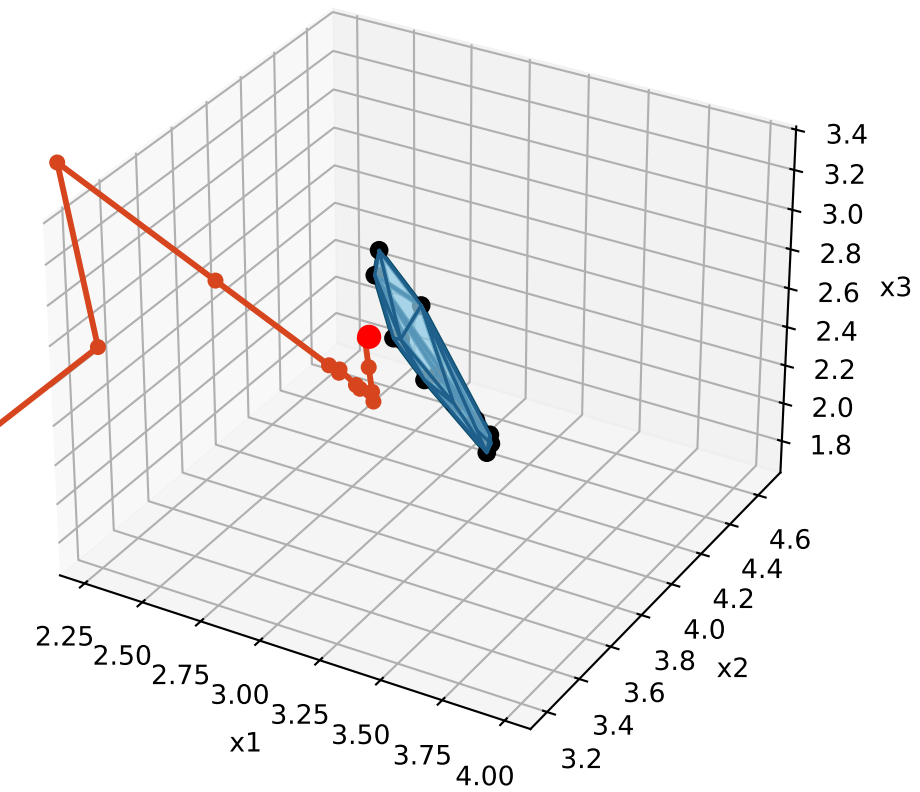
Current solution: $x_1=2.72645$, $x_2=4.13232$, $x_3=2.31321$

Tableau objective: -4.33562

	row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio				
Phase 1	R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.15	0.15	0	0	0	0	0	0	0	0	0	0.26	-0.26	0	0	0	0	0	0.03	-0.03	9.27355	296.808				
	R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.05	0.05	0	0	0	0	0	0	0	0	0	-0.18	0.18	0	0	0	0	0	0.21	-0.21	7.86768	36.021				
	R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	0	-0.1	0.1	0	0	0	0	-0.05	0.05	9.68679	inf					
	R4(u6)	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.5	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0.2	-0.2	0	0	0	0	0.1	-0.1	0.78293	7.57061		
	R5(s5)	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.05	-1.05	0	0	0	0	0	0	0	0	0	0	0	0	0.18	-0.18	0	0	0	0	0	-0.21	0.21	3.25405	inf	
	R6(s14)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	-0.5	0.5	0	0	0	0	0	0	0	0	0	0	0	-0.4	0.4	0	0	0	0	1.3	-1.3	0.524526	0.441821			
	R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.15	-0.15	0	0	0	0	0	0	0	0	0	0	0	-0.26	0.26	0	0	0	0	-0.03	0.03	2.72645	inf			
	R8(a8)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0.1	-0.1	0	0	0	0	1.05	-1.05	0.476438	0.490079		
	R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	-0.2	0.2	0	0	0	0	0	0	0	0	0	0	0	0.28	-0.28	0	0	0	0	0	0.84	-0.84	2.21856	2.58997		
	R10(a10)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0.7	-0.7	0	0	0	0	0	0	0	0	0	0	0	-0.48	0.48	0	0	0	0	1.06	-1.06	1.3261	1.25547			
	R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0.1	-0.1	0	0	0	0	0	0	0	0	0	0	0	0	-0.16	-0.16	0	0	0	0	0.98	-0.98	1.77959	1.79775		
	R12(a12)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	1.1	-1.1	0	0	0	0	0	0	0	0	0	0	0	0	-0.44	0.44	0	0	0	0	0.18	-0.18	0.397206	2.17291		
	R13(a13)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	-0.2	0.2	0	0	0	0	0	0	0	0	0	0	0	-0.52	0.52	0	0	0	0	1.44	-1.44	0.251967	0.222456			
	R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.05	-0.05	0	0	0	0	0	0	0	0	0	0	0	0.18	-0.18	0	0	0	0	-0.21	0.21	4.13232	inf			
	R15(u7)	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.35	-0.35	0	0	0	0	0	0	0	0	0	0	0	-0.34	0.34	0	0	0	0	-0.27	0.27	1.8149	inf			
	R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf	
	R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.35	0.35	0	0	0	0	0	0	0	0	0	1	-1	0.34	-0.34	0	0	0	0	-0.73	0.73	0.460686	inf			
	R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.2	-1.2	1	0	0	0	0	0	0	0	0	-0.28	0.28	0	0	0	0	0.16	-0.16	4.84838	29.1448					
	R19(a19)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.2	0.2	0	-1	1	0	0	0	0	0	0	0	0	0	0.08	-0.08	0	0	0	0	0.24	-0.24	0.0435621	0.228727		
	R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.65	0.65	0	0	0	1	0	0	0	0	0	0	-0.14	0.14	0	0	0	0	1.33	-1.33	3.57714	2.63647				
	R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.45	0.45	0	0	0	0	1	0	0	0	0	0	0	-0.02	0.02	0	0	0	0	0.69	-0.69	2.61007	3.68588			
	R22(a22)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.15	0.15	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	-0.34	0.34	0	0	0	0	1.23	-1.23	0.060763	0.101903
	R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0.6	-0.6	0	0	0	0	0	0	0	0	0	0	0	0.16	-0.16	0	0	0	0	-1.52	1.52	0.626972	inf		
	R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0.7	-0.7	0	0	0	1	-1	-1.15	1.15	1.22513	inf	
	R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.05	-0.05	0	0	0	0	0	0	0	0	0	0	0	0	-0.02	0.02	1	0	0	0	0	1.19	-1.19	5.58826	4.56266	
	R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0.1	-0.1	0	0	0	0	0.05	-0.05	2.31321	44.4681		
	R27(u36)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.7	0.7	0	0	0	0	0	0	0	0	0	0	0	0.48	-0.48	0	1	-1	0	0	-0.06	0.06	1.44257	inf		
	R28(u4)	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.8	-0.8	0	0	0	0	0	0	0	0	0	0	0	0	-0.32	0.32	0	0	0	0	-0.96	0.96	0.0544785	0.0544785		
												1	0	1	1	0	0	1	0	1	0	1	0	1	0	0	0	0	1	0	-1.1	2.1	0	1	0	0	0	1	0	0	1	1.44	-0.44	0	0	1	0	-6.18	7.18	-4.33562					

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 15/31 | PHASE I step 14 | ENTER: u28 | LEAVE: a22

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u28 enters, a22 leaves.

Reduced cost of entering variable: -6.18

Minimum ratio theta*: 0.0494008

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

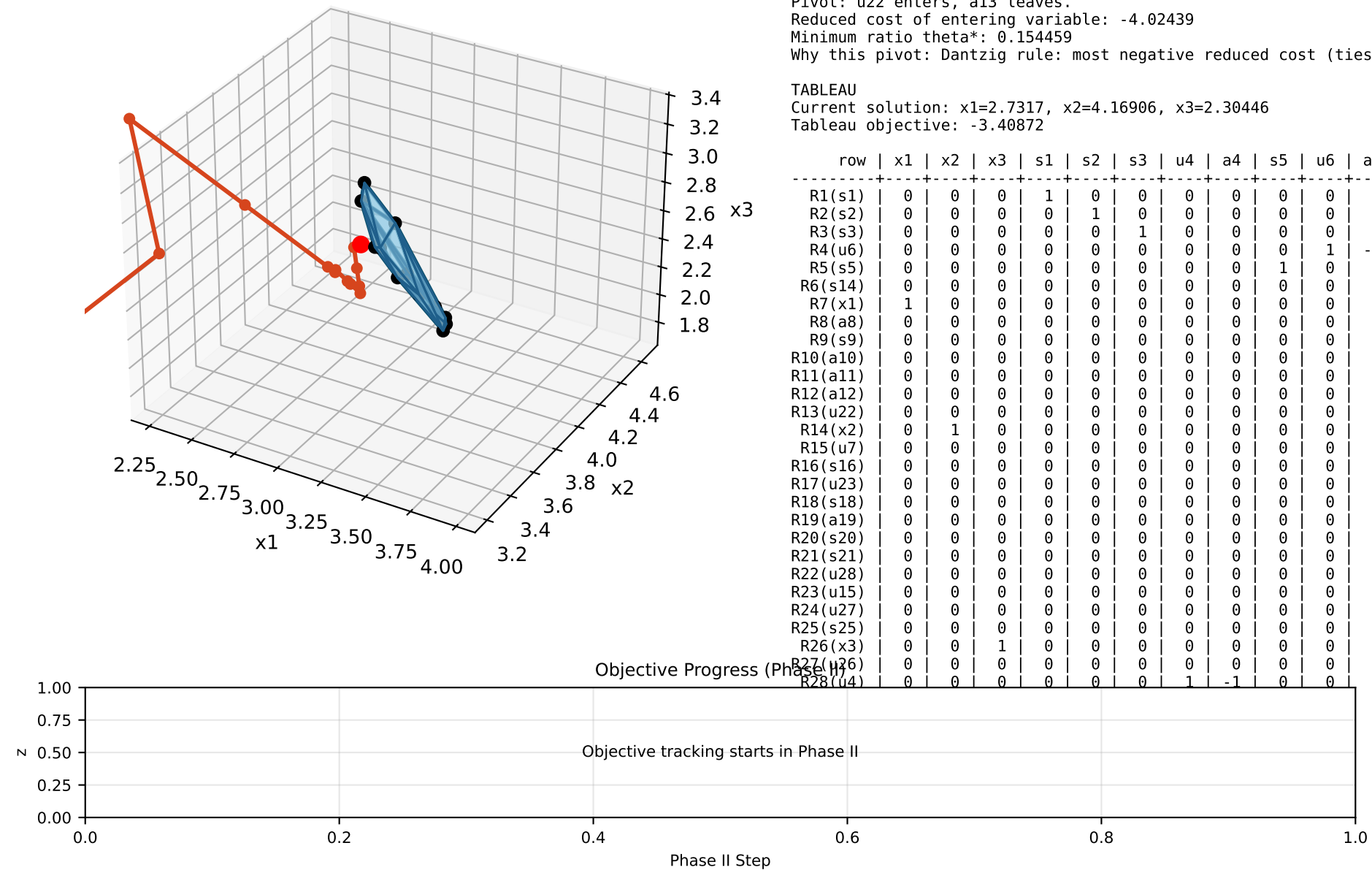
Current solution: x1=2.72793, x2=4.14269, x3=2.31074

Tableau objective: -4.03032

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio		
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.146341	0.146341	0	0	0	0	0	0.0243902	-0.0243902	0	0	0.268293	-0.268293	0	0	0	0	0	0	0	0	9.27207	309.118
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0243902	0.0243902	0	0	0	0	0	0.170732	-0.170732	0	0	-0.121951	0.121951	0	0	0	0	0	0	0	0	7.85731	37.4652
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.243902	-0.243902	0	0	0	0	0	-0.0406504	0.0406504	0	0	-0.113821	0.113821	0	0	0	0	0	0	0	0	9.68926	inf
R4(u6)	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.487805	0.487805	0	0	0	0	0	0.0813008	-0.0813008	0	0	0.227642	-0.227642	0	0	0	0	0	0	0	0	0.77799	7.8293
R5(s5)	0	0	0	0	0	0	0	0	1	0	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.02439	-1.02439	0	0	0	0	0	-0.170732	0.170732	0	0	0.121951	-0.121951	0	0	0	0	0	0	0	0	3.26443	inf
R6(s14)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	-0.341463	0.341463	0	0	0	0	0	1.05691	-1.05691	0	0	-0.0406504	0.0406504	0	0	0	0	0	0	0	0	0.460305	0.403481
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.146341	-0.146341	0	0	0	0	0	-0.0243902	0.0243902	0	0	-0.268293	0.268293	0	0	0	0	0	0	0	0	2.72793	inf
R8(a8)	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.121951	0.121951	0	0	0	0	0	0.853659	-0.853659	0	0	0.390244	-0.390244	0	0	0	0	0	0	0	0	0.424567	0.45375
R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	-0.097561	0.097561	0	0	0	0	0	0.682927	-0.682927	0	0	0.512195	-0.512195	0	0	0	0	0	0	0	0	2.17706	2.64114
R10(a10)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0.829268	-0.829268	0	0	0	0	0	0.861789	-0.861789	0	0	-0.186992	0.186992	0	0	0	0	0	0	0	0	1.27373	1.25103
R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0.219512	-0.219512	0	0	0	0	0	0.796748	-0.796748	0	0	0.430894	-0.430894	0	0	0	0	0	0	0	0	1.73118	1.81591
R12(a12)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	1.12195	-1.12195	0	0	0	0	0	0.146341	-0.146341	0	0	-0.390244	0.390244	0	0	0	0	0	0	0	0	0.388314	2.2067
R13(a13)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	-0.0243902	0.0243902	0	0	0	0	0	1.17073	-1.17073	0	0	-0.121951	0.121951	0	0	0	0	0	0	0	0	0.18083	0.174977
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0243902	-0.0243902	0	0	0	0	0	-0.170732	0.170732	0	0	0.121951	-0.121951	0	0	0	0	0	0	0	0	4.14269	inf	
R15(u7)	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.317073	-0.317073	0	0	0	0	0	-0.219512	0.219512	0	0	-0.414634	0.414634	0	0	0	0	0	0	0	0	1.82824	inf
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf			
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.439024	0.439024	0	0	0	0	0	-0.593496	0.593496	1	-1	0.138211	-0.138211	0	0	0	0	0	0	0	0	0.496748	inf
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.21951	-1.21951	1	0	0	0	0	0.130081	-0.130081	0	0	-0.235772	0.235772	0	0	0	0	0	0	0	0	4.84048	30.3024
R19(a19)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.170732	0.170732	0	-1	1	0	0	0.195122	-0.195122	0	0	0.146341	-0.146341	0	0	0	0	0	0	0	0	0.0317059	0.181509
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.487805	0.487805	0	0	0	1	0	1.0813	-1.0813	0	0	0.227642	-0.227642	0	0	0	0	0	0	0	0	3.51143	2.68958
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.365854	0.365854	0	0	0	0	1	0.560976	-0.560976	0	0	0.170732	-0.170732	0	0	0	0	0	0	0	0	2.57598	3.78271
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.121951	0.121951	0	0	0	0	0	-0.813008	0.813008	0	0	-0.276423	0.276423	0	0	0	0	0	0	1	-1	0.0494008	0.0494008
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0.414634	-0.414634	0	0	0	0	0	-1.23577	1.23577	0	0	-0.260163	0.260163	0	0	0	0	0	0	0	0	0.702061	inf
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.390244	0.390244	0	0	0	0	0	-0.934959	0.934959	0	0	0.382114	-0.382114	0	0	0	1	-1	0	0	0	1.28194	inf
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.195122	-0.195122	0	0	0	0	0	-0.96748	-0.96748	0	0	0.308943	-0.308943	1	0	0	0	0	0	0	0	5.52947	4.69602
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.243902	0.243902	0	0	0	0	0	0.0406504	-0.0406504	0	0	0.113821	-0.113821	0	0	0	0	0	0	0	0	2.31074	46.2642
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.707317	0.707317</																					

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 16/31 | PHASE I step 15 | ENTER: u22 | LEAVE: a13

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u22 enters, a13 leaves.

Reduced cost of entering variable: -4.02439

Minimum ratio theta*: 0.154459

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

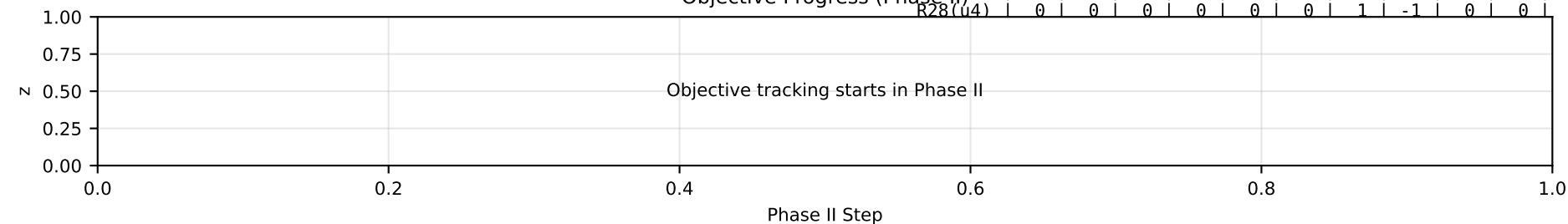
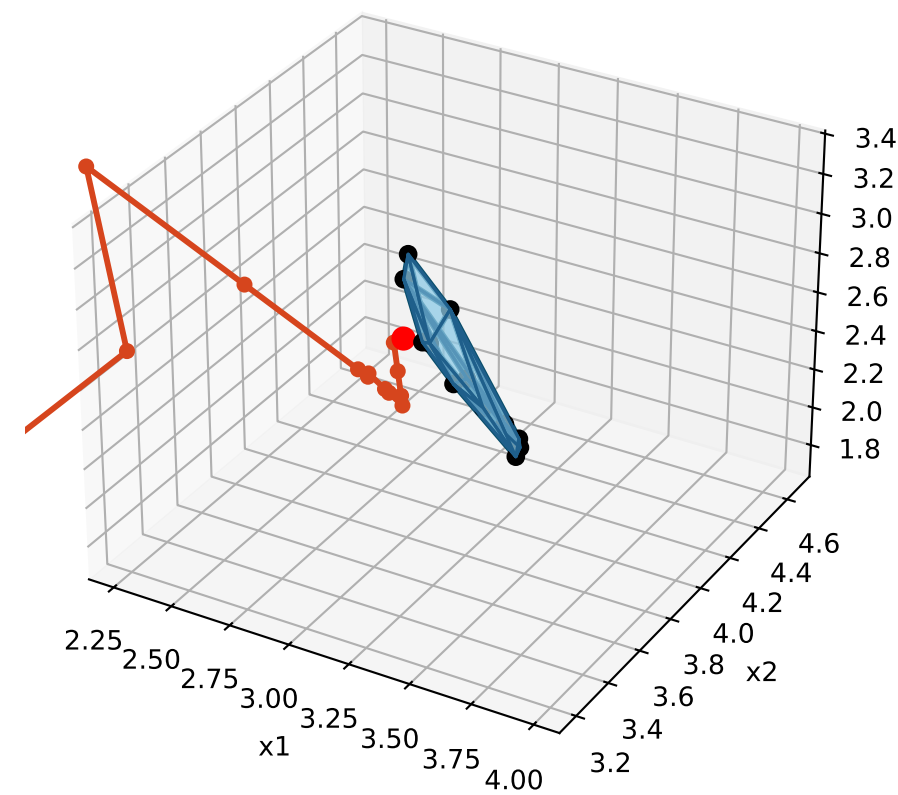
Current solution: x1=2.7317, x2=4.16906, x3=2.30446

Tableau objective: -3.40872

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio						
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0208333	-0.0208333	0	0	0	0	0	-0.145833	0.145833	0	0	0	0	0	0	0	0	0	0	0.270833	-0.270833	0	0	0	0	0	0	0	9.2683	380.155				
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.145833	-0.145833	0	0	0	0	0	-0.0208333	0.0208333	0	0	0	0	0	0	0	0	0	0	0	-0.104167	0.104167	0	0	0	0	0	0	0	7.83094	46.0214			
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0347222	0.0347222	0	0	0	0	0	0.243056	-0.243056	0	0	0	0	0	0	0	0	0	0	0	-0.118056	0.118056	0	0	0	0	0	0	0	9.69554	inf			
R4(u6)	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0.0694444	-0.0694444	0	0	0	0	0	-0.486111	0.486111	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.765433	9.56928						
R5(s5)	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.145833	0.145833	0	0	0	0	0	1.02083	-1.02083	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.2908	inf					
R6(s14)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.902778	-0.902778	1	0	0	0	0	-0.319444	0.319444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.297056	0.435519				
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0208333	0.0208333	0	0	0	0	0	0.145833	-0.145833	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.7317	inf				
R8(a8)	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0.729167	-0.729167	0	0	0	0	0	-0.104167	0.104167	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.292712	0.49735				
R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0.583333	-0.583333	0	0	0	0	0	-0.0833333	0.0833333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.07158	3.18784			
R10(a10)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0.736111	-0.736111	0	0	0	0	0	0.847222	-0.847222	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14062	1.47801		
R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0.680556	-0.680556	0	0	0	0	0	0.236111	-0.236111	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.60811	2.1728		
R12(a12)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0.125	-0.125	0	0	0	0	0	1.125	-1.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.36571	2.65348			
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.854167	0.854167	0	0	0	0	0	-0.0208333	0.0208333	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0.154459	0.154459			
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.145833	0.145833	0	0	0	0	0	0.0208333	-0.0208333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.16906	inf		
R15(u7)	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	-0.1875	0.1875	0	0	0	0	0	0.3125	-0.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.86215	inf		
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf				
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.506944	0.506944	0	0	0	0	0	-0.451389	0.451389	0	0	0	0	0	0	0	0	0	0	1	-1	0.0763889	-0.0763889	0	0	0	0	0	0	0	0	0	0.588419	inf
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.111111	-0.111111	0	0	0	0	0	1.22222	-1.22222	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.82039	37.2112	
R19(a19)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.166667	-0.166667	0	0	0	0	0	-0.166667	0.166667	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.00156767	0.162493		
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.923611	-0.923611	0	0	0	0	0	-0.465278	0.465278	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.34442	3.24742		
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.479167	-0.479167	0	0	0	0	0	-0.354167	0.354167	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.48934	4.59197		
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.694444	0.694444	0	0	0	0	0	-0.138889	0.138889	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.174977	inf	
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.05556	1.05556	0	1	-1	0	0	0.388889	-0.388889	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.892937	inf
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.798611	0.798611	0	0	0	0	0	-0.409722	0.409722	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.42635	inf	
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.826389	-0.826389	0	0	0	0	0	0.215278	-0.215278	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.38004	5.71534	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0347222	-0.0347222	0	0	0	0	0	-0.243056	0.243056	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.30446	56.8442		
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0416667	0.0416667	0	0	0	0	0	-0.708333	0.708333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.45307	inf	
R28(u4)	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.666667	0.666667	0	0	0	0	0	0.666667	-0.666667	0	0	0	0	0	0	0	0	0	0	0	0													

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 17/31 | PHASE I step 16 | ENTER: u13 | LEAVE: a19

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u13 enters, a19 leaves

Reduced cost of entering variable: -2.4375

Minimum ratio theta*: 0.00940

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

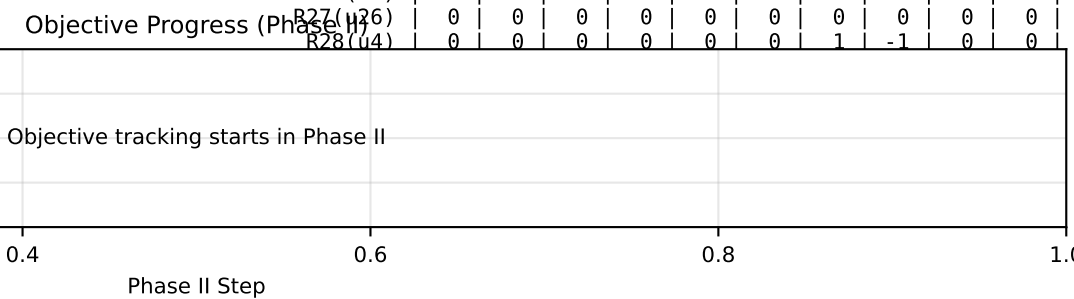
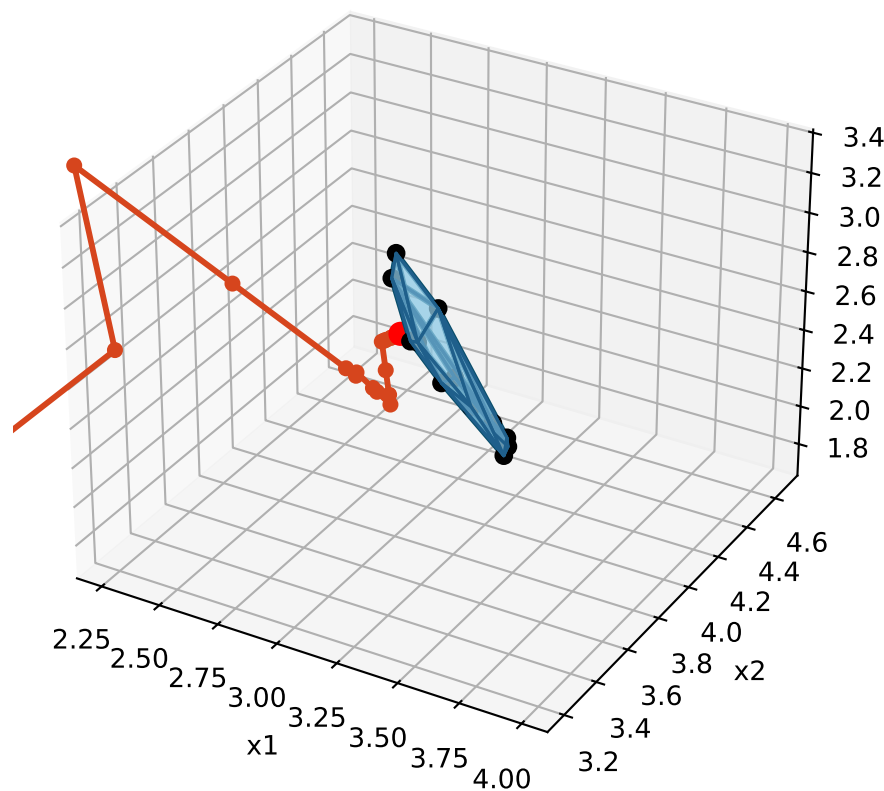
Current solution: $x_1=2.73189$, $x_2=4.17043$, $x_3=2.30414$

Tableau objective: -3.38579

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio																																																																																																																																																																																																																																																																																																																																												
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0.125	-0.125	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	9.26811	444.879																																																																																																																																																																																																																																																																																																																																												
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0.875	-0.875	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	7.82957	53.6979																																																																																																																																																																																																																																																																																																																																												
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.208333	-0.208333	0	-0.208333	0.208333	0	0	0	0	0	0	-0.0833333	0.0833333	0	0	0	0	0	0	9.69586	inf																																																																																																																																																																																																																																																																																																																																												
R4(u6)	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.416667	0.416667	0	0.416667	-0.416667	0	0	0	0	0	0	0.166667	-0.166667	0	0	0	0	0	0	0.764779	11.0222																																																																																																																																																																																																																																																																																																																																												
R5(s5)	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.875	-0.875	0	-0.875	0.875	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	3.29217	inf																																																																																																																																																																																																																																																																																																																																												
R6(s14)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0.583333	-0.583333	0	5.41667	-5.41667	0	0	0	0	0	0	-0.833333	0.833333	0	0	0	0	0	0	0.288564	0.329047																																																																																																																																																																																																																																																																																																																																												
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	-0.125	0.125	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	2.73189	inf																																																																																																																																																																																																																																																																																																																																												
R8(a8)	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.625	-0.625	0	4.375	-4.375	0	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	0.285853	0.401433																																																																																																																																																																																																																																																																																																																																												
R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.5	-0.5	0	3.5	-3.5	0	0	0	0	0	0	0	0	0	0	0	0	0	2.06609	3.55127																																																																																																																																																																																																																																																																																																																																													
R10(a10)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	1.58333	-1.58333	0	4.41667	-4.41667	0	0	0	0	0	-0.833333	0.833333	0	0	0	0	0	0	0	1.1337	1.54952																																																																																																																																																																																																																																																																																																																																												
R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0.916667	-0.916667	0	4.08333	-4.08333	0	0	0	0	0	-0.166667	0.166667	0	0	0	0	0	0	0	1.60171	2.36294																																																																																																																																																																																																																																																																																																																																												
R12(a12)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	1.25	-1.25	0	0.75	-0.75	0	0	0	0	0	-0.5	0.5	0	0	0	0	0	0	0.364535	2.92568																																																																																																																																																																																																																																																																																																																																													
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.875	0.875	0	-5.125	5.125	0	1	-1	0	0	0.75	-0.75	0	0	0	0	0	0	0	0.162493	inf																																																																																																																																																																																																																																																																																																																																												
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	-0.875	0.875	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	4.17043	inf																																																																																																																																																																																																																																																																																																																																													
R15(u7)	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	-1.125	1.125	0	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	1.86391	inf																																																																																																																																																																																																																																																																																																																																													
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	5.67389	inf																																																																																																																																																																																																																																																																																																																																														
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.958333	0.958333	0	-3.04167	3.04167	0	0	0	0	1	-1	0.583333	-0.583333	0	0	0	0	0	0	0.593187	inf																																																																																																																																																																																																																																																																																																																																												
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.33333	-1.33333	1	0.666667	-0.666667	0	0	0	0	0	-0.333333	0.333333	0	0	0	0	0	0	0	4.81934	43.3835																																																																																																																																																																																																																																																																																																																																												
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	-1	1	0	-6	6	0	0	0	0	0	0	0	1	-1	0	0	0	0	0.009406	0.009406																																																																																																																																																																																																																																																																																																																																													
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.458333	-0.458333	0	5.54167	-5.54167	1	0	0	0	0	0	-0.583333	0.583333	0	0	0	0	0	0	3.33573	3.62102																																																																																																																																																																																																																																																																																																																																												
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	2.875	-2.875	0	1	0	0	0	0	-0.25	0.25	0	0	0	0	0	0	2.48483	5.19514																																																																																																																																																																																																																																																																																																																																												
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.833333	0.833333	0	-4.16667	4.16667	0	0	0	0	0	0.333333	-0.333333	0	0	0	0	0	1	-1	0.181509	inf																																																																																																																																																																																																																																																																																																																																												
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	-0.666667	0.666667	0	-6.33333	6.33333	0	0	0	0	0	0.666667	-0.666667	0	0	0	0	0	0	0.902866	inf																																																																																																																																																																																																																																																																																																																																													
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.20833	1.20833	0	-4.79167	4.79167	0	0	0	0	0	0	1.08333	-1.08333	0	0	0	1	-1	0	1.43386	inf																																																																																																																																																																																																																																																																																																																																												
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.04167	-1.04167	0	4.95833	-4.95833	0	0	0	0	0	-0.416667	0.416667	1	0	0	0	0	0	5.37226	6.5103																																																																																																																																																																																																																																																																																																																																													
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.208333	0.208333	0	0.208333	-0.208333	0	0	0	0	0	0.0833333	-0.0833333	0	0	0	0	0	0	2.30414	66.3685																																																																																																																																																																																																																																																																																																																																													
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.75	0.75	0	-0.25	0.25	0	0	0	0	0	0.5	-0.5	0	1	-1	0	0	0	1.45346	inf																																																																																																																																																																																																																																																																																																																																													
R28(u4)	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.228727	inf																																																																																																																																																																																																																																																																																																																																														
base	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 18/31 | PHASE I step 17 | ENTER: u19 | LEAVE: s14

COMMENTS

Teaching Mode | Rule: DANTZIC

Pivot: u19 enters, s14 leaves

Reduced cost of entering variable: -13.625

Minimum ratio theta*: 0.0532734

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

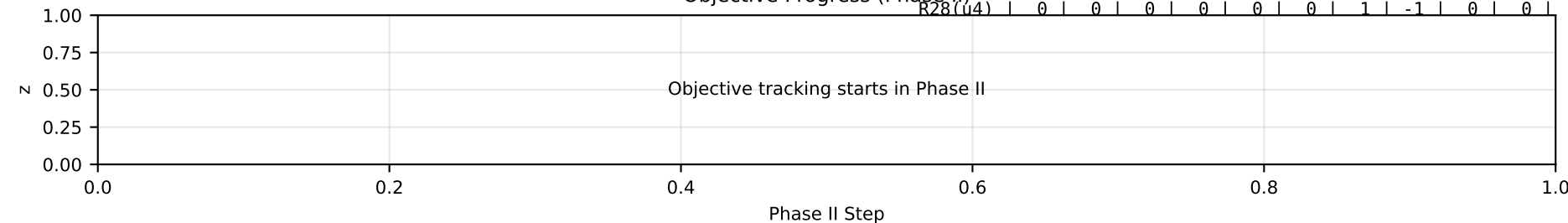
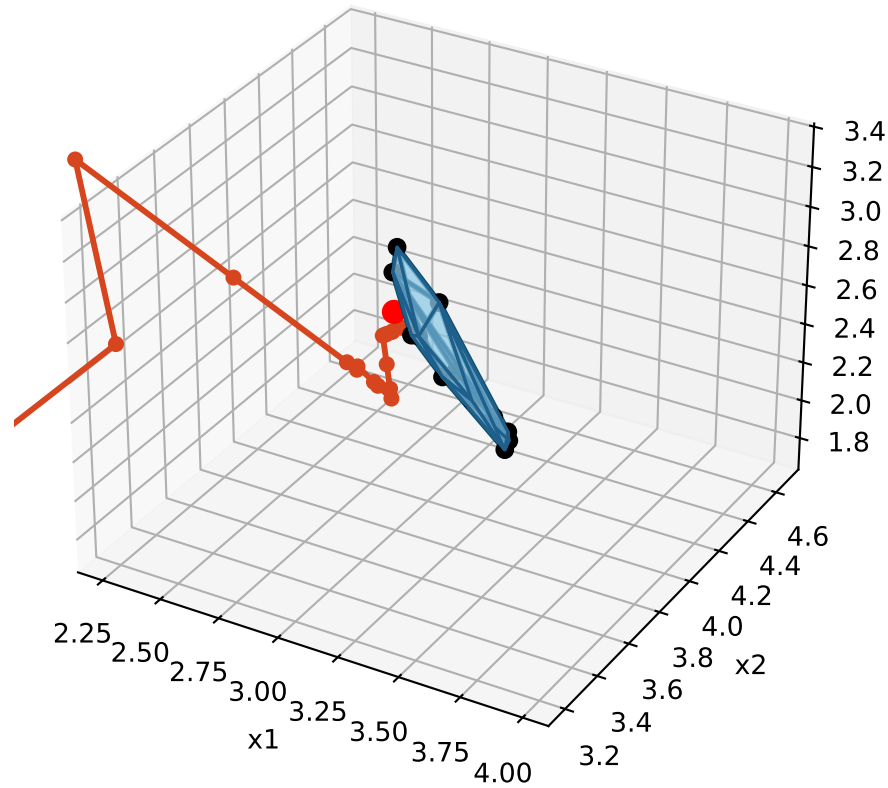
Current solution: $x_1=2.73855$, $x_2=4.21705$, $x_3=2.29304$

Tableau objective: -2.65994

	row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio								
has 28 rows	R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0230769	0	0	0	-0.138462	0.138462	0	0	0	0	0	0	0	0	0	0	0.269231	-0.269231	0	0	0	0	0	0	9.26145	74.1449								
	R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.161538	0	0	0	0.0307692	-0.0307692	0	0	0	0	0	0	0	0	0	0	-0.115385	0.115385	0	0	0	0	0	0	7.78295	8.94808								
	R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0384615	0	0	0	0.230769	-0.230769	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.70696	inf										
	R4(u6)	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0769231	0	0	0	-0.461538	0.461538	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.742582	1.83547											
	R5(s5)	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.161538	0	0	0	0.969231	-0.969231	0	0	0	0	0	0	0	0	0	0	0.115385	-0.115385	0	0	0	0	0	0	0	0	3.33878	inf					
	R6(u19)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.184615	0	0	0	0.107692	-0.107692	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0532734	0.0532734									
	R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0230769	0	0	0	0.138462	-0.138462	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.273855	inf						
	R8(a8)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	-0.807692	0	0	0	0.153846	-0.153846	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0527821	0.0653379								
	R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	-0.646154	0	0	0	0.123077	-0.123077	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.87963	0.590311						
	R10(a10)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	-0.815385	0	0	0	1.10769	-1.10769	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.898405	0.256686								
	R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	-0.753846	0	0	0	0.476923	-0.476923	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.38418	0.392256						
	R12(a12)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	-0.138462	0	0	0	1.16923	-1.16923	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.32458	0.486046								
	R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.946154	0	0	0	-0.323077	0.323077	0	0	0	0	0	1	-1	0	0	-0.0384615	0.0384615	0	0	0	0	0	0	0	0	0.435519	inf						
	R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.161538	0	0	0	-0.0307692	0.0307692	0	0	0	0	0	0	0	0	0	0	0.115385	-0.115385	0	0	0	0	0	0	0	0	4.21705	inf					
	R15(u7)	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0.207692	0	0	0	0.246154	-0.246154	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.92384	inf						
	R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf								
	R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.561538	0	0	0	-0.630769	0.630769	0	0	0	0	0	0	0	0	1	-1	0.115385	-0.115385	0	0	0	0	0	0	0	0	0	0	0.755227	inf			
	R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.123077	0	0	0	1.26154	-1.26154	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.78383	7.22901						
	R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	1.10769	0	0	0	-0.353846	0.353846	0	0	0	0	0	0	0	0	0	0	0.0769231	-0.0769231	0	0	0	0	0	0	0	0	0	0	0.329047	inf			
	R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.02308	0	0	0	-0.138462	0.138462	0	0	0	1	0	0	0	0	0	0	0.269231	-0.269231	0	0	0	0	0	0	0	0	3.04051	0.601936					
	R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.530769	0	0	0	-0.184615	0.184615	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.33167	0.864288						
	R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.769231	0	0	0	-0.384615	0.384615	0	0	0	0	0	0	0	0	0	0	-0.307692	0.307692	0	0	0	0	0	1	-1	0	0	0	0.403481	inf			
	R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.16923	1	-1	0	0.0153846	-0.0153846	0	0	0	0	0	0	0	0	0	0	-0.307692	0.307692	0	0	0	0	0	0	0	0	0	0	1.24026	inf			
	R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.884615	0	-0	0	-0.692308	0.692308	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	1.68913	inf
	R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.915385	0	0	0	0.507692	-0.507692	0	0	0	0	0	0	0	0	0	0	0.346154	-0.346154	1	0	0	0	0	0	0	0	0	0	5.10812	1.08348			
	R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0384615	0	0	0	-0.230769	0.230769	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.29304	11.0598				
	R27(u16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0461538	0	0	0	-0.723077	0.723077	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	1.46678	inf
	R28(u4)	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.738462	0	0	0	-0.430769	-0.430769	0	0	0	0	0	0	0	0	0	0	-0.615385	0.615385	0	0	0	0	0	0	0	0	0	0	0.441821	inf		
												1	0	1	1	0	0	1	0	1	0	1	0	0	1	2.51538	0	1	0	-2.90769	3.90769	0	0	1	0	0	1	0	1	0	1	-0.346154	1.34615	0	0	1	0	1	0	1	0	1	0	-2.65994					

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 19/31 | PHASE I step 18 | ENTER: u17 | LEAVE: a12

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u17 enters, a12 leaves

Reduced cost of entering variable: -2.90769

Minimum ratio theta*: 0.277601

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

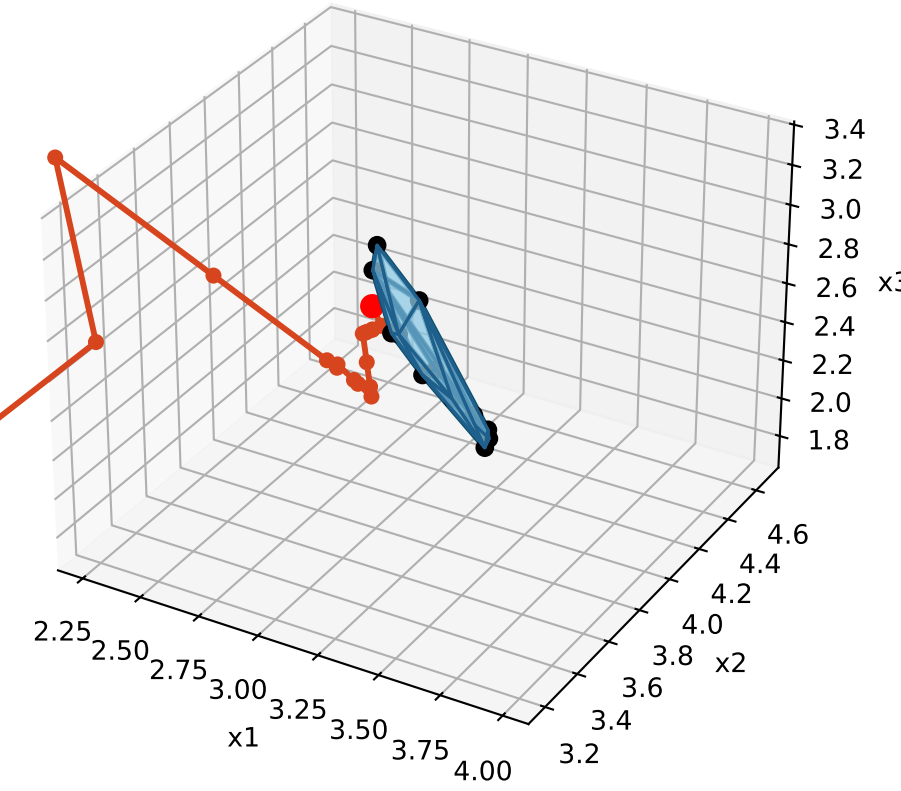
Current solution: $x_1=2.70011$, $x_2=4.22559$, $x_3=2.3571$

Tableau objective: -1.85277

[illegible]

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

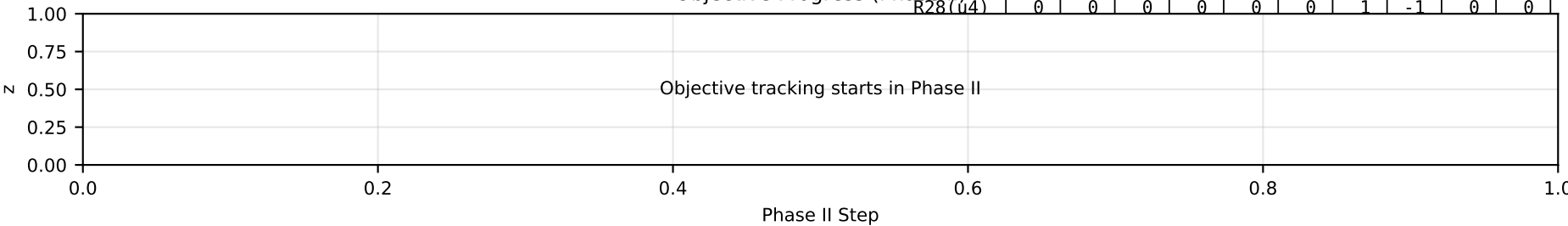


State 20/31 | PHASE I step 19 | ENTER: u12 | LEAVE: a8

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u12 enters, a8 leaves.
Reduced cost of entering variable: -1.48684
Minimum ratio theta*: 0.0765644
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

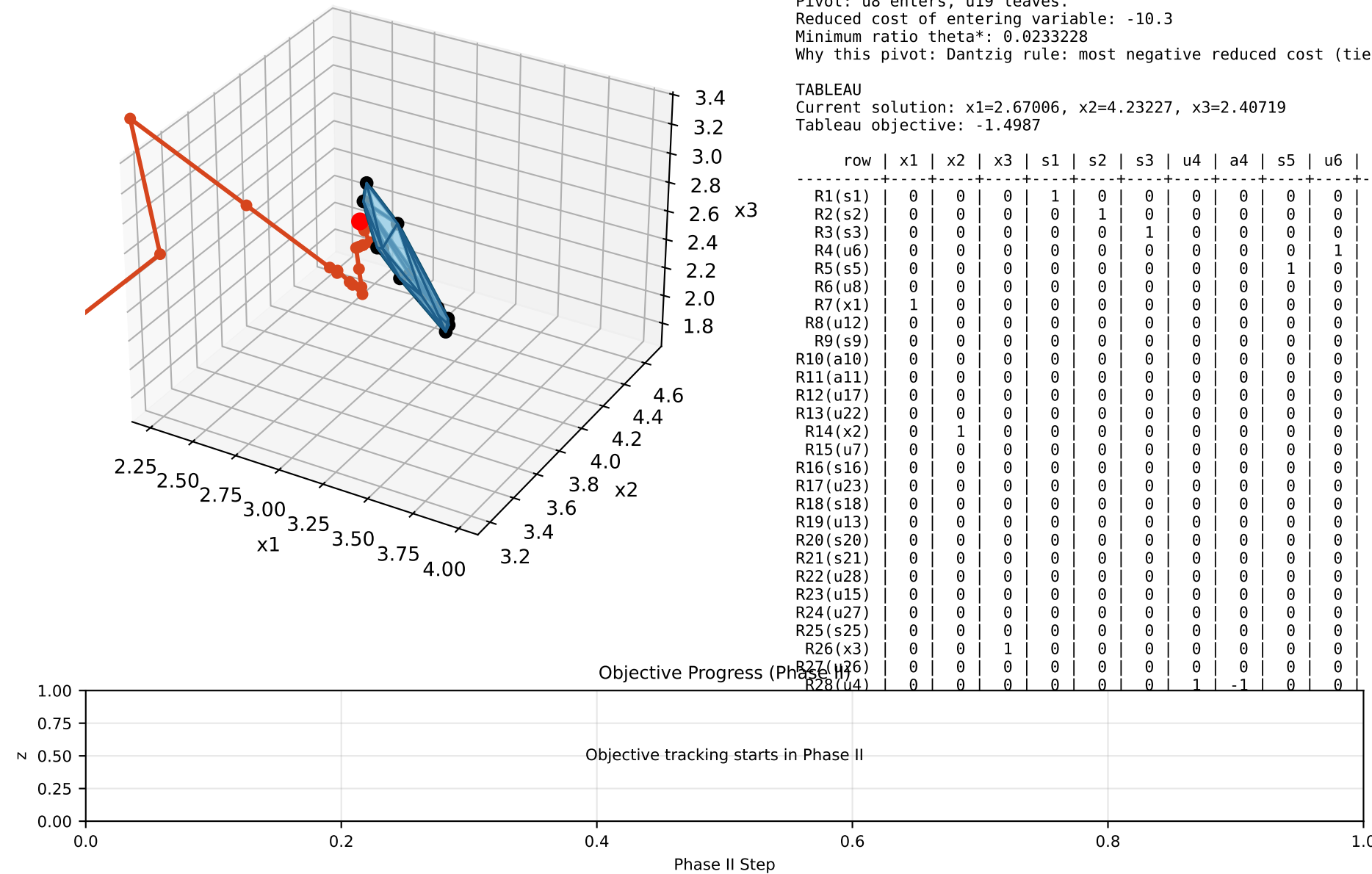
TABLEAU
Current solution: x1=2.69105, x2=4.2276, x3=2.37221
Tableau objective: -1.73893

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio					
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	0	-0.9	0.9	0	0	0	0	0	0	0	0	0	0	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0.65	-0.65	0	0	0	0	0	0	0	9.30895	inf					
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0	0.2	-0.2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7.7724	295.428						
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.62779	48.8574					
R4(u6)	0	0	0	0	0	0	0	0	0	1	-1	0	0	-3	3	0	0	0	0	0	0	0	0	0	0	-2.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.900928	inf					
R5(s5)	0	0	0	0	0	0	0	0	1	0	0	0	0	6.3	-6.3	0	0	0	0	0	0	0	0	0	0	5.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.00626	3.70316				
R6(u19)	0	0	0	0	0	0	0	0	0	0	0	0	0	0.7	-0.7	0	0	0	0	0	0	0	0	0	0	0.75	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0163259	0.253818					
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0.9	-0.9	0	0	0	0	0	0	0	0	0	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.69105	22.801				
R8(u12)	0	0	0	0	0	0	0	0	0	0	0	0	0	-7.6	7.6	0	0	0	0	0	1	-1	0	0	-6	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0765644	0.0765644				
R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	0	0.8	-0.8	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.83741	17.5319				
R10(a10)	0	0	0	0	0	0	0	0	0	0	0	0	0	7.2	-7.2	0	-1	1	0	0	0	0	0	0	0	5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.518374	0.623737			
R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	0	3.1	-3.1	0	0	0	-1	1	0	0	0	0	0	1.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.22055	3.06889			
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0	0	-6.5	6.5	0	0	0	0	0	0	0	0	0	0	-5.25	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.343084	inf			
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0	0	-2.1	2.1	0	0	0	0	0	0	0	0	0	0	-0.75	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0.85	-0.85	0	0	0	0	0	0	0	0	0.546362	inf			
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0	-0.2	0.2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.2276	inf				
R15(u7)	0	0	0	0	0	0	0	0	0	0	0	0	0	1.6	-1.6	0	0	0	0	0	0	0	0	0	0	1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.83939	8.81368			
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf			
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	0	-4.1	4.1	0	0	0	0	0	0	0	0	0	0	-2.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.971634	inf			
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0	8.2	-8.2	0	0	0	0	0	0	0	0	0	0	6.5	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.35101	4.10921	
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0	0	-2.3	2.3	0	0	0	0	0	0	0	0	1	-1	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.450445	inf			
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.9	0.9	0	0	0	0	0	0	0	0	0	0	-1.75	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	3.08801	inf			
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.2	1.2	0	0	0	0	0	0	0	0	0	0	-1.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.39501	inf			
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0	0	-2.5	2.5	0	0	0	0	0	0	0	0	0	0	-1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.535437	inf			
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0.1	-0.1	0	0	0	0	0	0	0	0	0	0	1.25	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.23499	93.9355		
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0	-4.5	4.5	0	0	0	0	0	0	0	0	0	0	-2.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.92665	inf		
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0	3.3	-3.3	0	0	0	0	0	0	0	0	0	0	1.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.93394	11.4396	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	-1.5	1.5	0	0	0	0	0	0	0	0	0	0	-1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.37221	inf		
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	0	-4.7	4.7	0	0	0	0	0	0	0	0	0	0	-3.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.71486	inf		
R28(u4)	0	0	0	0	0	0	1	-1	0	0	0	0	0	2.8	-2.8	0	0	0	0	0	0	0	0	0	0	3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.294031	0.874648			
											1	0	1	-10.3	11.3	0	1	0	1	0	0	1	0	1	0	-6.75	0	1	0	0	1	0	0	1	0	0	0	0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	-1.73893	



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 21/31 | PHASE I step 20 | ENTER: u8 | LEAVE: u19

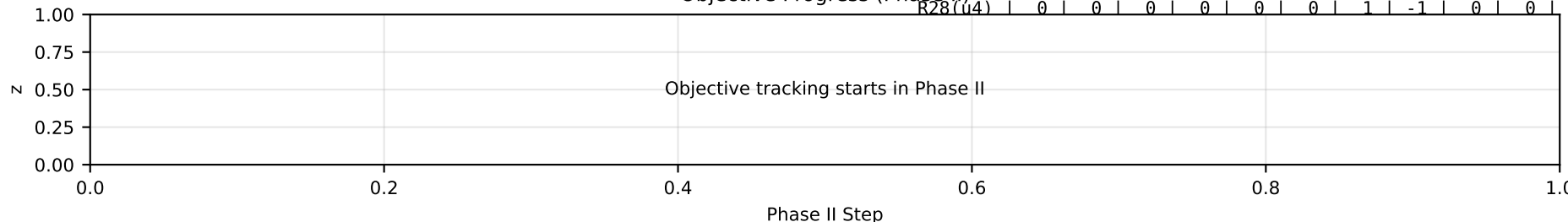
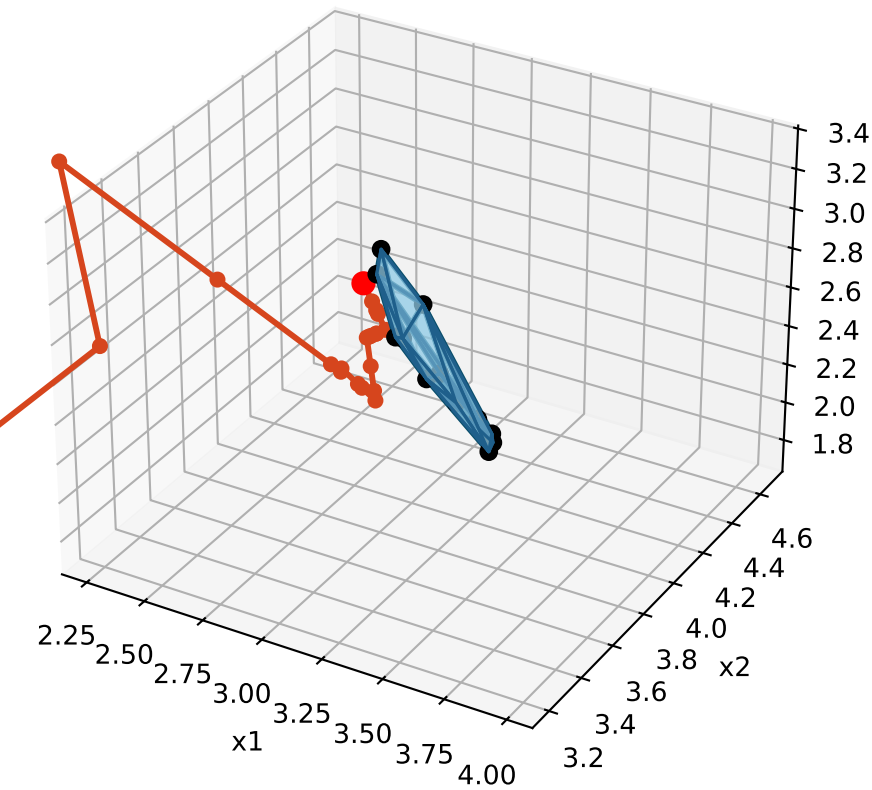
COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u8 enters, u19 leaves.
Reduced cost of entering variable: -10.3
Minimum ratio theta*: 0.0233228
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU
Current solution: x1=2.67006, x2=4.23227, x3=2.40719
Tableau objective: -1.4987

	row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13		s14	u15	a15	s16	u17	a17	s18		u19		a19	s20	s21	u22	a22	u23	a23		u24		a24	s25	u26	a26	u27	a27	u28	a28		rhs	ratio
	R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.214286	0	0	0	0	0	0	0	1.28571	-1.28571	0	0	0	0	0	0	0.0714286	-0.0714286	0	0	0	0	0	0	0	0	0	0	9.32994	inf	
	R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.214286	0	0	0	0	0	0	0	-0.285714	0.285714	0	0	0	0	0	0	-0.0714286	0.0714286	0	0	0	0	0	0	0	0	0	0	7.76773	38.862	
	R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.357143	0	0	0	0	0	0	0	-2.14286	2.14286	0	0	0	0	0	0	0.214286	-0.214286	0	0	0	0	0	0	0	0	0	0	9.59281	6.41853	
	R4(u6)	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.714286	0	0	0	0	0	0	0	4.28571	-4.28571	0	0	0	0	0	0	-0.428571	0.428571	0	0	0	0	0	0	0	0	0	0	0.970897	inf	
	R5(s5)	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.5	0	0	0	0	0	0	0	-9	9	0	0	0	0	0	0	1.5	-1.5	0	0	0	0	0	0	0	0	0	2.85932	0.477183		
	R6(u8)	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	1.07143	0	0	0	0	0	0	0	1.42857	-1.42857	0	0	0	0	0	0	-0.642857	0.642857	0	0	0	0	0	0	0	0	0	0	0.0233228	0.0233228	
	R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.214286	0	0	0	0	0	0	0	-1.28571	1.28571	0	0	0	0	0	0	-0.0714286	0.0714286	0	0	0	0	0	0	0	0	0	0	2.67006	2.99005	
	R8(u12)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.14286	0	0	0	0	0	0	0	10.8571	-10.8571	0	0	0	0	0	0	-1.28571	1.28571	0	0	0	0	0	0	0	0	0	0	0.253818	inf	
	R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	-0.857143	0	0	0	0	0	0	0	-1.14286	1.14286	0	0	0	0	0	0	0.714286	-0.714286	0	0	0	0	0	0	0	0	0	0	1.81875	2.29676	
	R10(a10)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	-2.71429	0	0	0	0	0	0	0	-10.2857	10.2857	0	0	0	0	0	0	1.42857	-1.42857	0	0	0	0	0	0	0	0	0	0	0.35045	0.0719964	
	R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1	1	0	0	0	0	0	-1.57143	0	0	0	0	0	0	0	-4.42857	4.42857	0	0	0	0	0	0	1.14286	-1.14286	0	0	0	0	0	0	0	0	0	0	1.14825	0.393727	
	R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.71429	0	0	0	1	-1	0	0	9.28571	-9.28571	0	0	0	0	0	0	-1.42857	1.42857	0	0	0	0	0	0	0	0	0	0	0.494682	inf	
	R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.5	0	0	0	0	0	0	0	3	-3	0	0	1	-1	0	0	-0.5	0.5	0	0	0	0	0	0	0	0	0	0.595339	inf		
	R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.214286	0	0	0	0	0	0	0	0.285714	-0.285714	0	0	0	0	0	0	0.0714286	-0.0714286	0	0	0	0	0	0	0	0	0	0	4.23227	inf	
	R15(u7)	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	-0.214286	0	0	0	0	0	0	0	-2.28571	2.28571	0	0	0	0	0	0	-0.0714286	0.0714286	0	0	0	0	0	0	0	0	0	0	1.80208	1.14962	
	R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf						
	R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.64286	0	0	0	0	0	0	0	5.85714	-5.85714	0	0	0	0	1	-1	-0.785714	0.785714	0	0	0	0	0	0	0	0	0	0	1.06726	inf	
	R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-2.28571	0	0	0	0	0	1	0	-11.7143	11.7143	0	0	0	0	0	0	1.57143	-1.57143	0	0	0	0	0	0	0	0	0	0	4.15977	0.530611	
	R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	1.71429	0	0	0	0	0	0	0	3.28571	-3.28571	0	0	0	0	0	0	-0.428571	0.428571	0	0	0	0	0	0	0	0	0	0	0.504088	inf		
	R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.785714	0	0	0	0	0	0	0	1.28571	-1.28571	1	0	0	0	0	0	0.0714286	-0.0714286	0	0	0	0	0	0	0	0	0	0	3.109	inf	
	R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.214286	0	0	0	0	0	0	0	1.71429	-1.71429	0	1	0	0	0	0	-0.0714286	0.0714286	0	0	0	0	0	0	0	0	0	0	2.42299	inf	
	R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.42857	0	0	0	0	0	0	0	3.57143	-3.57143	0	0	0	0	0	0	-0.857143	0.857143	0	0	0	0	0	0	0	0	1	-1	0.593744	inf	
	R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.14286	1	-1	0	0	0	0	0	-0.142857	0.142857	0	0	0	0	0	0	-0.285714	0.285714	0	0	0	0	0	0	0	0	0	0	1.23265	12.3499	
	R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.07143	0	0	0	0	0	0	0	6.42857	-6.42857	0	0	0	0	0	0	-0.642857	0.642857	0	0	0	0	1	-1	0	0	0	0	2.0316	inf	
	R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.78571	0	0	0	0	0	0	0	-4.71429	4.71429	0	0	0	0	0	0	1.07143	-1.07143	1	0	0	0	0	0	0	0	0	0	4.85697	1.49513	
	R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.357143	0	0	0	0	0	0	0	2.14286	-2.14286	0	0	0	0	0	0	-0.214286	0.214286	0	0	0	0	0	0	0	0	0	0	2.40719	inf	
	R27(u36)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0																																

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path



State 22/31 | PHASE I step 21 | ENTER: a19 | LEAVE: a10

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: a19 enters, a10 leaves.
Reduced cost of entering variable: -13.7143
Minimum ratio theta*: 0.0340715
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

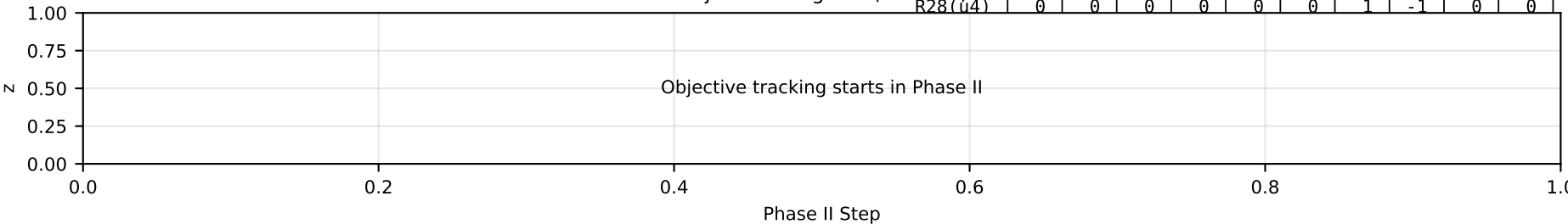
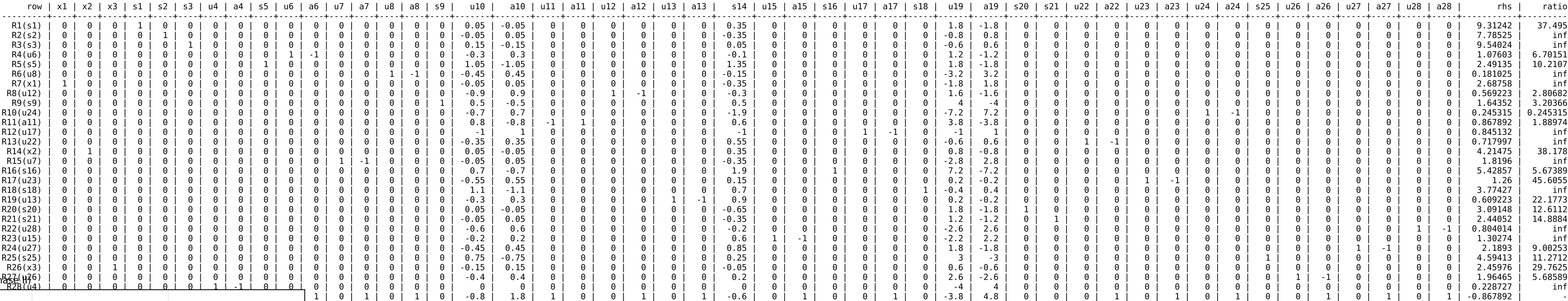
TABLEAU
Current solution: x1=2.62625, x2=4.242, x3=2.4802
Tableau objective: -1.03143

row	x1	x2	x3	s1	s2	s3	u4	a4	s5	u6	a6	u7	a7	u8	a8	s9	u10	a10	u11	a11	u12	a12	u13	a13	s14	u15	a15	s16	u17	a17	s18	u19	a19	s20	s21	u22	a22	u23	a23	u24	a24	s25	u26	a26	u27	a27	u28	a28	rhs	ratio	
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	-0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0.25	-0.25	0	0	0	0	0	0	0	0	9.37375	inf	
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0.0277778	-0.0277778	0	0	0	0	0	0	-0.138889	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.111111	0.111111	0	0	0	0	0	0	0	0	7.758	27.1871
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0.208333	-0.208333	0	0	0	0	0	0	0.208333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.5198	4.47664	
R4(u6)	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	-0.416667	0.416667	0	0	0	0	0	0	-0.416667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.11692	inf	
R5(s5)	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0.875	-0.875	0	0	0	0	0	0	0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.55268	0.317702	
R6(u8)	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	-0.138889	0.138889	0	0	0	0	0	0	0.694444	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0719964	inf	
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.125	-0.125	0	0	0	0	0	0	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.62625	2.07671
R8(u12)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-1.05556	1.05556	0	0	1	-1	0	0	-0.722222	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.623737	inf	
R9(s9)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0.111111	-0.111111	0	0	0	0	0	0	-0.555556	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.77981	1.59141	
R10(a19)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0972222	0.0972222	0	0	0	0	0	0	-0.263889	0	0	0	0	0	0	-1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0340715	0.0340715		
R11(a11)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.430556	-0.430556	-1	1	0	0	0	0	-0.402778	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.997363	0.259283	
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.902778	0.902778	0	0	0	0	0	0	-0.736111	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.81106	inf	
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.291667	0.291667	0	0	0	0	0	0	0.708333	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0	0	0	0.697554	inf	
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.0277778	0.0277778	0	0	0	0	0	0	0.138889	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.242	inf	
R15(u7)	0	0	0	0	0	0	0	0	0	0	0	1	-1	0	0	0	0.222222	-0.222222	0	0	0	0	0	0	0.388889	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.7242	0.788409
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5.67389	inf		
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.569444	0.569444	0	0	0	0	0	0	0.0972222	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.26682	inf	
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.13889	-1.13889	0	0	0	0	0	0	0.805556	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.76064	0.355102	
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.319444	0.319444	0	0	0	0	1	-1	0.847222	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.616037	inf	
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.125	0.125	0	0	0	0	0	0	-1.125	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	3.15281	inf	
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.166667	0.166667	0	0	0	0	0	0	-0.666667	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	2.4814	inf	
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.347222	0.347222	0	0	0	0	0	0	0.486111	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	-1	0.715428	inf		
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0138889	-0.0138889	0	0	0	0	0	0	1.18056	1	-1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.22779	8.62857
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.625	0.625	0	0	0	0	0	0	0.375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.25063	inf	
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.458333	-0.458333	0	0	0	0	0	0	-0.541667	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4.69635	1.03027	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.208333	0.208333	0	0	0	0	0	0	-0.208333	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.4802	inf	
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	-0.652778	0.652778	0	0	0	0	0	0	-0.486111	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.05324	inf	
R28(u4)	0	0	0	0	0	0	1	-1	0	0	0	0	0	0	0	0	0.388889	-0.388889	0	0	0	0	0	0	1.05556	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0924408	0.0571818	
									1	0	1	0	1	0	1	0	-0.333333	1.33333	1	0	0	1	0	1	0.666667	0	1	0	0	1	0	1	0	0	0	1	0	1	-0.666667	1.66667	0	0	1	0	1	0	1	0	-1.03143	-	

State 23/31 | PHASE I step 22 | ENTER: u24 | LEAVE: a19

```
COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u24 enters, a19 leaves.
Reduced cost of entering variable: -0.666667
Minimum ratio theta*: 0.245315
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).
```

TABLEAU
Current solution: $x_1=2.68758$, $x_2=4.21475$, $x_3=2.45976$
Tableau objective: -0.867892



State 24/31 | PHASE I step 23 | ENTER: u19 | LEAVE: a11

COMMENTS:

Teaching Mode | Rule: DANTZIG

Pivot: u19 enters, all leaves

Reduced cost of entering variable: -3.8

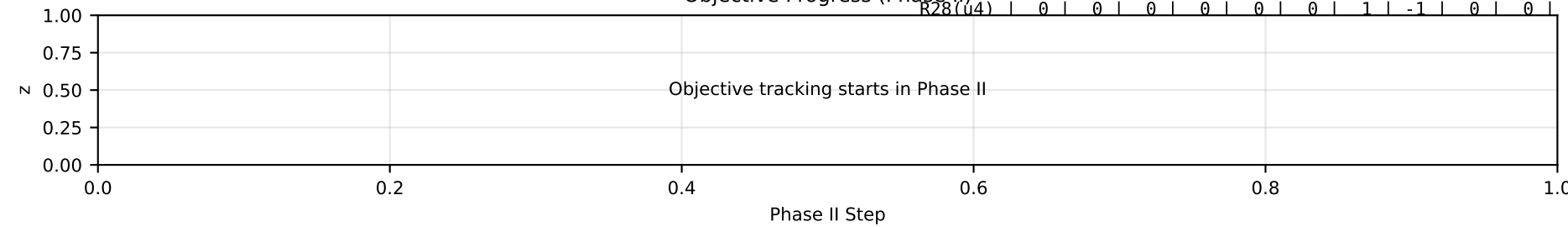
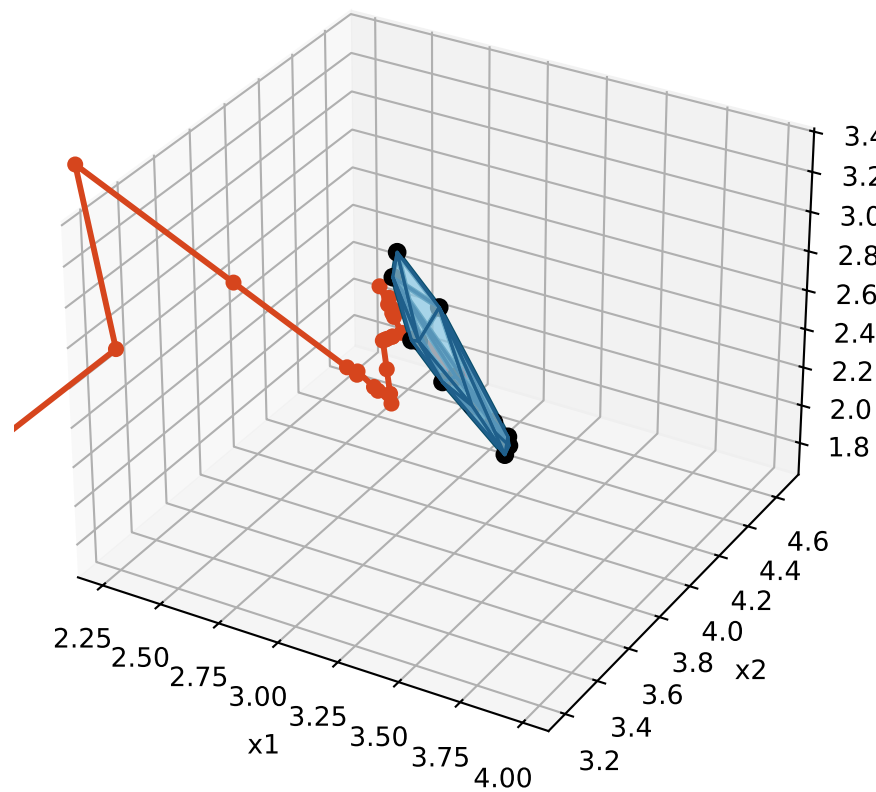
Minimum ratio theta*: 0.22839

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

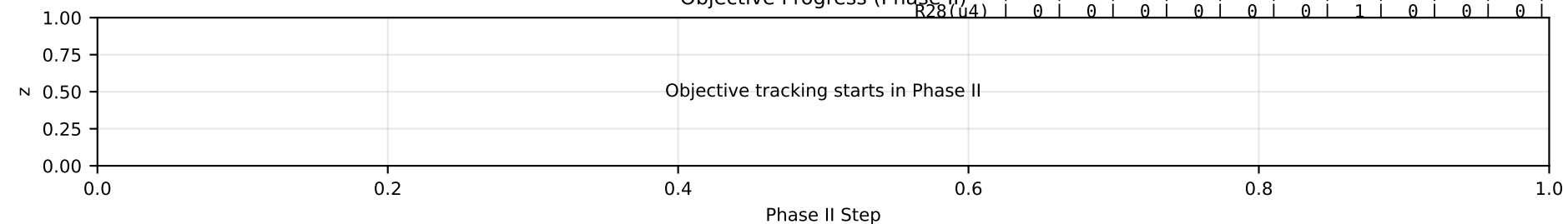
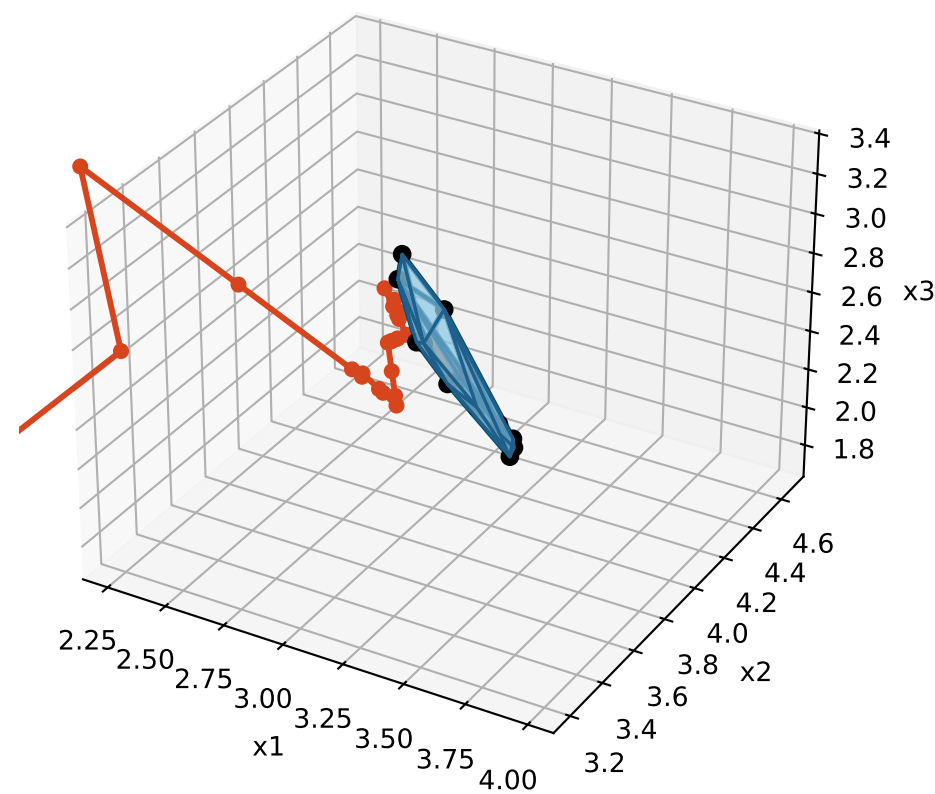
TABLEAU

Current solution: $x_1=3.09869$, $x_2=4.03203$, $x_3=2.32273$

Tableau objective: 0



Feasible polytope + extreme points + simplex path



State 25/31 | PHASE I -> PHASE II step 0

COMMENTS

Teaching Mode | Phase Transition

Phase I objective value: 7.06102e-14 (should be 0)

Artificial vars removed: a4, a6, a7, a8, a10, a11, a12, a13, a15, a17, a19, a22, a23, a24, a26, a27, a28

No artificial variable remained basic before cleanup.

Phase I complete. Artificial variables removed before restoring original objective.

TABLEAU

Current solution: $x_1=3.09869$, $x_2=4.03203$, $x_3=2.32273$

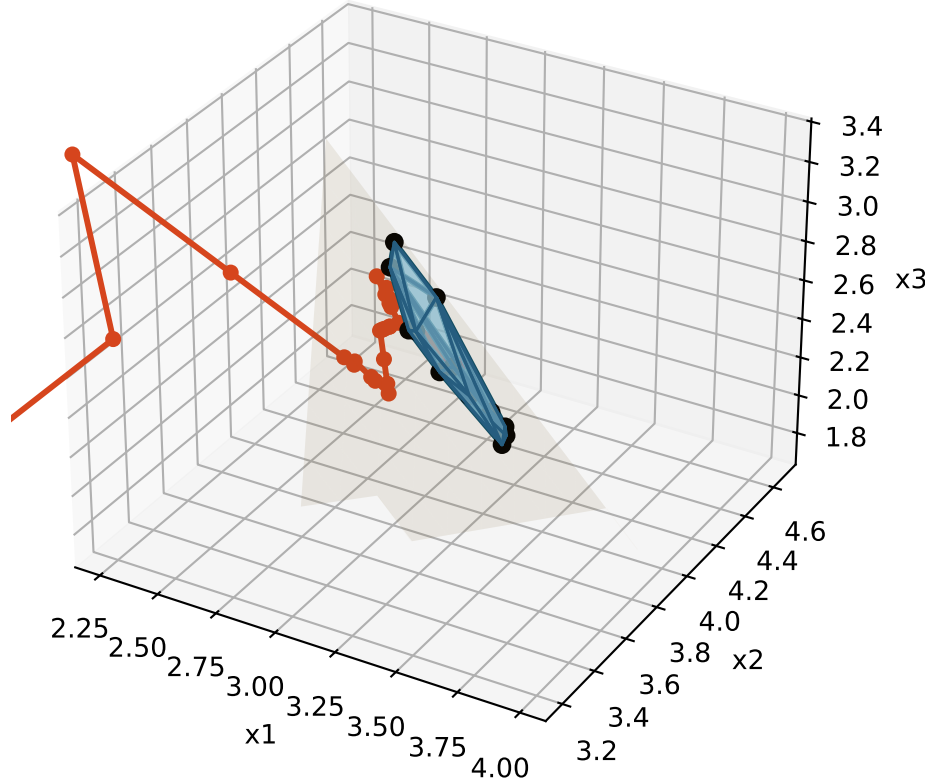
Tableau objective: 0

[illegible]

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$15x_1 + 10x_2 + 12x_3 = 115$



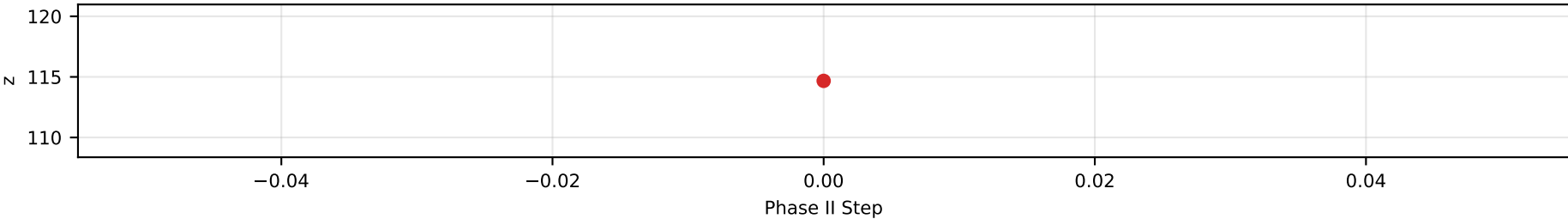
State 26/31 | PHASE II step 0 | Z=114.673

COMMENTS
Teaching Mode | PHASE II
Phase II objective restored and made basis-consistent.

TABLEAU
Current solution: x1=3.09869, x2=4.03203, x3=2.32273
Objective z: 114.673

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	8.90131	inf	
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	0.118421	-0.210526	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	7.96797	inf	
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	0.276316	-0.157895	0	0	0.144737	0	0	0	0	0	0	0	0	0	0	0	0	0	9.67727	inf	
R4(u6)	0	0	0	0	0	0	0	0	1	0	0	0	-0.552632	0.315789	0	0	-0.289474	0	0	0	0	0	0	0	0	0	0	0	0	0	0.801961	inf	
R5(s5)	0	0	0	0	0	0	0	1	0	0	0	0	0.671053	0.473684	0	0	1.06579	0	0	0	0	0	0	0	0	0	0	0	0	0	2.08024	inf	
R6(u8)	0	0	0	0	0	0	0	0	0	0	1	0	0.223684	-0.842105	0	0	0.355263	0	0	0	0	0	0	0	0	0	0	0	0	0	0.911881	inf	
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	0.328947	-0.473684	0	0	-0.0657895	0	0	0	0	0	0	0	0	0	0	0	0	0	3.09869	inf	
R8(u12)	0	0	0	0	0	0	0	0	0	0	0	0	-1.23684	0.421053	1	0	-0.552632	0	0	0	0	0	0	0	0	0	0	0	0	0	0.203795	inf	
R9(s9)	0	0	0	0	0	0	0	0	0	0	0	1	-0.342105	1.05263	0	0	-0.131579	0	0	0	0	0	0	0	0	0	0	0	0	0	0.729953	inf	
R10(u24)	0	0	0	0	0	0	0	0	0	0	0	0	0.815789	-1.89474	0	0	-0.763158	0	0	0	0	0	0	0	0	0	1	0	0	0	1.88974	inf	
R11(u19)	0	0	0	0	0	0	0	0	0	0	0	0	0.210526	-0.263158	0	0	0.157895	0	0	0	0	1	0	0	0	0	0	0	0	0	0.228393	inf	
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0	-0.789474	-0.263158	0	0	-0.842105	0	0	1	0	0	0	0	0	0	0	0	0	0	1.07352	inf	
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0	-0.223684	-0.157895	0	0	0.644737	0	0	0	0	0	0	0	1	0	0	0	0	0	0.855033	inf	
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	-0.118421	0.210526	0	0	0.223684	0	0	0	0	0	0	0	0	0	0	0	0	0	4.03203	inf	
R15(u7)	0	0	0	0	0	0	0	0	0	1	0	0	0.539474	-0.736842	0	0	0.0921053	0	0	0	0	0	0	0	0	0	0	0	0	0	2.4591	inf	
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	-0.815789	1.89474	0	0	0.763158	0	1	0	0	0	0	0	0	0	0	0	0	0	3.78415	inf	
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	-0.592105	0.0526316	0	0	0.118421	0	0	0	0	0	0	0	0	1	0	0	0	0	1.21433	inf	
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	1.18421	-0.105263	0	0	0.763158	0	0	0	1	0	0	0	0	0	0	0	0	0	3.86563	inf	
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0	-0.342105	0.0526316	0	1	0.868421	0	0	0	0	0	0	0	0	0	0	0	0	0	0.563544	inf	
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	-0.328947	0.473684	0	0	-0.934211	0	0	0	0	0	1	0	0	0	0	0	0	0	2.68037	inf	
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	-0.302632	0.315789	0	0	-0.539474	0	0	0	0	0	0	1	0	0	0	0	0	0	2.16645	inf	
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0	-0.0526316	-0.684211	0	0	0.210526	0	0	0	0	0	0	0	0	0	0	0	0	1	1.39783	inf	
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	0.263158	-0.578947	0	0	0.947368	1	0	0	0	0	0	0	0	0	0	0	0	0	1.80521	inf	
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	-0.828947	0.473684	0	0	0.565789	0	0	0	0	0	0	0	0	0	0	0	0	1	1.7782	inf	
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	0.118421	0.789474	0	0	-0.223684	0	0	0	0	0	0	0	0	0	0	1	0	0	3.90896	inf	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	-0.276316	0.157895	0	0	-0.144737	0	0	0	0	0	0	0	0	0	0	0	0	0	2.32273	inf	
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	-0.947368	0.684211	0	0	-0.210526	0	0	0	0	0	0	0	0	0	0	0	1	0	1.37083	inf	
R28(u4)	0	0	0	0	0	0	1	0	0	0	0	0	0.842105	-1.05263	0	0	0.631579	0	0	0	0	0	0	0	0	0	0	0	0	0	1.1423	inf	
Rz	0	0	0	0	0	0	0	0	0	0	0	0	0.434211	-3.10526	0	0	-0.486842	0	0	0	0	0	0	0	0	0	0	0	0	0	114.673	-	

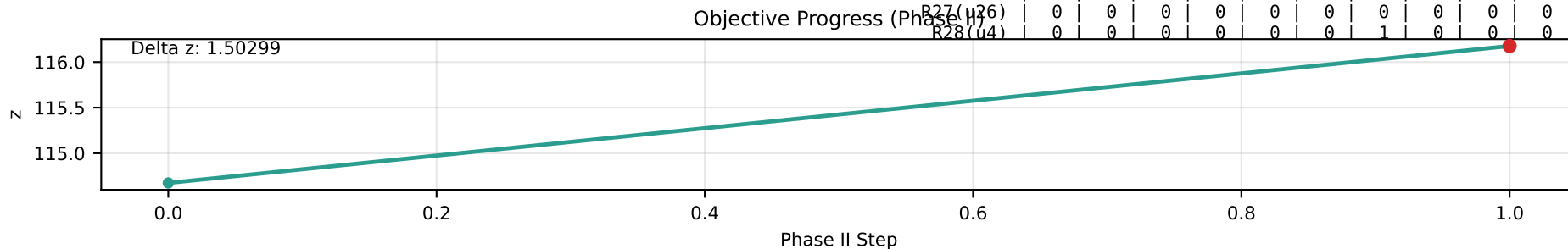
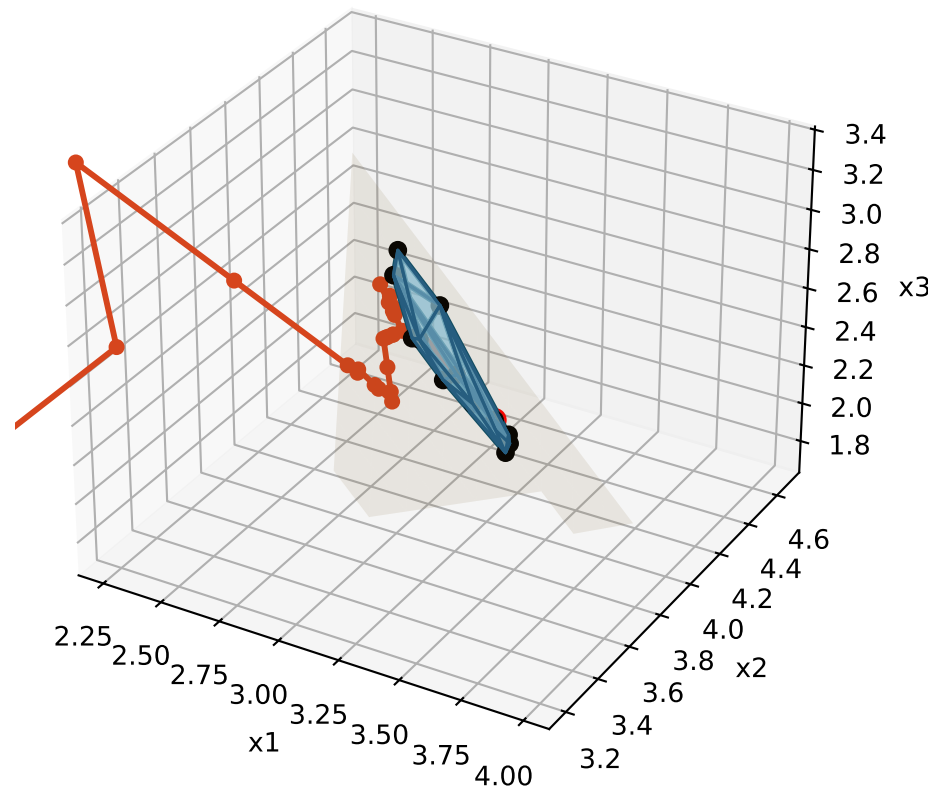
Objective Progress (Phase II)



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 116$$



State 27/31 | PHASE II step 1 | ENTER: u11 | LEAVE: u12 | Z=116.176

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u11 enters, u12 leaves.

Reduced cost of entering variable: -3.10526

Minimum ratio theta*: 0.484012

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

Current solution: $x_1=3.32795$, $x_2=3.93014$, $x_3=2.2463$

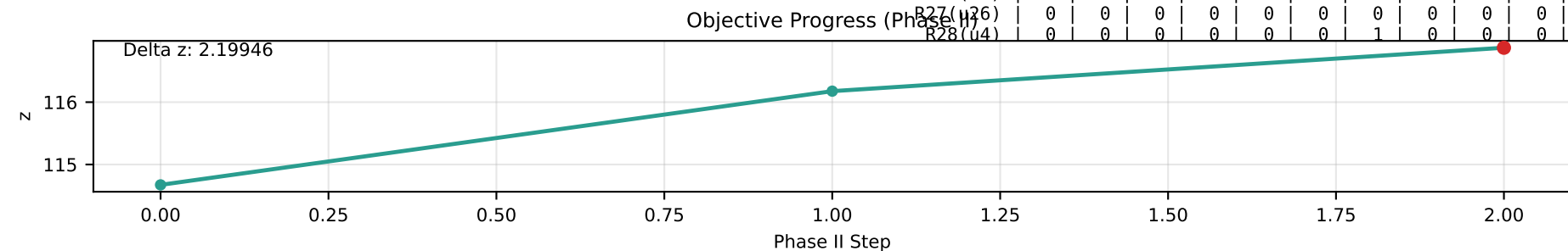
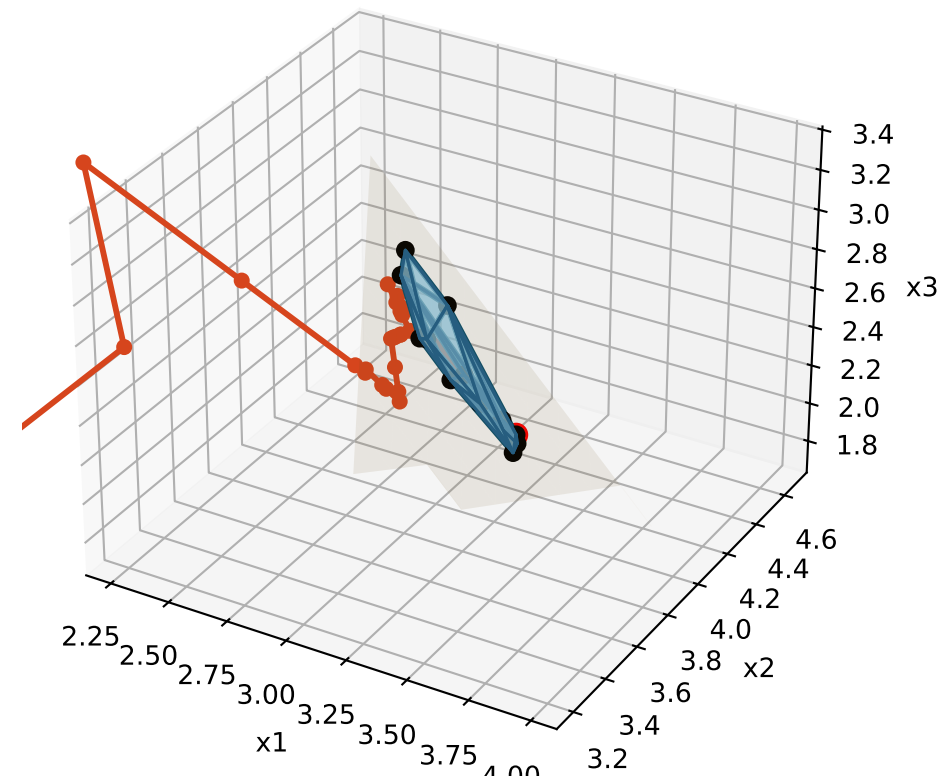
Objective z: 116.176

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	0	1.0625	0	-1.125	0	0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.67205	18.7917
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0	-0.5	0	0.5	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.06986	inf
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0	-0.1875	0	0.375	0	-0.0625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.7537	inf
R4(u6)	0	0	0	0	0	0	0	0	1	0	0	0	0.375	0	-0.75	0	0.125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.649115	2.53954
R5(s5)	0	0	0	0	0	0	0	1	0	0	0	0	2.0625	0	-1.125	0	1.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.85097	4.39162
R6(u8)	0	0	0	0	0	0	0	0	0	1	0	0	-2.25	0	2	0	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.31947	inf
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0	-1.0625	0	1.125	0	-0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.32795	inf
R8(u11)	0	0	0	0	0	0	0	0	0	0	0	0	-2.9375	1	2.375	0	-1.3125	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.484012	0.484012
R9(s9)	0	0	0	0	0	0	0	0	0	0	0	1	2.75	0	-2.5	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.220467	0.693456
R10(u24)	0	0	0	0	0	0	0	0	0	0	0	0	-4.75	0	4.5	0	-3.25	0	0	0	0	0	0	0	0	0	1	0	0	0	0	2.80682	inf
R11(u19)	0	0	0	0	0	0	0	0	0	0	0	0	-0.5625	0	0.625	0	-0.1875	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0.355764	inf
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0	-1.5625	0	0.625	0	-1.1875	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1.2009	inf
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0	-0.6875	0	0.375	0	0.4375	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0.931456	inf
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	0	0.5	0	-0.5	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.93014	19.1522
R15(u7)	0	0	0	0	0	0	0	0	0	1	0	0	-1.625	0	1.75	0	-0.875	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.81574	inf
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	0	4.75	0	-4.5	0	3.25	0	1	0	0	0	0	0	0	0	0	0	0	0	0	2.86707	1.99719
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0	-0.4375	0	-0.125	0	0.1875	0	0	0	0	0	0	0	0	0	1	0	0	0	0	1.18885	23.0722
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0	0.875	0	0.25	0	0.625	0	0	0	1	0	0	0	0	0	0	0	0	0	0	3.91658	inf
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0	-0.1875	0	-0.125	1	0.9375	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.53807	10.7073
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	0	1.0625	0	-1.125	0	-0.3125	0	0	0	0	0	1	0	0	0	0	0	0	0	0	2.4511	5.65856
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	0	0.625	0	-0.75	0	-0.125	0	0	0	0	0	0	1	0	0	0	0	0	0	0	2.0136	6.86041
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0	-2.0625	0	1.625	0	-0.6875	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.729	inf
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0	-1.4375	0	1.375	0	0.1875	1	0	0	0	0	0	0	0	0	0	0	0	0	0	2.08542	inf
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	0	0.5625	0	-1.125	0	1.1875	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1.54893	3.75397
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	0	2.4375	0	-1.875	0	0.8125	0	0	0	0	0	0	0	0	0	0	1	0	0	0	3.52684	4.95134
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	0	0.1875	0	-0.375	0	0.0625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.2463	14.7106
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	0	1.0625	0	-1.625	0	0.6875	0	0	0	0	0	0	0	0	0	0	0	1	0	0	1.03967	2.00352
R28(u4)	0	0	0	0	0	0	1	0	0	0	0	0	-2.25	0	2.5	0	-0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.65178	inf
base													-8.6875	0	7.375	0	-4.5625	0	0	0	0	0	0	0	0	0	0	0	0	0	0	116.176	

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

$$15x_1 + 10x_2 + 12x_3 = 117$$



State 28/31 | PHASE II step 2 | ENTER: u10 | LEAVE: s9 | Z=116.873

COMMENTS

Teaching Mode | Rule: DANTZIG

Pivot: u10 enters, s9 leaves.

Reduced cost of entering variable: -8.6875

Minimum ratio theta*: 0.0801697

Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU

Current solution: $x_1=3.41314$, $x_2=3.89005$, $x_3=2.23127$

Objective z: 116.873

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	-0.386364	0	0	-0.159091	0	0.204545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.58686	8.16193
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0.181818	0	0	0.0454545	0	-0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.10995	inf
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0.0681818	0	0	0.204545	0	0.0227273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.76873	inf
R4(u6)	0	0	0	0	0	0	0	0	1	0	0	-0.136364	0	0	-0.409091	0	-0.0454545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.619051	1.73097
R5(s5)	0	0	0	0	0	0	0	1	0	0	0	-0.75	0	0	0.75	0	0.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.68562	0.897442
R6(u8)	0	0	0	0	0	0	0	0	0	0	1	0.818182	0	0	-0.0454545	0	0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.49985	inf
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0.386364	0	0	0.159091	0	-0.204545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.41314	inf
R8(u11)	0	0	0	0	0	0	0	0	0	0	0	1.06818	0	1	-0.295455	0	0.0227273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.719511	inf
R9(u10)	0	0	0	0	0	0	0	0	0	0	0	0.363636	1	0	-0.909091	0	0.454545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.0801697	0.0801697
R10(u24)	0	0	0	0	0	0	0	0	0	0	0	1.72727	0	0	0.181818	0	-1.09091	0	0	0	0	0	0	0	0	0	1	0	0	0	0	3.18762	inf
R11(u19)	0	0	0	0	0	0	0	0	0	0	0	0.204545	0	0	0.113636	0	0.0681818	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0.40086	inf
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0.568182	0	0	-0.795455	0	-0.477273	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1.32616	inf
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0.25	0	0	-0.25	0	0.75	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0.986572	inf
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	-0.181818	0	0	-0.0454545	0	0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.89005	7.86027
R15(u7)	0	0	0	0	0	0	0	0	0	1	0	0.590909	0	0	0.272727	0	-0.136364	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.94601	inf
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	-1.72727	0	0	-0.181818	0	1.09091	0	1	0	0	0	0	0	0	0	0	0	0	0	0	2.48626	0.603594
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	0.159091	0	0	-0.522727	0	0.386364	0	0	0	0	0	0	0	0	0	1	0	0	0	0	1.22393	inf
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	-0.318182	0	0	1.04545	0	0.227273	0	0	0	1	0	0	0	0	0	0	0	0	0	0	3.84643	4.47609
R19(u13)	0	0	0	0	0	0	0	0	0	0	0	0.0681818	0	0	-0.295455	1	1.02273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.553102	inf
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	-0.386364	0	0	-0.159091	0	-0.795455	0	0	0	0	0	1	0	0	0	0	0	0	0	0	2.36592	2.30692
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	-0.227273	0	0	-0.181818	0	-0.409091	0	0	0	0	0	0	1	0	0	0	0	0	0	0	1.96349	3.22176
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0.75	0	0	-0.25	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.89435	inf
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0.522727	0	0	0.0681818	0	0.840909	1	0	0	0	0	0	0	0	0	0	0	0	0	0	2.20067	inf
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	-0.204545	0	0	-0.613636	0	0.931818	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1.50383	2.75365
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	-0.886364	0	0	0.340909	0	-0.295455	0	0	0	0	0	0	0	0	0	0	1	0	0	0	3.33143	1.44691
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	-0.0681818	0	0	-0.204545	0	-0.0227273	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.23127	11.9803
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	-0.386364	0	0	-0.659091	0	0.204545	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.954486	0.978509
R28(u4)	0	0	0	0	0	0	1	0	0	0	0	0.818182	0	0	0.454545	0	0.272727	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.83217	inf
phase 4												3.15909	0	0	-0.522727	0	-0.613636	0	0	0	0	0	0	0	0	0	0	0	0	0	0	116.873	

Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

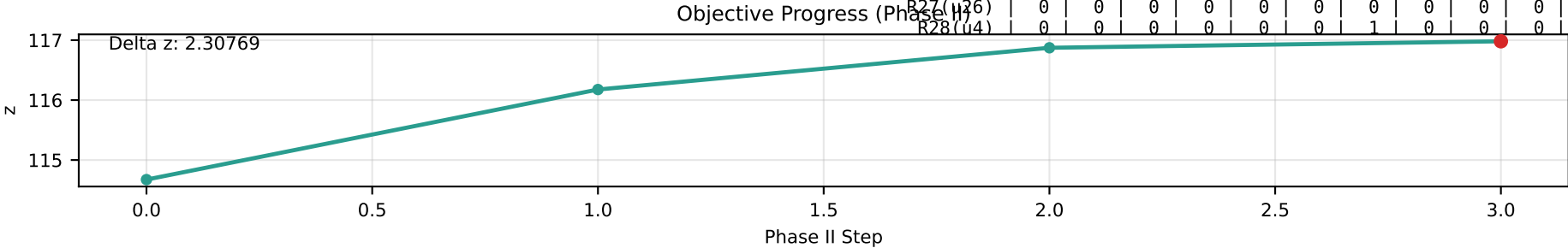
15x1 + 10x2 + 12x3 = 117

State 29/31 | PHASE II step 3 | ENTER: s14 | LEAVE: u10 | Z=116.981

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: s14 enters, u10 leaves.
Reduced cost of entering variable: -0.613636
Minimum ratio theta*: 0.176373
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU
Current solution: x1=3.44921, x2=3.84195, x3=2.23528
Objective z: 116.981

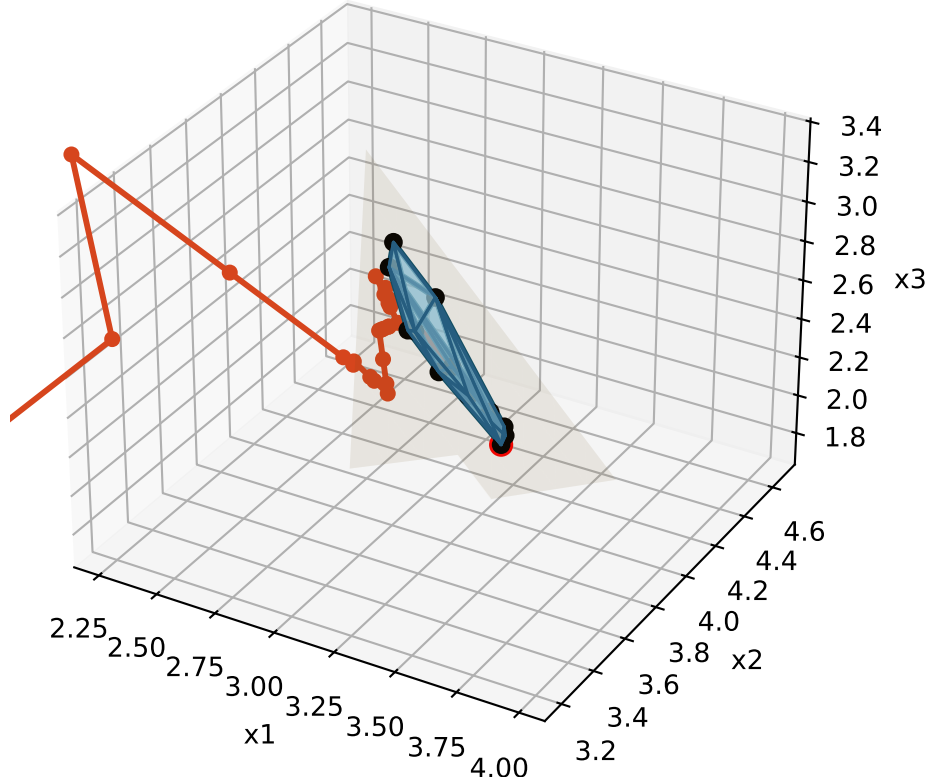
	row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8		s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28		rhs	ratio
	R1(s1)	0	0	0	1	0	0	0	0	0	0	0		-0.55	-0.45	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.55079	41.9802	
	R2(s2)	0	0	0	0	1	0	0	0	0	0	0		0.4	0.6	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.15805	inf	
	R3(s3)	0	0	0	0	0	1	0	0	0	0	0		0.05	-0.05	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.76472	429.824	
	R4(u6)	0	0	0	0	0	0	0	0	1	0	0		-0.1	0.1	0	-0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.627068	inf	
	R5(s5)	0	0	0	0	0	0	0	1	0	0	0		-1.35	-1.65	0	2.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.55334	2.2475	
	R6(u8)	0	0	0	0	0	0	0	0	0	0	1		0.6	-0.6	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.45175	5.49946	
	R7(x1)	1	0	0	0	0	0	0	0	0	0	0		0.55	0.45	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.44921	inf	
	R8(u11)	0	0	0	0	0	0	0	0	0	0	0		1.05	-0.05	1	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.715502	31.6585	
	R9(s14)	0	0	0	0	0	0	0	0	0	0	0		0.8	2.2	0	-2	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.176373	0.176373	
	R10(u24)	0	0	0	0	0	0	0	0	0	0	0		2.6	2.4	0	-2	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	3.38003	inf	
	R11(u19)	0	0	0	0	0	0	0	0	0	0	0		0.15	-0.15	0	0.25	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0.388834	5.87927	
	R12(u17)	0	0	0	0	0	0	0	0	0	0	0		0.95	1.05	0	-1.75	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	1.41034	inf
	R13(u22)	0	0	0	0	0	0	0	0	0	0	0		-0.35	-1.65	0	1.25	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0.854292	1.31543	
	R14(x2)	0	1	0	0	0	0	0	0	0	0	0		-0.4	-0.6	0	0.5	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.84195	14.2635	
	R15(u7)	0	0	0	0	0	0	0	0	0	1	0		0.7	0.3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.97007	inf
	R16(s16)	0	0	0	0	0	0	0	0	0	0	0		-2.6	-2.4	0	2	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	2.29386	2.27908
	R17(u23)	0	0	0	0	0	0	0	0	0	0	0		-0.15	-0.85	0	0.25	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	1.15578	3.16781
	R18(s18)	0	0	0	0	0	0	0	0	0	0	0		-0.5	-0.5	0	1.5	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	3.80634	16.9243
	R19(u13)	0	0	0	0	0	0	0	0	0	0	0		-0.75	-2.25	0	1.75	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.37272	0.540811	
	R20(s20)	0	0	0	0	0	0	0	0	0	0	0		0.25	1.75	0	-1.75	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	2.50622	inf
	R21(s21)	0	0	0	0	0	0	0	0	0	0	0		0.1	0.9	0	-1	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	2.03565	inf
	R22(u28)	0	0	0	0	0	0	0	0	0	0	0		0.55	-0.55	0	0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.85026	7.5774
	R23(u15)	0	0	0	0	0	0	0	0	0	0	0		-0.15	-1.85	0	1.75	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.05235	2.61701
	R24(u27)	0	0	0	0	0	0	0	0	0	0	0		-0.95	-2.05	0	1.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1.33949	1.61387	
	R25(s25)	0	0	0	0	0	0	0	0	0	0	0		-0.65	0.65	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	3.38354	inf	
	R26(x3)	0	0	1	0	0	0	0	0	0	0	0		-0.05	0.05	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.23528	inf
	R27(u26)	0	0	0	0	0	0	0	0	0	0	0		-0.55	-0.45	0	-0.25	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0.91841	4.66638	
base	R28(u4)	0	0	0	0	0	0	1	0	0	0	0		0.6	-0.6	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.78406	6.71794	
														0	3.65	1.35	0	-1.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	116.981		



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

15x1 + 10x2 + 12x3 = 117

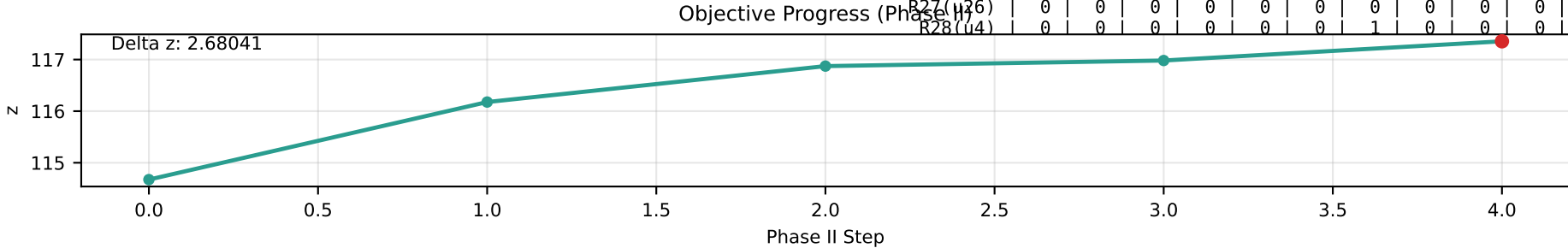


State 30/31 | PHASE II step 4 | ENTER: u12 | LEAVE: u13 | Z=117.354

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u12 enters, u13 leaves.
Reduced cost of entering variable: -1.75
Minimum ratio theta*: 0.212983
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU
Current solution: x1=3.50246, x2=3.73546, x3=2.28853
Objective z: 117.354

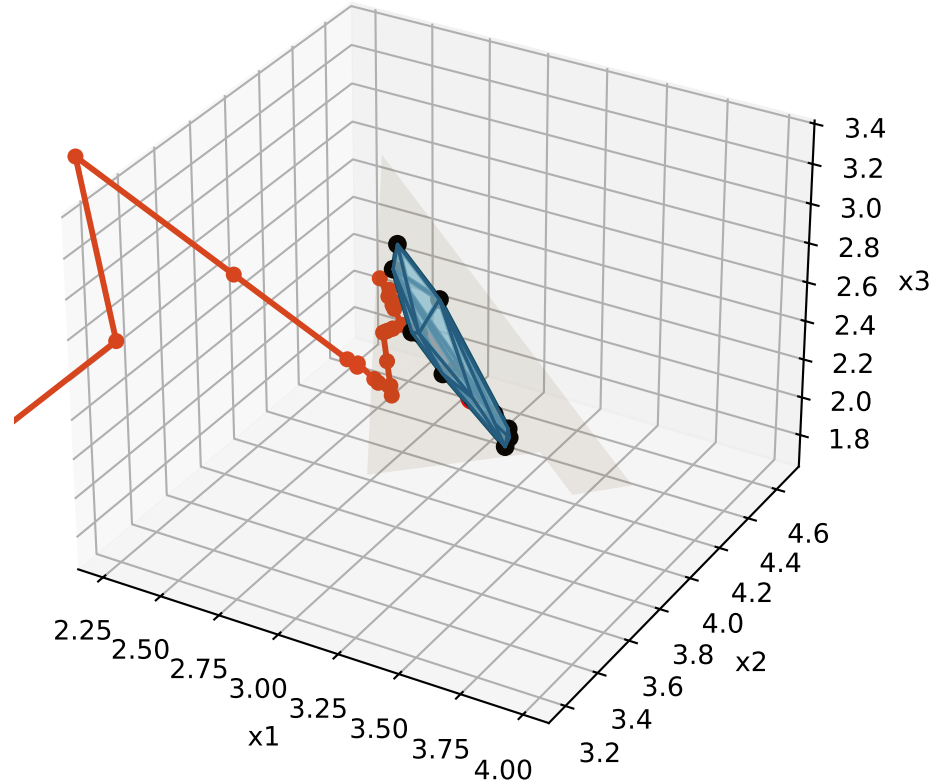
row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio	
R1(s1)	0	0	0	1	0	0	0	0	0	0	0	-0.442857	-0.128571	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.49754	34.2032		
R2(s2)	0	0	0	0	1	0	0	0	0	0	0	0.185714	-0.0428571	0	0	0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.26454	inf	
R3(s3)	0	0	0	0	0	1	0	0	0	0	0	0.157143	0.271429	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.71147	39.0589	
R4(u6)	0	0	0	0	0	0	0	0	1	0	0	-0.314286	-0.542857	0	0	0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.73356	inf	
R5(s5)	0	0	0	0	0	0	0	1	0	0	0	-0.385714	1.24286	0	0	-1.28571	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.07413	0.690375	
R6(u8)	0	0	0	0	0	0	0	0	0	0	1	0.814286	0.0428571	0	0	-0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.34526	2.9035	
R7(x1)	1	0	0	0	0	0	0	0	0	0	0	0.442857	0.128571	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.50246	inf	
R8(u11)	0	0	0	0	0	0	0	0	0	0	0	0.942857	-0.371429	1	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.768748	inf	
R9(s14)	0	0	0	0	0	0	0	0	0	0	0	-0.0571429	-0.371429	0	0	1.14286	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.602339	inf	
R10(u24)	0	0	0	0	0	0	0	0	0	0	0	1.74286	-0.171429	0	0	1.14286	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	3.806	inf	
R11(u19)	0	0	0	0	0	0	0	0	0	0	0	0.257143	0.171429	0	0	-0.142857	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0.335588	1.55534	
R12(u17)	0	0	0	0	0	0	0	0	0	0	0	0.2	-1.2	0	0	1	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	1.78306	inf	
R13(u22)	0	0	0	0	0	0	0	0	0	0	0	0.185714	-0.0428571	0	0	-0.714286	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0.588064	0.683434	
R14(x2)	0	1	0	0	0	0	0	0	0	0	0	-0.185714	0.0428571	0	0	-0.285714	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.73546	7.6839	
R15(u7)	0	0	0	0	0	0	0	0	0	1	0	0.7	0.3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.97007	inf	
R16(s16)	0	0	0	0	0	0	0	0	0	0	0	-1.74286	0.171429	0	0	-1.14286	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	1.86789	1.14693	
R17(u23)	0	0	0	0	0	0	0	0	0	0	0	-0.0428571	-0.528571	0	0	-0.142857	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	1.10254	4.62313	
R18(s18)	0	0	0	0	0	0	0	0	0	0	0	0.142857	1.42857	0	0	-0.857143	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	3.48687	2.53756
R19(u12)	0	0	0	0	0	0	0	0	0	0	0	-0.428571	-1.28571	0	1	0.571429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.212983	0.212983	
R20(s20)	0	0	0	0	0	0	0	0	0	0	0	-0.5	-0.5	0	0	1	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	2.87894	inf	
R21(s21)	0	0	0	0	0	0	0	0	0	0	0	-0.328571	-0.385714	0	0	0.571429	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	2.24863	inf	
R22(u28)	0	0	0	0	0	0	0	0	0	0	0	0.657143	-0.228571	0	0	-0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1.79701	7.40103
R23(u15)	0	0	0	0	0	0	0	0	0	0	0	0.6	0.4	0	0	-1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.67963	1.17277
R24(u27)	0	0	0	0	0	0	0	0	0	0	0	-0.414286	-0.442857	0	0	-0.714286	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1.07326	1.07159	
R25(s25)	0	0	0	0	0	0	0	0	0	0	0	-0.757143	0.328571	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	3.43678	inf	
R26(x3)	0	0	1	0	0	0	0	0	0	0	0	-0.157143	-0.271429	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.28853	inf	
R27(u26)	0	0	0	0	0	0	0	0	0	0	0	-0.657143	-0.771429	0	0	0.142857	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0.971655	inf	
R28(u4)	0	0	0	0	0	0	1	0	0	0	0	1.02857	0.685714	0	0	-0.571429	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.57108	1.78406	
base												2.9	-0.9	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	117.354		



Two-Phase Simplex Report

Feasible polytope + extreme points + simplex path

15x1 + 10x2 + 12x3 = 118



State 31/31 | PHASE II step 5 | ENTER: u10 | LEAVE: s5 | Z=118.132

COMMENTS
Teaching Mode | Rule: DANTZIG
Pivot: u10 enters, s5 leaves.
Reduced cost of entering variable: -0.9
Minimum ratio theta*: 0.864244
Why this pivot: Dantzig rule: most negative reduced cost (ties by smallest index). Minimum-ratio test (ties by smallest row index).

TABLEAU
Current solution: x1=3.39134, x2=3.69842, x3=2.52311
Objective z: 118.132

row	x1	x2	x3	s1	s2	s3	u4	s5	u6	u7	u8	s9	u10	u11	u12	u13	s14	u15	s16	u17	s18	u19	s20	s21	u22	u23	u24	s25	u26	u27	u28	rhs	ratio		
R1(s1)	0	0	0	1	0	0	0	0.103448	0	0	0	-0.482759	0	0	0	-0.275862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.60866	inf		
R2(s2)	0	0	0	0	1	0	0	0.0344828	0	0	0	0.172414	0	0	0	0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.30158	inf	
R3(s3)	0	0	0	0	0	1	0	-0.218391	0	0	0	0.241379	0	0	0	0.137931	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9.47689	35.7791	
R4(u6)	0	0	0	0	0	0	0	0.436782	1	0	0	-0.482759	0	0	0	-0.275862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.20272	inf	
R5(u10)	0	0	0	0	0	0	0	0.804598	0	0	0	-0.310345	1	0	0	-1.03448	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.864244	0.864244	
R6(u8)	0	0	0	0	0	0	0	-0.0344828	0	0	1	0.827586	0	0	0	0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.30822	31.3894
R7(x1)	1	0	0	0	0	0	0	-0.103448	0	0	0	0.482759	0	0	0	0.275862	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.39134	27.2413	
R8(u11)	0	0	0	0	0	0	0	0.298851	0	0	0	0.827586	0	1	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.08975	inf	
R9(s14)	0	0	0	0	0	0	0	0.298851	0	0	0	-0.172414	0	0	0	0.758621	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.923344	inf	
R10(u24)	0	0	0	0	0	0	0	0.137931	0	0	0	1.68966	0	0	0	0.965517	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	3.95415	inf	
R11(u19)	0	0	0	0	0	0	0	-0.137931	0	0	0	0.310345	0	0	0	0.0344828	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0.187432	1.9576	
R12(u17)	0	0	0	0	0	0	0	0.965517	0	0	0	-0.172414	0	0	0	-0.241379	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	2.82015	inf	
R13(u22)	0	0	0	0	0	0	0	0.0344828	0	0	0	0.172414	0	0	0	-0.758621	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0.625103	inf	
R14(x2)	0	1	0	0	0	0	0	-0.0344828	0	0	0	-0.172414	0	0	0	-0.241379	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	3.69842	87.1607	
R15(u7)	0	0	0	0	0	0	0	-0.241379	0	1	0	0.793103	0	0	0	0.310345	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.71079	9.90022	
R16(s16)	0	0	0	0	0	0	0	-0.137931	0	0	0	-1.68966	0	0	0	-0.965517	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1.71974	10.896	
R17(u23)	0	0	0	0	0	0	0	0.425287	0	0	0	-0.206897	0	0	0	-0.689655	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	1.55935	inf	
R18(s18)	0	0	0	0	0	0	0	-1.14943	0	0	0	0.586207	0	0	0	0.62069	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	2.25224	2.44081	
R19(u12)	0	0	0	0	0	0	0	1.03448	0	0	0	-0.827586	0	0	1	-0.758621	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.32415	inf	
R20(s20)	0	0	0	0	0	0	0	0.402299	0	0	0	-0.655172	0	0	0	0.482759	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	3.31106	inf	
R21(s21)	0	0	0	0	0	0	0	0.310345	0	0	0	-0.448276	0	0	0	0.172414	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	2.58198	inf	
R22(u28)	0	0	0	0	0	0	0	0.183908	0	0	0	0.586207	0	0	0	-0.37931	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1.99455	inf	
R23(u15)	0	0	0	0	0	0	0	-0.321839	0	0	0	0.724138	0	0	0	-0.586207	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.33394	4.19909	
R24(u27)	0	0	0	0	0	0	0	0.356322	0	0	0	-0.551724	0	0	0	-1.17241	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	1.45599	inf	
R25(s25)	0	0	0	0	0	0	0	-0.264368	0	0	0	-0.655172	0	0	0	0.482759	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	3.15282	10.4598	
R26(x3)	0	0	1	0	0	0	0	0.218391	0	0	0	-0.241379	0	0	0	-0.137931	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	2.52311	inf	
R27(u26)	0	0	0	0	0	0	0	0.62069	0	0	0	-0.896552	0	0	0	-0.655172	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	1.63836	inf	
R28(u4)	0	0	0	0	0	0	1	-0.551724	0	0	0	1.24138	0	0	0	0.137931	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0.978457	2.29116	
base u1												2.62069	0	0	0	0.0689655	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	118.132		

