# Logistic Regression on Hospital Dataset

Master of Science in Data Analytics Capstone: Data Analytics Report and Executive Summary

Brandi Enrietti, Graduate Student

Student ID 924116

Western Governors University

#### CAPSTONE: DATA ANALYTICS REPORT AND EXECUTIVE SUMMARY

2

## **Executive Summary**

This report is a written review of the data analysis conducted with logistic regression as a requirement of Western Governors Master of Science Data Analytics Capstone. The hypothesis for this analysis is:

H0: A predictive logistic regression model cannot be made from the Hospital Charges in High-Risk vs. Not High-Risk Patients who are admitted dataset.

H1: A predictive logistic regression model can be constructed from the Hospital Charges in High-Risk vs. Not High-Risk Patients who are admitted dataset.

The data was found to have a distribution of labels of 0.7 and 0.3. The first model showed an accuracy of 72% with 56% precision and a 14% recall. The data was limited by the distribution of the data. It is recommended that a more distributed dataset be obtained before running the model again.

## **Logistic Regression on Hospital Dataset**

### **Research Question**

This report is a written review of the data analysis conducted with logistic regression as a requirement of Western Governors Master of Science Data Analytics Capstone. The hypothesis for this analysis is:

H<sub>0</sub>: A predictive logistic regression model cannot be made from the Hospital Charges in High-Risk vs. Not High-Risk Patients who are admitted dataset.

H<sub>1</sub>: A predictive logistic regression model can be constructed from the Hospital Charges in High-Risk vs. Not High-Risk Patients who are admitted dataset.

Richard L. Fuller, Richard F. Averill, John Muldoon, and John S. Hughes published an article in the National Library of Medicine in 2016 that looked at clinical risk-adjustment the ability to standardize the comparison of individuals with different health needs is based upon 2 main alternative approaches: regression models and clinical categorical models. Their study utilized regression models to analyze variables of interest such as cost, complications, readmissions, or mortality. (Fuller, R. L., Averill, R. F., Muldoon, J. H., & Hughes, J. S. 2016).

The contribution of this study to the field of Data Analytics and the MSDA program is to create a reusable predictive model of logistic regression which can evaluate the relationship between diagnosis, hospital charges, number of discharges, and Medicare payments in the given dataset. To summarize, the logistic regression model supports a hypothesis that examines the given variables ability to predict outcomes. The variables will be defined, and the statistical framework will be specified. The model will test the association of the predictor variables and accuracy will be determined (Fuller, R. L., Averill, R. F., Muldoon, J. H., & Hughes, J. S. 2016).

### **Data Collection**

The data collected for this analysis is publicly available information and was provided by Data.gov The original data set obtained contained 163,065 rows and 13 columns.

The dataset is made available to Kaggle through Data.Gov. The data set includes the following variables: "diagnosis", "high\_risk" "provider\_id", "facility\_name", "facility\_address", "facility\_city", "facility\_state", "facility\_zip", "region", "total\_discharges", "total\_charge", "average total payments", and "average medicare payments".

https://www.kaggle.com/datasets/speedoheck/inpatient-hospitalcharges?select=inpatientCharges.csv

The predictor variables are broken down as follows:

Field	Туре
Diagnosis	Categorical
High_Risk	Object
Provider_ID	Continuous
Facility_Zip	Continuous
Region	Categorical
Average_Medicare_Payments	Categorical
Average_Total_Payments	Continuous
Total_Discharges	Continuous

There is no information that would make the hospitals associated with this analysis identifiable.

The dataset is limited to the total charge of the inpatient visit of each case. When looking at this data from a business perspective that information must be carefully considered in conjunction with this analysis when used to make any future predictions or determinations. There are no delimitations to this study.

## **Data Extraction and Preparation**

The data set was evaluated for data integrity by evaluating both quantitative and qualitative variables for null and duplicate values. This was done as part of the pre-process of the raw data so that it is easily and accurately analyzed, (DataCamp, nd). No null or duplicates were found in the dataset, had there been any, the solution would have been to impute or remove any missing variables and drop all duplicates. All categorical variables were converted to binary variables with the creation of dummy variables. The overall data sparsity percentage is less than 2%.

This analysis was conducted with Python. Python when compared to R for running predictive modeling has been found time and time again to be comparable and many of the differences in the systems come down to personal preference. However, visibility of the data is more advanced in Python (Kan, 2018). Comparison of Python to SAS for this type of analysis shows that SAS is more costly and while it is suitable for complex statistical operations it lacks data visualization and machine learning techniques, (TechVidVan, 2021). In conclusion, Python is the preferred language for data analysis and the packages available greatly support a sophisticated and yet easy method of examing the data set for this hypothesis, (cbtnuggets, 2020).

#### **Analysis**

Logistic regression is performed on the dataset utilizing Jupyter Notebook, Pandas and sklearn. The dependent variable is "High\_Risk" while the predictor variables are "total\_discharges", "total\_charge", and "average\_medicare\_payments". The data is visualized utilizing bivariate and univariate graphs to identify the variables that have a linear relationship.

The dependent and predictor variables identified above will be grouped together and separated to (x) features and (y) target, (Brownlee, 2022)

To build the logistic predictive model a train test split is required and was performed at an 75/25 split. Feature scaling with sklearn and StandardScaler was performed for normalization. The model was trained utilizing sklearn.linear\_model which gives access to LinearRegression, (Shilash, 2022).

This process involves fitting the model to learn the coefficients that will be interpreted next. The last step before evaluating the linear model was to make predictions based on the model. Finally, once the error metrics were obtained the model was used for feature selection. According to Massaron and Boschetti (2016) this process involves removing the features that have minimal impacts on (y) in hopes of increasing the accuracy of the model. This process is performed until an 80% or higher accuracy model is obtained.

8

```
#Logistic Regression Analysis
```

```
#Import Libraries and Packages
import pandas as pd
from pandas import Series
from pandas import DataFrame
import numpy as np
from numpy import ndarray
from numpy.random import randn
from numpy import loadtxt, where
import matplotlib
import matplotlib.pyplot as plt
%matplotlib inline
from matplotlib.patches import Patch
from matplotlib.lines import Line2D
plt.rc("font", size=14)
get_ipython().run_line_magic('matplotlib', 'inline')
import seaborn as sns
import random
import scipy
from tkinter import *
from scipy import stats
from statsmodels.stats.outliers_influence import variance_inflation_factor
import statsmodels.api as sm
import statsmodels.formula.api as smf
from sklearn import metrics
from sklearn.metrics import confusion_matrix
from sklearn import preprocessing
from sklearn import datasets
from sklearn.decomposition import PCA
from sklearn.model_selection import train_test_split
from sklearn.metrics import roc_auc_score
from sklearn.metrics import roc_curve
from sklearn.metrics import mean_squared_error
from sklearn.metrics import classification_report
from sklearn.feature_selection import RFE
from sklearn.linear_model import LogisticRegression
from sklearn.linear_model import LinearRegression
from sklearn.datasets import make_classification
from sklearn.pipeline import make_pipeline
from sklearn.preprocessing import StandardScaler
from sklearn.svm import SVR
from sklearn.metrics import log_loss, roc_auc_score, recall_score, precision_score, average_precision_score, f1_score, classi
from sklearn.datasets import load_digits
from IPython.core.display import HTML
from IPython.display import display
import os
import pylab
from pylab import scatter, show, legend, xlabel, ylabel
```

```
#Version data
     print("pandas version " + pd.__version__)
    print("numpy version " + np.__version__)
print("scipy version " + scipy.__version__
    print("matplotlib version " + matplotlib.__version__)
    print("seaborn version " + sns.__version__)
    print("statsmodels version " + sm.__version__)
     pandas version 1.4.2
     numpy version 1.21.5
     scipy version 1.7.3
     matplotlib version 3.5.1
    seaborn version 0.11.2
     statsmodels version 0.13.2
#Display adjustment
#pd.options.display.float_format = '{:,.6f}'.format
pd.set_option('display.max_columns', None) #show all columns
#Ignore future warning code
import warnings
warnings.filterwarnings('ignore')
#Read csv
df = pd.read_csv('inpatientcharges.csv')
#view data Layout
df.head()
        diagnosis high_risk provider_id facility_name facility_address facility_city facility_state facility_zip
                                                                                                        region total_discharges total_charge
                                       SOUTHEAST
            030 -
0 EXTRACRANIAL
                                         ALABAMA
MEDICAL
                       No
                                10001
                                                                     DOTHAN
                                                                                              36301 AL - Dothan
                                                                                                                                  32963.0
                                                   CLARK CIRCLE
    PROCEDURES
W/O CC/MCC
                                        MARSHALL
            039 -
                                                    2505 U S
HIGHWAY 431
 1 EXTRACRANIAL
                                          MEDICAL
                                                                                              35957 Birmingham
                                10005
                                                                        BOAZ
                                                                                                                                  15131.8
                       No
    PROCEDURES
W/O CC/MCC
                                                         NORTH
                                           SOUTH
           039 -
                                            ELIZA
2 EXTRACRANIAL
                                        COFFEE
                                                                                              35831 Birmingham
                                                    205 MARENGO
                                                                   FLORENCE
                                                                                                                                  37560.3
    PROCEDURES
W/O CC/MCC
                                                         STREET
                                         HOSPITAL
            039 -
                                               ST
                                                      50 MEDICAL
 3 EXTRACRANIAL
PROCEDURES
W/O CC/MCC
                                                                                              35235 Birmingham
                                10011
                                        VINCENT'S
                                                      PARK EAST
                                                                 BIRMINGHAM
                                                                                                                                  13998.2
                                            EAST
                                                          DRIVE
                                          SHELBY
BAPTIST
MEDICAL
           039 -
                                                      1000 FIRST
4 EXTRACRANIAL
                                                                                              35007 Birmingham
                                                         STREET
                                10016
                                                                   ALABASTER
                                                                                                                                  31633.2
    PROCEDURES
W/O CC/MCC
                                          CENTER
#Number of columns and rows
df.shape
```

(163065, 13)

```
#Check data for null values
df.isnull().sum()
diagnosis
                                          0
high_risk
                                          0
provider_id
                                          0
facility_name
                                          0
facility_address
                                          0
facility_city
                                          0
facility_state
                                          0
facility_zip
                                          0
                                          0
region
total_discharges
                                          0
total_charge
average_total_payments
                                          0
average_medicare_payments
                                          0
dtype: int64
#Check data for duplicates
df.duplicated().sum()
#Index, Datatype
df.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 163065 entries, 0 to 163064
Data columns (total 13 columns):
                                             Non-Null Count Dtype
 # Column
                                             -----
                                           163065 non-null object
 Ø diagnosis
 1 high_risk
2 provider_id
                                          163065 non-null object
163065 non-null int64
2 provider_id 163065 non-null int64
3 facility_name 163065 non-null object
4 facility_address 163065 non-null object
5 facility_city 163065 non-null object
6 facility_state 163065 non-null object
7 facility_zip 163065 non-null int64
8 region 163065 non-null object
 7 facility_zip
8 region

        8
        region
        163065 non-null object

        9
        total_discharges
        163065 non-null int64

        10
        total_charge
        163065 non-null float64

 11 average_total_payments 163065 non-null float64
12 average_medicare_payments 163065 non-null float64
dtypes: float64(3), int64(3), object(7)
memory usage: 16.2+ MB
#Drop provider_id column as it is just a unique id
df.drop("provider_id",inplace=True,axis=1)
```

#Count # of variables in relationship to cardiac disease or no cardiac disease df.groupby('high\_risk').count() diagnosis facility\_name facility\_address facility\_city facility\_state facility\_zip region total\_discharges total\_charge average\_total\_payments high\_risk No 116081 116081 116081 116081 116081 116081 116081 116081 116081 116081 46984 46984 46984 46984 46984 48984 48984 46984 46984 46984 yes 4 print(df.total\_charge.max()) 929118.9 #Convert Categorical variable to Continous variable with dummy function df['dummy\_high\_risk'] = [1 if v == 'yes' else 0 for v in df['high\_risk']] #Drop y/n column df = df.drop(columns=['high\_risk']) #Summary statistics df.describe() facility\_zip total\_discharges total\_charge average\_total\_payments average\_medicare\_payments dummy\_high\_risk count 163085.000000 163085.000000 163085.000000 163065.000000 163065.000000 163065.000000 mean 47938.121908 42.776304 36133.954224 9707.473804 8494.490964 0.288131 std 27854.323080 51.104042 35085.365931 7884.842598 7309.467261 0.452894 min 1040.000000 11.000000 2459.400000 1148.900000 0.000000 2873.000000 **25%** 27281.000000 17.000000 15947.160000 5234.500000 4192.350000 0.000000 27.000000 25245.820000 6158.460000 50% 44309.000000 7214.100000 0.000000 **75%** 72901.000000 49.000000 43232.590000 11288.400000 10056.880000 1.000000 max 99835 000000 3383 000000 929118 900000 158158 180000 154820.810000 1.000000

1.0

0.8

9000

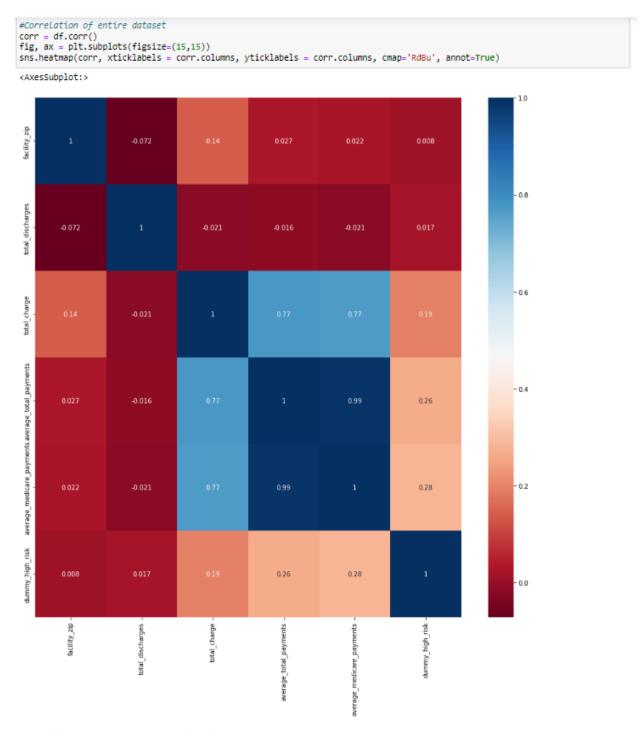
0.0

0.2

0.4

0.6 dummy\_high\_risk

```
#LinepLot
sns.lineplot(x= "dummy_high_risk", y= "total_charge", data=df)
<AxesSubplot:xlabel='dummy_high_risk', ylabel='total_charge'>
   46000
   44000
   42000
   40000
 lata
D
   38000
   36000
   34000
   32000
          0.0
                  0.2
                            0.4
                                    0.6
                                              0.8
                                                       1.0
                           dummy_high_risk
sns.lineplot(x= "dummy_high_risk", y= "average_total_payments", data=df)
<AxesSubplot:xlabel='dummy_high_risk', ylabel='average_total_payments'>
   13000
 설 12000
 average_total_payme
00000
```



# **Data Summary and Implications**

In conclusion, the initial model was found to have a distribution of labels of 0.7 and 0.3. The first model showed an accuracy of 72% with 56% precision and a 14% recall. The data was

limited by the distribution of the data. It is recommended that a more distributed dataset be obtained before running the model again. The reduced model with "total\_charge", "average\_total\_payments", and "total\_discharges" showed an accuracy score of 71% with an AUC score of 75%. Based on these results the hypothesis that a predictive logistic regression model cannot be made from the Hospital Charges in High-Risk vs. Not High-Risk Patients who are admitted dataset is accepted. Further distribution of data is required for acceptance of the null

hypothesis, (Thorpe, 1988).

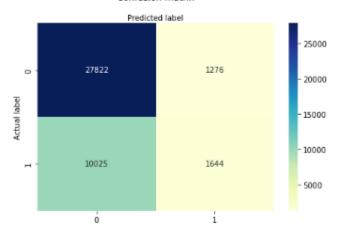
```
#Convert columns to a list
df.columns.tolist()
['diagnosis',
 'facility_name',
 'facility_address',
 'facility_city',
 'facility_state',
 'facility_zip',
 'region',
 'total_discharges',
 'total_charge',
 'average_total_payments';
 'average_medicare_payments',
 'dummy_high_risk']
#Initial model
#Split dataset in features and target variable
feature_cols = ['total_charge', 'average_medicare_payments', 'average_total_payments', 'total_discharges']
X = df[feature_cols] # Features
y = df.dummy_high_risk # Target variable
#Split X and y into training and testing sets
X_train,X_test,y_train,y_test=train_test_split(X,y,test_size=0.25,random_state=0)
#Feature scaling(normalizing)
scale=StandardScaler()
X_train = scale.fit_transform(X_train)
X_test = scale.transform(X_test)
#check for distribution of Labels
y_train.value_counts(normalize=True)
    0.711238
   0.288762
Name: dummy_high_risk, dtype: float64
#Instantiate the model (using the default parameters)
logreg = LogisticRegression()
#Fit the model with data
logreg.fit(X_train,y_train)
y_pred=logreg.predict(X_test)
print(logreg.score(X_test, y_test))
0.7227904923099566
#Confusion matrix
cnf_matrix = metrics.confusion_matrix(y_test, y_pred)
cnf_matrix
array([[27822, 1276],
[10025, 1644]], dtype=int64)
```

```
#Classes
class_names=[0,1] # name of classes
fig, ax = plt.subplots()
tick_marks = np.arange(len(class_names))
plt.xticks(tick_marks, class_names)
plt.yticks(tick_marks, class_names)

#Create heatmap to visualize results of the model
sns.heatmap(pd.DataFrame(cnf_matrix), annot=True, cmap="YlGnBu" ,fmt='g')
ax.xaxis.set_label_position("top")
plt.tight_layout()
plt.title('Confusion matrix', y=1.1)
plt.ylabel('Actual label')
plt.xlabel('Predicted label')
```

Text(0.5, 257.44, 'Predicted label')

#### Confusion matrix



```
#Accuracy, Precision, Recall
print("Accuracy:",metrics.accuracy_score(y_test, y_pred))
print("Precision:",metrics.precision_score(y_test, y_pred))
print("Recall:",metrics.recall_score(y_test, y_pred))
```

Accuracy: 0.7227904923099566 Precision: 0.563013698630137 Recall: 0.1408861084925872

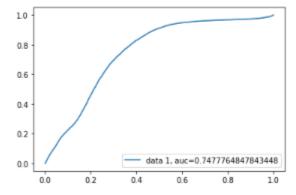
```
#AUC/ROC Curve
y_pred_proba = logreg.predict_proba(X_test)[::,1]
fpr, tpr, _ = metrics.roc_curve(y_test, y_pred_proba)
auc = metrics.roc_auc_score(y_test, y_pred_proba)
plt.plot(fpr,tpr,label="data 1, auc="+str(auc))
plt.legend(loc=4)
plt.show()
 1.0
 0.8
 0.4
 0.2
                       data 1, auc=0.7614739092773337
 0.0
     0.0
              0.2
                              0.6
                                       0.8
#Reduced ModeL
#Split dataset in features and target variable
feature_cols = ['total_charge', 'average_total_payments', 'total_discharges']
X = df[feature_cols] # Features
y = df.dummy_high_risk # Target variable
\#Split \ X \ and \ y \ into \ training \ and \ testing \ sets
X_train,X_test,y_train,y_test=train_test_split(X,y,test_size=0.25,random_state=0)
#Feature scaling
scale=StandardScaler()
X_train = scale.fit_transform(X_train)
X_test = scale.transform(X_test)
#check for distribution of labels
y_train.value_counts(normalize=True)
0 0.711238
    0.288762
1
Name: dummy_high_risk, dtype: float64
#Instantiate the model (using the default parameters)
Rlogreg = LogisticRegression()
#Fit the model with data
logreg.fit(X_train,y_train)
y_pred=logreg.predict(X_test)
print(logreg.score(X_test, y_test))
```

0.7141315279515295

```
#Confusion matrix
  cnf_matrix = metrics.confusion_matrix(y_test, y_pred)
  cnf_matrix
array([[27854, 1244],
[10410, 1259]], dtype=int64)
#CLasses
  class_names=[0,1] # name of classes
fig, ax = plt.subplots()
  tick_marks = np.arange(len(class_names))
  plt.xticks(tick_marks, class_names)
plt.yticks(tick_marks, class_names)
  #Create heatmap to visualize results of the model
  sns.heatmap(pd.DataFrame(cnf_matrix), annot=True, cmap="YlGnBu" ,fmt='g')
  ax.xaxis.set_label_position("top")
  plt.tight_layout()
  plt.title('Confusion matrix', y=1.1)
  plt.ylabel('Actual label')
plt.xlabel('Predicted label')
Text(0.5, 257.44, 'Predicted label')
                         Confusion matrix
                            Predicted label
                                                                  25000
                   27854
                                             1244
                                                                  20000
   Actual label
                                                                  15000
                                                                  10000
                   10410
                                             1259
                                                                  5000
                    ò
#Accuracy, Precision, Recall
  print("Accuracy:",metrics.accuracy_score(y_test, y_pred))
print("Precision:",metrics.precision_score(y_test, y_pred))
  print("Recall:",metrics.recall_score(y_test, y_pred))
```

Accuracy: 0.7141315279515295 Precision: 0.5029964043148222 Recall: 0.10789270717285114

```
#AUC/ROC Curve
y_pred_proba = logreg.predict_proba(X_test)[::,1]
fpr, tpr, _ = metrics.roc_curve(y_test, y_pred_proba)
auc = metrics.roc_auc_score(y_test, y_pred_proba)
plt.plot(fpr,tpr,label="data 1, auc="+str(auc))
plt.legend(loc=4)
plt.show()
```

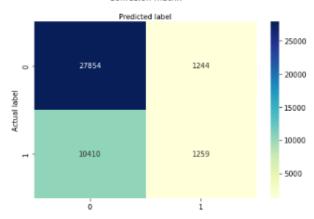


```
#Final model
features = ['total_charge',]
target = 'dummy_high_risk'
m = len(X)
X = df[features]
y = df[target]
model = sm.OLS(y, X).fit()
predictions = model.predict(X)
model.summary()
OLS Regression Results
    Dep. Variable: dummy_high_risk R-squared (uncentered): 0.249
         Model:
                         OLS Adj. R-squared (uncentered):
                                                             0.249
        Method: Least Squares
                                              F-statistic: 5.394e+04
           Date: Wed, 01 Jun 2022
                                        Prob (F-statistic):
                                                              0.00
                     15:55:10
                                     Log-Likelihood: -1.0883e+05
          Time:
                       163065
                                                   AIC: 2.133e+05
 No. Observations:
    Df Residuals:
                     163064
                                                   BIC: 2.133e+05
       Df Model:
                 nonrobust
 Covariance Type:
                coef std err t P>|t| [0.025 0.975]
 total_charge 5.315e-08 2.29e-08 232.248 0.000 5.27e-08 5.36e-08
 Omnibus: 7827.774 Durbin-Watson: 0.098
 Prob(Omnibus): 0.000 Jarque-Bera (JB): 9012.981
     Skew: 0.575 Prob(JB):
      Kurtosis: 3.072 Cond. No.
                                          1.00
Notes:
[1] R2 is computed without centering (uncentered) since the model does not contain a constant.
[2] Standard Errors assume that the covariance matrix of the errors is correctly specified
#Confusion matrix
cnf_matrix = metrics.confusion_matrix(y_test, y_pred)
cnf_matrix
array([[27854, 1244],
[10410, 1259]], dtype=int64)
```

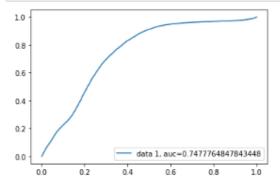
```
#Classes
class_names=[0,1] # name of classes
fig, ax = plt.subplots()
tick_marks = np.arange(len(class_names))
plt.xticks(tick_marks, class_names)
plt.yticks(tick_marks, class_names)
#Create heatmap to visualize results of the model
sns.heatmap(pd.DataFrame(cnf_matrix), annot=True, cmap="YlGnBu" ,fmt='g')
ax.xaxis.set_label_position("top")
plt.tight_layout()
plt.title('Confusion matrix', y=1.1)
plt.ylabel('Actual label')
plt.xlabel('Predicted label')
```

Text(0.5, 257.44, 'Predicted label')

#### Confusion matrix



```
#AUC/ROC Curve
y_pred_proba = logreg.predict_proba(X_test)[::,1]
fpr, tpr, _ = metrics.roc_curve(y_test, y_pred_proba)
auc = metrics.roc_auc_score(y_test, y_pred_proba)
plt.plot(fpr,tpr,label="data 1, auc="+str(auc))
plt.legend(loc=4)
plt.show()
```



#### References

- Aryal, P. (2016, September 19). *Hospital charges for inpatients*. Kaggle. Retrieved May 28, 2022, from <a href="https://www.kaggle.com/datasets/speedoheck/inpatient-hospital-charges?select=inpatientCharges.csv">https://www.kaggle.com/datasets/speedoheck/inpatient-hospital-charges?select=inpatientCharges.csv</a>
- Brownlee, J. (2020, August 14). *Linear regression for machine learning*. Machine Learning Mastery. Retrieved May 28, 2022, from <a href="https://machinelearningmastery.com/linear-regression-for-machine-learning/">https://machinelearningmastery.com/linear-regression-for-machine-learning/</a>
- CBTNuggets. (2018, September 20). Why Data Scientists Love Python.
- https://www.cbtnuggets.com/blog/technology/data/why-data-scientists-love-python
- Massaron, L. & Boschetti, A. (2016). Regression Analysis with Python. Packt Publishing.
- DataCamp. (n.d.). *Data preparation with Pandas*. Retrieved May 29, 2022, from <a href="https://www.datacamp.com/tutorial/data-preparation-with-pandas">https://www.datacamp.com/tutorial/data-preparation-with-pandas</a>
- Fuller, R. L., Averill, R. F., Muldoon, J. H., & Hughes, J. S. (2016). Comparison of the Properties of Regression and Categorical Risk-Adjustment Models. The Journal of ambulatory care management, 39(2), 157–165. https://doi.org/10.1097/JAC.000000000000135
- Kan, E. (2018, December 10). *Data science 101: Is python better than R?* Medium. Retrieved May 29, 2022, from <a href="https://towardsdatascience.com/data-science-101-is-python-better-than-r-b8f258f57b0f">https://towardsdatascience.com/data-science-101-is-python-better-than-r-b8f258f57b0f</a>
- Linear Regression Project Exercise. (n.d.). Amete.github.io. Retrieved April 27, 2022, from <a href="https://amete.github.io/DataSciencePortfolio/Udemy/Python-DS-and-ML-Bootcamp/Linear\_Regression\_Project.html">https://amete.github.io/DataSciencePortfolio/Udemy/Python-DS-and-ML-Bootcamp/Linear\_Regression\_Project.html</a>
- Mawardi, D. (2017, August 22). *Linear regression in python*. Medium. Retrieved May 28, 2022, from <a href="https://towardsdatascience.com/linear-regression-in-python-9a1f5f000606">https://towardsdatascience.com/linear-regression-in-python-9a1f5f000606</a>
- SAS vs R vs python the battle for data science! TechVidvan. (2021, July 6). Retrieved May 29, 2022, from https://techvidvan.com/tutorials/sas-vs-r-vs-python/
- Shilash, M. (2022, March 22). *Linear regression with python implementation*. Analytics Vidhya. Retrieved May 28, 2022, from <a href="https://www.analyticsvidhya.com/blog/2022/02/linear-regression-with-python-implementation/">https://www.analyticsvidhya.com/blog/2022/02/linear-regression-with-python-implementation/</a>

Sklearn.linear\_model.linearregression. scikit. (n.d.). Retrieved May 29, 2022, from <a href="https://scikit-">https://scikit-</a>

learn.org/stable/modules/generated/sklearn.linear\_model.LinearRegression.html

Thorpe, K. E. (1988). The Use of Regression Analysis to Determine Hospital Payment: The Case of Medicare's Indirect Teaching Adjustment. *Inquiry*, 25(2), 219–231. <a href="http://www.jstor.org/stable/29771954">http://www.jstor.org/stable/29771954</a>