

Observations about lookup speed

- We know that array lookups for a given index are $O(1)$
- Idea: we can store elements in an array, at their own index
- $A = [1, 2, 3, 4, 5, 6, \dots, n]$
- Then, we can check if an element is there by checking that index in $O(1)$ time
- Downside: space complexity will need to be $O(\max(A) - \min(A))$ to store elements uniquely, and will need to resize array whenever larger element is added.
 - Example: $A = [1, 1,000,000]$ will require 1,000,000 slots to store 2 items

Hashing

- Idea: put elements into a fixed-size array by taking the remainder
 - $A = [1, 5, 6, 3, 16, 20]$, with size of hash table = 6
 - This gives hash table $H = [6, 1, 20, 3, 16, 5]$
- Okay in the above example, but what about $A = [6, 12, 1, 13, 2, 14]$? Now have multiple elements that hash to same thing: $6 \bmod 6 = 12 \bmod 6 = 0$.
- Solution: use a list to keep track of all elements that hash to same index, and instead just store a pointer to the list in H if needed:
 - $H = [[6, 12], [1, 13], [2, 14], -1, -1, -1]$ (fill unused slots with -1)