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Modeling Female Sex Worker Distribution And  
Determinants In Sub Saharan Africa To Enhance HIV  
Prevention Strategies

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## 1 INTRODUCTION

HIV continues to be a significant public health challenge in sub-Saharan Africa, which bears a disproportionate burden of the global epidemic. Given the critical role of Female Sex Workers (FSWs) in HIV transmission dynamics, understanding their distribution is essential for the targeted implementation of HIV-prevention services. This study investigates the abundance of FSWs within sub-Saharan Africa by examining various factors that may influence their distribution. The analysis considers variables such as the country (`country`: Mozambique, Malawi, Zimbabwe, Zambia, and Botswana) and the region (`region`) within each country, along with the year (`dataYear`) and month (`month`) the data were collected. Other important factors include the number of Female Sex Workers observed (`FSWCount`), population density within the surveyed transect (`popDensity`), and the built-up index (`built`), which reflects urbanization levels. Environmental variables such as the average length of the growing season (`growingSeason`), average annual rainfall (`rain`), and average annual temperature (`temperature`) are included in the analysis. Additionally, the study evaluates night-time light activity (`nightLight`), distance to the nearest clean water source (`cleanWater`), and proximity to the nearest protected area (`protected`). Health-related factors include the HIV prevalence rate among the population (`hivRate`), average fear of contracting HIV (`hivFear`), and the percentage of the population using insect nets (`insectNet`). Sociological dimensions, such as the average age of first sexual experience (`ageFirstSex`), wealth index relative to the sub-Saharan African region (`wealthIndex`), and the size of the surveyed transect (`surveyArea`), are also considered, along with an indicator of whether the crime rate is high in the transect (`highCrime`). By assessing the influence of these variables, this study aims to provide critical insights into the factors shaping the distribution of FSWs in sub-Saharan Africa. These findings will guide the prioritization of environmental and sociological factors in future data collection efforts and the implementation of HIV-prevention strategies.

## 2 EXPLORATORY DATA ANALYSIS

The dataset comprises 750 observations, of which 675 are retained for analysis in this study. The response variable, `FSWCount`, represents the number of female sex workers recorded and is a discrete, non-negative integer. Summary statistics, presented in Table 1, were generated using the `summary` function in R (R Core Team, 2020). The recorded counts of female sex workers range from a minimum of 0 to a maximum of 134, with an average count of approximately 5.564. A histogram, displayed in Figure 1 and created using the `ggplot2` package (Wickham, 2019), illustrates the distribution of female sex worker counts. Correlation analysis, as shown in Table 2, reveals that the variables `built`, `growingSeason`, `rain`, `nightLight`, and `cleanWater` exhibit weak negative correlations with `FSWCount`. Conversely, `temperature` shows a positive correlation with `FSWCount`. To further explore these relationships, a scatterplot and correlation matrix are presented in Figures 2 and 3, created using the `GGally` package (Schloerke, 2024). The scatterplot/correlation matrix highlights that most observations cluster around zero counts for variables such as `built`, `growingSeason`, `rain`, `nightLight`, `cleanWater`, and `wealthIndex`. In contrast, a positive correlation was observed between temperature (`temperature`) and FSW counts. These findings provide an overview of the relationships between the response variable and key predictors in the dataset.

## 3 STATISTICAL PROCEDURE

The model incorporates `country`, `region`, `dataYear`, and `month` as random effects to account for unobserved heterogeneity and variability attributable to spatial and temporal factors. The variable `surveyArea` is specified as an offset term to normalize the response variable, `FSWCount`, by the size of the surveyed regions, ensuring that larger areas do not disproportionately influence the model outcomes. Given the discrete and non-negative integer nature of `FSWCount`, count regression mixed-effects models are deemed appropriate. These models are estimated using the `glmmTMB` function from the `glmmTMB` package (Mollie, 2017), allowing for flexible handling of fixed and random effects while accommodating the characteristics of count data.

## 4 DISTRIBUTION SELECTION USING ENVIRONMENTAL VARIABLES

An initial Poisson mixed-effects model was developed to analyze `FSWCount` as the response variable. The model incorporated `country`, `region`, `dataYear`, and `month` as random effects to account for spatial and temporal variability, along with environmental variables as fixed covariates. Diagnostic evaluations, presented in Figure 4, identified potential issues with overdispersion. Specifically, the Residuals vs. Fitted plot (Figure 4) indicated an increasing spread of residuals with higher fitted values, consistent with overdispersion. Additionally, the QQ plot (Figure 4) revealed

deviations from the normality assumption, with residuals exhibiting heavy-tailed behavior. A formal overdispersion test confirmed the presence of overdispersion, with a dispersion parameter ( $\theta = 6.977929$ ) exceeding what would be expected under a Poisson distribution. To address these challenges, alternative mixed-effects models were considered, including the negative binomial, zero-inflated Poisson, zero-inflated negative binomial, hurdle Poisson, and hurdle negative binomial models. Model selection was guided by the Akaike Information Criterion (AIC), as shown in Table 3. The negative binomial mixed-effects model emerged as the best-performing model, with the lowest AIC value (2873.769), indicating a superior balance between model fit and complexity. Given the observed proportion of zero counts in **FSWCount**, a zero-inflated negative binomial model was also evaluated due to its comparable AIC score. However, upon fitting, the estimated proportion of excess zeros was found to be negligible, suggesting that a zero-inflated structure was unnecessary as the data did not exhibit significant zero inflation. The negative binomial mixed-effects model was therefore deemed the most appropriate for modeling the response variable.

## 5 DISTRIBUTION SELECTION USING SOCIOLOGICAL VARIABLES

To identify the appropriate distribution using the sociological variables, a Poisson mixed-effects model was fitted with **FSWCount** as the response variable. The model included **country**, **region**, **dataYear**, and **month** as random effects to account for spatial and temporal variability, while all other sociological variables were included as fixed covariates. Diagnostic plots, presented in Figure 5, revealed evidence of overdispersion. Specifically, the Residuals vs. Fitted plot (Figure 5) showed increasing residual variability with higher fitted values, suggesting overdispersion. The QQ plot (Figure 5) provided moderate to strong evidence against the normality assumption, as residuals exhibited heavy-tailed behavior. A formal overdispersion test further confirmed this, with a dispersion parameter ( $\theta = 6.324017$ ) exceeding what would be expected under a Poisson distribution. To address the overdispersion, several alternative mixed-effects models were considered, including negative binomial, zero-inflated Poisson, zero-inflated negative binomial, hurdle Poisson, and hurdle negative binomial models. Model selection was guided by the Akaike Information Criterion (AIC), as shown in Table 4. Among these, the negative binomial mixed-effects model achieved the lowest AIC score (2872.943), indicating the best balance between model fit and information loss. Given the high proportion of zero counts in **FSWCount**, the zero-inflated negative binomial model was also evaluated due to its comparable AIC score. However, after fitting, the estimated proportion of excess zeros was found to be negligible, indicating that the zero-inflated structure did not significantly improve the model fit. Consequently, the negative binomial mixed-effects model was deemed the most appropriate for modeling the response variable.

## 6 VARIABLE SELECTION USING ENVIRONMENTAL VARIABLES

Using the negative binomial mixed-effects model, the next step is to identify the variables to include in the final model. A preliminary model is fitted with **country**, **region**, **dataYear**, and **month** as random effects, and **popDensity**, **built**, **growingSeason**, **rain**, **temperature**, **nightlight**, and **cleanWater** as covariates, with **surveyArea** specified as an exposure. To determine the random effects structure, Restricted Maximum Likelihood (REML) estimation is used, and an ANOVA test is performed to assess the necessity of including random effects. The test yields a p-value of  $<0.001$  ( $\chi^2_4 = 56.25$ ), providing strong evidence to include random effects in the model. To refine the random effects structure, the random components **month** and **dataYear** are individually removed, and the model is refitted each time. ANOVA tests after each removal yield p-values of 0.6554 ( $\chi^2_1 = 0.1991$ ) for **month** and 0.2255 ( $\chi^2_1 = 1.4692$ ) for **dataYear**, suggesting weak to moderate evidence against the necessity of these components. Consequently, both **month** and **dataYear** are excluded from the model, leading to a slight improvement in the AIC score. With only **country** and **region** retained as random effects, the model is further evaluated to determine whether a random intercept or random slope is necessary. The residuals of the model, grouped by **country** and **region**, are assessed against the seven covariates. The analysis indicates no systematic patterns in the residuals, suggesting that random slopes are not needed for these variables. Next, the fixed effects are selected using Maximum Likelihood (ML) estimation. A preliminary model is fitted with all seven covariates: **popDensity**, **built**, **growingSeason**, **rain**, **temperature**, **nightlight**, and **cleanWater**. The AIC score for this model is 2870.634. The p-values indicate that **growingSeason**, **rain**, **nightlight**, and **cleanWater** are not significant. An ANOVA test confirms this result, with a p-value of 0.1476 ( $\chi^2_4 = 6.7866$ ), leading to the removal of these variables. The revised model, with **popDensity**, **built**, and **temperature** as fixed effects, achieves an improved AIC score of 2869.42. Further evaluation of this model shows that all three remaining covariates are statistically significant. To validate these findings, an ANOVA test against an intercept-only model is conducted, yielding strong evidence (p-value =  $7.1 \times 10^{-6}$ ,  $\chi^2_4 = 29.209$ ) that **popDensity**, **built**, and **temperature** are essential for the model. The final negative binomial mixed-effects model is refitted using Maximum Likelihood estimation. The model includes **popDensity**, **built**, and **temperature** as fixed effects, **country** and **region** as random effects, and **surveyArea** as an exposure. This optimized model provides a robust representation of the data, with all

included variables demonstrating significance and contributing to the explanation of the response variable.

#### Model Specification:

$$\text{FSWCount}_i \sim \text{Negative Binomial}(\mu_i, \eta)$$

$$\log(\mu_i) = \beta_0 + \beta_1 \cdot \text{popDensity}_i + \beta_2 \cdot \text{built}_i + \beta_3 \cdot \text{temperature}_i + \alpha_{\text{country}[i]} + \beta_{\text{region}[i]} + \log(\text{surveyArea}_i)$$

$$\alpha_{\text{country}} \sim \text{Normal}(0, \sigma_\alpha^2), \quad \beta_{\text{region}} \sim \text{Normal}(0, \sigma_\beta^2), \quad \eta \quad (\text{Overdispersion Parameter})$$

## 7 VARIABLE SELECTION USING SOCIOLOGICAL VARIABLES

Using the negative binomial mixed-effects model, the next step involves selecting the variables required for the final model. A preliminary model is fitted with `country`, `region`, `dataYear`, and `month` as random effects, and `hivRate`, `protected`, `hivFear`, `highCrime`, `insectNet`, `ageFirstSex`, and `wealthIndex` as covariates, with `surveyArea` specified as an exposure. Restricted Maximum Likelihood (REML) estimation is employed to determine the appropriate random effects structure. An ANOVA test yields a p-value of  $2.89 \times 10^{-13}$  ( $\chi_4^2 = 64.76$ ), providing strong evidence in favor of including random effects in the model. To refine the random effects structure, the random components `month` and `dataYear` are individually removed, and the model is refitted after each removal. ANOVA tests after these removals indicate that `month` has a p-value of 0.7424 ( $\chi_1^2 = 0.1081$ ), suggesting little to no evidence against excluding it, and it is subsequently removed. In contrast, `dataYear` has a p-value of 0.01456 ( $\chi_1^2 = 5.9688$ ), providing moderate to strong evidence for its inclusion, so it is retained in the model. With this refinement, the model's AIC improves slightly. An ANOVA test confirms the necessity of `country`, `region`, and `dataYear` as random effects, with a p-value of  $5.96 \times 10^{-14}$  ( $\chi_3^2 = 64.65$ ). Using the refined random effects structure, the fixed effects are selected through Maximum Likelihood (ML) estimation. A preliminary model is fitted with all seven covariates: `hivRate`, `protected`, `hivFear`, `highCrime`, `insectNet`, `ageFirstSex`, and `wealthIndex`. This model yields an AIC score of 2870.943. However, the p-values indicate that `hivRate`, `protected`, `hivFear`, `ageFirstSex`, and `wealthIndex` are not significant. An ANOVA test is conducted, resulting in a p-value of 0.5092 ( $\chi_7^2 = 0.5092$ ), which provides weak evidence against the null hypothesis that these variables are unnecessary. Consequently, these five variables are removed from the model. The updated model, which retains `highCrime` and `insectNet` as fixed effects, achieves an improved AIC score of 2863.208. Further analysis confirms that both `highCrime` and `insectNet` are significant. To validate this finding, an ANOVA test is conducted against an intercept-only model, yielding strong evidence with a p-value of  $2.6 \times 10^{-7}$  ( $\chi_3^2 = 33.421$ ). This result confirms the necessity of `highCrime` and `insectNet` in the model. Fixed-effect selection is performed using ML estimation, with REML set to `false` in the R code. The final negative binomial mixed-effects model is refitted using Maximum Likelihood estimation. The model includes `highCrime` and `insectNet` as fixed effects, `country`, `region`, and `dataYear` as random effects, and `surveyArea` as an exposure. This optimized model demonstrates no issues with linearity or overdispersion, and all included variables are significant, providing a robust representation of the data.

#### Model Specification:

$$\text{FSWCount}_i \sim \text{Negative Binomial}(\mu_i, \eta)$$

$$\log(\mu_i) = \beta_0 + \beta_1 \cdot \text{highCrime}_i + \beta_2 \cdot \text{insectNet}_i + \alpha_{\text{country}[i]} + \beta_{\text{region}[i]} + \gamma_{\text{dataYear}[i]} + \log(\text{surveyArea}_i)$$

$$\alpha_{\text{country}} \sim \text{Normal}(0, \sigma_\alpha^2), \quad \beta_{\text{region}} \sim \text{Normal}(0, \sigma_\beta^2), \quad \gamma_{\text{dataYear}} \sim \text{Normal}(0, \sigma_\gamma^2), \quad \eta \quad (\text{Overdispersion Parameter})$$

## 8 RESULTS AND CONCLUSION

The analysis revealed significant associations between environmental and sociological variables and the distribution of Female Sex Workers (FSWs) across sampled regions. Statistical modeling provided valuable insights into the influence of both fixed and random effects on FSW counts. Among the environmental variables, **popDensity** was significantly associated with FSW counts, with lower-density areas exhibiting higher prevalence. This suggests that sparsely populated regions may have unique socio-economic or demographic factors influencing FSW distribution. Similarly, the **built** index was negatively correlated with FSW counts, indicating that less urbanized areas tend to have higher counts, potentially due to disparities in infrastructure or economic conditions. Additionally, **temperature** showed a positive relationship with FSW counts, which may reflect region-specific environmental or cultural dynamics.

Sociological variables also played a critical role. **highCrime** was associated with a significant increase in FSW counts, suggesting that socio-economic vulnerabilities or unsafe environments contribute to the observed patterns. **insectNet** usage was positively correlated with FSW counts. While the mechanism underlying this association is unclear, it may serve as a proxy for regional variations in public health resources or living conditions. The random effects structure of the model accounted for additional unmeasured variability across spatial and temporal dimensions. Random intercepts for **country**, **region**, and **dataYear** were statistically significant, with variance component estimates capturing hierarchical clustering in the data. This highlights the importance of controlling for contextual factors when modeling complex phenomena such as FSW distribution.

The final negative binomial mixed-effects model demonstrated improved model fit, with the lowest AIC score of 2863.208. Likelihood ratio tests confirmed the significance of the fixed effects and the necessity of including random effects. These results underscore the importance of integrating both environmental and sociological dimensions to understand the factors influencing FSW counts. This study highlights the complex interplay between environmental and sociological variables in shaping FSW distribution. However, the findings are generalizable only to the sampled regions and timeframes or to other contexts with similar characteristics. As this was an observational study, causal inferences cannot be drawn. Nonetheless, the statistical evidence provides valuable insights to inform targeted public health interventions and policies. Future research should consider incorporating additional covariates, such as economic indicators or access to healthcare, and explore longitudinal data to capture dynamic changes over time. Such approaches could refine our understanding of the factors affecting FSW distribution and guide effective public health strategies.

## REFERENCES

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## 9 APPENDIX

### 9.1 TABLES

Table 1: Summary Statistics of the response variable

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
FSWCount	0	0	0	5.564	5	134

Table 2: Correlation table between FSWCount and the other covariates.

Variable	Correlation
built	-0.2023
growingSeason	-0.1416
rain	-0.05463
temperature	0.2717
nightlight	-0.03247
cleanWater	-0.1469

Table 3: Table of AIC scores for 6 selected mixed-effect models using environmental variables.

Model	AIC
Poisson	5978
Negative Binomial	2874
Hurdle Poisson	4900
Hurdle Negative Binomial	2999
Zero-inflated Poisson	2876
Zero-inflated Negative Binomial	4861

Table 4: Table of AIC scores for 6 selected mixed-effect models using sociological variables.

Model	AIC
Poisson	5551
Negative Binomial	2873
Hurdle Poisson	4602
Hurdle Negative Binomial	2989
Zero-inflated Poisson	2875
Zero-inflated Negative Binomial	4562

## 9.2 FIGURES

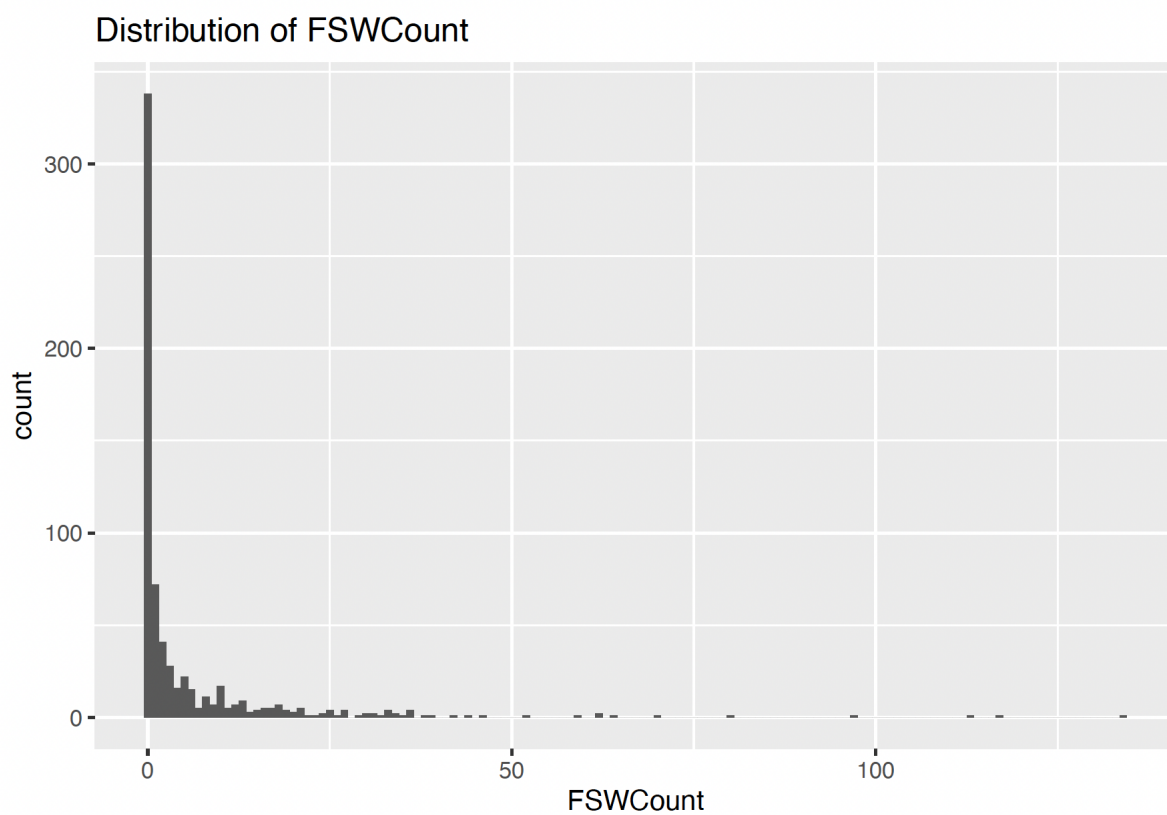


Figure 1: The distribution of female sex worker counts

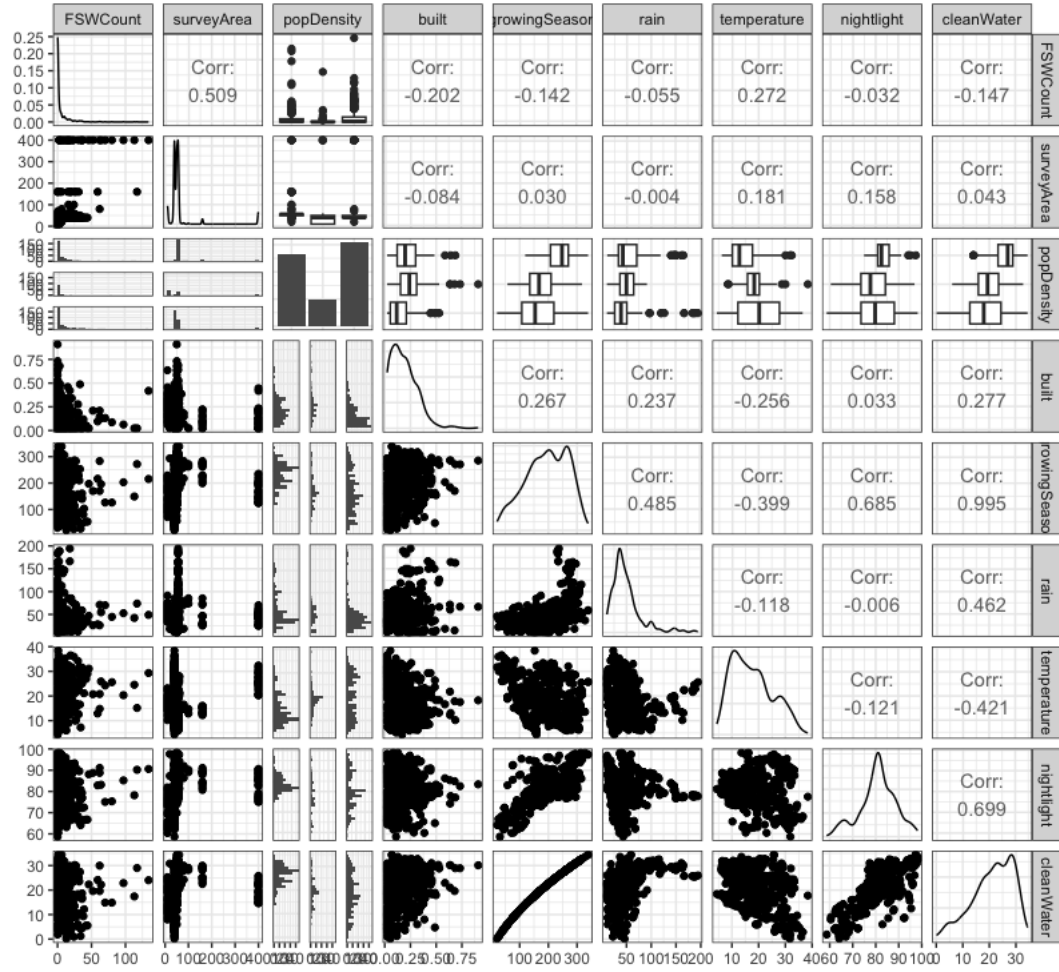


Figure 2: Correlation matrix of the variables showing the correlation between the variables.



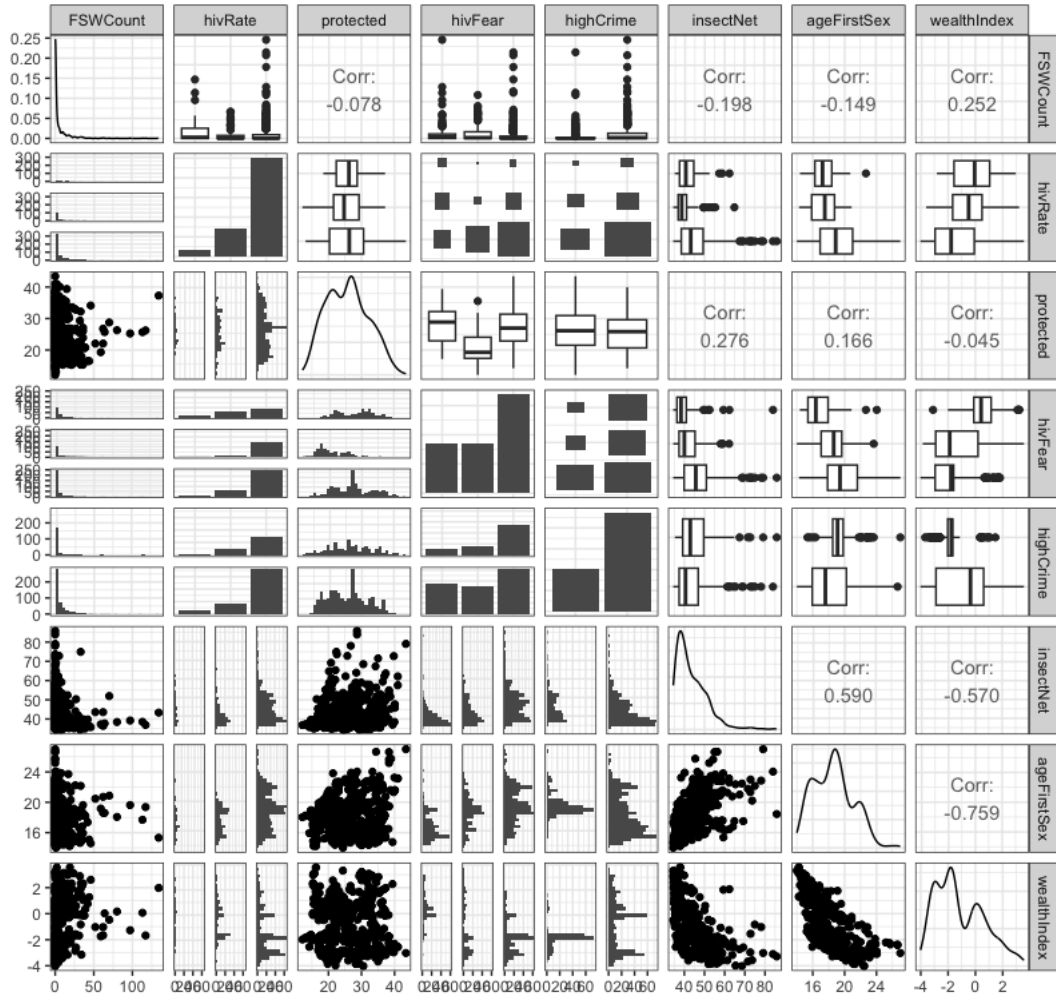


Figure 3: Correlation matrix of the variables showing the correlation between the variables

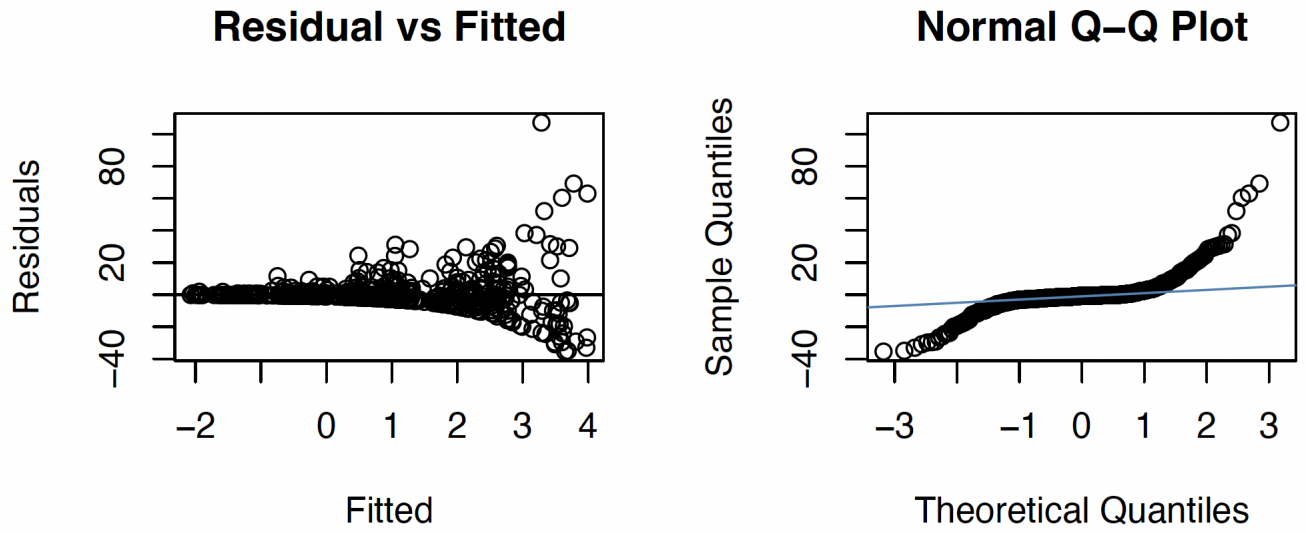


Figure 4: Diagnostic plot of the poisson mixed-effect model using environmental variables.

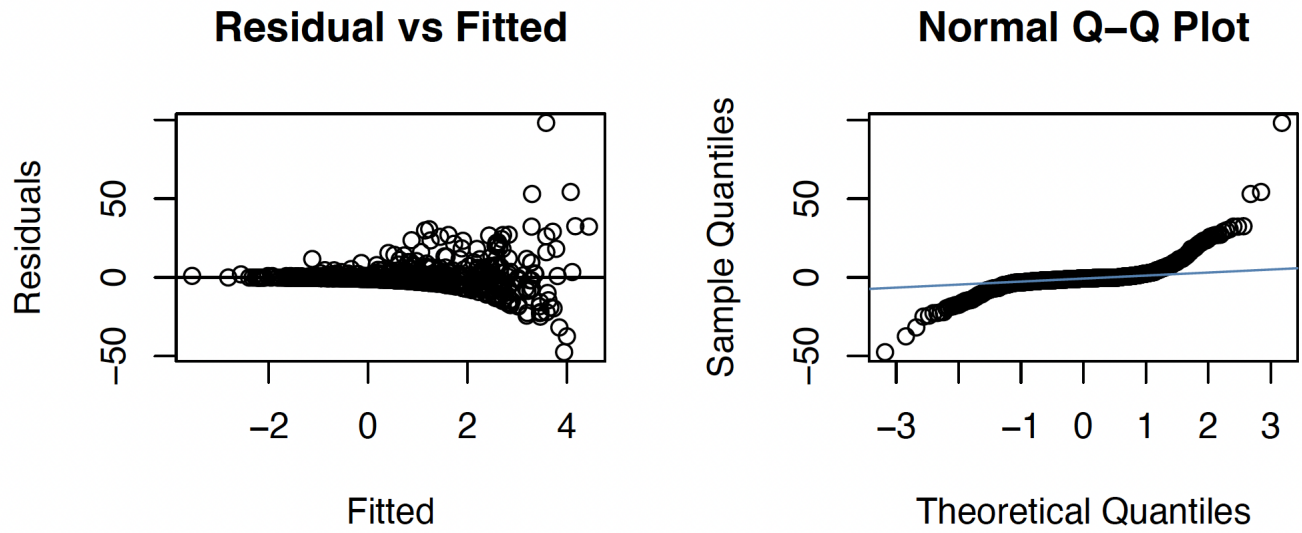


Figure 5: Diagnostic plot of the poisson mixed-effect model using sociological variables.