COSC 241 Lab 4: Arrays

Arrays are *the* fundamental data structure of many programming languages including Java. A clear, complete and deep understanding of their strengths and weaknesses is a prerequisite to becoming an effective programmer.

In this lab we will work with some special objects called Young tableaux, which are naturally represented as doubly indexed arrays of integers. These are very important objects in advanced algebra and discrete mathematics, but that will not concern us – we're just using the concept as a convenient foundation for some exercises on array manipulation.

A Young tableau is shown below:

1	4	5	10	11
2	6	8		
3	9	12		
7				

The key features of a Young tableau are as follows:

- it consists of cells which are filled with integers, and arranged in left-justified rows,
- no row is longer than a preceding row,
- from left to right in any row, and down any column the integers are increasing,
- the set of integers used is $\{1, 2, ..., n\}$ where n is the number of cells.

In Java, an obvious way to represent a tableau is as a doubly indexed array of integers, i.e, int[][]. The tableau above might be represented as:

```
int[][] tableau = {{1, 4, 5, 10, 11}, {2, 6, 8}, {3, 9, 12}, {7}};
```

A basic problem is that doubly indexed arrays of integers need have none of the properties that define tableaux. One of the objects of this lab is to write code that will check when such an array really is a tableau.

Problem description

The main objective of this lab is to write a function isTableau which takes an int[][] as input and returns a boolean as output, where the result is true if the array represents a tableau, and false otherwise. Because the defining properties of a tableau sep-

COSC 241 Lab 4: Arrays

arate naturally into various individual properties, this is a good opportunity to practice bottom up design, and some form of test driven development – building and testing your code a piece at a time.

The conditions that a tableau must satisfy are listed above. The first is represented automatically by the representation as a doubly indexed array of integers, so the main issue is to test the remaining three conditions, noting that the third of the four conditions splits into two parts.

Part one (1%)

There is a skeleton class TableauApp. java provided in the usual coursework pickup directory. This includes a basic utility function for String representations of doubly indexed arrays of integers as if they were tableaux.

Add a couple of static functions to the skeleton code class which implement condition two and the first part of condition three:

rowLengthsDecrease(int[][] t) A method that returns true if no row is longer than a preceding row, otherwise false.

rowValuesIncrease(int[][] t) A method that returns true if from left to right in any row, the integers are increasing, otherwise false.

Implement each one separately, testing as you go. Your methods need not work sensibly if passed a **null** argument, but should work properly on the empty tableau, i.e.,

```
int[][] t = {};
```

which those peculiar mathematicians insist is a proper tableau (with n = 0).

Part two (1%)

Add two more static functions to the skeleton code class which implement the second part of condition three, and condition four:

columnValuesIncrease(int[][] t) A method that returns true if from top to
bottom in any column, the integers are increasing, otherwise false.

isSetOfltoN(int[][] t) A method that returns true if the set of integers used is $\{1, 2, ..., n\}$ where n is the number of cells, otherwise false.

COSC 241 Lab 4: Arrays

Finally, use the separate methods above to complete the **isTableau** method for determining whether an **int[][]** represents a tableau.

Marking

Check that your program works correctly, and then use the command 241-check to make sure it passes all of our tests. If all is well then you can submit using 241-submit as usual. If you only complete part one or part two then 241-submit will allow you to submit the completed part.

Reflection and extension

- What is the complexity of your method for checking that the entries of the tableau form the set $\{1, 2, \ldots, n\}$? One natural implementation is of quadratic (i.e., $O(n^2)$) but not linear (O(n)) complexity. Can you think of a linear one or convince yourself that yours is?
- How could the tableauToString function be improved so that the result is nicely aligned even if some of the numbers are quite large? That is, it should dynamically take into account the size of the entries in the doubly indexed array.
- Your mathematician friend who wants to work with tableaux only now gets around to telling you that the tableaux she is interested in are generated by a sequence of additions of cells. Her plan is to test some conjectures about tableaux which will involve building up millions or possibly billions of tableaux in this way. Why is the tableau representation we have been using here *not* a good idea for this project?
- If you look at a tableau on its side (i.e., read each column from top to bottom as a row from left to right) you get another tableau called its *conjugate*. How would you write a method that, given a tableau, returned the conjugate tableau?