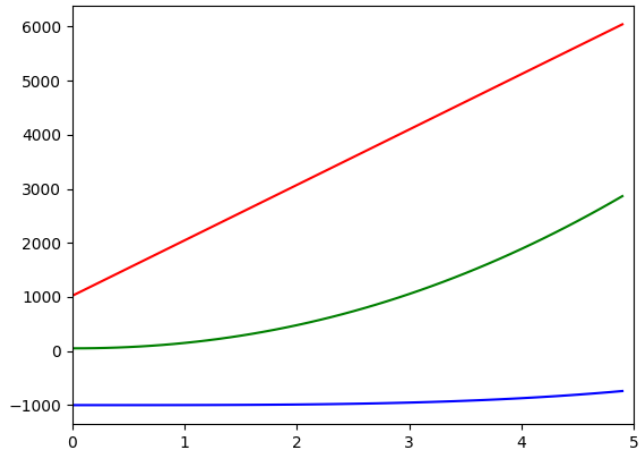
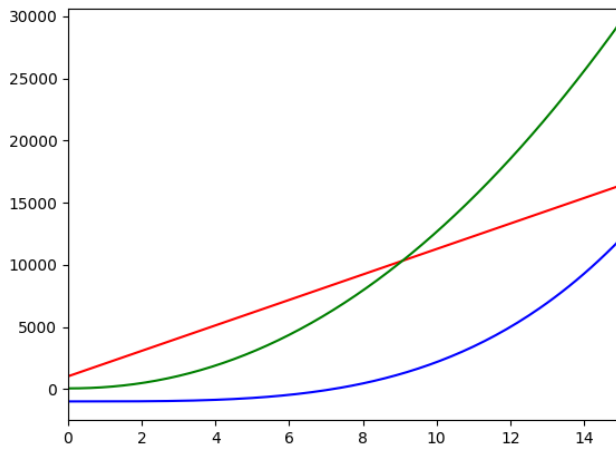


Q1:

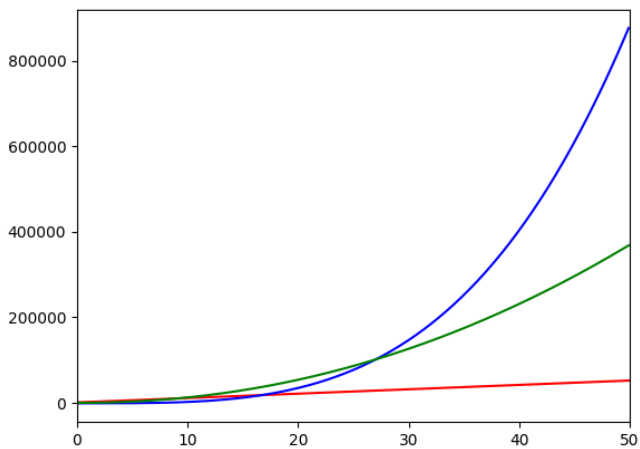
As n starts off and is small, f_1 has the greatest value, followed by f_3 and finally f_2 .



As n continues to increase, f_3 overtakes f_1 in value, while f_2 is the least but showing exponential growth



As n is very large, f_2 has the largest value, and f_3 has the second highest, while f_1 is the least. f_3 and f_1 have lower rates of growth than f_2 .



Python Code:

```
import math
import numpy as np
import matplotlib.pyplot as plt

msize = [5, 15, 50]

# red dashes, blue squares and green triangles
# plt.plot(t, t, 'r--', t, t**3.5 - 2**10, 'bs', t, 100*t**2.1 + 50, 'g^')
for item in msize:
    t = np.arange(0, item, 0.1)
    plt.plot(t, (2**10)*t + (2**10), 'red', t, t**3.5 - 1000, 'blue', t,
100*t**2.1 + 50, 'green')
    plt.xlim(0, item)
    plt.rcParams["figure.figsize"] = (7,7)
    plt.show()
```

Q2:

$$2^{(n+1) \cdot 3} \leq c \cdot 2^n$$
$$2^{1 \cdot 3} \cdot 2^n \leq c \cdot 2^n$$

$$n_0 = 1 \quad c = 3$$

$$f(n) = O(2^n) \text{ since for } c=3, 3(2^n) > f(n) \text{ when } n > 1$$

$$3^{(2 \cdot n)} \leq c \cdot 3^n$$
$$3^2 \cdot 3^n \leq c \cdot 3^n$$

$$n_0 = 1 \quad c = 10$$

$$f(n) = O(3^n) \text{ since } c=10, 10(3^n) > f(n) \text{ when } n > 1$$

Q3:

$$3. a. (4n)^{150} + (2n + 1024)^{400} \leq c(20n^{400} + (n + 1024)^{200})$$

$$\text{If } n_0 = 1$$

$$(4^{150}) + (2(1) + 1024)^{400} \leq c(20(1)^{400} + (1 + 1024)^{200})$$

$$4^{150} + 1026^{400} \leq c(20^{400} + 1025^{200})$$

$$\frac{4^{150} + 1026^{400}}{20^{400} + 1025^{200}} \leq c$$

$$n_0 = 1 \quad c = \frac{4^{150} + 1026^{400}}{20^{400} + 1025^{200}} + 1$$

$$f(n) = O(g(n)) \text{ since when } c = \frac{4^{150} + 1026^{400}}{20^{400} + 1025^{200}} + 1, c \cdot g(n) > f(n) \text{ when } n > 1$$

$$b. n^{1.4} \cdot 4^n \leq c(n^{200} + 3.99)^n$$

$$\text{If } n_0 = 1$$

$$(1)^{1.4} \cdot 4^{(1)} \leq c(1^{200} + 3.99)^1$$

$$4 \leq c(4.99)$$

$$n_0 = 1 \quad c = 1$$

$$f(n) = O(g(n)) \text{ since when } c=1, c \cdot g(n) > f(n) \text{ when } n > 1$$

$$c. 2^{\log(n)} \leq c n^{1024}$$

$$\text{If } n_0 = 1$$

$$2^{\log(1)} \leq c \cdot (1)^{1024}$$

$$1 \leq c$$

$$n_0 = 1 \quad c = 2$$

$$f(n) = O(g(n)) \text{ since when } c=2, c \cdot g(n) > f(n) \text{ when } n > 1$$

Q4:

4

```

1: i = 1
2: while i ≤ n do
3:   A[i] = i
4:   i = i + 1
5: end while
6: for j ← 1 to n do
7:   i = j
8:   while i ≤ n do
9:     A[i] = i
10:    i = i + j
11:  end while
12: end for

```

Iterates n times since $i = i + 1$

For loop will run n times

As the for loop progresses, the while loop will under go less and less iterations as j increases, so its $\log(n)$. However, repeats n times, so $n \log(n)$

$$f(n) = C_1 + (C_2 + C_3 + C_4 + C_6 + C_7) \cdot n + (C_8 + C_9 + C_{10}) \cdot \log(n) \cdot n$$

$f(n)$ grows $n \log(n)$ as n grows large

Q5:

5

```

1: x = 0
2: for i ← 0 to n do
3:   for j ← 0 to (i × n) do
4:     x = x + 10
5:   end for
6: end for

```

$\frac{n(n(n+1))}{2}$

$\sum_{i=1}^n i \cdot n = n \sum_{i=1}^n i = n \frac{n(n+1)}{2}$

$$f(n) = C_1 + C_2 n + (C_3 + C_4) n \left(\frac{n(n+1)}{2} \right)$$

$f(n)$ grows n^3 as n grows very large