

1. Show $\hat{J}_z \hat{J}_x |+\rangle \neq \hat{J}_x \hat{J}_z |+\rangle$
for a $j = \frac{1}{2}$ particle

2. Townsend says that the eigenstates of some observable, let's call them $|\lambda\rangle$, satisfy $\langle \lambda | \lambda \rangle = 1$. Why?

3. Find the representation of \hat{J}_+ for a $j = \frac{1}{2}$ particle in the z representation. Check that it has the right effect on the $|+\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$ and $|-\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$ states

4. Use your result from 1 along with $\hat{J}_y = \frac{\hbar}{2} \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$ to verify $[\hat{J}_z, \hat{J}_x] = i\hbar \hat{J}_y$