

? Eigenvalues

`Eigenvalues[m]` gives a list of the eigenvalues of the square matrix m .

`Eigenvalues[{m, a}]` gives the generalized eigenvalues of m with respect to a .

`Eigenvalues[m, k]` gives the first k eigenvalues of m .

`Eigenvalues[{m, a}, k]` gives the first k generalized eigenvalues. >>

```
In[ ]:= sx = 1 / 2 { {0, 2, 0, 0, 0}, {2, 0,  $\sqrt{6}$ , 0, 0},  
                  {0,  $\sqrt{6}$ , 0,  $\sqrt{6}$ , 0}, {0, 0,  $\sqrt{6}$ , 0, 2}, {0, 0, 0, 2, 0} }
```

```
Out[ ]:= { {0, 1, 0, 0, 0}, {1, 0,  $\sqrt{\frac{3}{2}}$ , 0, 0},  
          {0,  $\sqrt{\frac{3}{2}}$ , 0,  $\sqrt{\frac{3}{2}}$ , 0}, {0, 0,  $\sqrt{\frac{3}{2}}$ , 0, 1}, {0, 0, 0, 1, 0} }
```

```
In[ ]:= MatrixForm[sx]
```

Out[]//MatrixForm=

$$\begin{pmatrix} 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & \sqrt{\frac{3}{2}} & 0 & 0 \\ 0 & \sqrt{\frac{3}{2}} & 0 & \sqrt{\frac{3}{2}} & 0 \\ 0 & 0 & \sqrt{\frac{3}{2}} & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \end{pmatrix}$$

```
In[ ]:= Eigenvalues[sx]
```

```
Out[ ]:= {-2, 2, -1, 1, 0}
```

Did we expect this?

Now let's get the eigenvectors

? IdentityMatrix

`IdentityMatrix[n]` gives the $n \times n$ identity matrix. >>

? Eigenvectors

Eigenvectors[m] gives a list of the eigenvectors of the square matrix m .
 Eigenvectors[$\{m, a\}$] gives the generalized eigenvectors of m with respect to a .
 Eigenvectors[m, k] gives the first k eigenvectors of m .
 Eigenvectors[$\{m, a\}, k$] gives the first k generalized eigenvectors. >>

```
In[ ]:= allEV = Eigenvectors[sx]
```

```
Out[ ]:= {{1, -2,  $\sqrt{6}$ , -2, 1}, {1, 2,  $\sqrt{6}$ , 2, 1},
          {-1, 1, 0, -1, 1}, {-1, -1, 0, 1, 1}, {1, 0,  $-\sqrt{\frac{2}{3}}$ , 0, 1}}
```

```
In[ ]:= myEV = allEV[[2]]
```

```
Out[ ]:= {1, 2,  $\sqrt{6}$ , 2, 1}
```

? Normalize

Normalize[v] gives the normalized form of a vector v .
 Normalize[z] gives the normalized form of a complex number z .
 Normalize[$expr, f$] normalizes with respect to the norm function f . >>

I'm guessing that the second vector above corresponds to +2 since this is the second Eigenvalue listed above.

```
In[ ]:= n = Normalize[myEV]
```

```
Out[ ]:= { $\frac{1}{4}$ ,  $\frac{1}{2}$ ,  $\frac{\sqrt{\frac{3}{2}}}{2}$ ,  $\frac{1}{2}$ ,  $\frac{1}{4}$ }
```

Let's check if we're using the right vector

```
In[ ]:= Dot[sx, n]
```

```
Out[ ]:= { $\frac{1}{2}$ , 1,  $\sqrt{\frac{3}{2}}$ , 1,  $\frac{1}{2}$ }
```

This looks like 2 times the normalized vector, so that confirms that we're dealing with the right Eigenvector.