

Homework 11 - Classification of Abelian Groups

1. List all abelian groups with the following orders.

(a) Order = 27

(b) Order = 500

(c) Order = 900

2. How many elements of order 2 are in the following groups of order 16?

(a) \mathbb{Z}_{16}

(b) $\mathbb{Z}_4 \times \mathbb{Z}_4$

(c) $\mathbb{Z}_4 \times \mathbb{Z}_2 \times \mathbb{Z}_2$

3. How many elements of order 4 are in the following groups of order 16?

(a) \mathbb{Z}_{16}

(b) $\mathbb{Z}_4 \times \mathbb{Z}_4$

(c) $\mathbb{Z}_4 \times \mathbb{Z}_2 \times \mathbb{Z}_2$

4. Answer the following question by computing the order (using the 1st isomorphism theorem) and then checking orders of elements.

Identify $(\mathbb{Z}_{16} \times \mathbb{Z}_{16}) / \langle (2, 2) \rangle$ as a product of cyclic groups (without a quotient).