

# Trigonometric Derivatives

## Trigonometric Derivatives

$$\begin{array}{lll} \frac{d}{dx} [\sin(x)] = \cos(x) & \frac{d}{dx} [\sec(x)] = \sec(x) \tan(x) & \frac{d}{dx} [\csc(x)] = -\csc(x) \cot(x) \\ \frac{d}{dx} [\cos(x)] = -\sin(x) & \frac{d}{dx} [\tan(x)] = \sec^2(x) & \frac{d}{dx} [\cot(x)] = -\csc^2(x) \end{array}$$

## Higher Derivatives of $\sin(x)$

$$\begin{array}{llll} f(x) = \sin(x) & f'(x) = \cos(x) & f''(x) = -\sin(x) & f'''(x) = -\cos(x) \\ f^{(4)}(x) = \sin(x) & f^{(5)}(x) = \cos(x) & f^{(6)}(x) = -\sin(x) & f^{(7)}(x) = -\cos(x) \end{array}$$

1. Use the product rule to compute derivative  $f'(x)$  of the following.

A.  $f(x) = 3x \sin x$

B.  $f(x) = 5x^3 \tan x$

C.  $f(x) = 3x^2 \cos x$

D.  $f(x) = 2x^5 \sec x$

E.  $f(x) = 5 \sin x \cos x$

F.  $f(x) = 7 \sin x \sec x$

G.  $f(x) = x^4 \sin x \tan x$

H.  $f(x) = \sin x \tan x \sec x$

2. Find the tangent line to  $y = x^2 \sin x$  at  $x = \frac{\pi}{2}$ .

**3.** Use the quotient rule to compute derivative  $f'(x)$  of the following.

**A.**  $f(x) = \frac{3 \sin x}{x + 1}$

**B.**  $f(x) = \frac{5x^3}{\tan x}$

**C.**  $f(x) = \frac{5 \cos x}{x^2 + x}$

**D.**  $f(x) = \frac{2 \sec x}{x^5 + x^3}$

**E.**  $f(x) = \frac{5 \sin x}{\cos x}$

**F.**  $f(x) = \frac{7 \sec x}{\cos x}$

**G.**  $f(x) = \frac{x^4 \tan x}{\sin x}$

**H.**  $f(x) = \frac{\sin x \sec x}{\tan x}$

**4.** Find the tangent line to  $y = \frac{\sin x}{x^2 + 1}$  at  $x = 0$ .