

# Applied Deep Learning

## Chapter 8: Representation and Generation

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# Generating New Data via AEs

*Let's keep the track of their applications*

- ① Compression
- ② Finding a sparse representation of data
- ③ Denoising
- ④ Data Generation

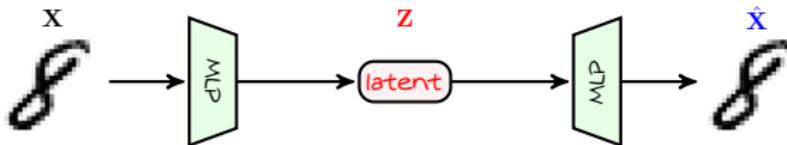
↳ We intend to generate a new sample by our decoder from a seed

- ↳ for instance we generate a random seed and give it to decoder
- ↳ the decoder returns an image which was not in the dataset

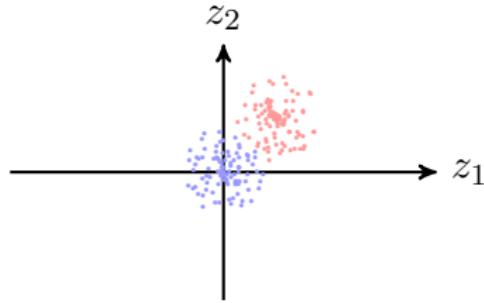
- + That sounds crazy!
- Well! It's not as crazy as it sounds

## Looking into Latent Space

Let's get back to our **MNIST** example: *assume that we set the dataset to only contain images of handwritten 1 and 8, and train an AE to compress them into 2-dimensional latent representations*

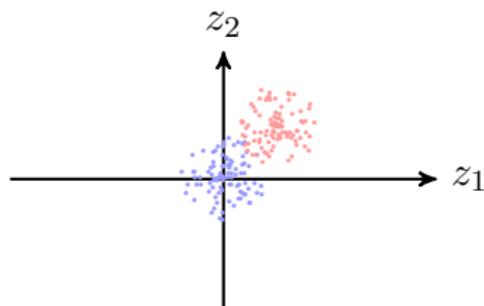


We now do a simple experiment: we pass all images of **1** and **8** that we have and mark their latent representations with **blue** and **red**



## Looking into Latent Space

These points show a specific behavior: *for each class, they are concentrated within an specific region*



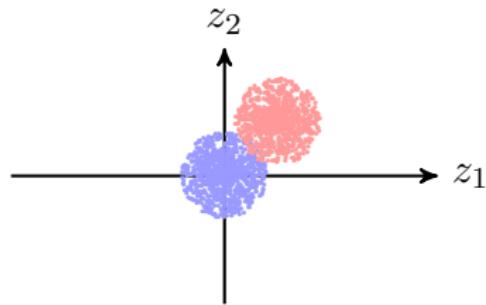
### Recall: Data Space and Distribution

In Chapter 3 we said that we can look at our dataset as a set of **samples** drawn by **some distribution** from a **data space** that contains all possible data-points

This means that we have actually lots of **other possible handwritten 1 and 8** that are not available in our dataset!

## Looking into Latent Space

- + What happens if we send all of them through our AE?
- Well! We can't say, as we have no access to them, but we may guess!



They are probably some **compact regions**

we call the union of those regions the **latent space**

Similar to data space, we **cannot** access it! We just **imagine** it!

# First Try for Generating Data

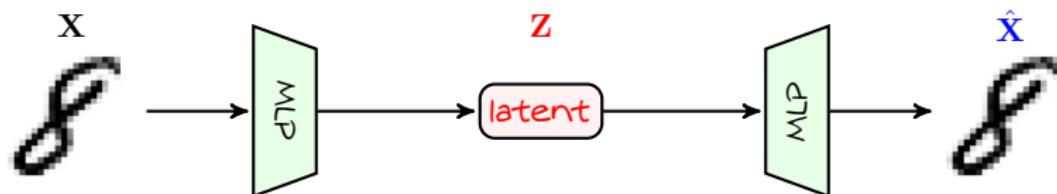
We could use this behavior to generate a new data

- We sample **a new point** in the region that we **guess** is the **latent space**
- We send this sample over **the decoder** of AE: if we are **lucky**
  - ↳ This sample is **latent representation** of a data-point that is **out of our dataset**
  - ↳ The decoder is trained well and can **reconstruct** that **data-point**
  - ↳ We have now a **data-point** out of our dataset

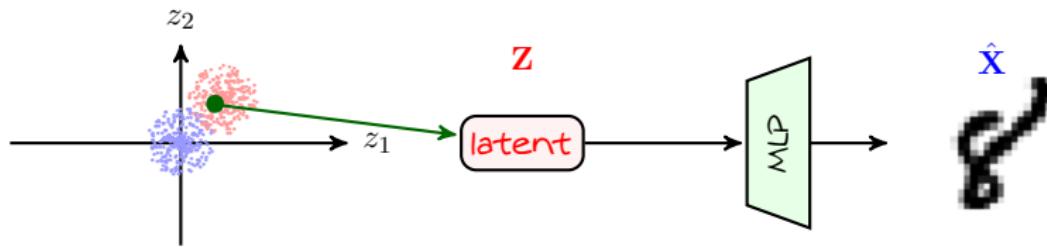
We have generated data out of some random **seed**  $\equiv$  **latent sample**

# First Try for Generating Data

We first train



We then sample the latent space



## Drawbacks of Generation via Vanilla AEs

Even though the idea seems to be **intuitive**: it turns out that it does **not** work very well when we use **basic AE architectures**

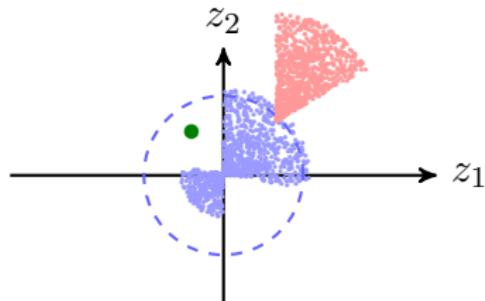
- Frequency of **invalid** generated data is quite high
  - ↳ For instance, the **decoder** returns an image which is **not** a digit
- This is **not** due to **bad training**: it happens even if AE **compresses perfectly**

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The main reason is our significant **lack of knowledge** about **latent space**

- We guessed that **latent space** is compact and **smoothly shaped**
  - ↳ Apparently, this is **not** the case!
- By **extensive experimental investigations**, we could see
  - ↳ **Latent space** can be **extremely asymmetric**
  - ↳ It can be **hugely discontinuous**

# Drawbacks of Generation via Vanilla AEs



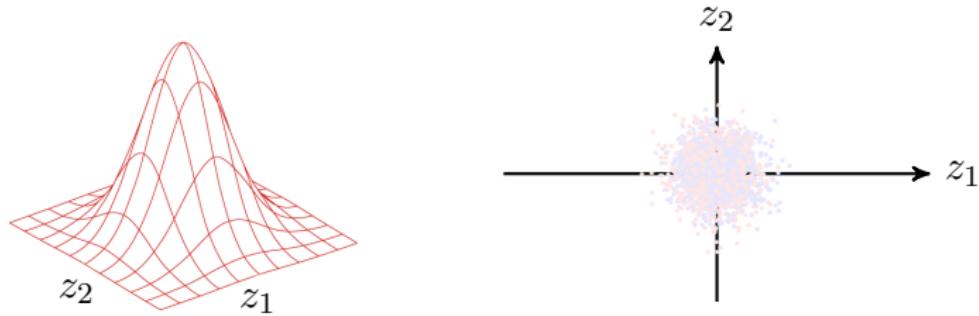
When we sample from the *postulated latent space*

- with *high chance* we could sample from a region out of true *latent space*
  - ↳ We hence send a *compressed* version of *invalid* image
- decoder returns an *invalid data-point!*
- + How can we resolve this issue?
  - We may *restrict* encoder to encode into *compact and symmetric* region

## Generating via Variational AEs

Variational AEs apply some trick to *make sure that*

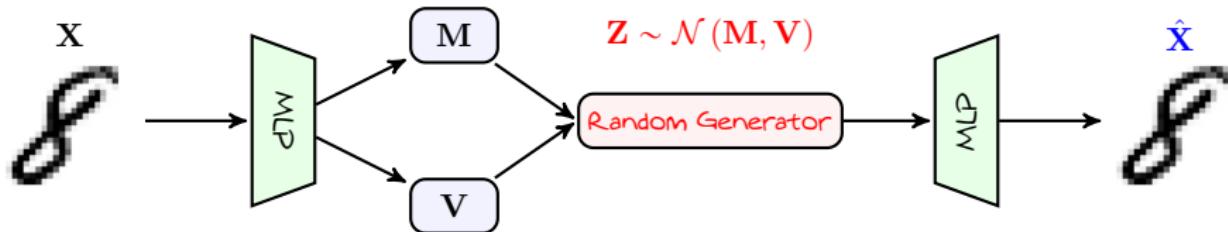
*latent representation* look like samples of a *Gaussian distribution*



Specifically, a Gaussian distribution with *mean zero* and *variance one*:  $\mathcal{N}(\mathbf{0}, \mathbf{1})$

- + How can we do it?
- Well! The trick is quite sophisticated!

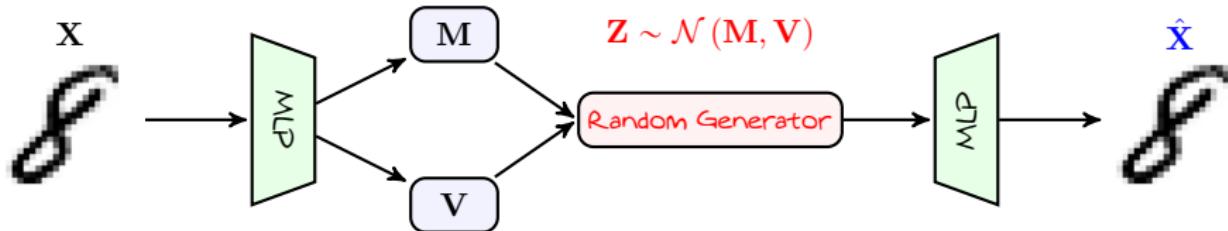
## Variational AE: Architecture



Let's formulate: say input is  $X$ , *latent representation* is  $Z$ , and  $\hat{X}$  is *output*

- We start by encoding: encoder gets  $X$  and returns
  - ↳  $M$  which is of same shape as  $Z$ : this plays the role of *mean*
  - ↳  $V$  which is of same shape as  $Z$ : this plays the role of *-variance*
- We also then generate *latent representations* at random
  - ↳  $Z$  is generated from a *Gaussian distribution*
  - ↳ *Mean* of  $Z$  is  $M$  and its *variance* is  $V$
- We give *latent representations* to the *decoder*
- We train such that *decoder* recovers the *input data*

## Variational AE: Loss



Let's specify the loss

- We need to recover from *latent representation*, i.e., we want  $\hat{\mathbf{X}} = \mathbf{X}$ 
  - ↳ Loss is proportional to the difference between  $\mathbf{X}$  and  $\hat{\mathbf{X}}$
- We want a *zero-mean* and *unit-variance* Gaussian *latent representation*
  - ↳ Distribution of  $\mathbf{Z}$  should be  $\mathcal{N}(\mathbf{0}, \mathbf{1})$
  - ↳ But  $\mathbf{Z}$  is generated as  $\mathcal{N}(\mathbf{M}, \mathbf{V})$
  - ↳ Loss should be *penalized* by difference between the two distribution

# Loss in VAEs

*Loss is proportional to recovery error and difference between actual and intended distributions of  $\mathbf{Z} \equiv$  let's call them  $p_{\mathbf{Z}}$  and  $q_{\mathbf{Z}}$ , respectively*

$$\hat{R} = \mathcal{L}(\hat{\mathbf{X}}, \mathbf{X}) + \lambda \text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}})$$

*for regularizer  $\lambda$  and a difference measure  $\text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}})$*

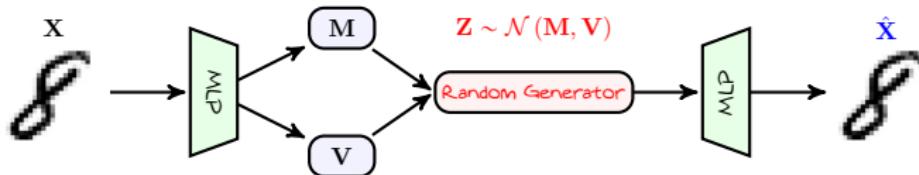
*The classical choice for  $\text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}})$  is the KL-divergence*

$$\begin{aligned} \text{Div}(p_{\mathbf{Z}}, q_{\mathbf{Z}}) &= \text{KL}(p_{\mathbf{Z}} \| q_{\mathbf{Z}}) \\ &= \int p_{\mathbf{Z}}(\mathbf{Z}) \log \frac{p_{\mathbf{Z}}(\mathbf{Z})}{q_{\mathbf{Z}}(\mathbf{Z})} d\mathbf{Z} = F(\mathbf{M}, \mathbf{V}) \end{aligned}$$

*So, we basically train by minimizing*

$$\hat{R} = \mathcal{L}(\hat{\mathbf{X}}, \mathbf{X}) + \lambda F(\mathbf{M}, \mathbf{V})$$

# Training VAEs



Let's see how training looks: say we are training with single sample  $\mathbf{X}$

- Pass forward  $\mathbf{X}$  through encoder and decoder
- Backpropagate by first computing  $\nabla_{\hat{\mathbf{x}}} \hat{R}$ 
  - ↳ Backpropagate till the **latent space**
  - ↳ At the **bottleneck**, we need to compute  $\nabla_M \hat{R}$  and  $\nabla_V \hat{R}$

$$\nabla_M \hat{R} = \underbrace{\nabla_{\hat{\mathbf{x}}} \hat{R} \circ \nabla_{\mathbf{M}} \hat{\mathbf{x}}}_{\text{computed by backpropagation}} + \lambda \nabla_{\mathbf{M}} F(\mathbf{M}, \mathbf{V})$$

- ↳ Start from  $\nabla_M \hat{R}$  and  $\nabla_V \hat{R}$  backpropagate till input
- Update weights and go for the next round

## VAEs: Final Remarks

### Attention!

We have skipped **too much details** to make it very simple: the concrete approach to understand VAEs is to

- ① Start with looking at the NNs as machines that realize distributions
- ② Get to the problem of **Variational Inference**
- ③ Develop an AE that performs **Variational Inference**

We then end up with VAEs

The above approach will be taken in the course **Generative AI**

But for now: you have the **main tools** to **implement a VAE**

- ↳ You may just be unsure about **some details**, e.g.,
  - ↳ Why particular expressions are defined that way?!
- ↳ You can find the answers in the course **Generative AI**

# The End!

Remember that you have the *main tools* to apply *deep learning*

- ↳ Always search for the *main three components*
  - ↳ Model, Dataset and Loss
- ↳ Always imagine how to *backpropagate* over the architecture
- ↳ You got into new challenges?
  - ↳ Search *online* 😊
  - ↳ Reach out to me! I would be more than happy!

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Next in line ...

- ↳ This Summer Semester
  - ↳ Generative AI
- ↳ Next Fall Semester
  - ↳ Creative Applications of NLP
  - ↳ Reinforcement Learning