## Application of Gaussian Naive Bayes (1)

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```
[]: import numpy as np
  import pandas as pd
  import seaborn as sns
  import matplotlib.pyplot as plt
  from sklearn.model_selection import train_test_split
  from sklearn.metrics import accuracy_score
  from sklearn.datasets import load_breast_cancer
```

```
[]: class GaussianNB:
         def __init__(self, priors=None, var_smoothing=1e-9):
             self.priors = priors
             self.var_smoothing = var_smoothing
             self.theta_ = None
             self.var_ = None
             self.class_priors_ = None
             self.classes_ = None
         def _check_input(self, X):
             """Ensure the input is a numpy array of numeric types."""
             if not isinstance(X, np.ndarray):
                 try:
                     X = np.array(X, dtype=np.float64)
                 except ValueError:
                     raise ValueError("Input data X must be a numeric array.")
             return X
         def logprior(self, class_ind):
             return np.log(self.class_priors_[class_ind])
         def loglikelihood(self, Xi, class_ind):
             mean = self.theta_[class_ind]
             var = self.var_[class_ind]
             # Debugging print statements
```

```
#print("Xi type:", type(Xi), "Xi shape:", Xi.shape)
       #print("Mean type:", type(mean), "Mean shape:", mean.shape)
       #print("Var type:", type(var), "Var shape:", var.shape)
       numerator = -0.5 * np.sum(np.log(2. * np.pi * var))
       denominator = -0.5 * np.sum(((Xi - mean) ** 2) / var)
       return numerator + denominator
  def posterior(self, Xi, class_ind):
       return self.logprior(class_ind) + self.loglikelihood(Xi, class_ind)
  def fit(self, X, y):
      n_samples, n_features = X.shape
       self.classes_ = np.unique(y)
       n_classes = len(self.classes_)
       self.theta_ = np.zeros((n_classes, n_features))
       self.var_ = np.zeros((n_classes, n_features))
       self.class_priors_ = np.zeros(n_classes)
       for c_ind, c_id in enumerate(self.classes_):
           X_{class} = X[y == c_{id}]
           self.theta_[c_ind, :] = np.mean(X_class, axis=0)
           self.var_[c_ind, :] = np.var(X_class, axis=0) + self.var_smoothing
           self.class_priors_[c_ind] = np.sum(y == c_id) / n_samples
  def predict(self, X):
       X = self._check_input(X) # Ensuring X is a NumPy array
       predictions = []
       for xi in X:
           # Debugging: Check the type of xi
           if isinstance(xi, str):
               print("Error: Non-numeric data found:", xi)
               continue
           post = [self.posterior(xi, class_ind) for class_ind in_
→range(len(self.classes_))]
           predictions.append(self.classes_[np.argmax(post)])
       return np.array(predictions)
```

```
[]: cancer = load_breast_cancer()
    X, y = cancer.data, cancer.target
    feature_names = cancer.feature_names
    feature_names
```

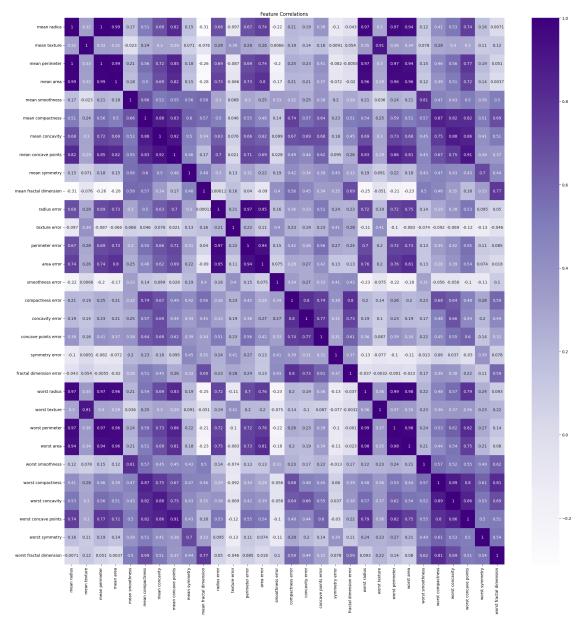
```
[]: array(['mean radius', 'mean texture', 'mean perimeter', 'mean area',
             'mean smoothness', 'mean compactness', 'mean concavity',
             'mean concave points', 'mean symmetry', 'mean fractal dimension',
             'radius error', 'texture error', 'perimeter error', 'area error',
            'smoothness error', 'compactness error', 'concavity error',
            'concave points error', 'symmetry error',
            'fractal dimension error', 'worst radius', 'worst texture',
            'worst perimeter', 'worst area', 'worst smoothness',
             'worst compactness', 'worst concavity', 'worst concave points',
             'worst symmetry', 'worst fractal dimension'], dtype='<U23')
[]: # this pandas dataframe for easier data manipulation
     df_cancer = pd.DataFrame(X, columns=feature_names)
[]: df_cancer
[]:
          mean radius
                                      mean perimeter
                                                                   mean smoothness \
                       mean texture
                                                        mean area
                 17.99
                               10.38
                                               122.80
                                                           1001.0
                                                                            0.11840
                20.57
                               17.77
     1
                                               132.90
                                                           1326.0
                                                                            0.08474
     2
                19.69
                               21.25
                                               130.00
                                                           1203.0
                                                                            0.10960
     3
                11.42
                               20.38
                                                77.58
                                                                            0.14250
                                                            386.1
     4
                20.29
                               14.34
                                               135.10
                                                           1297.0
                                                                            0.10030
     . .
                   . . .
                                  . . .
                                                              . . .
     564
                21.56
                               22.39
                                               142.00
                                                           1479.0
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     565
                20.13
                               28.25
                                               131.20
                                                           1261.0
                                                                            0.09780
                16.60
                               28.08
                                               108.30
                                                            858.1
     566
                                                                            0.08455
     567
                20.60
                               29.33
                                                           1265.0
                                                                            0.11780
                                               140.10
     568
                 7.76
                               24.54
                                                47.92
                                                            181.0
                                                                            0.05263
                            mean concavity
                                              mean concave points
                                                                    mean symmetry \
          mean compactness
     0
                    0.27760
                                     0.30010
                                                           0.14710
                                                                            0.2419
     1
                    0.07864
                                     0.08690
                                                           0.07017
                                                                            0.1812
     2
                    0.15990
                                     0.19740
                                                           0.12790
                                                                            0.2069
     3
                    0.28390
                                     0.24140
                                                           0.10520
                                                                            0.2597
     4
                    0.13280
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     564
                    0.11590
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     565
                    0.10340
                                     0.14400
                                                           0.09791
                                                                            0.1752
     566
                    0.10230
                                     0.09251
                                                           0.05302
                                                                            0.1590
     567
                    0.27700
                                     0.35140
                                                           0.15200
                                                                            0.2397
     568
                    0.04362
                                     0.00000
                                                           0.00000
                                                                            0.1587
          mean fractal dimension
                                                       worst texture \
                                   . . .
                                         worst radius
     0
                          0.07871
                                               25.380
                                                                17.33
     1
                          0.05667
                                               24.990
                                                                23.41
     2
                          0.05999
                                               23.570
                                                                25.53
     3
                          0.09744
                                               14.910
                                                                26.50
                                   . . .
```

```
4
                     0.05883 ...
                                           22.540
                                                             16.67
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564
                     0.05623
                                           25.450
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565
                     0.05533
                                           23.690
566
                     0.05648
                                           18.980
                                                             34.12
567
                     0.07016
                                           25.740
                                                             39.42
568
                     0.05884
                                                             30.37
                                            9.456
     worst perimeter worst area worst smoothness worst compactness
0
               184.60
                            2019.0
                                              0.16220
                                                                   0.66560
                                              0.12380
1
               158.80
                                                                   0.18660
                            1956.0
2
                            1709.0
               152.50
                                              0.14440
                                                                   0.42450
3
                98.87
                             567.7
                                              0.20980
                                                                   0.86630
                            1575.0
4
               152.20
                                              0.13740
                                                                   0.20500
                               . . .
                                                   . . .
564
               166.10
                            2027.0
                                                                   0.21130
                                              0.14100
565
               155.00
                            1731.0
                                              0.11660
                                                                   0.19220
                                              0.11390
566
               126.70
                            1124.0
                                                                   0.30940
567
               184.60
                            1821.0
                                              0.16500
                                                                   0.86810
568
                59.16
                             268.6
                                              0.08996
                                                                   0.06444
     worst concavity worst concave points worst symmetry
0
               0.7119
                                       0.2654
                                                        0.4601
1
               0.2416
                                       0.1860
                                                        0.2750
2
               0.4504
                                       0.2430
                                                        0.3613
3
               0.6869
                                       0.2575
                                                        0.6638
4
               0.4000
                                       0.1625
                                                        0.2364
. .
                  . . .
                                          . . .
                                                            . . .
               0.4107
                                       0.2216
                                                        0.2060
564
565
               0.3215
                                       0.1628
                                                        0.2572
566
               0.3403
                                       0.1418
                                                        0.2218
567
               0.9387
                                       0.2650
                                                        0.4087
568
               0.0000
                                       0.0000
                                                        0.2871
     worst fractal dimension
0
                       0.11890
1
                       0.08902
2
                       0.08758
3
                       0.17300
4
                       0.07678
. .
                          . . .
                      0.07115
564
565
                       0.06637
566
                       0.07820
567
                       0.12400
568
                      0.07039
```

#### [569 rows x 30 columns]

```
[]: #korelasyon matrisi
corr = df_cancer.corr()

plt.figure(figsize=(25, 25))
sns.heatmap(corr, annot=True, cmap='Purples')
plt.title("Feature Correlations")
plt.show()
```



1. Naive Bayes modeli, özelliklerin (features) birbirinden bağımsız olduğu varsayımı üzerine ku-

- ruludur. Yani, bir özelliğin değeri değiştiğinde, bu değişikliğin diğer özellikler üzerinde hiçbir etkisi olmadığını varsayar.
- 2. Eğer özellikler arasında yüksek korelasyon (birbirleriyle ilişki) varsa, bu Naive Bayes modelinin performansını olumsuz etkileyebilir. Korelasyon, iki özelliğin birbirine bağlı olduğunu gösterir, bu da Naive Bayes'in temel varsayımına aykırıdır.
- 3. Bu nedenle, modelin performansını artırmak için, birbirleriyle daha az korele olan özelliklerin bir alt kümesini seçmek önerilir. Bu, modelin doğruluğunu artırabilir çünkü özellikler arasındaki bağımsızlık varsayımına daha yakın bir durum sağlar.

burada düşük korelesyonu olan featurelardan seçeceğim bunları sıralamak istersem:

```
[]: # Korelasyon değerlerini sıralama (büyükten küçüğe)
sorted_corr = corr.unstack().sort_values(kind="quicksort", ascending=True)

# Kendi ile olan korelasyonları (1.0) hariç tutma
sorted_corr = sorted_corr[sorted_corr != 1]

# Sıralı korelasyon değerlerini gösterme
sorted_corr.head(10) # İlk 10 korelasyon çiftini gösteriyoruz.
```

```
[]: mean fractal dimension mean radius
                                                       -0.311631
                             mean fractal dimension
    mean radius
                                                       -0.311631
    mean fractal dimension mean area
                                                       -0.283110
                             mean fractal dimension
                                                      -0.283110
    mean area
    mean perimeter
                             mean fractal dimension
                                                       -0.261477
    mean fractal dimension mean perimeter
                                                       -0.261477
                             worst radius
                                                       -0.253691
     worst radius
                             mean fractal dimension
                                                       -0.253691
                                                       -0.231854
                             mean fractal dimension
     worst area
    mean fractal dimension worst area
                                                       -0.231854
    dtype: float64
```

# Can you use all of the features? Remember the fundamental assumption of naive bayes. Explain your thinking.

Using all the features in a Naive Bayes classifier requires careful consideration due to the fundamental assumption of this model: **feature independence**.

Naive Bayes assumes that the presence (or absence) of a particular feature of a class is unrelated to the presence (or absence) of any other feature. This is often a strong and somewhat unrealistic assumption, especially in complex datasets like the breast cancer dataset, where features can be correlated.

In the context of the breast cancer dataset:

1. **Feature Correlation**: If features are highly correlated, it violates the independence assumption of Naive Bayes. For example, various measurements related to the size and shape of a tumor might be highly interrelated. Using all such features without consideration might lead to redundant or biased information being fed into the model.

- 2. **Dimensionality**: The more features you include, the higher the dimensionality of your data. High dimensionality can lead to overfitting in Naive Bayes, especially if some features do not significantly contribute to the model's predictive power.
- 3. **Noise in Data**: Including all features might introduce noise, especially if some features are not relevant to the target variable. This can decrease the model's overall accuracy.
- 4. **Computation Efficiency**: Using all features can increase the computational complexity and decrease the efficiency of the model, especially if some features are not significantly contributing to the model's performance.

Therefore, while it's technically possible to use all features, it's often beneficial to perform feature selection. This process involves choosing a subset of relevant features for use in model training, which can lead to better model performance and efficiency. In the case of the breast cancer dataset, one could start by examining the features' correlations and eliminating those that are highly correlated with others. Additionally, feature importance techniques, like mutual information or principal component analysis (PCA), can be used to reduce the number of features while retaining most of the informational content.

```
[]: # Naive Bayes assumes independence between features.
# Highly correlated features might affect the performance.
# Select a subset of features that are less correlated.
selected_features = ['mean fractal dimension', 'mean radius', 'mean area', 'mean_
→perimeter'] # Example features
```

[]: df\_cancer.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 569 entries, 0 to 568
Data columns (total 30 columns):

#	Column	Non-Null Count	Dtype
0	mean radius	569 non-null	float64
1	mean texture	569 non-null	float64
2	mean perimeter	569 non-null	float64
3	mean area	569 non-null	float64
4	mean smoothness	569 non-null	float64
5	mean compactness	569 non-null	float64
6	mean concavity	569 non-null	float64
7	mean concave points	569 non-null	float64
8	mean symmetry	569 non-null	float64
9	mean fractal dimension	569 non-null	float64
10	radius error	569 non-null	float64
11	texture error	569 non-null	float64
12	perimeter error	569 non-null	float64
13	area error	569 non-null	float64
14	smoothness error	569 non-null	float64
15	compactness error	569 non-null	float64
16	concavity error	569 non-null	float64
17	concave points error	569 non-null	float64

```
18 symmetry error
                                 569 non-null
                                                 float64
     19 fractal dimension error 569 non-null
                                                 float64
     20 worst radius
                                 569 non-null
                                                 float64
     21 worst texture
                                569 non-null
                                                 float64
     22 worst perimeter
                                569 non-null
                                                 float64
     23 worst area
                                569 non-null
                                                 float64
     24 worst smoothness
                                569 non-null
                                                float64
                               569 non-null
     25 worst compactness
                                                 float64
     26 worst concavity
                                569 non-null
                                                float64
     27 worst concave points
                                569 non-null
                                                 float64
     28 worst symmetry
                                 569 non-null
                                                 float64
     29 worst fractal dimension 569 non-null
                                                 float64
    dtypes: float64(30)
    memory usage: 133.5 KB
[]: # Extract selected features
    X_selected = df_cancer[selected_features]
     # Split the data
    X_train, X_test, y_train, y_test = train_test_split(X_selected, y, test_size=0.
     \rightarrow3, random_state=42)
[]: print("X_train shape:", X_train.shape)
    print("X_test shape:", X_test.shape)
    X_train shape: (398, 4)
    X_test shape: (171, 4)
[]: # Initialize and train the Gaussian Naive Bayes classifier
    clf = GaussianNB()
    clf.fit(X_train, y_train)
     # Make predictions
    predictions = clf.predict(X_test)
     # Print accuracy score
    print("Accuracy score:", accuracy_score(y_test, predictions))
```

Accuracy score: 0.9239766081871345