HOMEWORK 4 - ECE 4560 ERICKSON, BRETT

HOMEWORK HOURS:
LAB HOURS:
DIFFICULTY:

1) a)
$\hat{\xi} = \begin{bmatrix} 0 & \pi/2 & 10 \\ -\pi/2 & 0 & 2 \\ 0 & 0 & 0 \end{bmatrix}$ BASED ON $\begin{bmatrix} [w]_x & v_1 \\ 0 & 0 \end{bmatrix}$ WHERE $v_1 = \begin{bmatrix} 10 \\ 2 \end{bmatrix}$
& $w = -\pi/2$ $[\star]_x = \begin{bmatrix} 0 & -\star \\ \star & 0 \end{bmatrix}$

b) $\hat{\xi} = \begin{bmatrix} 0 & -\pi/2 & \pi/4 & 4 \\ \pi/2 & 0 & -\pi & 2 \\ -\pi/4 & \pi & 0 & 3 \\ 0 & 0 & 0 & 0 \end{bmatrix}$ WHERE $w = \begin{bmatrix} \pi \\ \pi/4 \\ \pi/2 \end{bmatrix}$ AND $v = \begin{bmatrix} 4 \\ 2 \\ 3 \end{bmatrix}$

c) $\xi = [7, -3\ \pi/8]^T$

2) a) $[v]_x = \begin{bmatrix} 0 & -3 & 2 \\ 3 & 0 & -1 \\ -2 & 1 & 0 \end{bmatrix}$ BY DEF OF SKEW SYM. MATRIX

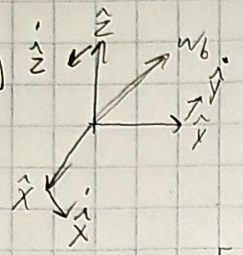
b) $v = [3, 5, 2]^T$

3) a) SPATIAL TWIST, A REPRESENTATION OF THE LINEAR VELOCITY AND ROTATION RATE OF A RIGID BODY, AS EXPERIENCED BY A POINT AT THE WORLD ORIGIN, HAD THAT POINT BEEN DEFINED AS PART OF THE RIGID BODY
FOR SE(2), REQ 3 ENTRIES
FOR SE(3), REQ 6 ENTRIES

b) BODY TWIST, SIMILAR TO ABOVE, BUT DEFINED BY A POINT WITHIN THE BODY

4) $R_{ba} = R_{ab}^T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix}$ $p_b = R_{ba} p_a = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} = \begin{bmatrix} 1 \\ 3 \\ -2 \end{bmatrix}$

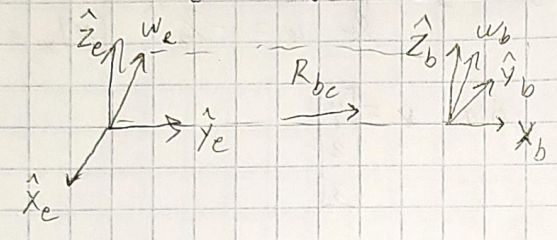
5) a)




$$\dot{\hat{x}}_b = \begin{bmatrix} 0 & -1 & 1 \\ 1 & 0 & 0 \\ -1 & 0 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ -1 \end{bmatrix} \qquad \dot{\hat{y}} = [\omega_b]_\times \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} -1 \\ 0 \\ 0 \end{bmatrix} \qquad \dot{\hat{z}} = [\omega_b]_\times \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

b)

$$R_{be} = \begin{bmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \qquad R_{eb} = \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \Rightarrow \omega_e = R_{eb}\,\omega_b = \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix}$$



Lab Component:

Code at: https://github.com/berickon3/ECE-4560_Lab.git
Video at: https://youtu.be/dmS4EUwlUAU

Had a little difficulty with resolving the path as written, so added a bit of code there to find the .xml file.

Group brainstormed and thought of a long exposure light drawing to be done by the robot arm.