# worksheet 10

December 9, 2021

# Worksheet 10 - Clustering

#### 1.0.1 Lecture and Tutorial Learning Goals:

After completing this week's lecture and tutorial work, you will be able to:

- Describe a case where clustering would be an appropriate tool, and what insight it would bring from the data.
- Explain the k-means clustering algorithm.
- Interpret the output of a k-means cluster analysis.
- Perform k-means clustering in R using k-means
- Visualize the output of k-means clustering in R using a coloured scatter plot
- Identify when it is necessary to scale variables before clustering and do this using R
- Use the elbow method to choose the number of clusters for k-means
- Describe advantages, limitations and assumptions of the k-means clustering algorithm.

```
[1]: ### Run this cell before continuing.
     library(tidyverse)
     library(forcats)
     library(repr)
     library(broom)
     options(repr.matrix.max.rows = 6)
     source('tests_worksheet_10.R')
     source("cleanup worksheet 10.R")
```

# Attaching packages

tidyverse

1.3.0

```
ggplot2 3.3.2
                            0.3.4
                    purrr
tibble 3.0.3
                    dplyr
                            1.0.2
tidyr
        1.1.2
                    stringr 1.4.0
        1.3.1
                    forcats 0.5.0
readr
```

Warning message:

"package 'ggplot2' was built under R version 4.0.1"

Warning message:

"package 'tibble' was built under R version 4.0.2"

Warning message:

"package 'tidyr' was built under R version 4.0.2"

```
Warning message:
"package 'dplyr' was built under R version 4.0.2"
  Conflicts
tidyverse_conflicts()
 dplyr::filter() masks stats::filter()
 dplyr::lag()
                  masks stats::lag()
Warning message:
"package 'broom' was built under R version 4.0.2"
Attaching package: 'testthat'
The following object is masked from 'package:dplyr':
    matches
The following object is masked from 'package:purrr':
    is_null
The following object is masked from 'package:tidyr':
    matches
Question 0.0 Multiple Choice: {points: 1}
In which of the following scenarios would clustering methods likely be appropriate?
A. Identifying sub-groups of houses according to their house type, value, and geographical location
B. Predicting whether a given user will click on an ad on a website
C. Segmenting customers based on their preferences to target advertising
D. Both A. and B.
```

and is surrounded by quotation marks (e.g. "F").

[2]: # your code here

Assign your answer to an object called answer 0.0. Make sure your answer is an uppercase letter

```
[3]: test_0.0()
```

[1] "Success!"

E. Both A. and C.

answer0.0 <- "E"

#### Question 0.1 Multiple Choice: {points: 1}

Which step in the description of the k-means algorithm below is *incorrect*?

- 0. Choose the number of clusters
- 1. Randomly assign each of the points to one of the clusters
- 2. Calculate the position for the cluster centre (centroid) for each of the clusters (this is the middle of the points in the cluster, as measured by straight-line distance)
- 3. Re-assign each of the points to the cluster who's centroid is furthest from that point
- 4. Repeat steps 1 2 until the cluster centroids don't change very much between iterations

Assign your answer to an object called answer0.1. Your answer should be a single numerical character surrounded by quotes.

```
[4]: # your code here
answer0.1 <- "3"
```

```
[5]: test_0.1()
```

[1] "Success!"

## 1.1 Hoppy Craft Beer

Craft beer is a strong market in Canada and the US, and is expanding to other countries as well. If you wanted to get into the craft beer brewing market, you might want to better understand the product landscape. One popular craft beer product is hopped craft beer. Breweries create/label many different kinds of hopped craft beer, but how many different kinds of hopped craft beer are there really when you look at the chemical properties instead of the human labels?

We will start to look at the question by looking at a craft beer data set from Kaggle. In this data set, we will use the alcoholic content by volume (abv column) and the International bittering units (ibu column) as variables to try to cluster the beers. The abv variable has values 0 (indicating no alcohol) up to 1 (pure alcohol) and the ibu variable quantifies the bitterness of the beer (higher values indicate higher bitterness).

#### Question 1.0 $\{points: 1\}$

Read in the beers.csv data using read\_csv() and assign it to an object called beer. The data is located within the worksheet\_10/data/ folder.

Assign your dataframe answer to an object called beer.

```
[6]: # your code here
beer <- read_csv("data/beers.csv")
beer</pre>
```

```
Warning message:
"Missing column names filled in: 'X1' [1]"
Parsed with column specification:
cols(
```

```
X1 = col_double(),
abv = col_double(),
ibu = col_double(),
id = col_double(),
name = col_character(),
style = col_character(),
brewery_id = col_double(),
ounces = col_double()
```

	X1	abv	ibu	$\operatorname{id}$	name	style
-	<dbl $>$	<dbl $>$	<dbl $>$	<dbl $>$	<chr $>$	<chr $>$
	0	0.050	NA	1436	Pub Beer	American Pale Lager
	1	0.066	NA	2265	Devil's Cup	American Pale Ale (APA)
A spec_tbl_df: $2410 \times 8$	2	0.071	NA	2264	Rise of the Phoenix	American IPA
	2407	0.055	NA	620	B3K Black Lager	Schwarzbier
	2408	0.055	40	145	Silverback Pale Ale	American Pale Ale (APA)
	2409	0.052	NA	84	Rail Yard Ale (2009)	American Amber / Red A

## [7]: test\_1.0()

#### [1] "Success!"

## Question 1.1 {points: 1}

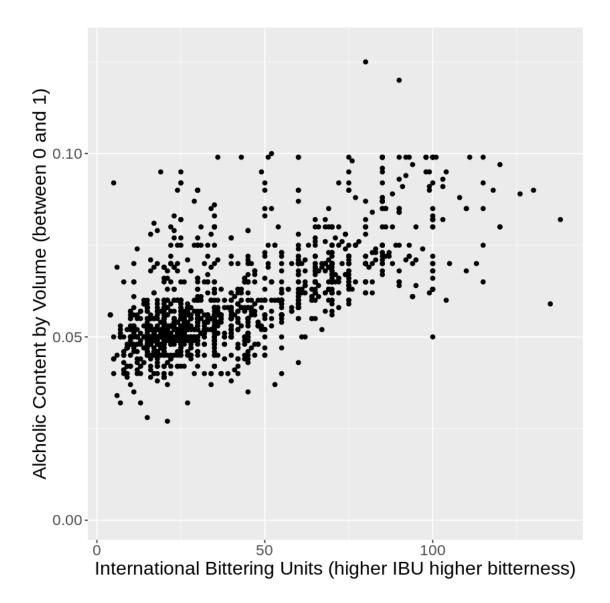
Let's start by visualizing the variables we are going to use in our cluster analysis as a scatter plot. Put ibu on the horizontal axis, and abv on the vertical axis. Name the plot object beer\_eda.

Remember to follow the best visualization practices, including adding human-readable labels to your plot.

```
[8]: # your code here
beer_eda <- ggplot(beer, aes(x = ibu, y = abv)) +
    geom_point() +
    xlab("International Bittering Units (higher IBU higher bitterness)") +
    ylab("Alcholic Content by Volume (between 0 and 1)")+
    theme(text = element_text(size = 17))
beer_eda</pre>
```

#### Warning message:

"Removed 1005 rows containing missing values (geom\_point)."



# [9]: test\_1.1()

# [1] "Success!"

# Question 1.2 $\{points: 1\}$

We need to clean this data a bit. Specifically, we need to remove the rows where ibu is NA, and select only the columns we are interested in clustering, which are ibu and abv.

Assign your answer to an object named clean\_beer.

	ibu	abv
	<dbl $>$	<dbl $>$
	60	0.061
	92	0.099
A tibble: $1405 \times 2$	45	0.079
	50	0.060
	45	0.067
	40	0.055

## [11]: test 1.2()

[1] "Success!"

# Question 1.3.1 Multiple Choice: {points: 1}

Why do we need to scale the variables when using k-means clustering?

- A. k-means uses the Euclidean distance to compute how similar data points are to each cluster center
- B. k-means is an iterative algorithm
- C. Some variables might be more important for prediction than others
- D. To make sure their mean is 0

Assign your answer to an object named answer1.3.1. Make sure your answer is an uppercase letter and is surrounded by quotation marks (e.g. "F").

```
[12]: # your code here
answer1.3.1 <- "A"
```

# [13]: test\_1.3.1()

[1] "Success!"

#### **Question 1.3.2** {points: 1}

Let's do that scaling now. Recall that we used a **recipe** for scaling when doing classification and regression. This is because we needed to be able to split train and test data, compute a standardization on *just* training data, and apply the standardization to *both* train and test data.

But in clustering, there is no train/test split. So let's use the much simpler scale function in R. scale takes in a column of a dataframe and outputs the standardized version of it. We can therefore apply scale to all variables in the cleaned data frame using the map df function.

Note: you could still use a recipe to do this, using prep/bake appropriately. But scale is much simpler.

Assign your answer to an object named scaled\_beer. Use the scaffolding provided.

#### [15]: test\_1.3.2()

#### [1] "Success!"

#### Question 1.4 {points: 1}

From our exploratory data visualization, 2 seems like a reasonable number of clusters. Use the kmeans function with centers = 2 to perform clustering with this choice of k.

Assign your model to an object named beer\_cluster\_k2. Note that since k-means uses a random initialization, we need to set the seed again; don't change the value!

```
[16]: # DON'T CHANGE THE SEED VALUE!
set.seed(1234)

# ... <- kmeans(..., centers = 2)
# your code here
beer_cluster_k2 <- kmeans(scaled_beer, centers = 2)
beer_cluster_k2</pre>
```

K-means clustering with 2 clusters of sizes 917, 488

```
Cluster means:
```

```
ibu abv
1 -0.5830271 -0.5506271
2 1.0955653 1.0346824
```

#### Clustering vector:

```
[297] 1 1 2 2 2 1 1 2 1 1 2 1 1 2 1 1 2 2 2 2 2 2 2 2 2 2 2 1 1 2 2 1 2 2 1 1 2
    [334] \ 1\ 2\ 1\ 1\ 2\ 1\ 1\ 2\ 2\ 1\ 1\ 1\ 1\ 1\ 2\ 2\ 1\ 2\ 2\ 1\ 1\ 2\ 1\ 1\ 1\ 1\ 2\ 1\ 1\ 1\ 1\ 2
    oxed{[}1000oxed{]} oxed{1} oxed{1}
    [1037] 1 2 1 2 2 2 1 1 1 2 1 2 1 1 2 1 2 2 2 1 1 2 2 2 2 1 1 1 2 2 1 1 1 2 2 2 1 1
   Within cluster sum of squares by cluster:
   [1] 465.5831 644.5188
    (between SS / total SS = 60.5 %)
   Available components:
                           "totss"
   [1] "cluster"
                 "centers"
                                                 "tot.withinss"
                                      "withinss"
   [6] "betweenss"
                 "size"
                           "iter"
                                      "ifault"
[17]: test_1.4()
   [1] "Success!"
   Question 1.5 \{points: 1\}
```

Use the augment function from the broom package to get the cluster assignment for each point in the scaled\_beer data frame.

Assign your answer to an object named tidy\_beer\_cluster\_k2.

```
[18]: # ... <- augment(..., ...)
# your code here
tidy_beer_cluster_k2 <- augment(beer_cluster_k2, scaled_beer)
tidy_beer_cluster_k2</pre>
```

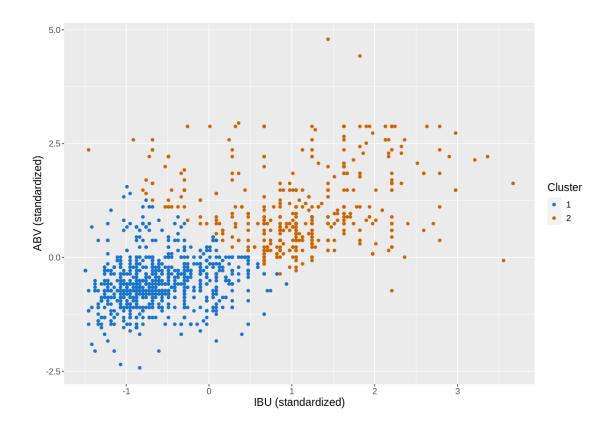
```
ibu
                                  abv
                                                 .cluster
                    <dbl[,1]>
                                  <dbl[,1]>
                                                 <fct>
                    0.66605490
                                  0.08000109
                                                 2
                                                 2
                    1.89900237
                                  2.87899086
                                                 2
A tibble: 1405 \times 3 \quad 0.08811077
                                  1.40583835
                    0.28075881 \quad 0.006343468
                                                 1
                    0.08811077
                                  0.521946846
                                                 2
                    -0.10453727 -0.361944659 1
```

## [19]: test\_1.5()

[1] "Success!"

#### Question 1.6 {points: 1}

Create a scatter plot of abv on the y-axis versus ibu on the x-axis (using the data in tidy\_beer\_cluster\_k2) where the points are labelled by their cluster assignment. Name the plot object tidy\_beer\_cluster\_k2\_plot.



## [21]: test\_1.6()

#### [1] "Success!"

# Question 1.7.1 Multiple Choice: {points: 1}

We do not know, however, that two clusters (k = 2) is the best choice for this data set. What can we do to choose the best K?

- A. Perform cross-validation for a variety of possible k's. Choose the one where within-cluster sum of squares distance starts to decrease less.
- B. Perform cross-validation for a variety of possible k's. Choose the one where the within-cluster sum of squares distance starts to decrease more.
- C. Perform *clustering* for a variety of possible k's. Choose the one where within-cluster sum of squares distance starts to *decrease less*.
- D. Perform *clustering* for a variety of possible k's. Choose the one where the within-cluster sum of squares distance starts to *decrease more*.

Assign your answer to an object called answer1.7.1. Make sure your answer is an uppercase letter and is surrounded by quotation marks (e.g. "F").

```
[22]: # your code here
answer1.7.1 <- "C"
```

## [23]: test\_1.7.1()

[1] "Success!"

# **Question 1.7.2** {points: 1}

Use the glance function from the broom library to get the model-level statistics for the clustering we just performed, including total within-cluster sum of squares.

Assign your answer to an object named beer\_cluster\_k2\_model\_stats.

```
[24]: # your code here
beer_cluster_k2_model_stats <- glance(beer_cluster_k2)
beer_cluster_k2_model_stats</pre>
```

## [25]: test\_1.7.2()

[1] "Success!"

# Question 1.8 $\{points: 1\}$

Let's now choose the best K for this clustering problem. To do this we need to create a tibble with a column named k, where k has values 1 to 10.

Assign your answer to an object named beer\_ks.

A tibble:  $10 \times 1$  3

8 9 10

# [27]: test\_1.8()

[1] "Success!"

#### Question 1.9 {points: 1}

Next we use mutate to create a new column named models in beer\_ks, where we use map to apply the kmeans function to our scaled\_beer data set for each of the k's.

This is a more complicated use of the map function than we have seen previously in the course. This is because we need to iterate over the different values of k, which is the second argument to the kmeans function. In the past, we have used map only to iterate over values of the first argument of a function. Since that is the default, we could simply write map(data\_frame, function\_name). This won't work here; we need to provide our data frame as the first argument to the kmeans function. You might want to refer back to the section of the textbook that explains before completing this question: K-means in R

This will give us a data frame with two columns, the first being k, which holds the values of the k's we mapped (i.e, iterated) over. The second will be models, which holds the k-means model fits for each of the k's we mapped over.

This second column is a new type of column, that we have not yet encountered in this course. It is called a list column. It can contain more complex objects, like models and even data frames (as we will see in a later question). In Jupyter it is easier to preview and understand this more complex data frame using the print function as opposed to calling the data frame itself as we usually do. This is a current limitation of Jupyter's rendering of R's output and will hopefully be fixed in the future.

Assign your answer to an object named beer\_clustering.

Question 2.0 {points: 1}

```
[28]: set.seed(1234) # DO NOT REMOVE
      # ... <- ... %>%
          # mutate(models = map(..., ~kmeans(scaled beer, .x)))
      # your code here
      beer clustering <- beer ks %>%
          mutate(models = map(k, ~kmeans(scaled_beer, .x)))
      print(beer_clustering)
     # A tibble: 10 x 2
            k models
         <int> <list>
      1
             1 <kmeans>
      2
             2 <kmeans>
      3
             3 <kmeans>
      4
             4 <kmeans>
      5
             5 <kmeans>
      6
             6 <kmeans>
      7
             7 <kmeans>
      8
             8 <kmeans>
      9
             9 <kmeans>
     10
            10 <kmeans>
[29]: test 1.9()
     [1] "Success!"
```

Next we use mutate again to create a new column called model\_statistics where we use map to apply the glance function to each of our models (in the models column) to get the model-level statistics (this is where we can get the value for total within sum of squares that we use to choose K).

Here, because we are interating over the first argument to the glance function (which is the models column), we can use the simpler syntax for map as we did earlier in the course.

Assign your answer to an object named beer model stats.

```
[30]: # ... <- ... %>%
           # mutate(... = map(models, ...))
       # your code here
      beer_model_stats <- beer_clustering %>%
            mutate(model statistics = map(models, glance))
      print(beer_model_stats)
      # A tibble: 10 x 3
              k models
                          model statistics
         <int> <list>
      st>
              1 <kmeans> <tibble [1 \times 4]>
       1
              2 <kmeans> <tibble [1 \times 4]>
       2
              3 < means > < tibble [1 \times 4] >
       3
       4
              4 < kmeans > < tibble [1 \times 4] >
       5
              5 < kmeans > < tibble [1 \times 4] >
              6 <kmeans> <tibble [1 \times 4]>
       7
              7 < kmeans > < tibble [1 \times 4] >
       8
             8 <kmeans> <tibble [1 \times 4]>
       9
              9 <kmeans> <tibble [1 \times 4]>
      10
             10 <kmeans> <tibble [1 \times 4]>
[31]: test_2.0()
```

#### [61]:

#### [1] "Success!"

Here when we create our third column, called model\_statistics, we can see it is another list column! This time it contains data frames instead of models! Run the cell below to see how you can look at the data frame that is stored as the first element of the model\_statistics column (model where we used k = 1):

```
1. A tibble: 1 \times 4 totss tot.withinss betweenss iter class (dbl> cdbl> cdbl> cint> 2808 2808 -2.273737e-12 1
```

## Question 2.1 {points: 1}

Now we use the unnest function to expand the data frames in the model\_statistics column so that we can access the values for total within sum of squares as a column.

Assign your answer to an object named beer\_clustering\_unnested.

```
[33]: # ... <- ... %>% unnest(model statistics)
      # your code here
      beer_clustering_unnested <- beer_model_stats %>% unnest(model_statistics)
      print(beer_clustering_unnested)
     # A tibble: 10 x 6
                        totss tot.withinss betweenss iter
             k models
        <int> <list>
                        <dbl>
                <dbl> <int>
     <dbl>
             1 <kmeans> 2808.
                                      2808.
     -2.27e-12
                    1
             2 <kmeans> 2808.
                                      1110.
     1.70e+ 3
      3
             3 <kmeans> 2808.
                                       803.
     2.00e+3
      4
             4 <kmeans> 2808.
                                       624.
     2.18e+ 3
             5 <kmeans> 2808.
                                       567.
     2.24e+ 3
             6 <kmeans> 2808.
                                       417.
     2.39e + 3
      7
             7 <kmeans> 2808.
                                       361.
     2.45e+3
                   6
             8 <kmeans> 2808.
                                       318.
     2.49e + 3
                   5
             9 <kmeans> 2808.
                                       294.
     2.51e+ 3
            10 <kmeans> 2808.
                                       264.
     2.54e + 3
```

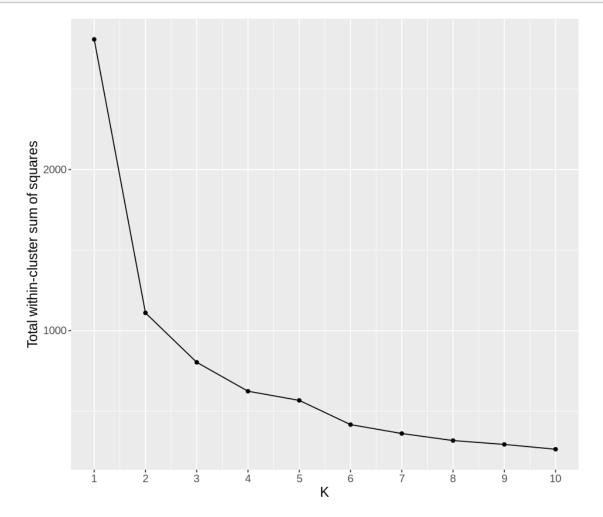
#### [34]: test\_2.1()

#### [1] "Success!"

#### Question 2.2 $\{points: 1\}$

We now have the values for total within-cluster sum of squares for each model in a column (tot.withinss). Let's use it to create a line plot with points of total within-cluster sum of squares versus k, so that we can choose the best number of clusters to use.

Assign your plot to an object called **choose\_beer\_k**. Total within-cluster sum of squares should be on the y-axis and K should be on the x-axis. Remember to follow the best visualization practices, including adding human-readable labels to your plot.



```
[36]: test_2.2()
```

[1] "Success!"

Question 2.3 {points: 1}

From the plot above, which k should we choose?

Assign your answer to an object called answer2.3. Make sure your answer is a single numerical character surrounded by quotation marks.

```
[37]: # your code here
answer2.3 <- "2"
```

```
[38]: test_2.3()
```

[1] "Success!"

#### Question 2.4 {points: 1}

Why did we choose the k we chose above?

- A. It had the greatest total within-cluster sum of squares
- B. It had the smallest total within-cluster sum of squares
- C. Increasing k further than this only decreased the total within-cluster sum of squares a small amount
- D. Increasing k further than this only increased the total within-cluster sum of squares a small amount

Assign your answer to an object called answer2.4. Make sure your answer is an uppercase letter and is surrounded by quotation marks (e.g. "F").

```
[39]: # your code here answer2.4 <- "C"
```

```
[40]: test_2.4()
```

[1] "Success!"

#### Question 2.5 Multiple Choice: {points: 1}

What can we conclude from our analysis? How many different types of hoppy craft beer are there in this data set using the two variables we have?

- A. 1
- B. 2
- C. 3
- D. 4

Assign your answer to an object called answer2.5. Make sure your answer is an uppercase letter and is surrounded by quotation marks (e.g. "F").

```
[41]: # your code here
answer2.5 <- "B"
```

```
[42]: test_2.5()
```

[1] "Success!"

Question 2.6 True or false: {points: 1}

Our analysis might change if we added additional variables, true or false?

Assign your answer to an object called answer2.6. Make sure your answer is written in lowercase and is surrounded by quotation marks (e.g. "true" or "false").

```
[43]: # your code here
answer2.6 <- "true"
```

```
[44]: test_2.6()
```

[1] "Success!"

```
[45]: source("cleanup_worksheet_10.R")
```