

# CENG499

## Homework 1

### Part 1

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- $a_{ik}^{(0)} = a_{ik}^{(0)} - \alpha \frac{\partial SSE(y, O_0^{(2)})}{\partial a_{ik}^{(0)}}$ 
  1.  $\Delta a_{ik}^{(0)} = -\alpha \sum_k \frac{\partial S}{\partial O_0^{(2)}} \frac{\partial O_0^{(2)}}{\partial O_k^{(1)}} \frac{\partial O_k^{(1)}}{\partial a_{ik}^{(0)}}$
  2. Replacing  $S$  with  $(y - O_0^{(2)})^2$
  3. Addressing the outcome of  $\frac{\partial O_0^{(2)}}{\partial O_k^{(1)}}$  as  $t_k$  and the derivative of the weighted sum with respect to  $a_{ik}$  as  $z_k$
  4.  $\Delta a_{ik}^{(0)} = -\alpha \sum_k -(2y - 2O_0^{(2)}) * t_k * O_k^{(1)} (1 - O_k^{(1)}) z_k$
  5.  $a_{ik}^{(0)} = a_{ik}^{(0)} + \alpha \sum_k (2y - 2O_0^{(2)}) * t_k * O_k^{(1)} (1 - O_k^{(1)}) z_k$
- $a_{ik}^{(1)} = a_{ik}^{(1)} - \alpha \frac{\partial SSE(y, O_0^{(2)})}{\partial a_{ik}^{(1)}}$ 
  1.  $\Delta a_{ik}^{(1)} = -\alpha \sum_k \frac{\partial S}{\partial O_0^{(2)}} \frac{\partial O_0^{(2)}}{\partial a_{ik}^{(1)}}$
  2. Replacing  $S$  with  $(y - O_0^{(2)})^2$
  3. Addressing the derivative of the weighted sum with respect to  $a_{ik}$  as  $z_k$
  4.  $\Delta a_{ik}^{(1)} = -\alpha \sum_k -(2y - 2O_0^{(2)}) O_k^{(2)} (1 - O_k^{(2)}) z_k$
  5.  $a_{ik}^{(1)} = a_{ik}^{(1)} + \alpha \sum_k (2y - 2O_0^{(2)}) O_k^{(2)} (1 - O_k^{(2)}) z_k$

- $a_{ik}^{(0)} = a_{ik}^{(0)} - \alpha \frac{\partial CE([l_0, l_1, l_2], O^{(2)} = [O_0^{(2)}, O_1^{(2)}, O_2^{(2)}])}{\partial a_{ik}^{(0)}}$ 
  1.  $\Delta a_{ik}^{(0)} = -\alpha \sum_{k,i} \frac{\partial CE}{\partial O_i^{(2)}} \frac{\partial O_i^{(2)}}{\partial O_k^{(1)}} \frac{\partial O_k^{(1)}}{\partial a_{ik}^{(0)}}$
  2. Replacing  $CE$  with the cross-entropy function.
  3. Addressing the outcome of  $\frac{\partial O_i^{(2)}}{\partial O_k^{(1)}}$  as  $t_{ik}$  and the derivative of the weighted sum with respect to  $a_{ik}$  as  $z_k$
  4.  $\Delta a_{ik}^{(0)} = -\sum_{k,i} \frac{l_i}{O_i^{(2)}} * t_{ik} * O_k^{(1)} (1 - O_k^{(1)}) z_k$
  5.  $a_{ik}^{(0)} = a_{ik}^{(0)} + \sum_{k,i} \frac{l_i}{O_i^{(2)}} * t_{ik} * O_k^{(1)} (1 - O_k^{(1)}) z_k$
- $a_{ik}^{(1)} = a_{ik}^{(1)} - \alpha \frac{\partial CE([l_0, l_1, l_2], O^{(2)} = [O_0^{(2)}, O_1^{(2)}, O_2^{(2)}])}{\partial a_{ik}^{(1)}}$ 
  1.  $\Delta a_{ik}^{(1)} = -\alpha \sum_{k,i} \frac{\partial CE}{\partial O_i^{(2)}} \frac{\partial O_i^{(2)}}{\partial a_{ik}^{(1)}}$
  2. Replacing  $CE$  with the cross-entropy function.
  3. Addressing the derivative of the weighted sum with respect to  $a_{ik}$  as  $z_k$
  4.  $\Delta a_{ik}^{(1)} = -\sum_{k,i} \frac{l_i}{O_i^{(2)}} O_i^{(2)} (1 - O_i^{(2)}) z_k$
  5.  $a_{ik}^{(1)} = a_{ik}^{(1)} + \sum_{k,i} \frac{l_i}{O_i^{(2)}} O_i^{(2)} (1 - O_i^{(2)}) z_k$