

ELMFIRE Verification Suite — Master Report

Verification Team

September 16, 2025

Contents

How to Read This Report	3
1 ignition_mask_bp_convergence	4
1.1 Assumptions	4
1.2 Simulation Setup	4
1.2.1 Parameter Table	4
1.2.2 Method (MATLAB Reference)	4
1.2.3 Input Data	5
1.2.4 Numerical Controls	5
1.3 Expected Results and Reasoning	5
1.4 Verification Plan with ELMFIRE Ensembles	5
1.5 Acceptance Criteria	5
1.6 Results (Mask-Implied Reference)	6
1.7 Results (ELMFIRE Ensembles)	6
1.8 Discussion	6
1.9 Discussion	6
2 wue_transient_heatflux	7
2.1 Methods	7
2.1.1 Theory	7
2.1.2 Assumptions	9
2.1.3 Simulation Setup	9
2.1.4 Input Data	9
2.1.5 Numerical Controls	9
2.2 Expected Results and Reasoning	10
2.3 Acceptance Criteria	10
2.4 Results	10
2.5 Discussion	10

How to Read This Report

Each section includes a full PDF of a verification case report. Cases are ordered by directory name in `cases/`. To add or remove a case from the master report, run the automation script `tools/build_all.sh`.

1 ignition_mask_bp_convergence

Case Summary

Case ID: ignition_mask_bp_convergence

Objective: Justify the Monte Carlo (MC) method used by ELMFIRE for ignition sampling by deriving the expected time-of-arrival (ToA) statistics at a target pixel when ignition is drawn uniformly from a specified mask (square or circle). We compare the empirical ToA distribution from ensembles to the mask-implied expectation, and quantify how many ensembles are needed for convergence.

1.1 Assumptions

- Flat terrain: slope = 0, aspect arbitrary but unused for $SLP = 0$.
- Homogeneous fuel: IFBFM = 102, fixed moisture: $M_1 = 0.03$, $M_{10} = 0.04$, $M_{100} = 0.05$, $M_{lh} = 0.30$, $M_{lw} = 0.60$.
- Steady wind: direction WD20 = 180° (blowing to the north), speed WS20 = 15 mph; canopy terms set to zero ($CC = CH = 0$).
- No spotting/suppression; acceleration factor = 1; length/width cap $LOW_{max} = 8$.
- Coordinates are meters; the ToA along a ray from source to target uses the directional ROS returned by the ellipse kinematics.
- Ignition location X is uniformly distributed on the mask region Ω (square or circle).

1.2 Simulation Setup

1.2.1 Parameter Table

Fuel model	IFBFM	102
Dead fuel moisture	M_1, M_{10}, M_{100}	0.03, 0.04, 0.05
Live fuel moisture	M_{lh}, M_{lw}	0.30, 0.60
Wind (20-ft)	(WD20, WS20)	(180°, 15 mph)
Slope / Aspect	(SLP, ASP)	(0°, 0°)
Adj. factors	($ADJ, ACCEL$)	(1, 1)
Ellipse cap	LOW_{max}	8
Target (m)	\mathbf{y}	(50, 200)
Square mask (m)	Ω_{\square}	$[0, 100] \times [0, 100]$
Circle mask (m)	Ω_{\circ}	center (50, 50), radius $R = 20$

1.2.2 Method (MATLAB Reference)

For a source $\mathbf{x} \in \Omega$, we compute a direction angle $\theta = \text{atan2}(y_y - x_y, y_x - x_x)$, set the fireline normal to $(\cos \theta, \sin \theta)$, update ellipse kinematics via `UX_AND_UY_ELLIPTICAL`, and obtain the directional rate of spread (ROS) magnitude $v(\mathbf{x})$ (ft/min). The straight-line source-to-target distance is $d(\mathbf{x}) = \|\mathbf{y} - \mathbf{x}\|$. Time of arrival is

$$T(\mathbf{x}) = \begin{cases} \frac{d(\mathbf{x})}{v(\mathbf{x}) \cdot \frac{0.3048}{60}}, & \text{if coordinates in meters} \\ \frac{d(\mathbf{x})}{v(\mathbf{x})}, & \text{if coordinates in feet.} \end{cases} \quad (1)$$

The MATLAB driver (provided) evaluates $T(\mathbf{x})$ for all grid points inside the mask (uniform discrete sampling) and produces histograms and sample moments (mean/min/max).

1.2.3 Input Data

Describe input rasters, constants, initial conditions.

1.2.4 Numerical Controls

Mesh resolution, Time step(CFL), level-set solver options, etc.

1.3 Expected Results and Reasoning

Let $X \sim \text{Unif}(\Omega)$ be the ignition location and $T = T(X)$ the induced ToA random variable. The *mask-implied* expected value and CDF are

$$\mathbb{E}[T] = \frac{1}{|\Omega|} \int_{\Omega} \frac{d(\mathbf{x})}{\tilde{v}(\mathbf{x})} d\mathbf{x}, \quad \tilde{v}(\mathbf{x}) = v(\mathbf{x}) \cdot \frac{0.3048}{60} \text{ (m/min)}, \quad (2)$$

$$F_T(t) = \mathbb{P}\left(\frac{d(\mathbf{x})}{\tilde{v}(\mathbf{x})} \leq t\right) = \frac{1}{|\Omega|} \int_{\{\mathbf{x} \in \Omega: d(\mathbf{x}) \leq t \tilde{v}(\mathbf{x})\}} d\mathbf{x}. \quad (3)$$

In special cases:

- If $v(\mathbf{x}) \equiv v_0$ (isotropic ROS), then $T(\mathbf{x}) = d(\mathbf{x})/v_0$ and the ToA distribution is the distance distribution over Ω scaled by $1/v_0$.
- With an anisotropic ellipse (wind-aligned), $v(\mathbf{x})$ varies only through the direction from \mathbf{x} to \mathbf{y} ; the expectation remains an area integral, efficiently approximated by uniform quadrature on the same grid the script uses.

Thus, the MATLAB “all-points-in-mask” evaluation *is* a numerical quadrature for $\mathbb{E}[T]$ and the full F_T , which we treat as the *expected* mask-implied reference.

1.4 Verification Plan with ELMFIRE Ensembles

ELMFIRE ensembles will use identical physics and environmental settings, but ignition locations will be drawn randomly from Ω with equal probability. For an ensemble size N , define the empirical CDF $\hat{F}_T^{(N)}$ and moments (mean $\hat{\mu}_N$, variance $\hat{\sigma}_N^2$). Convergence is assessed against the mask-implied reference (F_T, μ, σ^2) via:

1. **Mean Relative Error (MRE):** $\text{MRE} = |\hat{\mu}_N - \mu|/\mu$.
2. **RMSE of histogram/bin means** over a fixed partition of t .
3. **Kolmogorov–Smirnov (KS) distance:** $D_N = \sup_t |\hat{F}_T^{(N)}(t) - F_T(t)|$.

A practical sample-size target for the mean uses the CLT:

$$N \gtrsim \left(\frac{z_{1-\alpha/2} \sigma}{\varepsilon \mu} \right)^2, \quad (4)$$

where ε is the desired relative error tolerance and $z_{1-\alpha/2}$ the normal quantile. We estimate σ from either the mask quadrature or pilot ensembles.

1.5 Acceptance Criteria

- **Mean:** $\text{MRE} \leq 5\%$.
- **Distribution:** KS distance $D_N \leq 0.05$ (typical); and visual agreement of PDF/CDF.
- **Stability:** Increasing N by a factor of two changes $\hat{\mu}_N$ by $\leq 2\%$ and D_N by ≤ 0.01 .

1.6 Results (Mask-Implied Reference)

This section presents the direct evaluation from the MATLAB loop over all source points inside the mask:

- Histogram/PDF of ToA for the *square* mask (uniform over $[0, 100]^2$).
- Histogram/PDF of ToA for the *circle* mask (center $(50, 50)$, $R = 20$).
- Empirical CDFs and summary moments (mean/min/max) for each mask.

1.7 Results (ELMFIRE Ensembles)

After running N -member ELMFIRE ensembles with random ignition draws on the same mask(s):

1. Compare ensemble histograms/CDFs vs. mask-implied reference.
2. Report $\hat{\mu}_N$, $\hat{\sigma}_N$, MRE, RMSE (bins), and KS D_N .
3. Increase N until criteria in § 5 are satisfied; record the smallest N meeting tolerance.

1.8 Discussion

- Interpret any persistent bias (e.g., due to anisotropic ellipse interacting with mask geometry).
- Note sensitivity to wind speed, fuel model, and target placement.
- Document computational cost vs. accuracy trade-offs for ensemble sizing.

Reproducibility

- MATLAB script commit: `<hash>` (code in repo appendix or link).
- ELMFIRE build: `<compiler/flags>`, binary: `<path>`.
- Command(s): `./run_case.sh`; environment: `<modules/conda env>`.
- Logs available under `cases/ignition_mask_bp_convergence/logs/`.

1.9 Discussion

2 wue_transient_heatflux

Case Summary

Case ID: wue_transient_heatflux

Objective: Verify the WU-E (urban structure) heat-flux prototype that couples a wind-aligned anisotropic fire ellipse (Hamada-style regression) with a piecewise transient design-fire curve for HRRPUA. We check that (i) geometric transformations, (ii) ellipse reach/coverage, (iii) per-cell HRR normalization, and (iv) heat-flux partitions (direct flame contact vs. radiation) reproduce expected behavior and conserve energy consistently.

2.1 Methods

2.1.1 Theory

Coordinate Transformations

Geometric angle from source to target cell:

$$\theta = \arctan(j, i) \quad (\text{rad}). \quad (5)$$

Wind-aligned major-axis angle (radians) from the 20-ft met direction (blowing *from*):

$$\theta_{\text{wind}} = \frac{\pi}{180} (270 - \text{WD}_{20ft}). \quad (6)$$

Relative angle for ellipse formulas:

$$\theta_f = \theta - \theta_{\text{wind}}, \quad R = \sqrt{(i \Delta)^2 + (j \Delta)^2}. \quad (7)$$

Wind-Aligned Ellipse (Hamada-Style)

Convert wind speed to m/s:

$$V = 0.447 \text{WS}_{20ft}. \quad (8)$$

Downwind (D_{\downarrow}), upwind (D_{\uparrow}), and sidewind (D_{\perp}) distances (m) are piecewise functions of V with coefficients depending on (A, D) and scaled by W_p :

$$\text{Low wind } (V < 10): \quad D_{\downarrow} = W_p (D_1 V + D_2), \quad D_{\perp} = W_p (S_1 V + S_2), \quad D_{\uparrow} = W_p (U_1 V + U_2), \quad (9)$$

$$\text{High wind } (V > 17.3): \quad D_{\downarrow} = W_p (D_1 V + D_2), \quad D_{\perp} = W_p (S_1 V + S_2), \quad D_{\uparrow} = W_p (U_1 V + U_2), \quad (10)$$

$$\begin{aligned} \text{Moderate } (10 \leq V \leq 17.3): \quad D_{\downarrow} &= W_p (D_1 V^2 + D_2 V + D_3), \\ D_{\perp} &= W_p (S_1 V^2 + S_2 V + S_3), \\ D_{\uparrow} &= W_p (U_1 V^2 + U_2 V + U_3). \end{aligned}$$

Ellipse parameters:

$$a = \frac{D_{\downarrow} + D_{\uparrow}}{2}, \quad \varepsilon = \min\left(\frac{a}{2}, a - D_{\uparrow}\right), \quad E_{b2} = 1 - \left(\frac{\varepsilon}{a}\right)^2, \quad (11)$$

$$b = \begin{cases} \frac{D_{\perp}}{\sqrt{E_{b2}}}, & E_{b2} > 0, \\ 0, & E_{b2} \leq 0. \end{cases} \quad (12)$$

State vector:

$$\mathbf{E} = [a, b, \varepsilon, D_{\downarrow}]^{\top}.$$

Ellipse Reach and Coverage

Maximum reach (scalar):

$$R_{\max} = 0.3 D_{\downarrow} \frac{a - \varepsilon}{b^2}. \quad (13)$$

Directional reach along θ_f :

$$R_{\text{ell}}(\theta_f) = \frac{R_{\max} b^2}{a - \varepsilon \cos \theta_f}. \quad (14)$$

DFC coverage fraction (cell-centered, clipped to $[0, 1]$):

$$C_{\text{DFC}} = \max \left\{ \min \left(\frac{R_{\text{ell}}(\theta_f) + \frac{1}{2} \Delta - R}{\Delta}, 1 \right), 0 \right\}. \quad (15)$$

Radiation annulus outside DFC, bounded by cutoff:

$$R_{\text{rad limit}}(\theta_f) = R_{\text{ell}}(\theta_f) + R_{\text{rad}}, \quad (16)$$

$$\Delta_{\text{rad}} = \max \left\{ \min \left(\frac{R_{\text{rad limit}}(\theta_f) + \frac{1}{2} \Delta - R}{\Delta}, 0 \right), 1 \right\}, \quad (17)$$

$$F_{\text{rad}} = \Delta_{\text{rad}} (1 - C_{\text{DFC}}). \quad (18)$$

Per-Cell HRR Normalization

To conserve total HRRPUA over the ellipse footprint, use the adjuster

$$C_{\text{HRR}} = \frac{\Delta^2}{\pi (b/a) a b} = \frac{\Delta^2}{\pi b^2}. \quad (19)$$

Transient HRRPUA

For burning time τ and parameters $(t_{\text{early}}, t_{\text{dev}}, t_{\text{decay}}, \text{HRRPUA}_{\text{peak}})$:

$$\text{HRRPUA}(\tau) = \begin{cases} \frac{\text{HRRPUA}_{\text{peak}}}{t_{\text{early}}} \tau, & 0 \leq \tau \leq t_{\text{early}}, \\ \text{HRRPUA}_{\text{peak}}, & t_{\text{early}} < \tau \leq t_{\text{dev}}, \\ \frac{\text{HRRPUA}_{\text{peak}}}{t_{\text{dev}} - t_{\text{decay}}} (\tau - t_{\text{decay}}), & t_{\text{decay}} < \tau, \\ 0, & \text{otherwise}, \end{cases} \quad \text{HRRPUA}(\tau) \leftarrow \max\{0, \text{HRRPUA}(\tau)\}. \quad (20)$$

Per-Cell Heat Fluxes

Let $C_{\text{burn}} = 1 - \text{NONBURNABLE_FRAC}$. Then

$$q_{\text{DFC}}'' = C_{\text{burn}} C_{\text{DFC}} \text{HRRPUA}(\tau) C_{\text{HRR}}, \quad (21)$$

$$q_{\text{rad}}'' = \frac{0.3 C_{\text{burn}} \alpha F_{\text{rad}} C_{\text{HRR}} \text{HRRPUA}(\tau) \Delta^2}{4\pi R_{\text{eff}}^2}, \quad R_{\text{eff}} = \begin{cases} \Delta (1 - C_{\text{DFC}}), & 0 < C_{\text{DFC}} < 1, \\ R - R_{\text{ell}}(\theta_f), & \text{otherwise.} \end{cases} \quad (22)$$

Algorithm (Per Time Step)

1. Set $\tau = t - t_0$ and compute $\text{HRRPUA}(\tau)$.
2. From $(\text{WS}_{20ft}, A, D, W_p)$ compute $\mathbf{E} = [a, b, \varepsilon, D_{\downarrow}]$.
3. For each cell (i, j) with center $(i \Delta, j \Delta)$:
 - 3.1. Compute R, θ, θ_f and $R_{\text{ell}}(\theta_f)$.
 - 3.2. Compute $C_{\text{DFC}}, F_{\text{rad}}, R_{\text{eff}}$.
 - 3.3. Evaluate q''_{DFC} and q''_{rad} .

2.1.2 Assumptions

- Urban array represented on a uniform analysis grid of square cells of size Δ (m).
- Structures have a non-burnable fraction `NONBURNABLE_FRAC`; the remainder contributes to heat release/flux.
- HRRPUA follows a piecewise transient curve with early growth, plateau, and decay; negative segments are clipped to zero.
- Wind-aligned ellipse is derived from 20-ft wind inputs $(\text{WD}_{20ft}, \text{WS}_{20ft})$ and geometric parameters (A, D) with a proportionality W_p .
- Radiation is applied outside the ellipse up to a cutoff radius R_{rad} ; convective/design-fire contact (DFC) acts within the ellipse footprint.
- Units: distances in meters; heat flux in kW/m^2 .

2.1.3 Simulation Setup

Parameter Table (defaults)

Properties	Symbols	Values
Absorptivity	α	0.89
Radiation cutoff (m)	R_{rad}	100
Analysis cell size (m)	Δ	20
Wind direction (deg, from)	WD_{20ft}	0
Wind speed (mph)	WS_{20ft}	40
Footprint dim. (m)	A	10
Separation (m)	D	10
Wind proportionality	W_p	1
Non-burnable fraction	<code>NONBURNABLE_FRAC</code>	0
Early, dev., decay times (s)	$(t_{\text{early}}, t_{\text{dev}}, t_{\text{decay}})$	(300, 3900, 4200)
Peak HRRPUA (kW/m^2)	$\text{HRRPUA}_{\text{peak}}$	400

Grid and Indices

Cells are indexed by $i, j \in \{-5, \dots, 5\}$ with centers $(x, y) = (i \Delta, j \Delta)$ relative to the burning structure at $(0, 0)$.

2.1.4 Input Data

Describe input rasters, constants, initial conditions.

2.1.5 Numerical Controls

Mesh resolution, Time step(CFL), level-set solver options, etc.

2.2 Expected Results and Reasoning

- **Geometric consistency:** As V increases, D_{\downarrow} grows faster than D_{\perp} and D_{\uparrow} , increasing a and eccentricity (smaller b/a); $R_{\text{ell}}(\theta_f)$ elongates downwind.
- **Coverage partition:** Cells inside the ellipse ($C_{\text{DFC}} > 0$) receive q''_{DFC} proportional to HRRPUA and C_{HRR} ; outer annulus receives q''_{rad} diminishing with R_{eff}^{-2} .
- **Conservation:** With C_{HRR} , summing q''_{DFC} over the footprint tracks the design HRRPUA(τ) (up to discretization error).
- **Limits:** For $V \rightarrow 0$, the ellipse tends toward isotropic ($D_{\downarrow} \approx D_{\perp} \approx D_{\uparrow}$); for very large V , footprint becomes highly elongated downwind; q''_{rad} shifts outward.

2.3 Acceptance Criteria

- **Shape metrics:** Measured $\{a, b, \varepsilon\}$ vs. regression predictions within 2%.
- **Energy consistency:** $|\sum_{\text{cells}} q''_{\text{DFC}} - \text{HRRPUA}(\tau)| / \text{HRRPUA}(\tau) \leq 5\%$ (plateau phase).
- **Partition sanity:** $q''_{\text{rad}} \rightarrow 0$ as $R_{\text{eff}} \rightarrow \infty$ and vanishes inside pure DFC cells when $F_{\text{rad}} = 0$.
- **Directional response:** Downwind flux peak > side > upwind for V in moderate/high ranges.

2.4 Results

This section includes diagnostic figures:

- Footprint maps of C_{DFC} , F_{rad} , and q'' at selected times.
- Downwind/sidewind/upwind radial profiles of q''_{DFC} and q''_{rad} .
- Time histories of total $\sum q''_{\text{DFC}}$ and $\sum q''_{\text{rad}}$ vs. HRRPUA(τ).

2.5 Discussion

- Clarify parameter sensitivities (e.g., A, D, W_p) and wind-direction convention: $\theta_{\text{wind}} = \frac{\pi}{180}(270 - \text{WD}_{20ft})$ points the major axis toward $+x$ when $\text{WD}_{20ft} = 0^\circ$.
- Document any discretization effects at coarse Δ and how C_{HRR} compensates for footprint changes.
- Note corner cases: $E_{b2} \leq 0$ (degenerate b), transition regions in the piecewise wind regression, and clipping of coverage fractions.

Reproducibility

- MATLAB functions: `ellipse_ucb`, `hrr_transient`, `heat_flux_calc`.
- Command(s): `./run_case.sh`; environment: `<modules/conda env>`.
- Logs under `cases/wue_transient_heatflux/logs/`; figures in `cases/wue_transient_heatflux/figures/`.