

Matrices

R Data Objects

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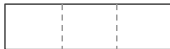
About

- ▶ Matrices

*single data type
(atomic)*

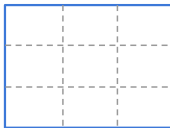
Vector

1D



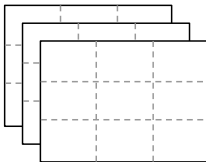
Matrix

2D



Array

nD



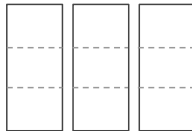
dimensions

*multiple data types
(non-atomic)*

List



Data Frame



From Vectors to Arrays

We can transform a vector in an **n-dimensional array** by giving it a dimensions attribute **dim**

```
# positive: from 1 to 8
```

```
x <- 1:8
```

```
# adding 'dim' attribute
```

```
dim(x) <- c(2, 4)
```

```
x
```

```
##      [,1] [,2] [,3] [,4]
## [1,]    1    3    5    7
## [2,]    2    4    6    8
```

From Vectors to Arrays

- ▶ a vector can be given a `dim` attribute
- ▶ a `dim` attribute is a numeric vector of length `n`
- ▶ R will reorganize the elements of the vector into `n` dimensions
- ▶ each dimension will have as many rows (or columns, etc.) as the `n`-th value of the `dim` vector

From Vectors to Arrays

```
# dim attribute with 3 dimensions
```

```
dim(x) <- c(2, 2, 2)
```

```
x
```

```
## , , 1
```

```
##
```

```
##      [,1] [,2]
```

```
## [1,]    1    3
```

```
## [2,]    2    4
```

```
##
```

```
## , , 2
```

```
##
```

```
##      [,1] [,2]
```

```
## [1,]    5    7
```

```
## [2,]    6    8
```

From Vector to Matrix

A dim attribute of length 2 will convert a vector into a matrix

```
# vector to matrix  
A <- 1:8  
class(A)
```

```
## [1] "integer"
```

```
dim(A) <- c(2, 4)  
class(A)
```

```
## [1] "matrix" "array"
```

When using `dim()`, R always fills up each matrix by columns.

From Vector to Matrix

To have more control about how a matrix is filled, (by rows or columns), we use the `matrix()` function:

```
# vector to matrix
```

```
A <- 1:8
```

```
matrix(A, nrow = 2, ncol = 4)
```

```
##      [,1] [,2] [,3] [,4]  
## [1,]    1    3    5    7  
## [2,]    2    4    6    8
```


Matrices

- ▶ An R matrix provides a rectangular data object; i.e. to handle data in a two-dimensional array
- ▶ To create a matrix, give a vector to `matrix()` and specify number of rows and columns
- ▶ You can also assign row and column names to a matrix

Matrices

- ▶ R internally stores matrices as vectors.
- ▶ Which means that matrices are also atomic.
- ▶ Matrices in R are stored **column-major** (i.e. by columns).
- ▶ This is like Fortran, Matlab, and Julia, but not like C or Python (e.g. numpy)

Creating a Matrix

How do you create the following matrix?

```
##      [,1]      [,2]
## [1,] "Harry"  "Potter"
## [2,] "Ron"     "Weasley"
## [3,] "Hermione" "Granger"
```

Creating a Matrix

Here's one way to create the matrix of the previous slide

```
# vector of names  
hp <- c("Harry", "Ron", "Hermione",  
        "Potter", "Weasley", "Granger")
```

```
# matrix filled up by rows  
matrix(hp, nrow = 3)
```

```
##      [,1]      [,2]  
## [1,] "Harry"   "Potter"  
## [2,] "Ron"     "Weasley"  
## [3,] "Hermione" "Granger"
```

Creating a Matrix

Here's another way to create the preceding matrix

```
# vector of names  
hp <- c("Harry", "Potter", "Ron", "Weasley",  
        "Hermione", "Granger")
```

```
# matrix filled up by rows  
matrix(hp, nrow = 3, byrow = TRUE)
```

```
##      [,1]      [,2]  
## [1,] "Harry"  "Potter"  
## [2,] "Ron"     "Weasley"  
## [3,] "Hermione" "Granger"
```

Row and Column Names

R provides functions that let you set / get the names for either the rows or the columns (or both) of a matrix:

- ▶ `rownames()`
- ▶ `colnames()`
- ▶ `dimnames()`

Row and Column Names

```
set.seed(123)
A <- matrix(runif(12), nrow = 3, ncol = 4)
rownames(A) <- paste0("row", 1:nrow(A))
A
```

```
##           [,1]      [,2]      [,3]      [,4]
## row1 0.2875775 0.8830174 0.5281055 0.4566147
## row2 0.7883051 0.9404673 0.8924190 0.9568333
## row3 0.4089769 0.0455565 0.5514350 0.4533342
```

```
rownames(A)
```

```
## [1] "row1" "row2" "row3"
```

Row and Column Names

```
set.seed(123)
B <- matrix(runif(12), nrow = 3, ncol = 4)
colnames(B) <- paste0("col", 1:ncol(B))
B
```

```
##           col1      col2      col3      col4
## [1,] 0.2875775 0.8830174 0.5281055 0.4566147
## [2,] 0.7883051 0.9404673 0.8924190 0.9568333
## [3,] 0.4089769 0.0455565 0.5514350 0.4533342
```

```
colnames(B)
```

```
## [1] "col1" "col2" "col3" "col4"
```


Row and Column Names

```
set.seed(123)
C <- matrix(runif(12), nrow = 3, ncol = 4)
rownames(C) <- paste0("row", 1:nrow(C))
colnames(C) <- paste0("col", 1:ncol(C))
C
```

```
##           col1      col2      col3      col4
## row1 0.2875775 0.8830174 0.5281055 0.4566147
## row2 0.7883051 0.9404673 0.8924190 0.9568333
## row3 0.4089769 0.0455565 0.5514350 0.4533342
```

```
dimnames(C)
```

```
## [[1]]
## [1] "row1" "row2" "row3"
##
## [[2]]
## [1] "col1" "col2" "col3" "col4"
```

Row and Column Names

```
set.seed(123)
D <- matrix(runif(12), nrow = 3, ncol = 4)
dimnames(D) <- list(
  paste0("row", 1:nrow(D)),
  paste0("col", 1:ncol(D))
)
D
```

```
##           col1      col2      col3      col4
## row1 0.2875775 0.8830174 0.5281055 0.4566147
## row2 0.7883051 0.9404673 0.8924190 0.9568333
## row3 0.4089769 0.0455565 0.5514350 0.4533342
```

Recycling

Recycling rules also apply to matrices

```
x <- letters[1:4]  
X <- matrix(x, nrow = 4, ncol = 3)  
X
```

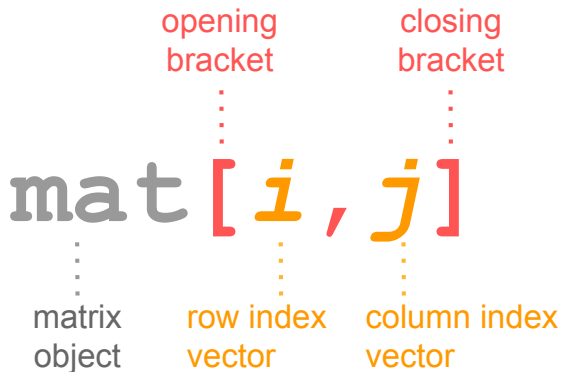
```
##      [,1] [,2] [,3]  
## [1,] "a"  "a"  "a"  
## [2,] "b"  "b"  "b"  
## [3,] "c"  "c"  "c"  
## [4,] "d"  "d"  "d"
```

Recycling

```
# "empty" matrices  
mat_chr <- matrix("", nrow = 4, ncol = 3)  
  
mat_num <- matrix(0, nrow = 4, ncol = 3)  
  
mat_lgl <- matrix(NA, nrow = 4, ncol = 3)
```

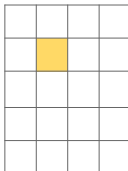
Matrix Manipulation

Subsetting: Bracket Notation

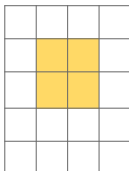


Subsetting Cells

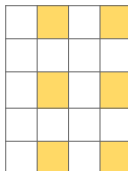
`mat[2,2]`



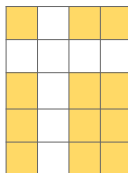
`mat[2:3,2:3]`



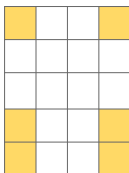
`mat[c(1,3,5),
c(2,4)]`



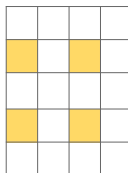
`mat[-2,-2]`



`mat[-(2:3),
-(2:3)]`



`mat[-c(1,3,5),
-c(2,4)]`



Subsetting Rows

`mat[2,]`

`mat[2:3,]`

`mat[c(1,3,5),]`

`mat[-2,]`

`mat[-(2:3),]`

`mat[-c(1,3,5),]`

Subsetting Columns

`mat[,2]`

`mat[,2:3]`

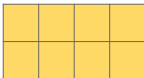
`mat[,c(2,4)]`

`mat[,-2]`

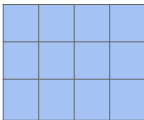
`mat[,-(2:3)]`

`mat[,-c(2,4)]`

mat1

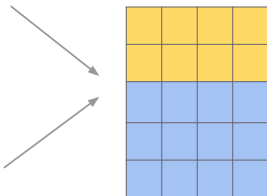


mat2

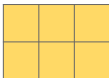


row binding

`mat3 <- rbind(mat1, mat2)`



mat1

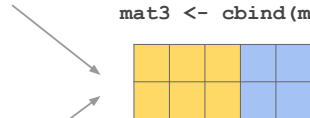


mat2



column binding

`mat3 <- cbind(mat1, mat2)`



apply() function

```
X = matrix(rep(1:3, each = 5), nrow = 5, 3)
```

```
X
```

```
##      [,1] [,2] [,3]
## [1,]    1    2    3
## [2,]    1    2    3
## [3,]    1    2    3
## [4,]    1    2    3
## [5,]    1    2    3
```

```
X
```

```
##      [,1] [,2] [,3]
## [1,]    1    2    3
## [2,]    1    2    3
## [3,]    1    2    3
## [4,]    1    2    3
## [5,]    1    2    3
```

```
# sum of elements in each row (INDEX = 1)
apply(X, MARGIN = 1, FUN = sum)
```

```
## [1] 6 6 6 6 6
```

```
X
```

```
##      [,1] [,2] [,3]
## [1,]    1    2    3
## [2,]    1    2    3
## [3,]    1    2    3
## [4,]    1    2    3
## [5,]    1    2    3
```

```
# sum of elements in each column (INDEX = 2)
apply(X, MARGIN = 2, FUN = sum)
```

```
## [1]  5 10 15
```

```
Y = matrix(1:15, nrow = 5, 3)
Y
```

```
##      [,1] [,2] [,3]
## [1,]    1    6   11
## [2,]    2    7   12
## [3,]    3    8   13
## [4,]    4    9   14
## [5,]    5   10   15
```

```
# mean of elements in each row (INDEX = 1)
apply(Y, MARGIN = 1, FUN = mean)
```

```
## [1]  6  7  8  9 10
```

```
Y
```

```
##      [,1] [,2] [,3]  
## [1,]    1    6   11  
## [2,]    2    7   12  
## [3,]    3    8   13  
## [4,]    4    9   14  
## [5,]    5   10   15
```

```
# mean of elements in each column (INDEX = 2)
```

```
apply(Y, MARGIN = 2, FUN = mean)
```

```
## [1]  3  8 13
```



```
set.seed(123)
Z = matrix(runif(15), nrow = 5, 3)
Z
```

```
##           [,1]      [,2]      [,3]
## [1,] 0.2875775 0.0455565 0.9568333
## [2,] 0.7883051 0.5281055 0.4533342
## [3,] 0.4089769 0.8924190 0.6775706
## [4,] 0.8830174 0.5514350 0.5726334
## [5,] 0.9404673 0.4566147 0.1029247
```

```
# median of elements in each row (INDEX = 1)
apply(Z, MARGIN = 1, FUN = median)
```

```
## [1] 0.2875775 0.5281055 0.6775706 0.5726334 0.4566147
```

Z

```
##           [,1]      [,2]      [,3]
## [1,] 0.2875775 0.0455565 0.9568333
## [2,] 0.7883051 0.5281055 0.4533342
## [3,] 0.4089769 0.8924190 0.6775706
## [4,] 0.8830174 0.5514350 0.5726334
## [5,] 0.9404673 0.4566147 0.1029247
```

median of elements in each column (INDEX = 2)

```
apply(Z, MARGIN = 2, FUN = median)
```

```
## [1] 0.7883051 0.5281055 0.5726334
```

```
# descriptive stats of elements in each row (INDEX = 1)  
apply(Z, MARGIN = 1, FUN = summary)
```

##	[,1]	[,2]	[,3]	[,4]	[,5]
## Min.	0.0455565	0.4533342	0.4089769	0.5514350	0.1029247
## 1st Qu.	0.1665670	0.4907198	0.5432738	0.5620342	0.2797697
## Median	0.2875775	0.5281055	0.6775706	0.5726334	0.4566147
## Mean	0.4299891	0.5899149	0.6596555	0.6690286	0.5000022
## 3rd Qu.	0.6222054	0.6582053	0.7849948	0.7278254	0.6985410
## Max.	0.9568333	0.7883051	0.8924190	0.8830174	0.9404673

```
# descriptive stats of elements in each column (INDEX = 2)  
apply(Z, MARGIN = 2, FUN = summary)
```

```
##           [,1]      [,2]      [,3]  
## Min.      0.2875775 0.0455565 0.1029247  
## 1st Qu.   0.4089769 0.4566147 0.4533342  
## Median   0.7883051 0.5281055 0.5726334  
## Mean     0.6616689 0.4948262 0.5526592  
## 3rd Qu.  0.8830174 0.5514350 0.6775706  
## Max.     0.9404673 0.8924190 0.9568333
```

Matrix Algebra

Operators

Operator	Description	Example
+	addition	$A + B$
-	subtraction	$A - B$
*	elementwise product	$A * B$
%*%	matrix product	$A \%*\% B$
t()	transpose	$t(A)$
det()	determinant	$\det(A)$
diag()	extract diagonal	$\text{diag}(A)$
solve()	inverse	$\text{solve}(A)$

Note: make sure the dimensions of matrices are conformable when using an operator or some calculation on them.

Other Functions

Function	Description
<code>upper.tri()</code>	upper triangular part of a matrix
<code>lower.tri()</code>	lower triangular part of a matrix
<code>eigen()</code>	eigenvalue decomp.
<code>svd()</code>	singular value decomp.
<code>lu()</code>	Triangular decomposition
<code>qr()</code>	QR decomposition
<code>chol()</code>	Cholesky decomposition