

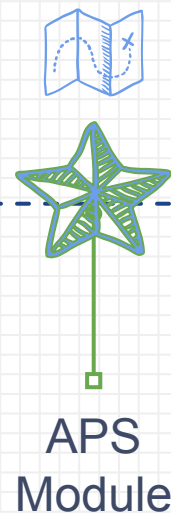
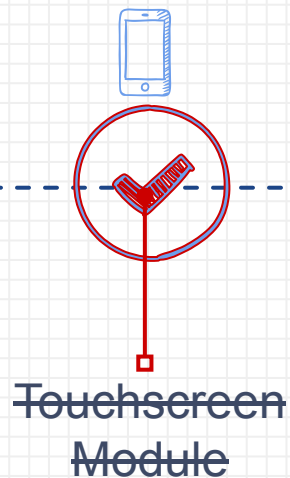
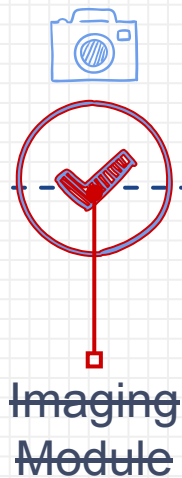
# EECS16A

## Acoustic Positioning System 1

TA, ASE, ASE, ASE



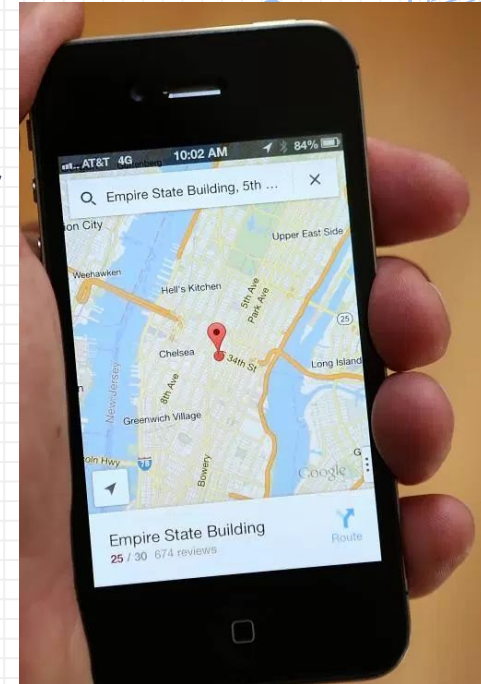
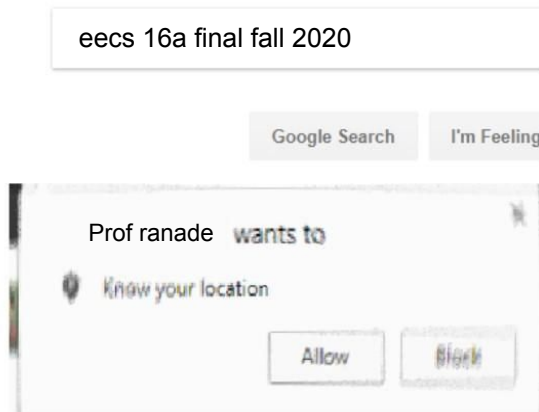
# Where Are We Now?



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- A photograph of a breadboard with a large red 'X' drawn over it, indicating it is a bad example of wiring. The breadboard is densely packed with a chaotic mess of multi-colored jumper wires. Some components, like integrated circuits and resistors, are visible but obscured by the wires. The breadboard is labeled 'Bread Board Model' and '40 Pin'. The background is a dark surface with some blueprints or diagrams visible on the right side.

# Today's lab: Acoustic Positioning System

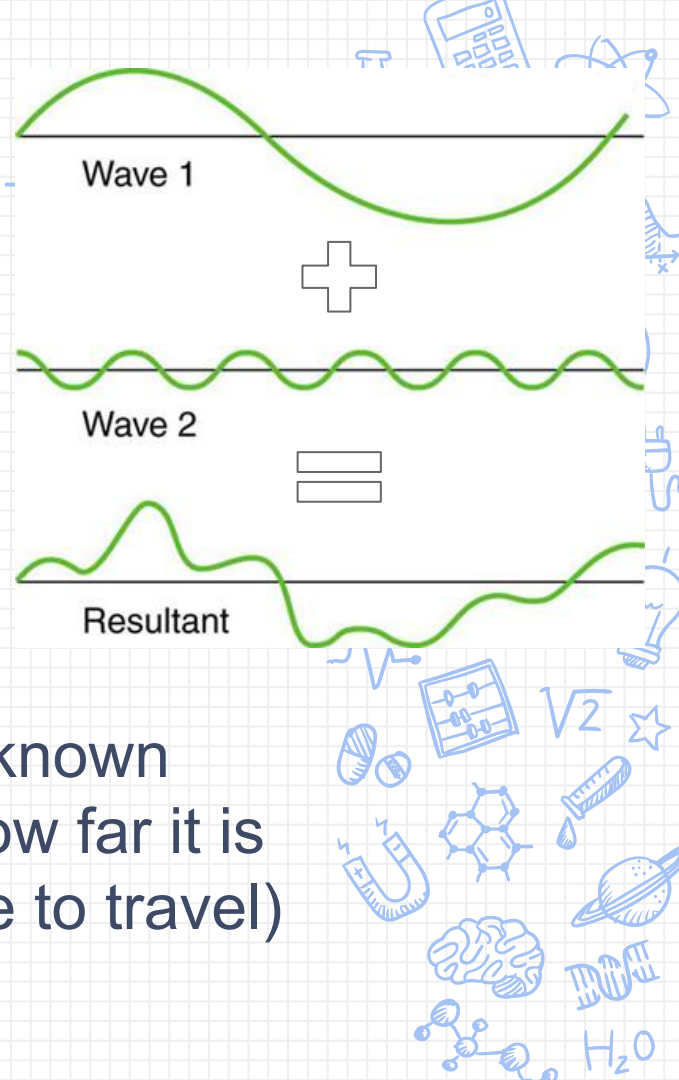
- Global Positioning System (GPS)
  - Uses radio waves instead of sound waves
- Understand mathematical tools used for shifting and detecting signals
  - Think about cross correlation!



- Known: Location of each satellite and what beacon signal each satellite is playing
- Unknown: Location of receiver ← what we want to figure out!

# Set-up

- Satellite:
  - Known, periodic waveforms
  - Know satellite location
- Receiver:
  - Will record the waveform
    - Sum of all shifted beacons
  - Waveform will be shifted from known satellite waveform based on how far it is from satellite (sound takes time to travel)

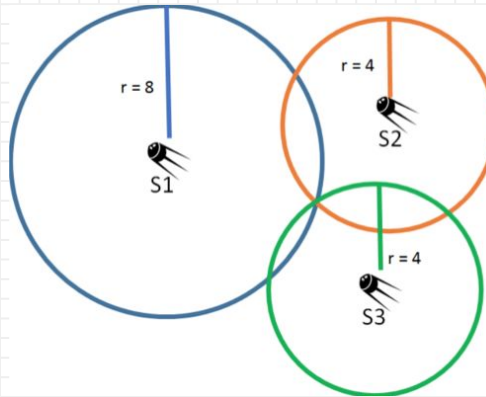


# Let's go backwards

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Assume we know the **distance** between the receiver and every satellite

- Use **lateration** and the satellites' locations to locate the receiver!
- How many satellites do we need in a 2D world?











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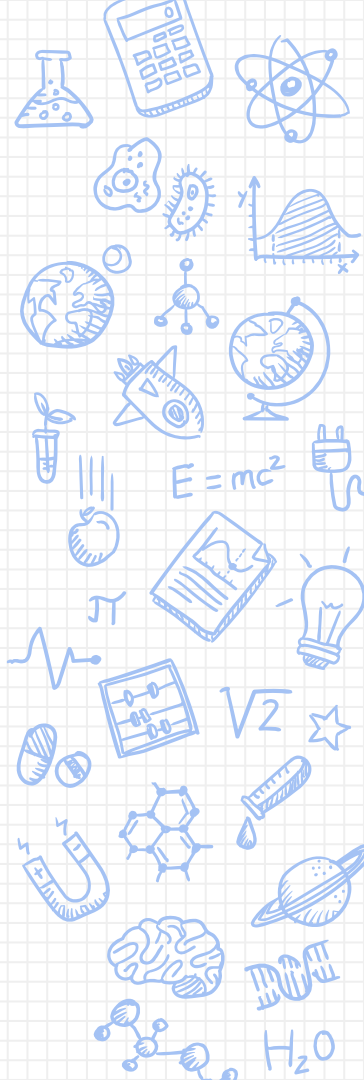
## Poll Time!

Let the sampling frequency be 1000 Hz and the speed of sound be 343 m/s. If I detect a signal with a delay of 100 samples, what is the distance between the speaker and the mic?

- 3430 m
- **34.3 m** →
- 343 m
- 3.43 m

$$\text{time delay} = \frac{\text{samples}}{\text{sampling frequency}} = \frac{100 \text{ samples}}{1000 \text{ Hz}} = 0.1 \text{ s}$$

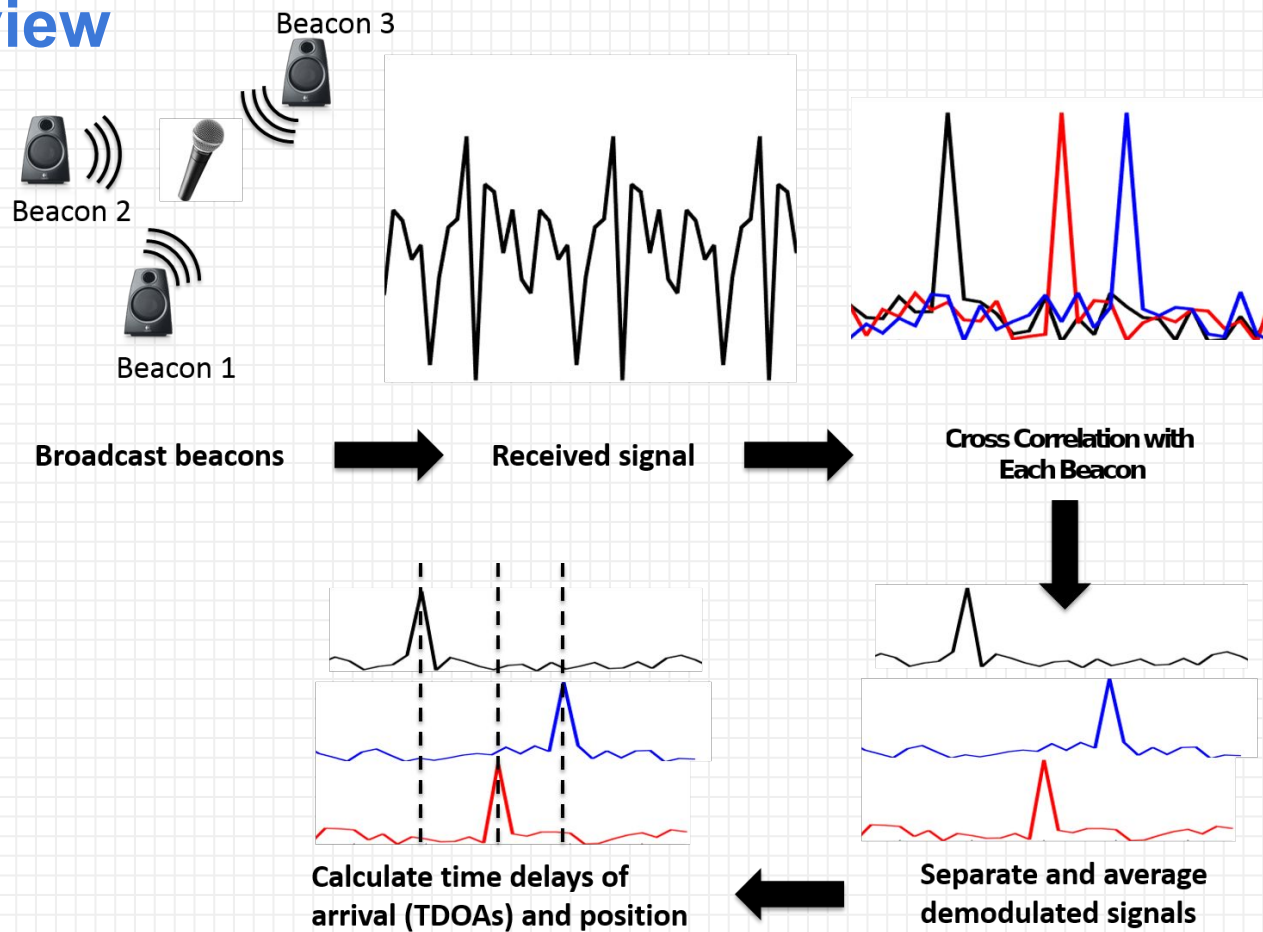
$$d = v \cdot t = 343 \text{ m/s} \cdot 0.1 \text{ s} = \boxed{34.3 \text{ m}}$$



- $$E = mc^2$$



# Overview





$$\langle \vec{x}, \vec{y} \rangle = \|\vec{x}\| \|\vec{y}\| \cos \theta$$

### An alternate form of the dot product

- Given this expression, with  $\|x\| = \|y\|$ , when is this expression maximized?
  - $\theta = 0$
  - vectors point in the **SAME DIRECTION**, so they are the **SAME SIGNAL**

The **bigger** the dot product, the more “**similar**” the two vectors are



[illegible]

## In Python:

```
cross_correlation(r, BA)[k]
```

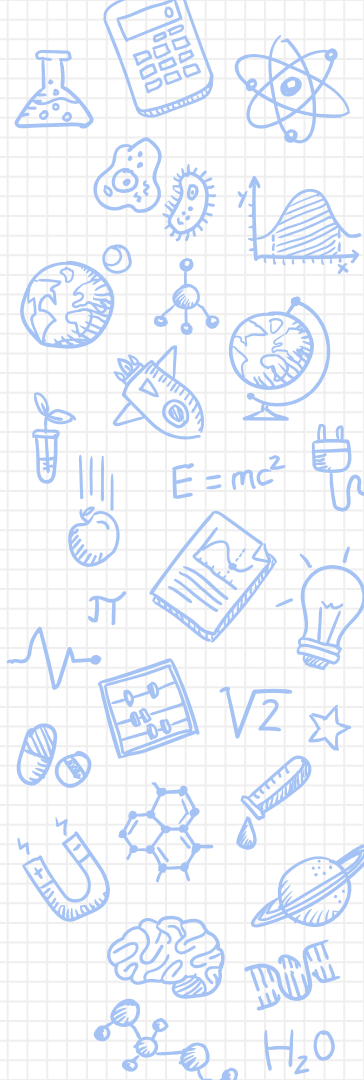
- Mathematical tool for finding similarities between signals
- **Idea:** Computes dot product between  $r$  and signal  $B_A$  shifted by  $k$  samples
- From the previous slide, the peak of the cross-correlation vector tells us which shift amount makes  $B_A$  “most similar” to  $r$

## Poll Time!

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Given the inner product expression, with  $\|x\| = \|y\|$ , when is this expression maximized?

- $\theta = 0$
- $\theta = 90$
- $\theta = 180$
- $\theta = -90$

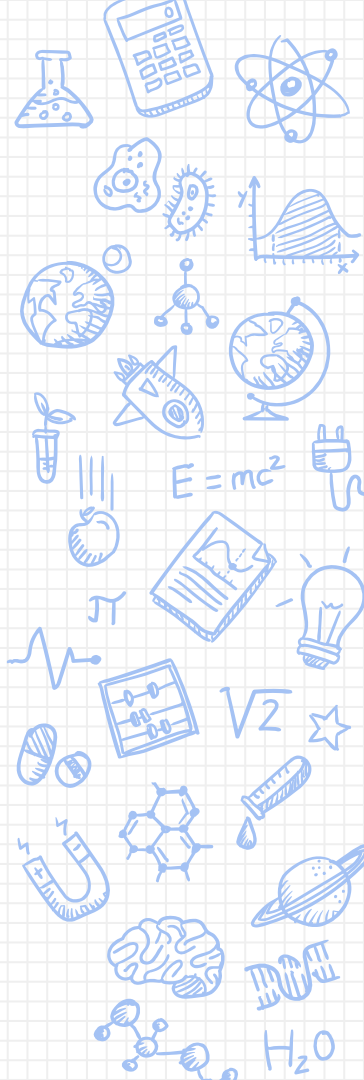


## Poll Time!

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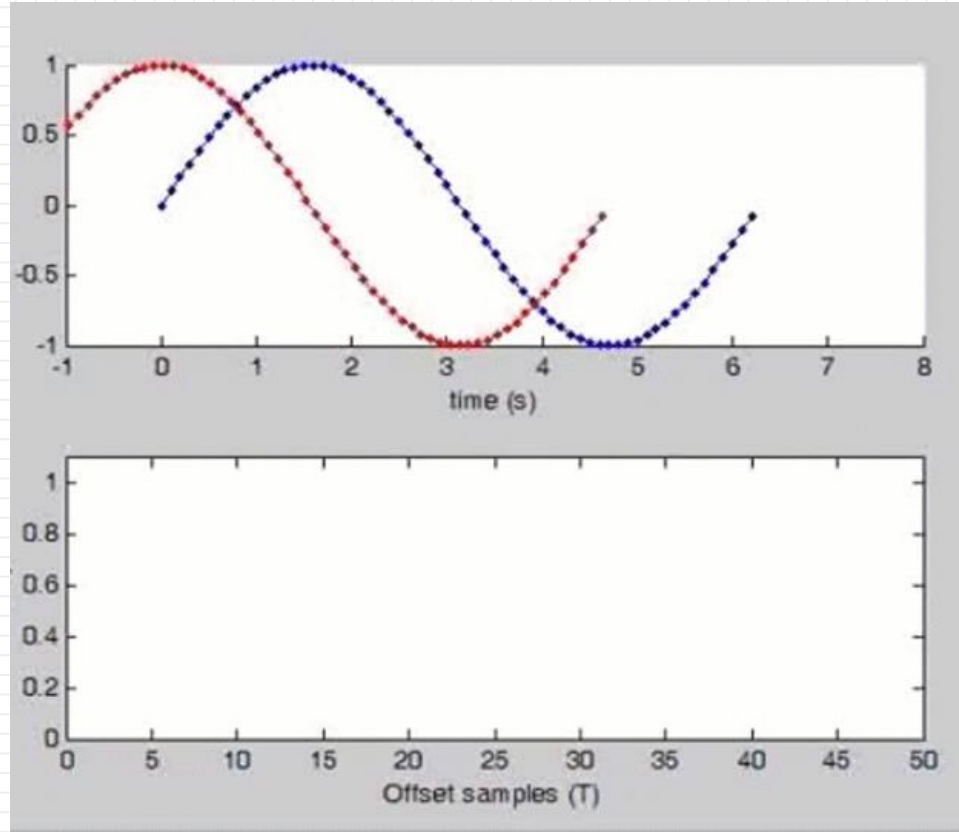
Given the inner product expression, with  $\|x\| = \|y\|$ , when is this expression maximized?

- **theta = 0**
- theta = 90
- theta = 180
- theta = -90



- At ~ how many offset samples are the signals most similar?

blue =  $r$   
red =  $B_A$



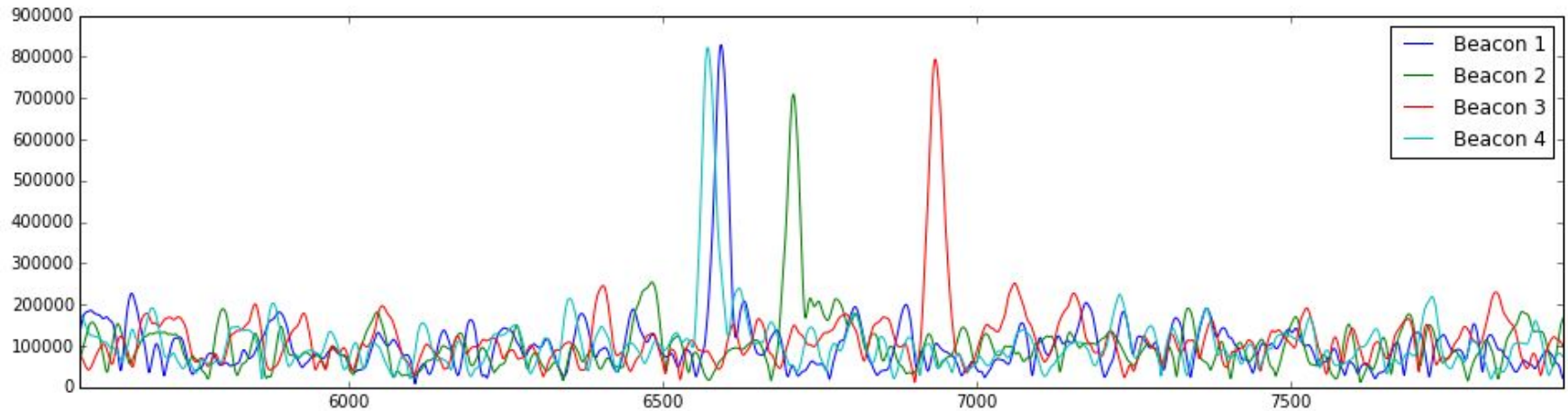
Note: zero pad signals to match length



# How to use?

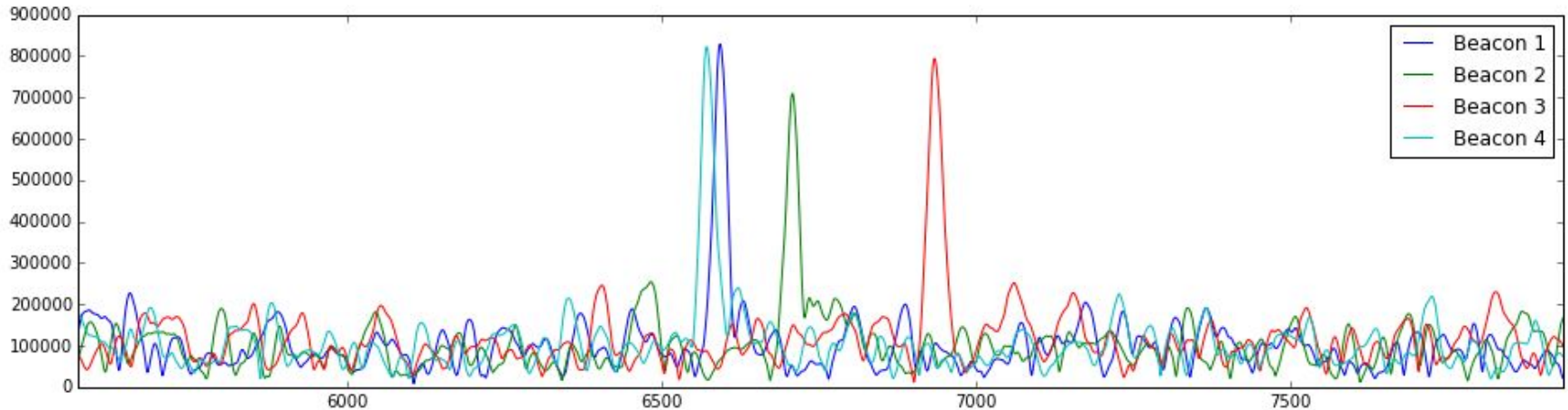
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- Cross correlating should tell us where each beacon arrived in our recorded signal
- Let's cross-correlate each of the known beacon signals with what we recorded and plot the result



# Absolute or relative sample delays?

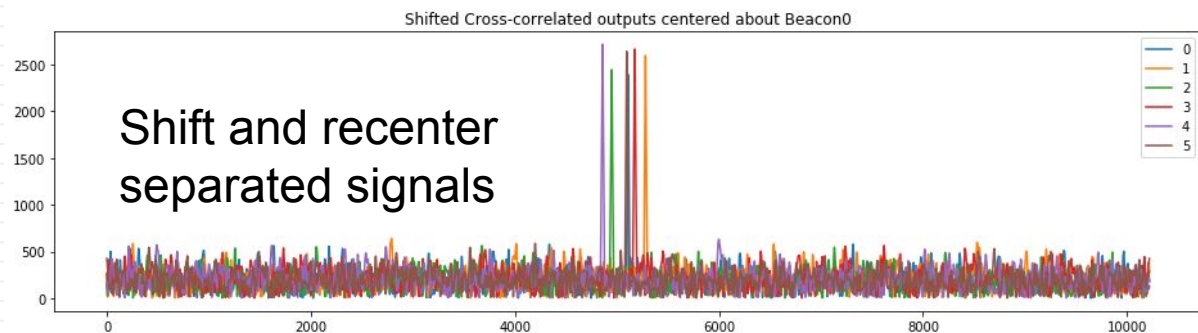
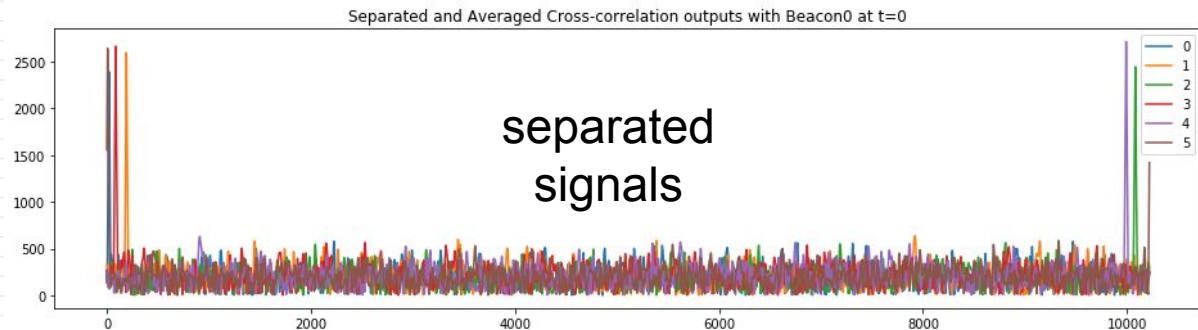
- We can see peaks where each beacon arrived!
- But notice it only gives us **relative** sample delays
  - Still can't tell how many absolute samples each beacon is delayed, we don't know when it was supposed to arrive
- Arbitrarily pick a beacon to be the reference point



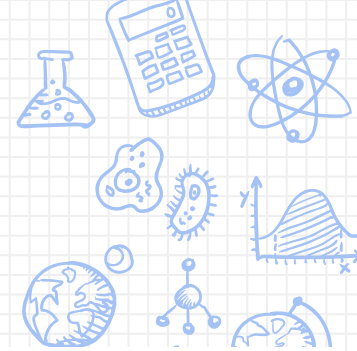


# “Sacrificing” a beacon

- Let's shift our axis so beacon 0 has a delay of 0
- We could pick any beacon to be the center
  - 0 is arbitrary



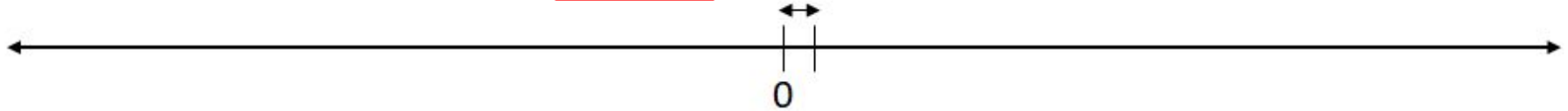




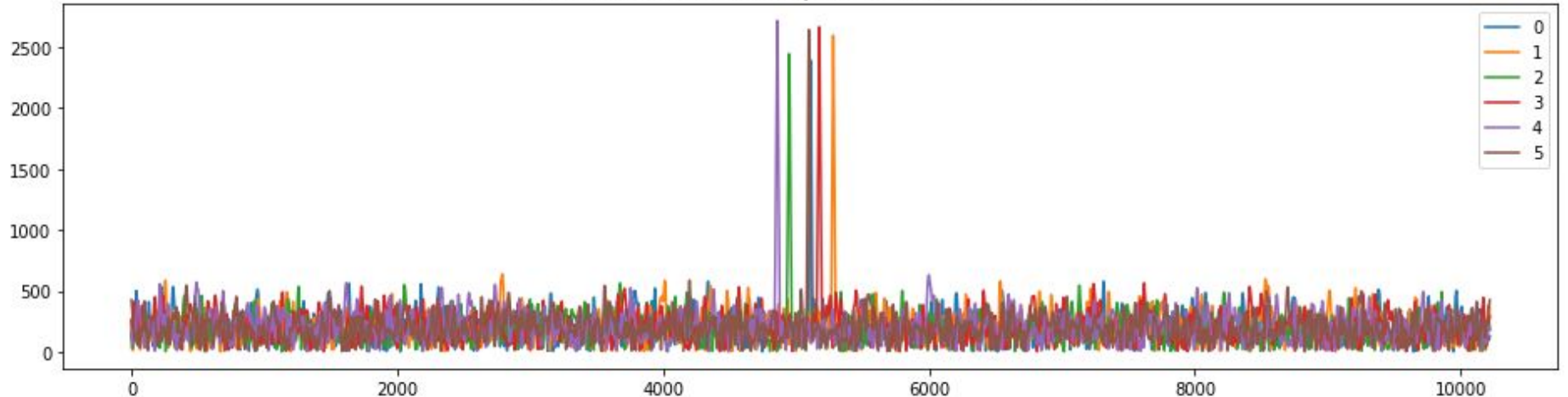
## “Sacrificing” a beacon

Now beacon 0 is at our new “origin” and all computations are relative to the new “0”

Relative offset of beacon 1



Shifted Cross-correlated outputs centered about Beacon0



# Relative Measurements

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- Now, we are able to compute **relative** sample delays, then **relative** time delays
- How do we get from **relative** time delays to **absolute** distances?
  - With the current set-up, we can't :(



- What if we knew the absolute sample delay of beacon 0?
  - Now we can adjust all our relative measurements to absolute ones!
  - Assume  $\text{delay}_0$  is given, then
$$\text{delay}_i = \text{delay}_i \text{ relative to } 0 + \text{delay}_0$$
- Then we can use absolute time-delays to get distances then location!

## Notes + next lab:

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- If we know the absolute sample delay of beacon 0, we can locate the receiver
  - Note that this is the same as telling you exactly how far the receiver is from satellite 0
- This week, this value will be given to you
- Find out how to get around this assumption in APS 2!

