6. (20 points) Palindromes

Definition. A palindrome is a sequence that has the same elements in normal and reverse order.

(a) (3 pt) Implement pal, which takes a positive integer n and returns a positive integer with the digits of n followed by the digits of n in reverse order.
 Important: You may not write str, repr, list, tuple, [, or].

(b) (4 pt) Implement contains, which takes non-negative integers a and b. It returns whether all of the digits of a also appear in order among the digits of b.

Important: You may not write str, repr, list, tuple, [, or].

```
def contains(a, b):
    """Return whether the digits of a are contained in the digits of b.

>>> contains(357, 12345678)
    True
    >>> contains(753, 12345678)
    False
    >>> contains(357, 37)
    False
    """
    if a == b:
```

if _____:

return False

if _____:

return contains(______)

else:

return contains(______, , ______)

Name:	
Nama.	h

4. (10 points) Editor

Definitions. An *edit* is a pure function that takes a non-negative integer and returns a non-negative integer. An *editor* for a non-negative integer **n** is a function that takes an *edit*, applies it to **n**, displays the result, and then returns an editor for the result.

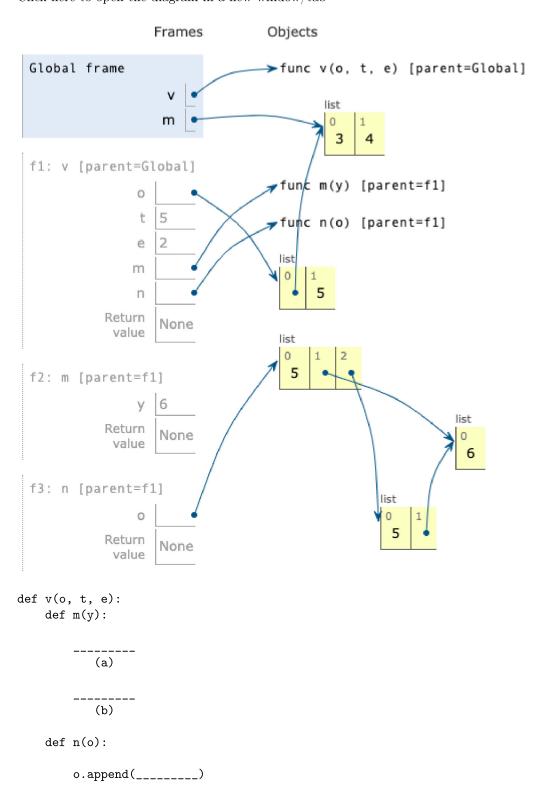
- (a) (3 pt) Implement make_editor, which takes a non-negative integer n and a one-argument function pr. It returns an *editor* for n that uses pr to display the result of each *edit*.
- (b) (5 pt) Implement insert, which takes a single digit d (from 0 to 9) and a non-negative position k. It returns an *edit* that inserts d into its argument n at position k, where k counts the number of digits from the end of n. Assume that k is not larger than the number of digits in n. Your solution must be recursive.
- (c) (2 pt) Implement delete, which takes a non-negative integer k and returns an *edit* that deletes the last k digits of its argument n. You may use pow or ** in your solution.

```
def make_editor(n, pr):
  """Return an editor for N.
  >>> f = make_editor(2018, lambda n: print('n is now', n))
  >>> f = f(delete(3))
                   # delete the last 3 digits from the end of 2018
  n is now 2
  >>> f = f(insert(4, 0)) # insert digit 4 at the end of 2 (position 0)
  n is now 24
  >>> f = f(insert(3, 1)) # insert digit 3 in the middle of 24 (position 1)
  n is now 234
  >>> f = f(insert(1, 3)) # insert digit 1 at the start of 234 (position 3)
  n is now 1234
  >>> f = make_editor(123, print)(delete(10)) # delete 10 digits from the end of 123
  11 11 11
  def editor(edit):
     result = ______
  return editor
def insert(d, k):
  def edit(n):
     if _____:
        return _____ + 10 * _____
     else:
        return _____ + 10 * insert _____
  return edit
delete = ______
```

1. (8.0 points) Political Environment

Fill in each blank in the code example below so that executing it would generate the following environment diagram.

RESTRICTIONS. You must use all of the blanks. Each blank can only include one statement or expression. Click here to open the diagram in a new window/tab

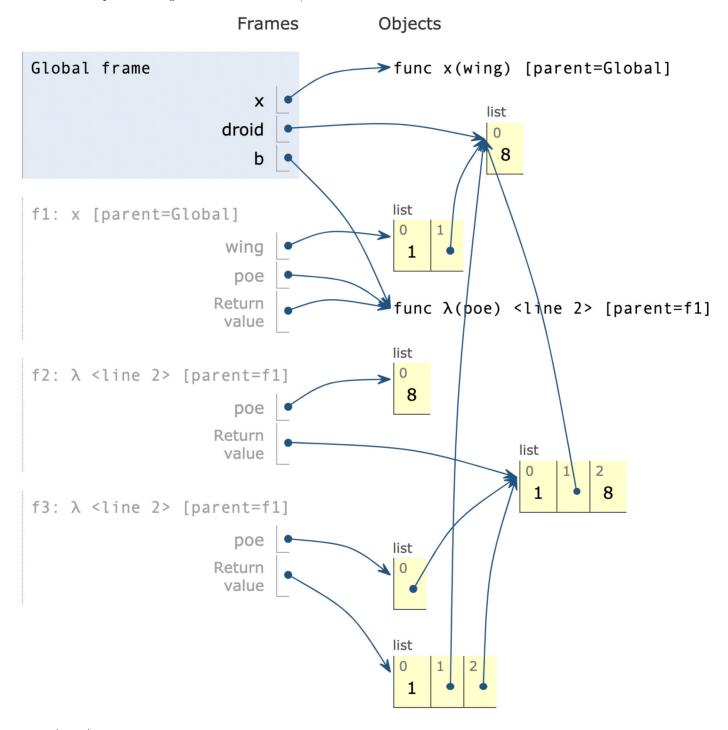


	(c)	
	o.append() (d)	
	m(e) n([t]) e = 2	
m =	[3, 4]	
v(m,	5, 6)	
(a)	(2.0 pt) Fill in blank (a). You may not write any numbers or arithmetic operators (+, -, *, //, **) in your solution.	/,
(b)	(2.0 pt) Fill in blank (b). You may not write any numbers or arithmetic operators (+, -, *, //, **) in your solution.	/,
(c)	(2.0 pt) Fill in blank (c). You may not write any numbers or arithmetic operators (+, -, *, //, **) in your solution.	/,
(d)	(2.0 pt) Which of these could fill in blank (d)? Check all that apply.	
	☐ list(o)	
	☐ [list(o)]	
	☐ list([o])	
	□ o + []	
	<pre>□ [o[0], o[1]]</pre>	
	□ o[:]	

1. (6.0 points) The Droids You're Looking For

Fill in each blank in the code example below so that executing it would generate the following environment diagram on tutor.cs61a.org.

RESTRICTIONS. You must use all of the blanks. Each blank can only include one statement or expression. Click here to open the diagram in a new window/tab



def x(wing):

poe = lambda poe: _____

	# (a)
	wing.append() # (b)
	return # (c)
droi	d = [8]
ъ =	x([1])
 # (d)
(a)	(1.0 pt) Which of these could fill in blank (a)? Check all that apply.
	☐ wing + poe
	☐ wing.extend(poe)
	☐ wing.append(poe)
	☐ list(wing).extend(poe)
	☐ list(wing).append(poe)
(b)	(1.0 pt) Fill in blank (b).
(c)	(1.0 pt) Which of these could fill in blank (c)?
	O poe
	O poe(droid)
	<pre>poe(wing)</pre>
	O poe(b)
(d)	(3.0 pt) Fill in blank (d).

7. (10 points) Summer Camp

(a) (6 pt) Implement sums, which takes two positive integers n and k. It returns a list of lists containing all the ways that a list of k positive integers can sum to n. Results can appear in any order. def sums(n, k): """Return the ways in which K positive integers can sum to ${\tt N.}$ >>> sums(2, 2)[[1, 1]]>>> sums(2, 3)>>> sums(4, 2) [[3, 1], [2, 2], [1, 3]] >>> sums(5, 3)[[3, 1, 1], [2, 2, 1], [1, 3, 1], [2, 1, 2], [1, 2, 2], [1, 1, 3]] if _____: return _____ y = []for x in _____: return y (b) (4 pt) Why so many lines? Implement f and g for this alternative version of the sums function. f = lambda x, y: (x and [_____ for z in y] + f(____, ___)) or [] def sums(n, k): """Return the ways in which K positive integers can sum to N.""" g = lambda w: (w and f(______)) or [[]]

return [v for v in g(k) if sum(v) == n]

True
False

2. (10.0 points) Yield, Fibonacci!

(a) (4.0 points)

Implement fibs, a generator function that takes a one-argument pure function f and yields all Fibonacci numbers x for which f(x) returns a true value.

The Fibonacci numbers begin with 0 and then 1. Each subsequent Fibonacci number is the sum of the previous two. Yield the Fibonacci numbers in order.

```
def fibs(f):
    """Yield all Fibonacci numbers x for which f(x) is a true value.
    >>> odds = fibs(lambda x: x % 2 == 1)
    >>> [next(odds) for i in range(10)]
    [1, 1, 3, 5, 13, 21, 55, 89, 233, 377]
    >>> bigs = fibs(lambda x: x > 20)
    >>> [next(bigs) for i in range(10)]
    [21, 34, 55, 89, 144, 233, 377, 610, 987, 1597]
    >>> evens = fibs(lambda x: x \% 2 == 0)
    >>> [next(evens) for i in range(10)]
    [0, 2, 8, 34, 144, 610, 2584, 10946, 46368, 196418]
    n, m = 0, 1
    while ____:
        if ____:
              (b)
               (c)
           (d)
 i. (1.0 pt) Which of these could fill in blank (a)?
   (n)
   (m)
   \bigcirc f(n) or f(m)
   \bigcirc f(n) and f(m)
```

ii.	(1.0 pt) Which of these could fill in blank (b)?
	(n)
	(m)
	∫ f(n) or f(m)
	Of(n) and f(m)
	○ True
	○ False
iii.	(1.0 pt) Fill in blank (c).
iv.	(1.0 pt) Fill in blank (d).

5. (7 points) Do You Yield?

(a) (6 pt) Implement partitions, which is a generator function that takes positive integers n and m. It yields strings describing all partitions of n using parts up to size m. Each partition is a sum of non-increasing positive integers less than or equal to m that totals n. The partitions function yields a string for each partition exactly once.

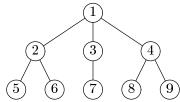
You may <u>not</u> use lambda, if, and, or, lists, tuples, or dictionaries in your solution (other than what already appears in the template).

```
def partitions(n, m):
  """Yield all partitions of N using parts up to size M.
  >>> list(partitions(1, 1))
  ['1']
  >>> list(partitions(2, 2))
  ['2', '1 + 1']
  >>> list(partitions(4, 2))
  ['2 + 2', '2 + 1 + 1', '1 + 1 + 1 + 1']
  >>> for p in partitions(6, 4):
       print(p)
  4 + 2
  4 + 1 + 1
  3 + 3
  3 + 2 + 1
  3 + 1 + 1 + 1
  2 + 2 + 2
  2 + 2 + 1 + 1
  2 + 1 + 1 + 1 + 1
  1 + 1 + 1 + 1 + 1 + 1
  if _____:
    yield _____
  if n > 0 and m > 0:
    yield ______
    yield from partitions(______, _____)
```

(b) (1 pt) Circle the order of growth of the value of len(list(partitions(n, 2))) as a function of n. For example, the value of len(list(partitions(3, 2))) is 2, because there are 2 partitions of 3 using parts up to size 2: 2+1 and 1+1+1. Assume partitions is implemented correctly.

Constant Logarithmic Linear Quadratic Exponential None of these

5. (13 points) Level-Headed Trees A level-order traversal of a tree, T, traverses the root of T (level 0), then the roots of all the branches of T (level 1) left to right, then all the roots of the branches of the nodes traversed in level 1, (level 2) and so forth. Thus, a level-order traversal of the tree



visits nodes with labels 1, 2, 3, 4, 5, 6, 7, 8, 9 in that order.

(a) (9 pt) Fill in the following generator function to yield the labels of a given tree in level order. All trees are of the class Tree, defined on page 2 of the Midterm 2 Study Guide. The strategy is to use a helper function that yields nodes at one level, and then to call this function with increasing levels until a level does not yield any labels. You may not need all the lines.

	level_order(tree):
	"""Generate all labels of tree in level order.""" def one_level(tree, k):
,	"""Generate the labels of tree at level k."""
	*
	if:
	else:
	for child in:
-	
-	level, count = 0, True
7	while count:
	count = 0
	for label in:

Name: 5

5. (6 points) To-Do Lists

t.remove(self)

Implement the TodoList and Todo classes. When a Todo is complete, it is removed from all the TodoList instances to which it was ever added. Track both the number of completed Todo instances in each list and overall so that printing a TodoList instance matches the behavior of the doctests below. Assume the complete method of a Todo instance is never invoked more than once.

```
class TodoList:
   """A to-do list that tracks the number of completed items in the list and overall.
   >>> a, b = TodoList(), TodoList()
   >>> a.add(Todo('Laundry'))
   >>> t = Todo('Shopping')
   >>> a.add(t)
   >>> b.add(t)
   >>> print(a)
   Remaining: ['Laundry', 'Shopping']; Completed in list: 0; Completed overall: 0
   >>> print(b)
   Remaining: ['Shopping']; Completed in list: 0; Completed overall: 0
   >>> t.complete()
   >>> print(a)
   Remaining: ['Laundry']; Completed in list: 1; Completed overall: 1
   >>> print(b)
   Remaining: []; Completed in list: 1; Completed overall: 1
   >>> Todo('Homework').complete()
   >>> print(a)
   Remaining: ['Laundry']; Completed in list: 1; Completed overall: 2
   def __init__(self):
      self.items, self.complete = [], 0
   def add(self, item):
      self.items.append(item)
   def remove(self, item):
           _____ += 1
      self.items.remove(______)
   def __str__(self):
      return ('Remaining: ' + str(_____) +
             '; Completed in list: ' + str(self.complete) +
             ' ; Completed overall: ' + str(______))
class Todo:
   done = 0
   def __init__(self, task):
      self.task, self.lists = task, []
   def complete(self):
                  ______ += 1
      for t in self.lists:
```

Name:	
Nama.	h

5.	(8	points'	Midterm	Elections

(a) (6 pt) Implement the Poll class and the tally function, which takes a choice c and returns a list describing the number of votes for c. This list contains pairs, each with a name and the number of times vote was called on that choice at the Poll with that name. Pairs can be in any order. Assume all Poll instances have distinct names. Hint: the dictionary get(key, default) method (MT 2 guide, page 1 top-right) returns the value for a key if it appears in the dictionary and default otherwise.

```
class Poll:
   s = []
   def __init__(self, n):
      self.name = ______
      self.votes = {}
   def vote(self, choice):
      self._____ = _____
def tally(c):
   """Tally all votes for a choice c as a list of (poll name, vote count) pairs.
   >>> a, b, c = Poll('A'), Poll('B'), Poll('C')
   >>> c.vote('dog')
   >>> a.vote('dog')
   >>> a.vote('cat')
   >>> b.vote('cat')
   >>> a.vote('dog')
   >>> tally('dog')
   [('A', 2), ('C', 1)]
   >>> tally('cat')
   [('A', 1), ('B', 1)]
   return _____
   (b) (2 pt) Implement the vote method of the Crooked class, which only records every other vote call for
     each Crooked instance. Only odd numbered calls to vote are recorded, e.g., first, third, fifth, etc.
class Crooked(Poll):
   """A poll that ignores every other call to vote.
   >>> d = Crooked('D')
   >>> for s in ['dog', 'cat', 'dog', 'cat', 'cat']:
         d.vote(s)
   . . .
   >>> d.votes
   {'dog': 2, 'cat': 1}
   record = True
   def vote(self, choice):
      if self.record:
```

6 Trees

4. (11 points) Tree Time

Definition. A runt node is a node in a tree whose label is smaller than all of the labels of its siblings. A sibling is another node that shares the same parent. A node with no siblings is a runt node.

(a) (7 pt) Implement runts, which takes a Tree instance t in which every label is different and returns a list of the labels of all runt nodes in t, in any order. Also implement apply_to_nodes, which returns nothing and is part of the implementation. Do not mutate any tree. The Tree class is on the Midterm 2 Guide. def runts(t): """Return a list in any order of the labels of all runt nodes in t. >>> sorted(runts(Tree(9, [Tree(3), Tree(4, [Tree(5, [Tree(6)]), Tree(7)]), Tree(2)]))) [2, 5, 6, 9]result = [] def g(node): if _____: result.append(_____) apply_to_nodes(______) return ______ def apply_to_nodes(f, t): """Apply a function f to each node in a Tree instance t.""" for b in t.branches: -----(b) (4 pt) Implement max_label, which takes a Tree t and returns its largest label. Do not mutate any tree. def max label(t): """Return the largest label in t. >>> max_label(Tree(4, [Tree(5), Tree(3, [Tree(6, [Tree(1), Tree(2)])])))) def f(node): _____ max(_____, _____, key=lambda n: _____) apply_to_nodes(f, t) # Assume that apply_to_nodes above is implemented correctly.

return t.label

Name:

6. (15 points) Trie this

A Trie is a Tree where every node in the tree contains a single letter except for the root which is always the empty string. Every path from the root to a leaf forms a word. You may assume no words are substrings of other words in the trie (e.g., "hi" and "him"). The figure below is a trie generated by storing the words ["this", "is", "the", "trie"]. The Tree class is defined on Page 2 of the Midterm 2 Study Guide.

(a) (7 pt) Implement add_word which takes a Trie and a word and adds the word to the trie.

```
def make_trie(words):
   """ Makes a tree where every node is a letter of a word.
      All words end as a leaf of the tree.
      words is given as a list of strings.
   .....
   trie = Tree('')
   for word in words:
      add_word(trie, word)
   return trie
def add_word(trie, word):
   if ____
      return
   branch =
         branch =
```

(b) (8 pt) Implement get_words, which takes a Trie and returns a list of all the words the Trie is storing.

3. (21.0 points) College Party

In a US presidential election, each state has a number of electors.

Definition: For some collection of states s, a win by at least k is a (possibly empty) subset w of s such that the total number of electors for the states in w is at least k more than the total number of electors for the states not in w but in s.

For example, in the battleground states below, Arizona (AZ), Pennsylvania (PA), and Michigan (MI) have a total of 11 + 20 + 16 = 47 electors. The remaining states have a total of 6 + 16 + 10 = 32 electors. So, the subset <AZ PA MI> is a win by 47 - 32 = 15.

(a) (8.0 points)

Implement wins, a generator function that takes a list of State instances states and an integer k. For every possible win by at least k among the states, it yields a linked list containing strings of the two-letter codes for the states in that win.

Any order of the wins and any order of the states within a win is acceptable.

A linked list is a Link instance or Link.empty. The Link class appears on the Midterm 2 Study Guide.

```
def wins(states, k):
```

"""Yield each linked list of two-letter state codes that describes a win by at least k.

```
>>> print_all(wins(battleground, 50))
<AZ PA NV GA WI MI>
<AZ PA NV GA MI>
<AZ PA GA WI MI>
<PA NV GA WI MI>
>>> print_all(wins(battleground, 75))
<AZ PA NV GA WI MI>
"""

if _____:
    # (a)
    yield Link.empty

if states:
    first = states[0].electors
```

	for win in wins(states[1:],): # (b)
	yield Link(, win) # (c)
	<pre>yield from wins(states[1:],) # (d)</pre>
i.	(2.0 pt) Which of the these could fill in blank (a)?
	○ k >= 0
	○ k <= 0
	○ k == 0
	O not states
	\bigcirc k >= 0 and not states
	\bigcirc k <= 0 and not states
	\bigcirc k == 0 and not states
ii.	(2.0 pt) Which of the these could fill in blank (b)?
	○ k - first
	○ k + first
	○ k
	○ -k
	O 0
	○ first
	○ min(k, first)
	<pre>max(k, first)</pre>
iii.	(2.0 pt) Fill in blank (c).
iv.	(2.0 pt) Which of the these could fill in blank (d)?
	○ k - first
	○ k + first
	○ k
	○ -k
	O 0
	O first
	<pre>min(k, first)</pre>
	<pre> max(k, first)</pre>

(b) (7.0 points)

Implement $must_win$, which takes a list of State instances states and an integer k. It returns a list of two-letter state codes (strings) for all states that appear in every $win\ by\ at\ least\ k$ among the states. Assume wins is implemented correctly.

def	<pre>must_win(states, k): """List all states that must be won in every scenario that wins by k.</pre>	
	<pre>>>> must_win(battleground, 50) ['PA', 'GA', 'MI'] >>> must_win(battleground, 75) ['AZ', 'PA', 'NV', 'GA', 'WI', 'MI'] """</pre>	
	<pre>def contains(s, x): """Return whether x is a value in linked list s."""</pre>	
	return () and () # (a) (b)	
	return [for s in states if([for w in wins(states, k) # (c) (d) (e)])]
i.	(1.0 pt) Which of these could fill in blank (a)?	
	Os is Link.empty	
	Os is not Link.empty	
	\bigcirc x in s	
	O x not in s	
	○ x == s.first	
	○ x != s.first	
i.	(2.0 pt) Fill in blank (b).	
iii.	(1.0 pt) Fill in blank (c).	
iv.	(1.0 pt) Fill in blank (d) with a single function name.	

v.	(2.0 pt) Fill in blank (e).

	:				_	!
4. ((11 points) Both	n Ways				
(a)	some value is in bo	oth of them. The	Link class is o	lefined on the m	idterm 2 study gu	ects and returns whether ide. n, or list comprehensions
lef	both(a, b): """Return whether	er there is any	y value that	appears in bo	th a and b, two	sorted Link instanc
	>>> both(Link(1, False	, Link(3, Link	(5, Link(7))), Link(2, Li	nk(4, Link(6))))
	>>> both(Link(1, True	, Link(3, Link	(5, Link(7))), Link(2, Li	nk(7, Link(9)))) # both have 7
	True) # both have 4 and
	if					
	return False	е				
	if					
	a, b = b, a					
	roturn					
	recurn					
(b)		Θ expression that	at describes the	e minimum num		s (e.g., <, >, <=,==, or > common.
(b)	(2 pt) Circle the	Θ expression that	at describes the	e minimum num	ntain no values in	
	(2 pt) Circle the expressions) require $\Theta(1)$ (5 pt) Implement argument functions such that $f_1(f_2)$	Θ expression that ed to verify that $\Theta(\log n)$ t ways, which takes actions. It retrify $(f_j(start)))$ equa	at describes the two sorted list $\Theta(n)$ are two values arms the number θ and θ	e minimum num s of length n cos $\Theta(n^2)$ start and end , are of ways of cho k . The same ac	ntain no values in $\Theta(2^n)$ a non-negative intensing functions f_1 , tion function can be	common. None of these eger k , and a list of one $f_2,, f_j$ from actions
(c)	(2 pt) Circle the expressions) require $\Theta(1)$ (5 pt) Implement argument functions such that $f_1(f_2)$	Θ expression that ed to verify that $\Theta(\log n)$ t ways, which takes actions. It retrifications reaches end to k, actions:	that describes the two sorted list $\Theta(n)$ are two values arms the number i , then no furth	e minimum num s of length n cos $\Theta(n^2)$ start and end, at er of ways of chock. The same actions can be	ntain no values in $\Theta(2^n)$ a non-negative intensing functions f_1 , tion function can be applied (see the	None of these eger k , and a list of one of $f_2,, f_j$ from actions be chosen multiple times first example below).
(c)	(2 pt) Circle the expressions) require $\Theta(1)$ (5 pt) Implement argument functions such that $f_1(f_2())$ If a sequence of act ways(start, end, """Return the number of the sequence of act ways(start, end, """Return the number of the sequence of act ways(start, end, """Return the number of the sequence of the seque	Θ expression that $\Theta(\log n)$ that $\Theta(\log n)$ the ways, which takes actions. It returns that $f_j(start)))$ equations reaches ending, k, actions):	that describes the two sorted list $\Theta(n)$ are two values two values arms the number i , then no further of reaching i	e minimum num s of length n corrected $\Theta(n^2)$ start and end, a er of ways of chock. The same actions can be end from start	ntain no values in $\Theta(2^n)$ a non-negative interesting functions f_1 , tion function can be applied (see the	None of these eger k , and a list of one $f_2,, f_j$ from actions be chosen multiple time first example below).
(c)	(2 pt) Circle the expressions) require $\Theta(1)$ (5 pt) Implement argument functions such that $f_1(f_2)$ (If a sequence of act ways(start, end, """Return the number of the sequence of the	Θ expression that $\Theta(\log n)$ the ways, which takes actions. It retained that $(f_j(start)))$ equations reaches endured, k, actions: sumber of ways of the start	the describes the two sorted list $\Theta(n)$ are two values arms the number a and a and a are the period of reaching a and a are the period a are a are a and a are a are a are a and a are a	e minimum num s of length n corrections $\Theta(n^2)$ start and end, at the end of the end of the end from start $\#$ abs(-1) or	ntain no values in $\Theta(2^n)$ a non-negative interesting functions f_1 , tion function can be applied (see the by taking up to f_1), but not	None of these eger k , and a list of one of $f_2,, f_j$ from actions be chosen multiple times first example below). o k actions. abs(abs(-1))
(c)	(2 pt) Circle the expressions) require $\Theta(1)$ (5 pt) Implement argument functions such that $f_1(f_2)$ (If a sequence of act ways(start, end, """Return the number of act ways(1, 10, 3) ways(1, 20, 3) ways(1, 20, 20)	Θ expression that ed to verify that ed to sactions. It returns the following formula ed to sactions reaches end , k, actions): ed to sample of ways of ed to ed	the describes the two sorted list $\Theta(n)$ kees two values arms the number i , then no furth of reaching i at i	e minimum num s of length n corresponds to $\Theta(n^2)$ start and end, are of ways of chock. The same accer actions can be end from start # abs(-1) or x: x+4]) # 1	ntain no values in $\Theta(2^n)$ a non-negative interesting functions f_1 , tion function can be applied (see the by taking up to f_1), but not	None of these eger k , and a list of one of $f_2,, f_j$ from actions be chosen multiple times first example below). o k actions. abs(abs(-1))
(c)	(2 pt) Circle the expressions) require $\Theta(1)$ (5 pt) Implement argument functions such that $f_1(f_2)$ (If a sequence of act ways(start, end, """Return the number of act ways(1, 10, 3) ways(1, 20, 0) ways(1, 20, 0) ways(13], [23]	Θ expression that ed to verify that $\Theta(\log n)$ the ways, which takes actions. It returns that the sactions reaches end that the sactions is actions? It is actions reaches end that the sactions of the sacti	the describes the two sorted list $\Theta(n)$ are set two values arms the number i , then no furth of reaching i and i and i are i and i are i and i are i are i and i are i are i and i are i and i are i are i are i and i are i are i and i are i and i are i are i and i are i are i and i are i	e minimum num s of length n corrected $\Theta(n^2)$ start and end, a er of ways of chock. The same accer actions can be end from start # abs(-1) or x: x+4]) # 1	ntain no values in $\Theta(2^n)$ a non-negative interestion functions f_1 , tion function can be applied (see the by taking up to $-1+2$, but not $+1+4+4$, $1+4+4+1$	None of these eger k , and a list of one $f_2,, f_j$ from actions be chosen multiple times first example below). o k actions. abs(abs(-1)) , or 1+4+1+4
(c)	(2 pt) Circle the expressions) require $\Theta(1)$ (5 pt) Implement argument functions such that $f_1(f_2)$ (If a sequence of act ways(start, end, """Return the number of act ways(1, 10, 3) ways(1, 10, 3) ways(1, 20, 0) $\Theta(1)$ ways(1, 20, 0) $\Theta(1)$ ways(1, 20, 10, 3) $\Theta(1)$	Θ expression that ed to verify that $\Theta(\log n)$ the ways, which takes actions. It retractions reaches end to the property of	the describes the two sorted list $\Theta(n)$ sees two values arms the number i , then no furth of reaching i at i	e minimum num s of length n corrections $\Theta(n^2)$ start and end, a er of ways of chock. The same accer actions can be end from start # abs(-1) or x: x+4]) # 1 x: x+4]) # 1 x: x+4])	ntain no values in $\Theta(2^n)$ a non-negative interesting functions f_1 , tion function can be applied (see the by taking up to f_1), but not f_1 , but not f_2 , but not f_1 , f_2 , f_3 , f_4	None of these eger k , and a list of one of $f_2,, f_j$ from actions be chosen multiple times first example below). To k actions. abs(abs(-1)) To r 1+4+1+4
(c)	(2 pt) Circle the expressions) require $\Theta(1)$ (5 pt) Implement argument functions such that $f_1(f_2)$ (If a sequence of act ways(start, end, """Return the number of act ways(1, 10, 3) ways(1, 10, 3) ways(1, 20, 0) $\Theta(1)$ ways(1, 20, 0) $\Theta(1)$ ways(1, 20, 10, 3) $\Theta(1)$	Θ expression that ed to verify that $\Theta(\log n)$ the ways, which takes actions. It retractions reaches end to the property of	the describes the two sorted list $\Theta(n)$ sees two values arms the number i , then no furth of reaching i at i	e minimum num s of length n corrections $\Theta(n^2)$ start and end, a er of ways of chock. The same accer actions can be end from start # abs(-1) or x: x+4]) # 1 x: x+4]) # 1 x: x+4])	ntain no values in $\Theta(2^n)$ a non-negative interesting functions f_1 , tion function can be applied (see the by taking up to f_1), but not f_1 , but not f_2 , but not f_1 , f_2 , f_3 , f_4	None of these eger k , and a list of one $f_2,, f_j$ from actions be chosen multiple times first example below). o k actions. abs(abs(-1)) , or 1+4+1+4

return _____([______ for f in actions])

Name: 7

3. (8 points) Seeing Double

return result

Fill in the functions below to produce linked lists in which each item of the original list is repeated immediately after that item. Your solutions should be iterative, not recursive.

(a) (4 pt) The function double1 is non-destructive, and produces a new list without disturbing the old. def double1(L): """Returns a list in which each item in L appears twice in sequence. It is non-destructive. >>> Q = Link(3, Link(4, Link(1)))>>> double1(Q) Link(3, Link(3, Link(4, Link(4, Link(1, Link(1)))))) >>> Q Link(3, Link(4, Link(1))) >>> double1(Link.empty) () 11 11 11 result = ______ last = None while L is not Link.empty: if last is None: _____ else: ______ ______ return result (b) (4 pt) The function double2 is destructive, and reuses Link objects in the original list wherever possible. def double2(L): """Destructively modifies L to insert duplicates of each item immediately following the item, returning the result. >>> Q = Link(3, Link(4, Link(1))) >>> double2(Q) Link(3, Link(3, Link(4, Link(4, Link(1, Link(1)))))) Link(3, Link(3, Link(4, Link(4, Link(1, Link(1)))))) result = _____ while L is not Link.empty: ______ _____