EECS 182   Deep Neural Networks

Fall 2022   Anant Sahai   # Homework 6

This homework is due on Saturday, Nov 5, 2022, at 10:59PM.

Deliverables: Please submit the code/notebooks to the code gradescope assignment. Submit your written answers in the written gradescope assignment, and attach a pdf printout of the notebook.

1. Redo the Midterm

Please redo the midterm exam (linked at `https://static.us.edusercontent.com/files/hQ7lNcAn75o6lyD0KMtVssl7`) as homework. Attach your answers to the written part of this homework.

2. Implementing Simple Transformers

(a) Implementing a simple transformer. Fill out Section (a) in the notebook. No written portion.

(b) Designing a transformer that selects by content. Fill out Section (b) in the notebook and **comment on the similarities and differences between the weights and intermediate outputs of the learned and hand-coded model.**

(c) Designing a transformer that selects by position. Fill out Section (b) in the notebook and **comment on the similarities and differences between the weights and intermediate outputs of the learned and hand-coded model.**

(d) (optional) Designing a transformer that selects by position. Fill out Section (b) in the notebook and **comment on the similarities and differences between the weights and intermediate outputs of the learned and hand-coded model.**

Please submit your notebook and your written answers to Gradescope.

3. Regularization and Dropout [Optional]

(This is an extension on Q11 on the midterm.)

You saw one perspective on the implicit regularization of dropout in HW, and here, you will see another one. Recall that linear regression optimizes the following learning objective:

$$\mathcal{L}(\mathbf{w}) = ||\mathbf{y} - X\mathbf{w}||_2^2 \tag{1}$$

One way of using *dropout* during SGD on the d-dimensional input features $\mathbf{x}_i$ involves keeping each feature at random $\sim_{i.i.d} Bernoulli(p)$ (and zeroing it out if not kept) and then performing a traditional SGD step.

It turns out that such dropout makes our learning objective effectively become

$$\mathcal{L}(\check{\mathbf{w}}) = E_{R \sim Bernoulli(p)}\left[||\mathbf{y} - (R \odot X)\check{\mathbf{w}}||_2^2\right] \tag{2}$$

where $\odot$ is the element-wise product and the random binary matrix $R \in \{0,1\}^{n \times d}$ is such that $R_{i,j} \sim_{i.i.d} Bernoulli(p)$. We use $\check{\mathbf{w}}$ to remind you that this is learned by dropout.

Recalling how Tikhonov-regularized (generalized ridge-regression) least-squares problems involve solving:

$$\mathcal{L}(\mathbf{w}) = ||\mathbf{y} - X\mathbf{w}||_2^2 + ||\Gamma\mathbf{w}||_2^2 \tag{3}$$

for some suitable matrix Γ,

show that we can manipulate (2) **to eliminate the expectations and get:**

$$\mathcal{L}(\check{\mathbf{w}}) = ||\mathbf{y} - pX\check{\mathbf{w}}||_2^2 + p(1-p)||\check{\Gamma}\check{\mathbf{w}}||_2^2 \tag{4}$$

with $\check{\Gamma}$ being a diagonal matrix whose j-th diagonal entry is the norm of the j-th column of the training matrix X.

4. Homework Process and Study Group

Citing sources and collaborators are an important part of life, including being a student!
We also want to understand what resources you find helpful and how much time homework is taking, so we can change things in the future if possible.

(a) **What sources (if any) did you use as you worked through the homework?**

(b) **If you worked with someone on this homework, who did you work with?**
List names and student ID's. (In case of homework party, you can also just describe the group.)

(c) **Roughly how many total hours did you work on this homework? Write it down here where you'll need to remember it for the self-grade form.**

Contributors:

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