

Last time:

- \* Capacitive Touchscreen Motiv.
- \* Intro to Capacitors
- \* Capacitor Equivalence

Note 16

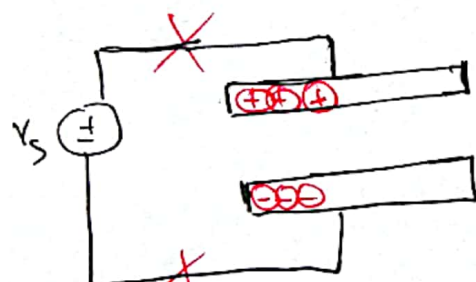
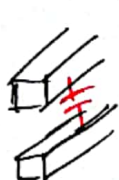
Today:

- \* Build Capacitive Touch Screen
- \* Charge Sharing

Note 17 + supplemental algorithm.

## "16-A" Capacitor Physics

Capacitor: Any two conductors separated by an insulator  
(material that cannot carry current)



Why are these structures called capacitors?

$$Q = C \cdot V \rightarrow \text{if } V \uparrow \rightarrow Q \uparrow$$

$$\rightarrow \text{if } C \uparrow \rightarrow Q \uparrow$$

Capacitors are charge storage mechanisms  
"buckets" of charge

$$V_c = \frac{dE}{dq} \Rightarrow dE = V_c \cdot dq = V_c \cdot C \cdot dV_c$$

$$\int \Rightarrow E = \frac{1}{2} C V_c^2$$

If I disconnect the voltage source, the charge will remain on the capacitor!!

**CHARGE IS CONSERVED!**

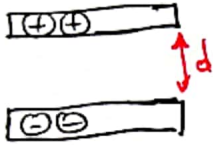
(P2)

Capacitor value depends on:

- 1) Geometry of the conductor
- 2) Material properties of the insulator

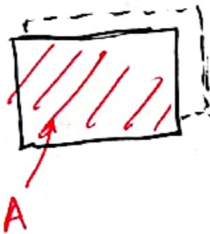
↳  $\epsilon$ : permittivity  $\left[\frac{F}{m}\right]$

Side - View



air  $\hookrightarrow \epsilon_0 = 8.85 \text{ pF/m}$       p: pico:  $10^{-12}$

Top - View



$$C = \epsilon \frac{A}{d}$$

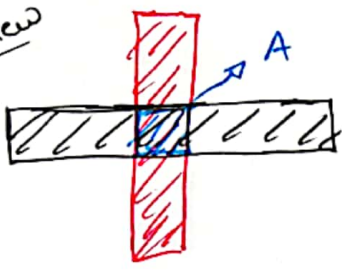
→ model capacitance  
in our touchscreen.  
as a "parallel plate"  
capacitance

P3

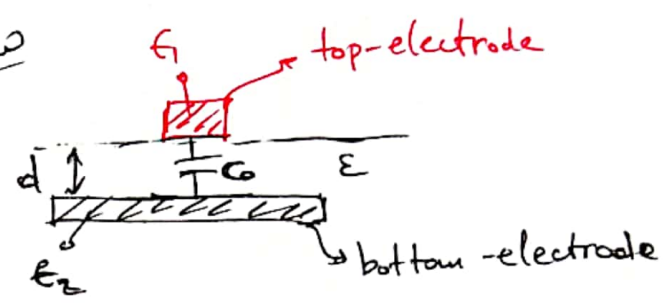
Let's get back to touchscreens:

- Single pixel

Top-View

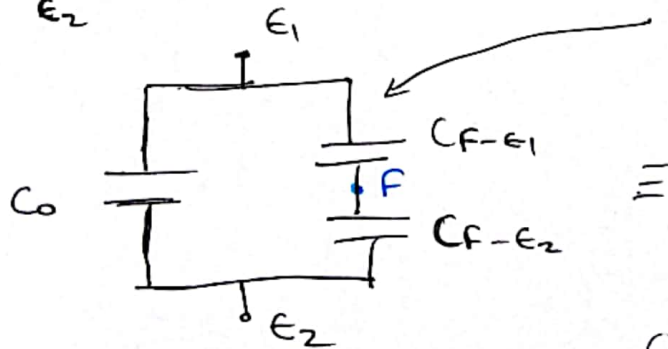
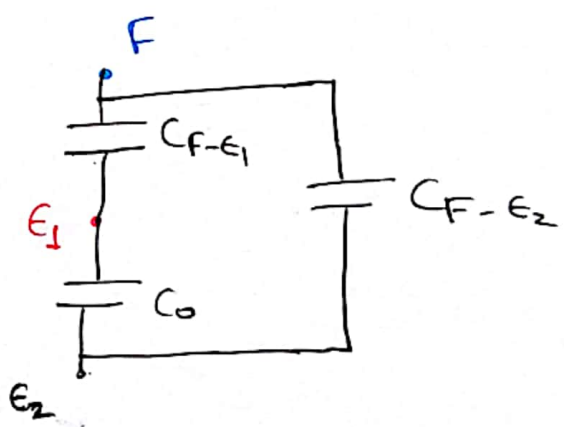
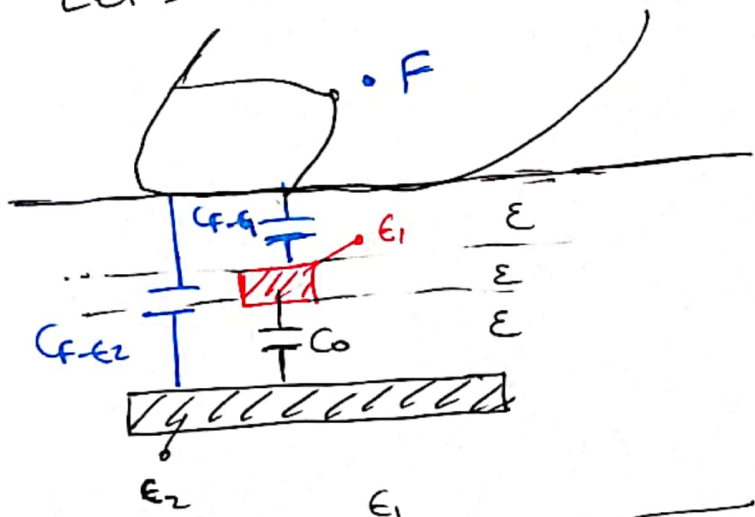


Side-View



$$C_{eq, no touch} = C_0 = \epsilon \frac{A}{d}$$

Let's touch it!

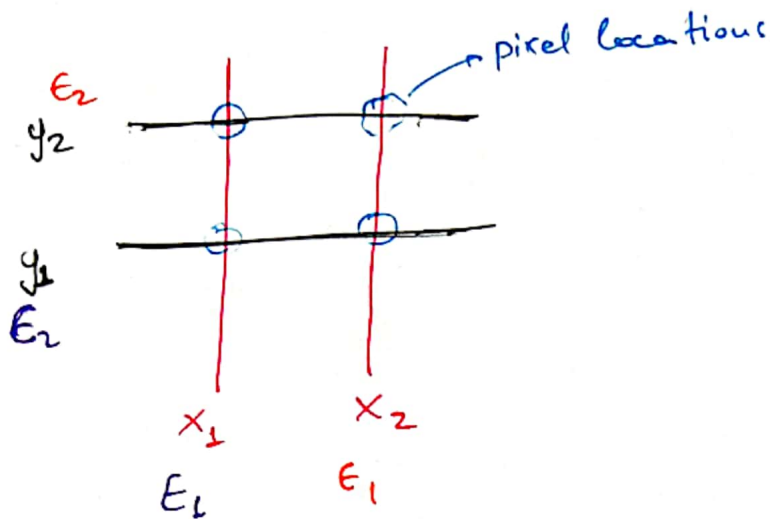


$$C_{eq, touch} = C_0 + \underbrace{C_{F-E1} \parallel C_{F-E2}}_{\Delta C} > C_0$$

Key Result:  $C_{eq, touch} > C_{eq, no touch}$

(p4)

## 2D-View

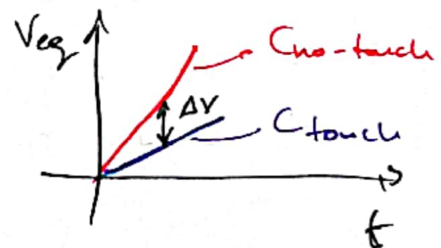


bottom-left corner:  
connect  $E_1, E_2$  to  $(x_1, y_1)$

top-right corner:  
connect  $E_1, E_2$  to  $(x_2, y_2)$

## How to measure capacitance (change in capacitance)

Proposal 1: Use a current source

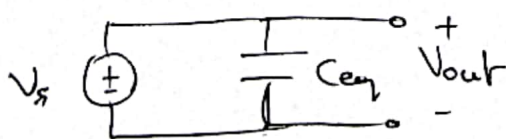


Problem: Current Sources are really hard to build!

Proposal 2: Use a voltage source

Key Idea:  $Q = C \cdot V$  (apply a fixed voltage and measure  $dQ$  due to  $dC$ )

Attempt #1:



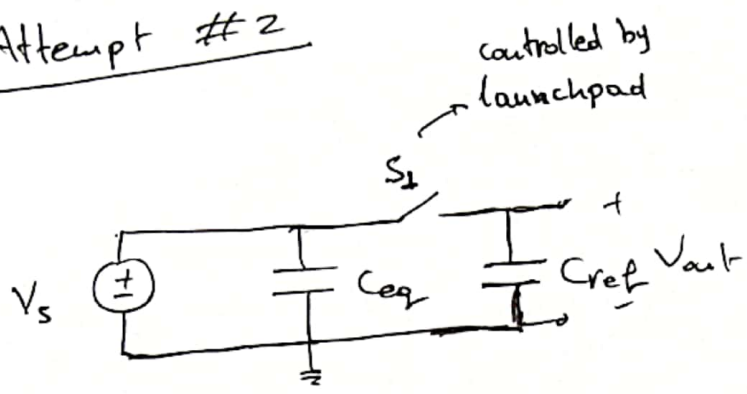
$V_{out} = V_s$  set by the voltage source  
 $\neq f(C_{eq})$



My goal was to detect a change  
in  $C_{eq}$ !

PS

# Attempt #2



$S_1$ : ON

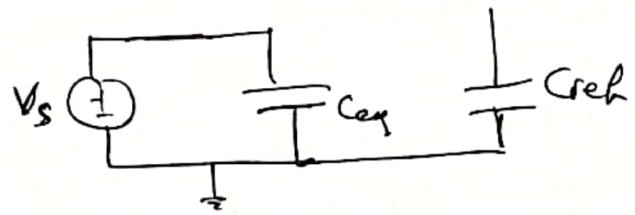
wire

$S_2$ : OFF

open-ckt

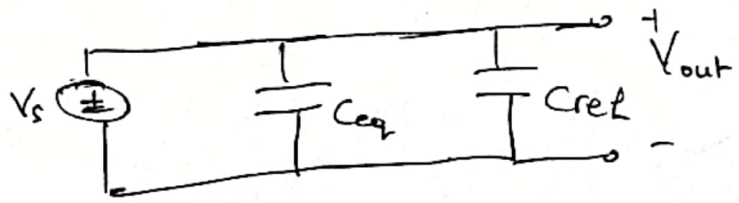
## Phase 1

$S_1$ : OFF



## Phase 2

$S_1$ : ON

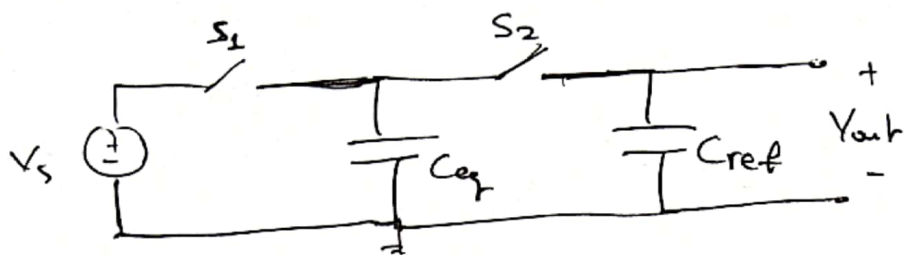


Same problem:  $V_{out} = V_s \neq f(C_{eq})$



pg

# Attempt #3 :



## Phase 1

$S_1 : ON$   
 $S_2 : OFF$



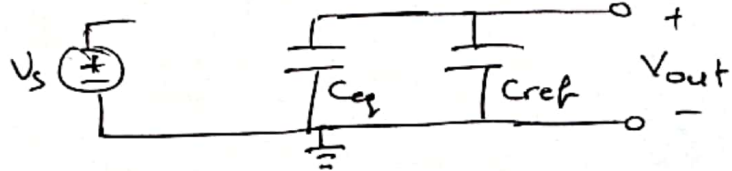
$V_{ref}(0) = ?$   
 $V_{out}(0) = ?$

Cannot calculate  $V_{out}$  at phase 2! (see attempt #4)

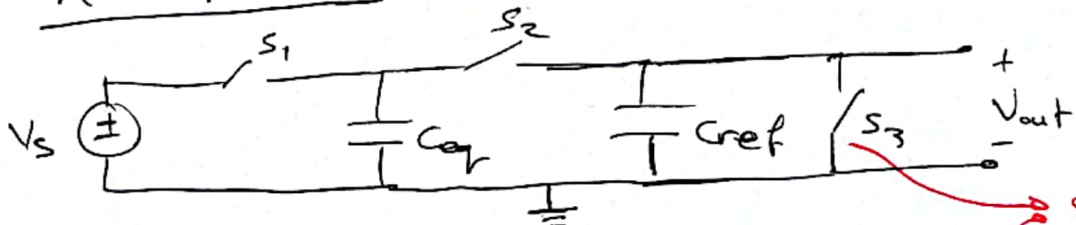


## Phase 2

$S_1 : OFF$   
 $S_2 : ON$



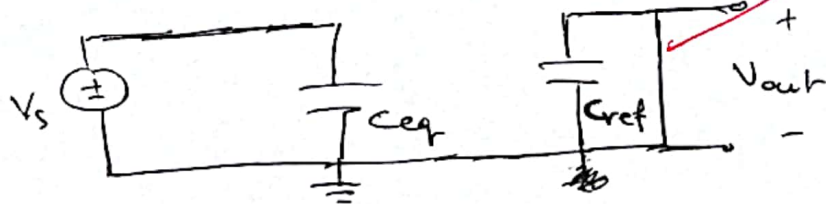
# Attempt #4 :



set  $V_{ref}(0) = 0$

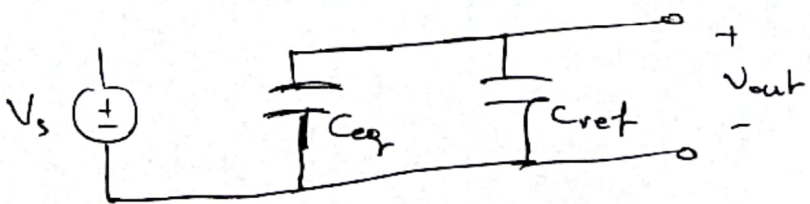
## Phase 1

$S_1 : ON$   
 $S_2 : OFF$   
 $S_3 : ON$



## Phase 2

$S_1 : OFF$   
 $S_2 : ON$   
 $S_3 : OFF$





(P7) Total Charge in Phase 1:

$$Q_{tot,1} = Q_{Ceq,1} + Q_{Cref,1} = C_{eq} \cdot V_s + 0 \quad (1)$$

Total Charge in Phase 2:

$$Q_{tot,2} = (C_{eq} + C_{ref}) \cdot V_{out} \quad (2)$$

↘  
 $C_{ref} \cdot V_{ref}(0)$   
 → in attempt #3  
 I did not know  
 $V_{ref}(0)$

Charge Conservation:  $Q_{tot,1} = Q_{tot,2}$

$$\Rightarrow C_{eq} \cdot V_s = (C_{eq} + C_{ref}) \cdot V_{out}$$

$$\Rightarrow V_{out} = \frac{C_{eq}}{C_{eq} + C_{ref}} \cdot V_s = f(C_{eq}) \quad \text{😊}$$

## Charge Sharing

Let's Recap:

Goal: Build a new touchscreen

- 1) Look into capacitors
- 2) Modeled finger touching screen as a  $C_{eq}$
- 3) Charge Sharing ckt to measure  $\Delta C_{eq}$

Op-amp (used as a comparator)

Symbol:

