

C2-UA.412: calc 2

Practice Exam

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Total: 100 points

1. Find the volume of the solid generated by revolving the region bounded by the curves $y = x^2$ and $y = 4x - x^2$ about the x-axis. Set up the integral and solve.

2. Evaluate the integral $\int_0^{\pi/6} \sin(2t) \cos(t) dt$. Use an appropriate trigonometric substitution. Show all steps of your work.

3. Determine whether the series $\sum_{n=0}^{\infty} \frac{(-1)^n (n+1)^2}{3^n}$ converges or diverges. Justify your answer using an appropriate convergence test.

4. Find the arc length of the curve $y = (x^3/6) + (1/(2x))$ from $x = 1$ to $x = 2$. Set up the integral and solve.

5. A tank is in the shape of an inverted cone with a height of 10 meters and a radius of 5 meters. The tank is filled with water to a depth of 6 meters. Find the work required to pump all the water out of the top of the tank. Assume the density of water is 1000 kg/m^3 and acceleration due to gravity is 9.8 m/s^2 .

6. Find the Taylor series for $f(x) = e^{(2x)}$ centered at $x = 1$. Write out the first four non-zero terms.

7. Use the method of partial fractions to evaluate the integral $\int_1^2 \frac{(3x + 1)}{(x^2 - x - 2)} dx$.

8. Determine the interval of convergence for the power series $\sum_{n=0}^{\infty} \frac{[(x-3)^n]}{(n+1)^2}$.

9. Find the area of the region enclosed by the polar curve $r = 2 + 2\cos(\theta)$.

10. Evaluate the improper integral $\int_1^{\infty} (1/x^2) dx$. Does this integral converge or diverge? If it converges, what is its value?