## **Parallel Computing Practice Exam**

Generated on June 26, 2025 Difficulty: Medium

- 1. Describe a parallel algorithm for finding the connected components in an undirected graph using a message-passing paradigm. Explain how the algorithm handles the distribution of work across multiple processors and how it detects termination. Detail the communication patterns between the processors and discuss potential bottlenecks.
- 2. Implement a parallel merge sort algorithm using the fork-join model. Assume you have access to a shared memory system. Describe the steps involved in recursively dividing the data, sorting sub-arrays in parallel, and merging the sorted sub-arrays. Analyze the time complexity of your algorithm in terms of the number of processors and the input size.
- 3. Consider the problem of matrix multiplication of two large matrices A and B. Design a parallel algorithm using a distributed memory model where each processor is responsible for a sub-matrix. Outline the algorithm's steps, detailing how the processors communicate to exchange data and how the final result is assembled. Discuss the impact of communication overhead on the algorithm's performance.
- 4. Explain how you would adapt Dijkstra's algorithm for finding the shortest paths in a graph to a parallel environment. Assume a shared-memory model. Discuss different strategies for parallelizing the algorithm, considering both the computational load and the synchronization requirements. Compare the potential speedups achieved with different parallelization strategies.
- 5. You are given a large unsorted array of integers. Design a parallel algorithm to find the kth smallest element in this array using a randomized selection algorithm. Describe how you would partition the array into smaller sub-arrays and how you would recursively select the kth smallest element within each sub-array. Analyze the expected time complexity of your algorithm, taking into account the overhead of parallel operations.