

## C2-UA.160: calc 2

### Practice Exam

Generated on August 28, 2025

**Total: 100 points**

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- Find the volume of the solid generated by revolving the region bounded by the curves  $y = x^2$  and  $y = 4$  about the  $x$ -axis. Use the disk/washer method.
  - Evaluate the integral  $\int (x^3 + 2x^2 - 5x + 1) / (x^2 + 1) dx$  using polynomial long division and partial fraction decomposition.
  - Determine the convergence or divergence of the series  $\sum_{n=1}^{\infty} \frac{(-1)^n (n^2 + 1)}{(n^3 + 2n)}$ . Justify your answer using an appropriate test.
  - Find the arc length of the curve  $y = (x^3/6) + (1/(2x))$  from  $x = 1$  to  $x = 2$ .
  - Find the area of the surface generated by revolving the curve  $y = \sqrt{x}$ ,  $1 \leq x \leq 4$ , about the  $x$ -axis.
  - A particle moves along a line so that its velocity at time  $t$  is given by  $v(t) = t^2 - 4t + 3$ . Find the total distance traveled by the particle from  $t = 0$  to  $t = 4$ .
  - Find the Taylor series for  $f(x) = e^{-x^2}$  centered at  $x = 0$ . Write out the first four non-zero terms.
  - Evaluate the improper integral  $\int_0^{\infty} x e^{-x^2} dx$ .
  - Use the method of cylindrical shells to find the volume of the solid generated by rotating the region bounded by  $y = x^3$  and  $y = x$  about the  $y$ -axis.
  - Find the interval of convergence for the power series  $\sum_{n=0}^{\infty} \frac{(-1)^n (x-2)^n}{(n^2 + 1)}$ . Include a check for convergence at the endpoints.