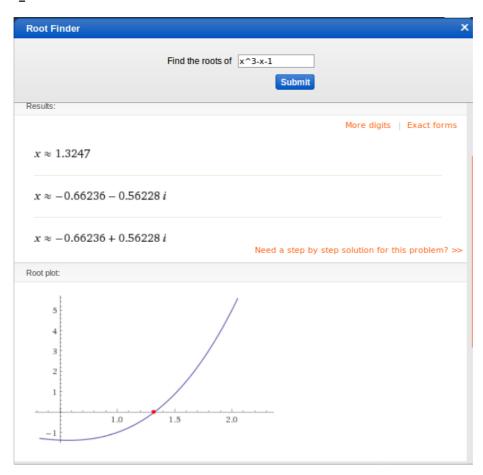
## <u>1. Örnek: x³ - x - 1 & Epsilon: 0.01 & Max Iteration: 20</u> POLİNOM:



Kaynak: http://www.wolframalpha.com/widgets/view.jsp?id=a7d8ae4569120b5bec12e7b6e9648b86

### 1.a.Newton Raphson(1) - $X_0 = 3$ için ÇIKTI:

```
spaced@spaced-Lenovo-ideapad-310-15IKB:~/Desktop$ ./a.out
Enter the coefficients of quartic polynomial.
a4: 0
a3: 1
a2: 0
a1: -1
a0: -1
Your polynomial is: 0*x^4 + 1*x^3 + 0*x^2 + -1*x^1 + -1
Enter the epsilon value: 0.01
Enter the maximum iteration: 20
        Find root with Regula Falsi Method.
1.
        Find root with Newton Raphson Method.
2.
Enter your choice (1 or 2): 2
Please enter the x0 value to estimate the root of the polynomial: 3
        xN: 3.000000
                        yN: 23.000000
1..
2..
        xN: 2.712500
                        yN: 16.245143
        xN: 2.436564
                        yN: 11.028942
3..
                        yN: 7.132939
        xN: 2.176426
4..
5..
        xN: 1.938091
                        yN: 4.341755
                        yN: 2.445709
6..
        xN: 1.729748
        xN: 1.561385
                        yN: 1.245151
7..
8..
        xN: 1.441884
                        yN: 0.555836
                        yN: 0.212236
9..
        xN: 1.372345
                        yN: 0.070145
10..
        xN: 1.340920
        xN: 1.329667
                        yN: 0.021203
Newton Raphson Method used successfully.
```

Computed root is Xi:1.326164 and f(Xi): 0.006174

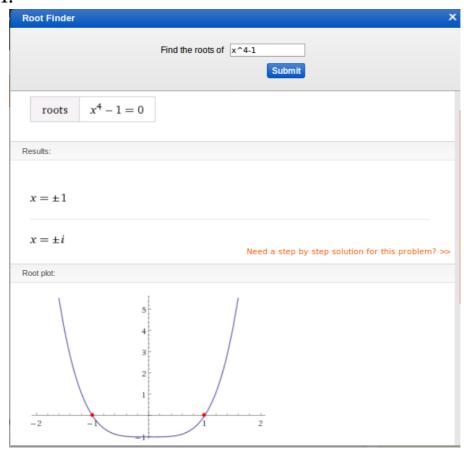
#### 1.b.Newton Raphson(2) - $X_0 = -10$ için ÇIKTI:

```
spaced@spaced-Lenovo-ideapad-310-15IKB:~/Desktop$ ./a.out
Enter the coefficients of quartic polynomial.
a4: 0
a3: 1
a2: 0
a1: -1
a0: -1
Your polynomial is: 0*x^4 + 1*x^3 + 0*x^2 + -1*x^1 + -1
Enter the epsilon value: 0.01
Enter the maximum iteration: 20
        Find root with Regula Falsi Method.
        Find root with Newton Raphson Method.
2.
Enter your choice (1 or 2): 2
Please enter the x0 value to estimate the root of the polynomial: -10
1..
        xN: -10.000000 yN: -991.000000
        xN: -10.330223 yN: -1093.044186
2..
        xN: -10.660635 yN: -1201.911497
3..
4..
        xN: -10.991220
                        yN: -1317.824160
        xN: -11.321962
                        yN: -1441.004404
5..
        xN: -11.652849
                        yN: -1571.674456
6..
        xN: -11.983868 yN: -1710.056543
7..
8..
        xN: -12.315010 yN: -1856.372892
        xN: -12.646265
                       yN: -2010.845728
9..
                       yN: -2173.697278
10..
        xN: -12.977624
        xN: -13.309080 yN: -2345.149765
11..
        xN: -13.640626
                        yN: -2525.425415
12..
        xN: -13.972256 yN: -2714.746453
13..
14..
        xN: -14.303963 yN: -2913.335102
        xN: -14.635744
                        yN: -3121.413588
15..
                        yN: -3339.204135
16..
        xN: -14.967592
17..
        xN: -15.299504
                        yN: -3566.928965
                        yN: -3804.810303
        xN: -15.631475
18..
                        yN: -4053.070372
19..
        xN: -15.963503
20. .
        xN: -16.295583
                        yN: -4311.931396
Newton Raphson Method used successfully.
Program reached the maximum number of iteration.
Computed root is Xi:-16.627712 and f(Xi): -4581.615599
```

#### 1.c.Regula Falsi - xL = -3, xR = 3 için ÇIKTI:

```
spaced@spaced-Lenovo-ideapad-310-15IKB:~/Desktop$ ./a.out
Enter the coefficients of quartic polynomial.
a4: 0
a3: 1
a2: 0
a1: -1
a0: -1
Your polynomial is: 0*x^4 + 1*x^3 + 0*x^2 + -1*x^1 + -1
Enter the epsilon value: 0.01
Enter the maximum iteration: 20
        Find root with Regula Falsi Method.
         Find root with Newton Raphson Method.
Enter your choice (1 or 2): 1
Estimate xLeft and xRight as initial values.
     (yRight = P(xRight)) and yLeft = P(xLeft) signs must be opposite)
xLeft: -3
xRight: 3
         xM:0.125000
                                                                                 xR:3.000000
                                                                                                   yR:23.000000
                           vM:-1.123047
                                             xL:0.125000
                                                               vL:-1.123047
                           yM:-1.241503
2..
3..
                                                               yL:-1.241503
yL:-1.335599
         xM:0.258845
                                             xL:0.258845
                                                                                 xR:3.000000
                                                                                                    yR:23.000000
                                                                                                   yR:23.000000
                           yM:-1.335599
                                             xL:0.399231
                                                                                 xR:3.000000
         xM:0.399231
                                                               yL:-1.382776
         xM:0.541968
                           yM:-1.382776
                                             xL:0.541968
                                                                                                    yR:23.000000
                                                                                 xR:3.000000
                           yM:-1.365035
                                                               yL:-1.365035
yL:-1.277330
5..
         xM:0.681365
                                             xL:0.681365
                                                                                 xR:3.000000
                                                                                                    yR:23.000000
                           yM:-1.277330
                                                                                                   yR:23.000000
         xM:0.811265
                                             xL:0.811265
                                                                                 xR:3.000000
         xM:0.926424
                           yM:-1.131310
                                             xL:0.926424
                                                               yL:-1.131310
                                                                                 xR:3.000000
                                                                                                    yR:23.000000
                           yM:-0.951039
8..
         xM:1.023636
                                             xL:1.023636
                                                               yL:-0.951039
                                                                                 xR:3.000000
                                                                                                    vR:23.000000
         xM:1.102113
                           yM:-0.763429
                                             xL:1.102113
                                                               yL:-0.763429
                                                                                 xR:3.000000
                                                                                                   yR:23.000000
                           yM:-0.589703
10..
         xM:1.163085
                                             xL:1.163085
                                                               yL:-0.589703
                                                                                 xR:3.000000
                                                                                                    yR:23.000000
                           yM:-0.441813
                                                               vL:-0.441813
11..
         xM:1.209004
                                             xL:1.209004
                                                                                 xR:3.000000
                                                                                                    vR:23.000000
12..
         xM:1.242760
                           yM:-0.323377
                                             xL:1.242760
                                                               yL:-0.323377
                                                                                 xR:3.000000
                                                                                                   yR:23.000000
                           yM:-0.232627
13..
         xM:1.267124
                                             xL:1.267124
                                                               yL:-0.232627
                                                                                 xR:3.000000
                                                                                                    yR:23.000000
                                                               vL:-0.165251
                                                                                 xR:3.000000
                                                                                                    vR:23.000000
14..
         xM:1.284475
                           vM:-0.165251
                                             xL:1.284475
15..
         xM:1.296713
                           yM:-0.116337
                                             xL:1.296713
                                                               yL:-0.116337
                                                                                 xR:3.000000
                                                                                                   yR:23.000000
                           yM:-0.081382
16..
         xM:1.305285
                                             xL:1.305285
                                                               yL:-0.081382
                                                                                 xR:3.000000
                                                                                                    yR:23.000000
                           vM:-0.056675
                                                               vL:-0.056675
                                                                                 xR:3.000000
                                                                                                    vR:23.000000
17..
         xM:1.311260
                                             xL:1.311260
         xM:1.315411
                           yM:-0.039346
                                             xL:1.315411
                                                               yL:-0.039346
                                                                                 xR:3.000000
                                                                                                   yR:23.000000
19..
         xM:1.318288
                           yM:-0.027257
                                             xL:1.318288
                                                               yL:-0.027257
                                                                                 xR:3.000000
                                                                                                    yR:23.000000
                                                                                 xR:3.000000
                                                                                                   vR:23.000000
20.
         xM:1.320279
                           vM:-0.018853
                                             xL:1.320279
                                                               vL:-0.018853
Regula Falsi Method used successfully
Program reached the maximum number of iteration.
Root is approximately Xi: 1.320279 and f(Xi): -0.018853 between -3.00 and 3.00
```

### 2. Örnek: x<sup>4</sup> - 1 & Epsilon: 0.05 & Max Iteration: 20 POLİNOM:



Kaynak: http://www.wolframalpha.com/widgets/view.jsp id=a7d8ae4569120b5bec12e7b6e9648b86

Newton Raphson Method used successfully.

Computed root is Xi:1.000823 and f(Xi): 0.003295

#### 2.a.Newton Raphson- $X_0 = 100$ için ÇIKTI:

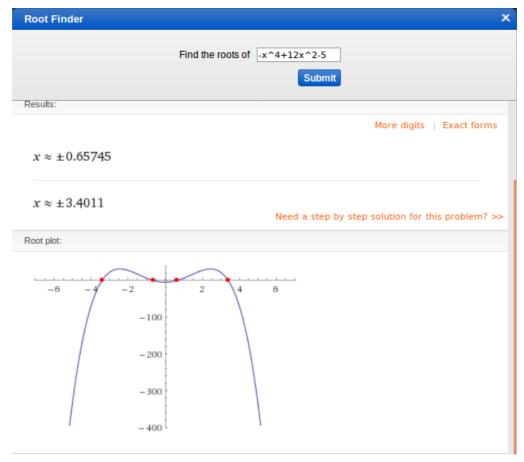
```
spaced@spaced-Lenovo-ideapad-310-15IKB:~/Desktop$ ./a.out
Enter the coefficients of quartic polynomial.
a4: 1
a3: 0
a2: 0
a1: 0
a0: -1
Your polynomial is: 1*x^4 + 0*x^3 + 0*x^2 + 0*x^1 + -1
Enter the epsilon value: 0.05
Enter the maximum iteration: 20
       Find root with Regula Falsi Method.
       Find root with Newton Raphson Method.
2.
Enter your choice (1 or 2): 2
Please enter the x0 value to estimate the root of the polynomial: 100
       xN: 100.000000 yN: 99999999.000000 xN: 75.000000 yN: 31640624.421875
1..
2..
       3..
4..
5..
       6..
7..
       xN: 17.797879
                       yN: 100338.744280
8..
       xN: 13.348454
                      yN: 31747.544091
9..
       xN: 10.011445
                      yN: 10044.859660
10..
       xN: 7.508833
                       yN: 3177.994679
       xN: 5.632215
                       yN: 1005.275727
11..
                       yN: 317.814014
12..
       xN: 4.225561
       xN: 3.172484
13..
                       yN: 100.297284
                      yN: 31.475056
14..
       xN: 2.387193
                       yN: 9.703725
15..
       xN: 1.808772
16..
       xN: 1.398825
                       yN: 2.828720
17..
                       yN: 0.691667
       xN: 1.140456
       xN: 1.023883
                       yN: 0.099008
18..
```

#### 2.b.Regula Falsi - xL = -2.385, xR = 0.385 için ÇIKTI:

```
spaced@spaced-Lenovo-ideapad-310-15IKB:~/Desktop$ ./a.out
Enter the coefficients of quartic polynomial.
a3: 0
a2: 0
a1: 0
a0: -1
Your polynomial is: 1*x^4 + 0*x^3 + 0*x^2 + 0*x^1 + -1
Enter the epsilon value: 0.05
Enter the maximum iteration: 20
        Find root with Regula Falsi Method.
1.
        Find root with Newton Raphson Method.
2.
Enter your choice (1 or 2): 1
Estimate xLeft and xRight as initial values.
    (yRight = P(xRight) and yLeft = P(xLeft) signs must be opposite)
xLeft: -2.385
xRight: 0.385
                        yM:-0.991768
                                                         yL:31.355904
                                                                                          yR:-0.991768
        xM:0.301214
                                        xL:-2.385000
                                                                        xR:0.301214
1..
2..
        xM:0.218855
                        yM:-0.997706
                                         xL:-2.385000
                                                         yL:31.355904
                                                                         xR:0.218855
                                                                                          yR:-0.997706
3..
        xM:0.138559
                        yM:-0.999631
                                         xL:-2.385000
                                                         yL:31.355904
                                                                         xR:0.138559
                                                                                          yR:-0.999631
4..
        xM:0.060593
                        yM:-0.999987
                                         xL:-2.385000
                                                         yL:31.355904
                                                                        xR:0.060593
                                                                                          yR:-0.999987
                                                                                          yR:-1.000000
        xM:-0.014990
                        yM:-1.000000
                                         xL:-2.385000
                                                         yL:31.355904
                                                                        xR:-0.014990
5..
                        yM:-0.999939
                                         xL:-2.385000
                                                                                          yR:-0.999939
        xM:-0.088238
                                                                        xR:-0.088238
6..
                                                         vL:31.355904
                                                         yL:31.355904
7..
        xM:-0.159219
                        yM:-0.999357
                                         xL:-2.385000
                                                                        xR:-0.159219
                                                                                          yR:-0.999357
8..
        xM:-0.227966
                        yM:-0.997299
                                         xL:-2.385000
                                                         yL:31.355904
                                                                         xR:-0.227966
                                                                                          yR:-0.997299
        xM:-0.294458
                        yM:-0.992482
                                         xL:-2.385000
                                                         yL:31.355904
                                                                         xR:-0.294458
                                                                                          yR:-0.992482
9..
10..
        xM:-0.358598
                        yM:-0.983464
                                         xL:-2.385000
                                                         yL:31.355904
                                                                        xR:-0.358598
                                                                                          yR:-0.983464
        xM:-0.420222
                        yM:-0.968817
                                         xL:-2.385000
                                                         vL:31.355904
                                                                        xR:-0.420222
                                                                                          yR:-0.968817
11..
                        yM:-0.947309
                                         xL:-2.385000
                                                                        xR:-0.479109
                                                                                          yR:-0.947309
        xM:-0.479109
                                                         yL:31.355904
12..
13..
        xM:-0.535000
                        vM:-0.918075
                                         xL:-2.385000
                                                         vL:31.355904
                                                                        xR:-0.535000
                                                                                          vR:-0.918075
14..
        xM:-0.587626
                        yM:-0.880765
                                         xL:-2.385000
                                                         yL:31.355904
                                                                         xR:-0.587626
                                                                                          yR:-0.880765
                                         xL:-2.385000
                                                                         xR:-0.636734
15..
        xM:-0.636734
                        yM:-0.835627
                                                         yL:31.355904
                                                                                          yR:-0.835627
16..
        xM:-0.682115
                        yM:-0.783514
                                         xL:-2.385000
                                                         yL:31.355904
                                                                        xR:-0.682115
                                                                                          yR:-0.783514
                                         xL:-2.385000
                                                         yL:31.355904
                                                                                          yR:-0.725802
        xM:-0.723629
                        vM:-0.725802
                                                                        xR:-0.723629
17..
                                                                                          yR:-0.664240
                                         xL:-2.385000
                                                         yL:31.355904
18..
        xM:-0.761215
                        vM:-0.664240
                                                                        xR:-0.761215
19..
        xM:-0.794900
                        yM:-0.600746
                                         xL:-2.385000
                                                         yL:31.355904
                                                                        xR:-0.794900
                                                                                          yR:-0.600746
20..
        xM:-0.824792
                        yM:-0.537218
                                         xL:-2.385000
                                                         yL:31.355904
                                                                         xR:-0.824792
                                                                                          yR:-0.537218
Regula Falsi Method used successfully.
Program reached the maximum number of iteration.
```

Root is approximately Xi: -0.824792 and f(Xi): -0.537218 between -2.38 and 0.39

# 3. Örnek: -x<sup>4</sup> +12x<sup>2</sup> - 5 & Epsilon: 0.5 & Max Iteration: 10 POLİNOM:



Kaynak: http://www.wolframalpha.com/widgets/view.jsp id=a7d8ae4569120b5bec12e7b6e9648b86

#### 3.a.Newton Raphson(1) - $X_0 = -2$ için ÇIKTI:

```
spaced@spaced-Lenovo-ideapad-310-15IKB:~/Desktop$ ./a.out
Enter the coefficients of quartic polynomial.
a4: -1
a3: 0
a2: 12
a1: 0
a0: -5
Your polynomial is: -1*x^4 + 0*x^3 + 12*x^2 + 0*x^1 + -5
Enter the epsilon value: 0.05
Enter the maximum iteration: 10
        Find root with Regula Falsi Method.
1.
        Find root with Newton Raphson Method.
2.
Enter your choice (1 or 2): 2
Please enter the x0 value to estimate the root of the polynomial: -2
        xN: -2.000000
1..
                        yN: 27.000000
2..
        xN: -0.312500
                        yN: -3.837662
3..
                        yN: 2.839075
       xN: -0.832654
                       yN: 0.215431
        xN: -0.672024
Newton Raphson Method used successfully.
Computed root is Xi:-0.657579 and f(Xi): 0.001946
```

```
3.b.Newton Raphson(2) - X_0 = -110 için ÇIKTI:
   spaced@spaced-Lenovo-ideapad-310-15IKB:~/Desktop$ ./a.out
   Enter the coefficients of quartic polynomial.
   a4: -1
   a3: 0
   a2: 12
   a1: 0
   a0: -5
   Your polynomial is: -1*x^4 + 0*x^3 + 12*x^2 + 0*x^1 + -5
   Enter the epsilon value: 0.05
   Enter the maximum iteration: 10
           Find root with Regula Falsi Method.
   2.
           Find root with Newton Raphson Method.
   Enter your choice (1 or 2): 2
   Please enter the x0 value to estimate the root of the polynomial: -110
           xN: -110.000000 yN: -146264805.000000
   1..
   2..
           xN: -82.513642 yN: -46273990.859423
           xN: -61.903424
   3..
                          yN: -14638504.673873
   4..
          xN: -46.451832 yN: -4630094.820155
   5..
          xN: -34.871243
                          yN: -1464077.718971
   6..
          xN: -26.196631
                           yN: -462727.429685
  7..
                           yN: -146117.424460
          xN: -19.705168
   8..
           xN: -14.856027
                           yN: -46065.747554
                           yN: -14479.478524
   9..
           xN: -11.245419
           xN: -8.573173
                           yN: -4525.154969
   Newton Raphson Method used successfully.
   Program reached the maximum number of iteration.
   Computed root is Xi:-6.618237 and f(Xi): -1397.919862
```

#### 3.c.Regula Falsi - xL = 2.65, xR = 4 için ÇIKTI:

```
spaced@spaced-Lenovo-ideapad-310-15IKB:~/Desktop$ ./a.out
Enter the coefficients of quartic polynomial.
a4: -1
a3: 0
a2: 12
a1: 0
a0: -5
Your polynomial is: -1*x^4 + 0*x^3 + 12*x^2 + 0*x^1 + -5
Enter the epsilon value: 0.05
Enter the maximum iteration: 10
1.
        Find root with Regula Falsi Method.
        Find root with Newton Raphson Method.
2.
Enter your choice (1 or 2): 1
Estimate xLeft and xRight as initial values.
    (yRight = P(xRight) and yLeft = P(xLeft) signs must be opposite)
xLeft: 2.65
xRight: 4
1..
        xM:3.058658
                        yM:19.741358
                                        xL:3.058658
                                                         yL:19.741358
                                                                        xR:4.000000
                                                                                         yR:-69.000000
2..
        xM:3.268069
                        yM:9.095049
                                        xL:3.268069
                                                         yL:9.095049
                                                                        xR:4.000000
                                                                                         yR:-69.000000
                                                                                         yR:-69.000000
3..
                        yM:3.493228
                                                         yL:3.493228
        xM:3.353310
                                        xL:3.353310
                                                                        xR:4.000000
4..
                        yM:1.246764
                                                         yL:1.246764
                                                                        xR:4.000000
                                                                                          yR:-69.000000
        xM:3.384472
                                        xL:3.384472
                        yM:0.433254
                                                         yL:0.433254
5..
        xM:3.395397
                                        xL:3.395397
                                                                        xR:4.000000
                                                                                         yR:-69.000000
6..
        xM:3.399170
                        yM:0.149157
                                        xL:3.399170
                                                         yL:0.149157
                                                                        xR:4.000000
                                                                                         yR:-69.000000
                        yM:0.051185
7..
        xM:3.400466
                                        xL:3.400466
                                                         yL:0.051185
                                                                        xR:4.000000
                                                                                         yR:-69.000000
        xM:3.400910
                                        xL:3.400910
                                                                        xR:4.000000
                                                                                         yR:-69.000000
                        vM:0.017545
                                                         vL:0.017545
Regula Falsi Method used successfully.
```

Root is approximately Xi: 3.400910 and f(Xi): 0.017545 between 2.65 and 4.00