



**EEE 391**  
**Basics of Signals and Systems**  
**2018-2019 Spring**

**Computer Assignment 2**

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## Implementation of Linearity Test:

### Matlab Code:

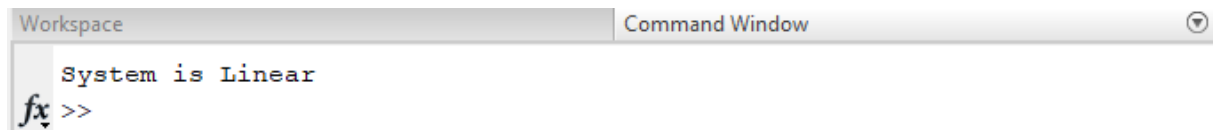
```
%-----linearity-----
x1 = [-3 -4 2 0 1 4 3 6 3 7];
x2 = [2 5 -1 7 -3 6 12 -9 8 -4];
% x1 = [9 23 15 -10 18 14 5 -1 6 11];
% x2 = [2 5 -1 7 -3 6 12 -9 8 -4];
amin=-5;
amax=5;
bmin=-5;
bmax=5;
N=10;
n=1:N;
a_val=[];%determine the a,b for wtich system is not Linear
b_val=[];
flag=1;%system is linear
for a = amin:amax;
    for b= bmin:bmax;
        y1=System2(x1,n);
        y2=System2(x2,n);
        w= a*y1+b*y2;
        xx = a*x1+b*x2;
        yy = System2(xx,n);
        if(isequal(w,yy)==0)
            flag=0;
            a_val=[a_val a];
            b_val=[b_val b];
        end
    end
end

if(length(a_val)==0) %#ok<ISMT>
    disp('System is Linear')
else
    for i =1:length(a_val)
        S= ['System is not Linear for a = ',num2str(a_val(i)),
' and b = ',num2str(b_val(i))];
        disp(S);
    end
end
```

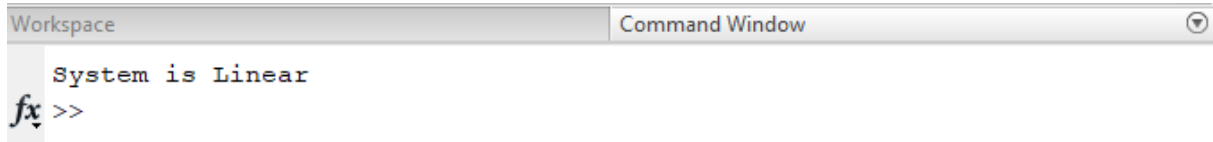
My code prints out the a and b values for which system is not linear. If the system is linear, the message ‘System is Linear’ is printed out on the Command Window.

**a) Output on the command window:**

For  $x_1 = [-3 \ -4 \ 2 \ 0 \ 1 \ 4 \ 3 \ 6 \ 3 \ 7]$ ; and  $x_2 = [2 \ 5 \ -1 \ 7 \ -3 \ 6 \ 12 \ -9 \ 8 \ -4]$ ;

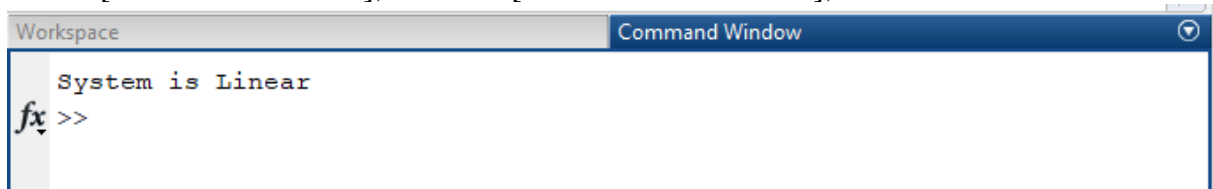
A screenshot of the MATLAB Command Window. The window has two tabs: 'Workspace' and 'Command Window'. The 'Command Window' tab is active, showing the text 'System is Linear' and a prompt 'fx >>'.

For  $x_1 = [9 \ 23 \ 15 \ -10 \ 18 \ 14 \ 5 \ -1 \ 6 \ 11]$ ; and  $x_2 = [2 \ 5 \ -1 \ 7 \ -3 \ 6 \ 12 \ -9 \ 8 \ -4]$ ;

A screenshot of the MATLAB Command Window. The window has two tabs: 'Workspace' and 'Command Window'. The 'Command Window' tab is active, showing the text 'System is Linear' and a prompt 'fx >>'.

**b) Output on the command window:**

For  $x_1 = [-3 \ -4 \ 2 \ 0 \ 1 \ 4 \ 3 \ 6 \ 3 \ 7]$ ; and  $x_2 = [2 \ 5 \ -1 \ 7 \ -3 \ 6 \ 12 \ -9 \ 8 \ -4]$ ;

A screenshot of the MATLAB Command Window. The window has two tabs: 'Workspace' and 'Command Window'. The 'Command Window' tab is active, showing the text 'System is Linear' and a prompt 'fx >>'.

For  $x_1 = [9 \ 23 \ 15 \ -10 \ 18 \ 14 \ 5 \ -1 \ 6 \ 11]$ ; and  $x_2 = [2 \ 5 \ -1 \ 7 \ -3 \ 6 \ 12 \ -9 \ 8 \ -4]$ ;

A screenshot of the MATLAB Command Window. The window has two tabs: 'Workspace' and 'Command Window'. The 'Command Window' tab is active, showing the text 'System is Linear' and a prompt 'fx >>'.

### c) Output on the command window:

For  $x1 = [-3 \ -4 \ 2 \ 0 \ 1 \ 4 \ 3 \ 6 \ 3 \ 7];$   
and  $x2 = [2 \ 5 \ -1 \ 7 \ -3 \ 6 \ 12 \ -9 \ 8 \ -4];$

```
Workspace Command Window
System is not Linear for a = 2 and b = -3
System is not Linear for a = 2 and b = -2
System is not Linear for a = 2 and b = 0
System is not Linear for a = 2 and b = 1
System is not Linear for a = 2 and b = 2
System is not Linear for a = 2 and b = 3
System is not Linear for a = 2 and b = 4
System is not Linear for a = 2 and b = 5
System is not Linear for a = 3 and b = -5
System is not Linear for a = 3 and b = -4
System is not Linear for a = 3 and b = -3
System is not Linear for a = 3 and b = -1
System is not Linear for a = 3 and b = 0
System is not Linear for a = 3 and b = 1
System is not Linear for a = 3 and b = 2
System is not Linear for a = 3 and b = 3
System is not Linear for a = 3 and b = 4
System is not Linear for a = 3 and b = 5
System is not Linear for a = 4 and b = -5
System is not Linear for a = 4 and b = -4
System is not Linear for a = 4 and b = -2
System is not Linear for a = 4 and b = -1
System is not Linear for a = 4 and b = 0
System is not Linear for a = 4 and b = 1
System is not Linear for a = 4 and b = 2
System is not Linear for a = 4 and b = 3
System is not Linear for a = 4 and b = 4
System is not Linear for a = 4 and b = 5
System is not Linear for a = 5 and b = -5
System is not Linear for a = 5 and b = -3
System is not Linear for a = 5 and b = -2
System is not Linear for a = 5 and b = -1
System is not Linear for a = 5 and b = 0
System is not Linear for a = 5 and b = 1
System is not Linear for a = 5 and b = 2
System is not Linear for a = 5 and b = 3
System is not Linear for a = 5 and b = 4
System is not Linear for a = 5 and b = 5
```

For  $x1 = [9 \ 23 \ 15 \ -10 \ 18 \ 14 \ 5 \ -1 \ 6 \ 11];$   
and  $x2 = [2 \ 5 \ -1 \ 7 \ -3 \ 6 \ 12 \ -9 \ 8 \ -4];$

System is non Linear

```
System is not Linear for a = -1 and b = 3
System is not Linear for a = -1 and b = 4
System is not Linear for a = -1 and b = 5
System is not Linear for a = 0 and b = -5
System is not Linear for a = 0 and b = -4
System is not Linear for a = 0 and b = -3
System is not Linear for a = 0 and b = -2
System is not Linear for a = 0 and b = -1
System is not Linear for a = 0 and b = 0
System is not Linear for a = 0 and b = 2
System is not Linear for a = 0 and b = 3
System is not Linear for a = 0 and b = 4
System is not Linear for a = 0 and b = 5
System is not Linear for a = 1 and b = -5
System is not Linear for a = 1 and b = -4
System is not Linear for a = 1 and b = -3
System is not Linear for a = 1 and b = -2
System is not Linear for a = 1 and b = -1
System is not Linear for a = 1 and b = 1
System is not Linear for a = 1 and b = 2
System is not Linear for a = 1 and b = 3
System is not Linear for a = 1 and b = 4
System is not Linear for a = 1 and b = 5
System is not Linear for a = 2 and b = -5
System is not Linear for a = 2 and b = -4
System is not Linear for a = 2 and b = -3
System is not Linear for a = 2 and b = -2
System is not Linear for a = 2 and b = 0
System is not Linear for a = 2 and b = 1
System is not Linear for a = 2 and b = 2
System is not Linear for a = 2 and b = 3
System is not Linear for a = 2 and b = 4
System is not Linear for a = 2 and b = 5
System is not Linear for a = 3 and b = -5
System is not Linear for a = 3 and b = -4
System is not Linear for a = 3 and b = -3
System is not Linear for a = 3 and b = -1
System is not Linear for a = 3 and b = 0
System is not Linear for a = 3 and b = 1
```

#### d) Output on the command window:

For  $x_1 = [-3 \ -4 \ 2 \ 0 \ 1 \ 4 \ 3 \ 6 \ 3 \ 7];$   
and  $x_2 = [2 \ 5 \ -1 \ 7 \ -3 \ 6 \ 12 \ -9 \ 8 \ -4];$

```
Workspace Command Window
System is not Linear for a = 2 and b = -3
System is not Linear for a = 2 and b = -2
System is not Linear for a = 2 and b = -1
System is not Linear for a = 2 and b = 1
System is not Linear for a = 2 and b = 2
System is not Linear for a = 2 and b = 3
System is not Linear for a = 2 and b = 4
System is not Linear for a = 2 and b = 5
System is not Linear for a = 3 and b = -5
System is not Linear for a = 3 and b = -4
System is not Linear for a = 3 and b = -3
System is not Linear for a = 3 and b = -2
System is not Linear for a = 3 and b = -1
System is not Linear for a = 3 and b = 1
System is not Linear for a = 3 and b = 2
System is not Linear for a = 3 and b = 3
System is not Linear for a = 3 and b = 4
System is not Linear for a = 3 and b = 5
System is not Linear for a = 4 and b = -5
System is not Linear for a = 4 and b = -4
System is not Linear for a = 4 and b = -3
System is not Linear for a = 4 and b = -2
System is not Linear for a = 4 and b = -1
System is not Linear for a = 4 and b = 1
System is not Linear for a = 4 and b = 2
System is not Linear for a = 4 and b = 3
System is not Linear for a = 4 and b = 4
System is not Linear for a = 4 and b = 5
System is not Linear for a = 5 and b = -5
System is not Linear for a = 5 and b = -4
System is not Linear for a = 5 and b = -3
System is not Linear for a = 5 and b = -2
System is not Linear for a = 5 and b = -1
System is not Linear for a = 5 and b = 1
System is not Linear for a = 5 and b = 2
System is not Linear for a = 5 and b = 3
System is not Linear for a = 5 and b = 4
System is not Linear for a = 5 and b = 5
```

For  $x_1 = [9 \ 23 \ 15 \ -10 \ 18 \ 14 \ 5 \ -1 \ 6 \ 11];$

and  $x_2 = [2 \ 5 \ -1 \ 7 \ -3 \ 6 \ 12 \ -9 \ 8 \ -4];$

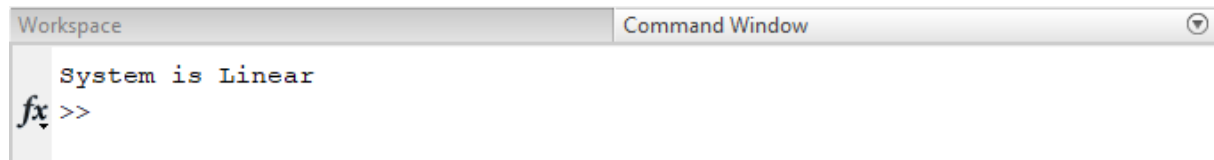
System is non Linear

```
System is not Linear for a = -2 and b = -1
System is not Linear for a = -2 and b = 0
System is not Linear for a = -2 and b = 1
System is not Linear for a = -2 and b = 2
System is not Linear for a = -2 and b = 3
System is not Linear for a = -2 and b = 4
System is not Linear for a = -2 and b = 5
System is not Linear for a = -1 and b = -5
System is not Linear for a = -1 and b = -4
System is not Linear for a = -1 and b = -3
System is not Linear for a = -1 and b = -2
System is not Linear for a = -1 and b = -1
System is not Linear for a = -1 and b = 0
System is not Linear for a = -1 and b = 1
System is not Linear for a = -1 and b = 2
System is not Linear for a = -1 and b = 3
System is not Linear for a = -1 and b = 4
System is not Linear for a = -1 and b = 5
System is not Linear for a = 0 and b = -5
System is not Linear for a = 0 and b = -4
System is not Linear for a = 0 and b = -3
System is not Linear for a = 0 and b = -2
System is not Linear for a = 0 and b = -1
System is not Linear for a = 1 and b = -5
System is not Linear for a = 1 and b = -4
System is not Linear for a = 1 and b = -3
System is not Linear for a = 1 and b = -2
System is not Linear for a = 1 and b = -1
System is not Linear for a = 1 and b = 1
System is not Linear for a = 1 and b = 2
System is not Linear for a = 1 and b = 3
System is not Linear for a = 1 and b = 4
System is not Linear for a = 1 and b = 5
System is not Linear for a = 2 and b = -5
System is not Linear for a = 2 and b = -4
System is not Linear for a = 2 and b = -3
System is not Linear for a = 2 and b = -2
System is not Linear for a = 2 and b = -1
System is not Linear for a = 2 and b = 1
```

### e) Output on the command window:

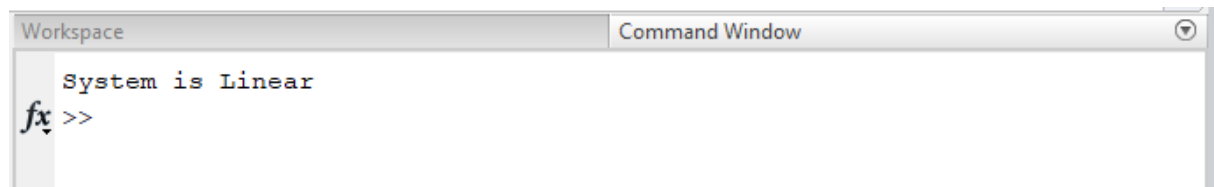
For x1 [-3 -4 2 0 1 4 3 6 3 7];

and x2 = [2 5 -1 7 -3 6 12 -9 8 -4];



For x1 = [9 23 15 -10 18 14 5 -1 6 11];

and x2 = [2 5 -1 7 -3 6 12 -9 8 -4];



System is Linear

### Implementation of Time Invariance Test:

#### Matlab Code:

```
x = [-3 -4 2 0 1 4 3 6 3 7];
% x = [5 -11 9 2 3 -6 0 -7 3 10];
N=10;
n=1:N;
n_val=[];
nmin=-50;
nmax=50;
for n0=nmin:nmax
    x0=delay(x,n0);
    w=System1(x0,n);
    y=System1(x,n);
    y0=delay(y,n0);
    if(isequal(w,y0)==0)
        n_val=[n_val n0];
    end
end
if(length(n_val)==0) %#ok<ISMT>
    disp('System is Time Invariant')
```

```

else
    for i = 1:length(n_val)
        S= ['System is not Time Invariant for n = 
',num2str(n_val(i))];
        disp(S);
    end
end

```

My code prints out the  $n_0$  values for which system is not time invariant. If the system is time invariant, the message 'System is Time Invariant' is printed out on the Command Window.

#### a) Output on the command window:

For  $x = [-3 \ -4 \ 2 \ 0 \ 1 \ 4 \ 3 \ 6 \ 3 \ 7]$ ;

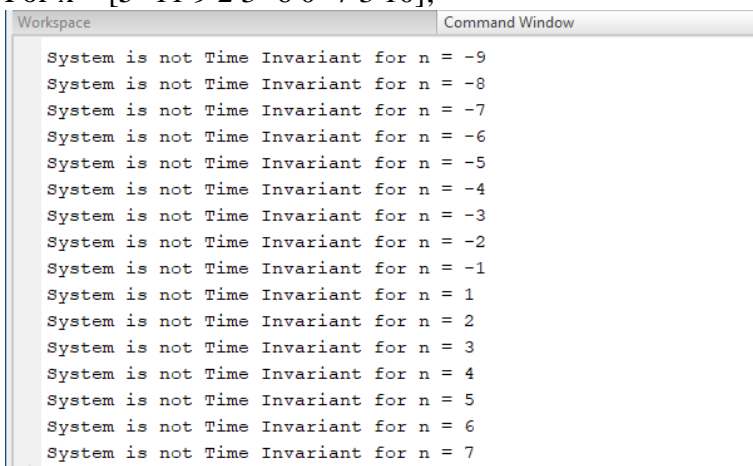


```

System is not Time Invariant for n = -9
System is not Time Invariant for n = -8
System is not Time Invariant for n = -7
System is not Time Invariant for n = -6
System is not Time Invariant for n = -5
System is not Time Invariant for n = -4
System is not Time Invariant for n = -3
System is not Time Invariant for n = -2
System is not Time Invariant for n = -1
System is not Time Invariant for n = 1
System is not Time Invariant for n = 2
System is not Time Invariant for n = 3
System is not Time Invariant for n = 4
System is not Time Invariant for n = 5
System is not Time Invariant for n = 6
System is not Time Invariant for n = 7

```

For  $x = [5 \ -11 \ 9 \ 2 \ 3 \ -6 \ 0 \ -7 \ 3 \ 10]$ ;



```

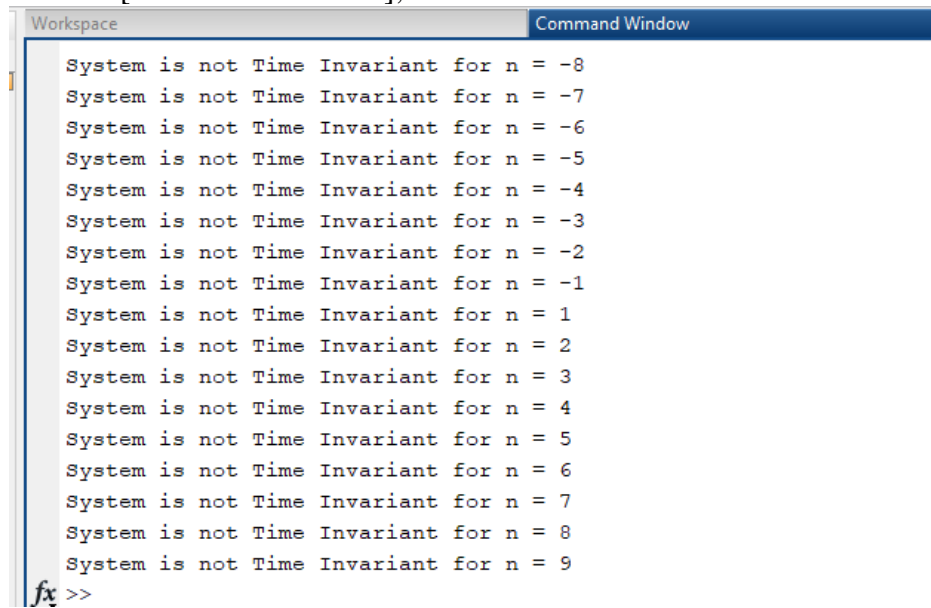
System is not Time Invariant for n = -9
System is not Time Invariant for n = -8
System is not Time Invariant for n = -7
System is not Time Invariant for n = -6
System is not Time Invariant for n = -5
System is not Time Invariant for n = -4
System is not Time Invariant for n = -3
System is not Time Invariant for n = -2
System is not Time Invariant for n = -1
System is not Time Invariant for n = 1
System is not Time Invariant for n = 2
System is not Time Invariant for n = 3
System is not Time Invariant for n = 4
System is not Time Invariant for n = 5
System is not Time Invariant for n = 6
System is not Time Invariant for n = 7

```

System is not Time invariant

**b) Output on the command window:**

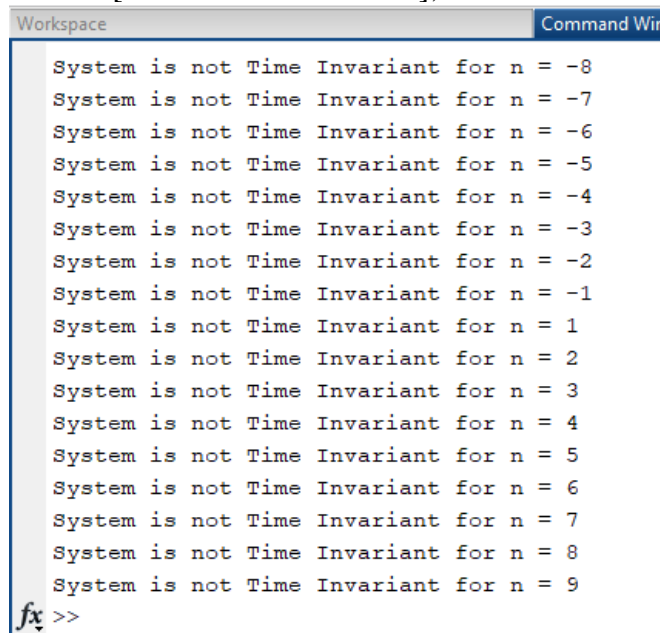
For  $x = [-3 \ -4 \ 2 \ 0 \ 1 \ 4 \ 3 \ 6 \ 3 \ 7]$ ;



A screenshot of the MATLAB Command Window. The window has a title bar with 'Workspace' and 'Command Window' tabs. The Command Window is active and displays 18 lines of text, each stating 'System is not Time Invariant for n = ' followed by a value from -8 to 9. At the bottom, the prompt 'fx >>' is visible.

```
System is not Time Invariant for n = -8
System is not Time Invariant for n = -7
System is not Time Invariant for n = -6
System is not Time Invariant for n = -5
System is not Time Invariant for n = -4
System is not Time Invariant for n = -3
System is not Time Invariant for n = -2
System is not Time Invariant for n = -1
System is not Time Invariant for n = 1
System is not Time Invariant for n = 2
System is not Time Invariant for n = 3
System is not Time Invariant for n = 4
System is not Time Invariant for n = 5
System is not Time Invariant for n = 6
System is not Time Invariant for n = 7
System is not Time Invariant for n = 8
System is not Time Invariant for n = 9
fx >>
```

For  $x = [5 \ -11 \ 9 \ 2 \ 3 \ -6 \ 0 \ -7 \ 3 \ 10]$ ;



A screenshot of the MATLAB Command Window. The window has a title bar with 'Workspace' and 'Command Window' tabs. The Command Window is active and displays 18 lines of text, each stating 'System is not Time Invariant for n = ' followed by a value from -8 to 9. At the bottom, the prompt 'fx >>' is visible.

```
System is not Time Invariant for n = -8
System is not Time Invariant for n = -7
System is not Time Invariant for n = -6
System is not Time Invariant for n = -5
System is not Time Invariant for n = -4
System is not Time Invariant for n = -3
System is not Time Invariant for n = -2
System is not Time Invariant for n = -1
System is not Time Invariant for n = 1
System is not Time Invariant for n = 2
System is not Time Invariant for n = 3
System is not Time Invariant for n = 4
System is not Time Invariant for n = 5
System is not Time Invariant for n = 6
System is not Time Invariant for n = 7
System is not Time Invariant for n = 8
System is not Time Invariant for n = 9
fx >>
```

System is not time invariant





**d) Output on the command window:**

For  $x = [-3 \ -4 \ 2 \ 0 \ 1 \ 4 \ 3 \ 6 \ 3 \ 7]$ ;

```
Workspace Command Window
System is Time Invariant
fx >>
```

For  $x = [5 \ -11 \ 9 \ 2 \ 3 \ -6 \ 0 \ -7 \ 3 \ 10]$ ;

```
Workspace Command Window
System is Time Invariant
fx >>
```

System is time invariant

**e) Output on the command window:**

For  $x = [-3 \ -4 \ 2 \ 0 \ 1 \ 4 \ 3 \ 6 \ 3 \ 7]$ ;

```
Workspace Command Window
System is not Time Invariant for n = 1
System is not Time Invariant for n = 2
System is not Time Invariant for n = 3
System is not Time Invariant for n = 4
System is not Time Invariant for n = 5
System is not Time Invariant for n = 6
System is not Time Invariant for n = 7
System is not Time Invariant for n = 8
System is not Time Invariant for n = 9
fx >>
```

For  $x = [5 \ -11 \ 9 \ 2 \ 3 \ -6 \ 0 \ -7 \ 3 \ 10]$ ;

```
Workspace Command Window
System is not Time Invariant for n = 1
System is not Time Invariant for n = 2
System is not Time Invariant for n = 3
System is not Time Invariant for n = 4
System is not Time Invariant for n = 5
System is not Time Invariant for n = 6
System is not Time Invariant for n = 7
System is not Time Invariant for n = 8
System is not Time Invariant for n = 9
fx >>
```

System is not time invariant

## Implementation of Time Invariance Test:

### Matlab Code:

```
%-----causality-----
n_val=[];
x=[2 0 -3 10 6 8 1 -5 -2 9];
n=1:N;
for i = 1:length(x)-1;
    z = x;
    z(i:end) = 0;
    w = System1(z,n);
    y = System1(x,n);
    w = w(1:i-1);
    y = y(1:i-1);
    if(isequal(w,y)==0)
        n_val=[n_val i];
    end
end

if(length(n_val)==0) %#ok<ISMT>
    disp('System is Causal')
else
    for i =1:length(n_val)
        S= ['System is not Causal for n =
',num2str(n_val(i))];
        disp(S);
    end
end

end
```

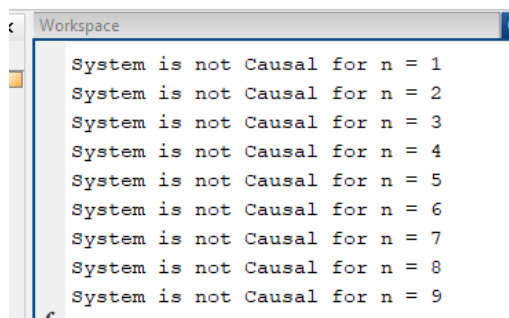
My code prints out the n values for which system is Causal. If the system is causal, the message 'System is Causal' is printed out on the Command Window.

Since we are not given any specific input, i created my own input as x=[2 0 -3 10 6 8 1 -5 -2 9];

**a) Output on the command window:**

```
System is not Causal for n = 1
System is not Causal for n = 2
System is not Causal for n = 3
System is not Causal for n = 4
System is not Causal for n = 5
System is not Causal for n = 6
System is not Causal for n = 7
System is not Causal for n = 8
System is not Causal for n = 9
```

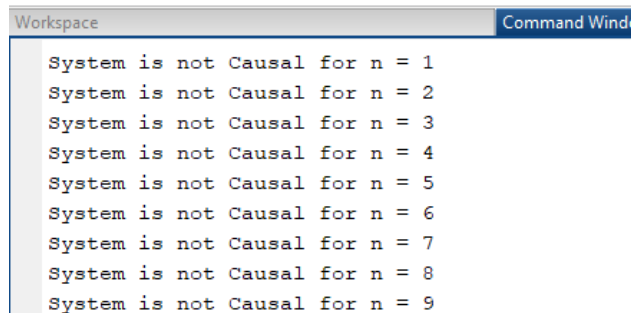
**b) Output on the command window:**



The image shows a screenshot of the MATLAB Command Window. The window has a title bar with 'Workspace' and 'Command Window'. The output text is as follows:

```
System is not Causal for n = 1
System is not Causal for n = 2
System is not Causal for n = 3
System is not Causal for n = 4
System is not Causal for n = 5
System is not Causal for n = 6
System is not Causal for n = 7
System is not Causal for n = 8
System is not Causal for n = 9
```

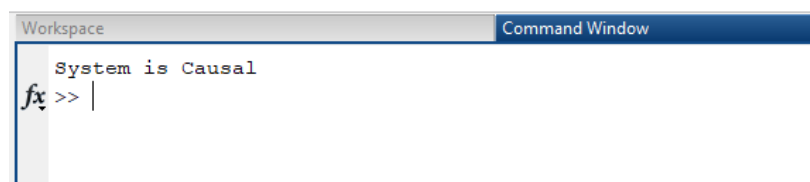
**c) Output on the command window:**



The image shows a screenshot of the MATLAB Command Window. The window has a title bar with 'Workspace' and 'Command Window'. The output text is as follows:

```
System is not Causal for n = 1
System is not Causal for n = 2
System is not Causal for n = 3
System is not Causal for n = 4
System is not Causal for n = 5
System is not Causal for n = 6
System is not Causal for n = 7
System is not Causal for n = 8
System is not Causal for n = 9
```

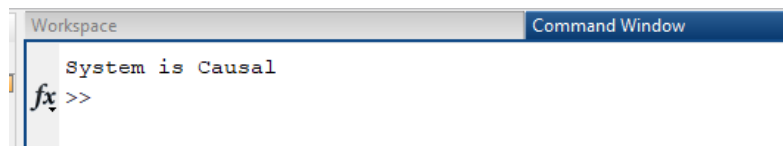
**d) Output on the command window:**



The image shows a screenshot of the MATLAB Command Window. The window has a title bar with 'Workspace' and 'Command Window'. The output text is as follows:

```
System is Causal
fx >> |
```

### e) Output on the command window:



### Full code:

```
% %-----linearity-----
x1 = [-3 -4 2 0 1 4 3 6 3 7];
x2 = [2 5 -1 7 -3 6 12 -9 8 -4];
x1 = [9 23 15 -10 18 14 5 -1 6 11];
x2 = [2 5 -1 7 -3 6 12 -9 8 -4];
amin=-5;
amax=5;
bmin=-5;
bmax=5;
N=10;
n=1:N;
a_val=[];%determine the a,b for wtich system is not Linear
b_val=[];
flag=1;%system is linear
for a = amin:amax;
    for b= bmin:bmax;
        y1=System5(x1,n);
        y2=System5(x2,n);
        w= a*y1+b*y2;
        xx = a*x1+b*x2;
        yy = System5(xx,n);
        if(isequal(w,yy)==0)
            flag=0;
            a_val=[a_val a];
            b_val=[b_val b];
        end
    end
end

if(length(a_val)==0) %#ok<ISMT>
    disp('System is Linear')
else
    for i =1:length(a_val)
        S= ['System is not Linear for a = ',num2str(a_val(i)),
' and b = ',num2str(b_val(i))];
        disp(S);
    end
end
```

```

%-----time invariance-----
x = [-3 -4 2 0 1 4 3 6 3 7];
% x = [5 -11 9 2 3 -6 0 -7 3 10];
N=10;
n=1:N;
n_val=[];
nmin=-50;
nmax=50;
for n0=nmin:nmax
    x0=delay(x,n0);
    w=System5(x0,n);
    y=System5(x,n);
    y0=delay(y,n0);
    if(isequal(w,y0)==0)
        n_val=[n_val n0];
    end
end
if(length(n_val)==0) %#ok<ISMT>
    disp('System is Time Invariant')
else
    for i =1:length(n_val)
        S= ['System is not Time Invariant for n =
',num2str(n_val(i))];
        disp(S);
    end
end

%-----causality-----
n_val=[];
x=[2 0 -3 10 6 8 1 -5 -2 9];
N=10;
n=1:N;
for i = 1:length(x)-1;
    z = x;
    z(i:end) = 0;
    w = System4(z,n);
    y = System4(x,n);
    w = w(1:i-1);
    y = y(1:i-1);
    if(isequal(w,y)==0)
        n_val=[n_val i];
    end
end
if(length(n_val)==0) %#ok<ISMT>
    disp('System is Causal')
else
    for i =1:length(n_val)
        S= ['System is not Causal for n =
',num2str(n_val(i))];

```

```

        disp(S);
    end

end

function y= System1(x,n)
% for i = 1:length(x)
%     y(i) = n*x(i);
% end
L = length(x);
for i = 1:L-2
    y(i) = n(i)*x(i+2);
end
y(L) = 0;
y(L-1) = 0;

function y= System2(x,n)
L = length(x);
c=1;
for i = 1:length(x)
    if (rem(i,2)==1)
        y(c)=x(i);
        c=c+1;
    end
end

function y= System3(x,n)
% for i = 1:length(x)
%     y(i) = n*x(i);
% end
L = length(x);
for i = 1:L-4
    y(i) = 3*x(i+4)+5;
end
y(L) = 5;
y(L-1) = 5;
y(L-2) = 5;
y(L-3) = 5;

function y= System4(x,n)
L = length(x);
for i = 1:length(x)
    if (x(i) < 0)
        y(i)=-x(i);
    else
        y(i)=x(i);
    end
end

function y= System5(x,n)
L = length(x);

```

```
for i = 1:L
    y(i) = sum(x(1:i));
end

function [ y ] = delay(x,n0)
L=length(x);
if ( n0<0)
    y = [zeros(1,(-n0)) x(1:end+n0)];
else
    y = [ x(n0+1:end) zeros(1,(n0))];
end
y = y(1:L);
```