

HW 4

Isaac Berman (berman.i)

3/15

Task 6.1

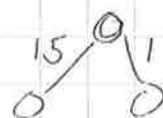
True: Kruskal's alg reduces the problem to sorting, and we can sort negative numbers

Task 6.2

True: As above, sorting negated edge weights will provide the ~~same~~ reverse ordering

Task 6.3

False: by counter example



Task 7.1

A, B, C, X, H, M

A, B, M, X, H, C

A, B, M, H, X, C

A, M, X, H, B, C

A, M, H, X, B, C

Task 8.1

Both percolate-up & percolate-down have logarithmic runtime

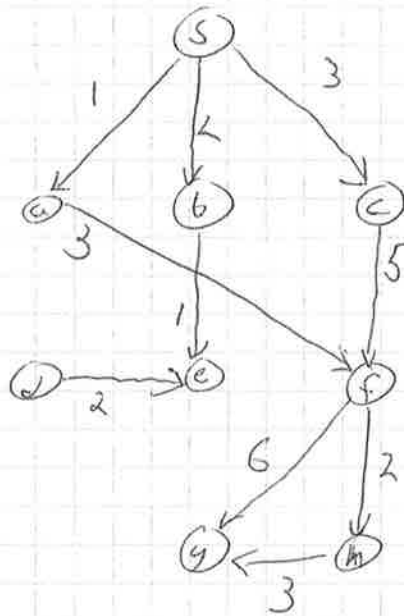
The loop on lines 6-8 runs $(n-2)$ times $\Rightarrow O(n \cdot \log n)$

The loop on lines 9-12 runs $(n-3)$ times $\Rightarrow O(n \cdot \log n)$

Note swap is $O(1) \Rightarrow O(n)$ total

The asymptotic runtime of this alg is equal to $O(\max\{n, n \log n, n \log n\}) \Rightarrow O(n \cdot \log n)$

Task 9.1



Time step	visited so far	Priority Queue
0	—	(0, s)
1	(0, s)	(1, a) (2, b) (3, c)
2	(0, s) (1, a)	(2, b) (3, c) (4, f)
3	(0, s) (1, a) (2, b)	(3, c) (3, e) (4, f)
4	(0, s) (1, a) (2, b) (3, c)	(3, e) (4, f)
5	(0, s) (1, a) (2, b) (3, c) (3, e)	(4, f)
6	(0, s) (1, a) (2, b) (3, c) (3, e) (4, f)	(6, h) (10, g)
7	(0, s) (1, a) (2, b) (3, c) (3, e) (4, f) (6, h)	(9, g)
8	(0, s) (1, a) (2, b) (3, c) (3, e) (4, f) (6, h) (9, g)	—
9	"	—
10	"	—

Note node d is not accessible from node s