# Package 'GPA rotation'

# April 23, 2007

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**Description** Gradient Projection Algorithm Rotation for Factor Analysis. See ?GPArotation.Intro for more details.

**Depends** R (>= 2.0.0)

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License GPL Version 2. See the LICENSE file for details.

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URL http://www.stat.ucla.edu/research/gpa

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```
00.GPArotation.Intro
```

GPA Rotation for Factor Analysis

# **Description**

See GPArotation-package (in the help system use package?GPArotation or ?"GPArotation-package") for an overview.

GPA

Rotation Optimization

#### **Description**

Gradient projection rotation optimization routine used by various rotation objective.

# Usage

```
GPForth(A, Tmat=diag(ncol(A)), normalize=FALSE, eps=1e-5, maxit=1000,
   method="varimax", methodArgs=NULL)
GPFoblq(A, Tmat=diag(ncol(A)), normalize=FALSE, eps=1e-5, maxit=1000,
   method="quartimin", methodArgs=NULL)
```

#### **Arguments**

A initial factor loadings matrix for which the rotation criterian is to be optimized.

Tmat initial rotation matrix.

method rotation objective criterian.

normalize see details.

eps convergence is assumed when the norm of the gradient is smaller than eps.

maxit maximum number of iterations allowed in the main loop.

methodArgs arguments passed to the rotation objective

# **Details**

Gradient projection rotation optimization routines developed by Coen A. Bernaards and Robert I. Jennrich. These functions can be used directly to rotate a loadings matrix, or indirectly through a rotation objective passed to a factor estimation routine such as factanal. For examples of the indirect use see the documention for rotations (such as oblimin).

GPForth is the main GP algorithm for orthogonal rotation. GPFoblq is the main GP algorithm for oblique rotation. Both algorithms require a loadings matrix A which fixes the equivalence class over which the optimization is done. It must be the solution to the orthogonal factor analysis problem. A rotation is defined as A %\*% t(solve(Tmat)). For the orthogonal case Tmat is orthonormal so this simplifies to A %\*% Tmat. The starting point for iterative optimization is given by the Tmat rotation of A. By default the initial rotation is the identity matrix. For some rotation criteria

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local optima may exist and it is recommended to check for this by starting with many different initial rotations. The function Random. Start will help to do this.

The argument method can be used to specify a string indicating the rotation objective. GPFoblq defaults to "quartimin" and GPForth defaults to "varimax". Available rotation objectives are "oblimin", "quartimin", "target", "pst", "oblimax", "entropy", "quartimax", "varimax", "simplimax", "bentler", "tandemI", "tandemII", "geomin", "cf", "infomax" and "mccammon". The string is prefixed with "vgQ." to give the actual function call. The vgQ.\* function call would typically not be used directly, so these methods are not exported from the package namespace. You can print these functions to see the code for calculating a criterion, but since they are not exported the package name needs to be specified. For example, use GPArotation:::vgQ.oblimin to view the function vgQ.oblimin.

Some rotation criteria (including "simplimax", "pst", "procrustes") require one or more additional arguments. For example, "simplimax" needs the number of 'close to zero loadings' which is given as the extra argument k. Check the rotation methods for details. (If a new rotation method is implemented and needs additional arguments then this is the way to pass them.)

The argument normalize gives an indication of if and how any normalization should be done before rotation, and then undone after rotation. If normalize is FALSE (the default) no normalization is done. If normalize is TRUE then Kaiser normalization is done. (So squared row entries of normalized A sum to 1.0. This is sometimes called Horst normalization.) If normalize is a vector of length equal to the number of indicators (= number of rows of A) then the colums are divided by normalize before rotation and multiplied by normalize after rotation. If normalize is a function then it should take A as an argument and return a vector which is used like the vector above.

#### Value

A GPArotation object which is a list with elements

loadings The rotated loadings, one column for each factor.

The rotation matrix, Lh %\*% t(Th) = A.

Table A matrix recording the iterations of the rotation optimization.

method A string indicating the rotation objective function.
orthogonal A logical indicating if the rotation is orthogonal.
convergence A logical indicating if convergence was obtained.

Phi t(Th) %\*% Th. The covariance matrix of the rotated factors. This will be the

identity matrix for orthogonal rotations so is omitted (NULL) for the result from

GPForth.

# Author(s)

Coen A. Bernaards and Robert I. Jennrich with some R modifications by Paul Gilbert

#### References

Additional information is available at http://www.stat.ucla.edu/research or http://www.stat.ucla.edu/research/gpa The software reference is

Bernaards, C.A. and Jennrich, R.I. (2005) Gradient Projection Algorithms and Software for Arbitrary Rotation Criteria in Factor Analysis. *Educational and Psychological Measurement*, **65**, 676–696.

Theory of gradient projection algorithms may be found in:

Jennrich, R.I. (2001). A simple general procedure for orthogonal rotation. *Psychometrika*, **66**, 289–306.

Jennrich, R.I. (2002). A simple general method for oblique rotation. *Psychometrika*, **67**, 7–19.

#### See Also

Random.Start, factanal, oblimin, quartimin, targetT, targetQ, pstT, pstQ, oblimax, entropy, quartimax, Varimax, varimax, simplimax, bentlerT, bentlerQ, tandemI, tandemII, geominT, geominQ, cfT, cfQ, infomaxT, infomaxQ, mccammon, promax

# **Examples**

GPArotation-package

GPA Rotation for Factor Analysis

# Description

GPArotation implements Gradient Projection Algorithms and several rotation objective functions for factor analysis.

# **Details**

Package: GPArotation
Depends: R (>= 2.0.0)
License: GPL Version 2.

URL: http://www.stat.ucla.edu/research or

http://www.stat.ucla.edu/research/gpa

The main optimization functions are GPForth and GPFoblq. Rotation objectives include oblimin and many others.

#### Author(s)

Coen A. Bernaards and Robert I. Jennrich with some R modifications by Paul Gilbert.

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Code is modified from original source 'splusfunctions.net' available at http://www.stat.ucla.edu/research/gpa.

Maintainer: Paul Gilbert <pgilbert@bank-banque-canada.ca>

#### References

The software reference is

Bernaards, C.A. and Jennrich, R.I. (2005) Gradient Projection Algorithms and Software for Arbitrary Rotation Criteria in Factor Analysis. *Educational and Psychological Measurement*, **65**, 676–696.

Theory of gradient projection algorithms may be found in:

Jennrich, R.I. (2001). A simple general procedure for orthogonal rotation. *Psychometrika*, **66**, 289–306.

Jennrich, R.I. (2002). A simple general method for oblique rotation. *Psychometrika*, **67**, 7–19.

#### See Also

rotations, GPForth, GPFoblq, factanal

Harman

Example Data from Harman

# Description

Harman8 is initial factor loading matrix for Harman's 8 physical variables.

#### Usage

data(Harman)

#### **Format**

The object Harman8 is a matrix.

# **Details**

The object Harman8 is loaded from the data file Harman.

#### **Source**

Harman, H. H. (1976) Modern Factor Analysis, Third Edition Revised, University of Chicago Press.

# See Also

GPForth, Thurstone, WansbeekMeijer

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NormalizingWeight Internal Utility for Normalizing Weights

# **Description**

See GPFobliq and GPForth.

# Usage

NormalizingWeight(A, normalize=FALSE)

# Arguments

A A loading matrix.

normalize An indication of if/how the matrix should be normalized.

#### Value

A matrix.

Random.Start

Generate a Random Orthogonal Rotation

# Description

Random orthogonal rotation to use as Tmat matrix to start GPForth or GPFoblq.

# Usage

Random.Start(k)

# **Arguments**

k

An integer indicating the dimension of the square matrix.

# **Details**

The random start function produces an orthogonal matrix with columns of length one based on the QR decompostion.

# Value

An orthogonal matrix.

# Author(s)

Coen A. Bernaards and Robert I. Jennrich with some R modifications by Paul Gilbert

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#### See Also

```
GPForth, GPFoblq, oblimin
```

#### **Examples**

```
Global.min <- function(A, method, B=10) {</pre>
   fv \leftarrow rep(0,B)
   seeds <- sample(1e+7, B)
   for(i in 1:B){
     cat(i," ")
     set.seed(seeds[i])
     gpout <- GPFoblq(A=A, Random.Start(ncol(A)), method=method)</pre>
     dtab <- dim(gpout$Table)</pre>
     fv[i] <- gpout$Table[dtab[1],2]</pre>
     cat(fv[i], "\n")
   }
   cat("Min is ",min(fv),"\n")
   set.seed(seeds[order(fv)[1]])
   ans <- GPFoblq(A=A, Random.Start(ncol(A)), method=method)</pre>
   ans
   }
data("Thurstone", package="GPArotation")
Global.min(box26, "simplimax", 10)
```

Thurstone

Example Data from Thurstone

# Description

box20 and box26 are initial factor loading matrices.

#### Usage

```
data(Thurstone)
```

# **Format**

The objects box20 and box26 are matrices.

# **Details**

The objects box20 and box26 are loaded from the data file Thurstone.

#### **Source**

Thurstone, L.L. (1947). Multiple Factor Analysis. Chicago: University of Chicago Press.

# See Also

```
GPForth, Harman, WansbeekMeijer
```

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WansbeekMeijer

Factor Example from Wansbeek and Meijer

# Description

Netherlands TV viewership example p 171, Wansbeek and Meijer (2000)

# Usage

```
data(WansbeekMeijer)
```

#### **Format**

The object NetherlandsTV is a correlation matrix.

#### **Details**

The object NetherlandsTV is loaded from the data file WansbeekMeijer.

#### **Source**

Tom Wansbeek and Erik Meijer (2000) *Measurement Error and Latent Variables in Econometrics*, Amsterdam: North-Holland.

# See Also

```
GPForth, Thurstone, Harman
```

eiv

Errors-in-Variables Rotation

# **Description**

Rotate to errors-in-variables representation.

# Usage

```
eiv(L, identity=seq(ncol(L)), ...)
```

# Arguments

```
L a factor loading matrix
```

identity indicates rows which should be identity matrix.

... additional arguments discarded.

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#### **Details**

This function rotates to an errors-in-variables representation. The optimization is not iterative and does not use the GPA algorithm. The function can be used directly or the function name can be passed to factor analysis functions like factanal.

The loadings matrix is rotated so the k rows indicated by identity form an identity matrix, and the remaining M-k rows are free parameters.  $\Phi$  is also free. The default makes the first k rows the identity. If inverting the matrix of the rows indicated by identity fails, the rotation will fail and the user needs to supply a different choice of rows.

Not all authors consider this representation to be a rotation. Viewed as a rotation method, it is oblique, with an explicit solution: given an initial loadings matrix L partitioned as  $L=(L_1^T,L_2^T)^T$ , then (for the default identity) the new loadings matrix is  $(I,(L_2L_1^{-1})^T)^T$  and  $\Phi=L_1L_1^T$ , where I is the k by k identity matrix. It is assumed that  $\Phi=I$  for the initial loadings matrix.

One use of this parameterization is for obtaining good starting values (so it looks a little strange to rotate towards this solution afterwards). It has a few other purposes: (1) It can be useful for comparison with published results in this parameterization; (2) The S.E.s are more straightfoward to compute, because it is the solution to an unconstrained optimization (though not necessarily computed as such); (3) One may have an idea about which reference variables load on only one factor, but not impose restrictive constraints on the other loadings, so, in a nonrestrictive way, it has similarities to CFA; (4) For some purposes, only the subspace spanned by the factors is important, not the specific parameterization within this subspace; (5) The back-predicted indicators (explained portion of the indicators) do not depend on the rotation method. Combined with the greater ease to obtain correct standard errors of this method, this allows easier and more accurate prediction-standard errors.

#### Value

A list (which includes elements used by factanal) with:

loadings The new loadings matrix.

Th The rotation.

method A string indicating the rotation objective function ("eiv").
orthogonal For consistency with other rotation results. Always FALSE.
convergence For consistency with other rotation results. Always TRUE.

Phi The covariance matrix of the rotated factors.

#### Author(s)

Erik Meijer and Paul Gilbert.

# References

Gösta Hägglund. (1982). "Factor Analysis by Instrumental Variables Methods." *Psychometrika*, 47, 209–222.

Sock-Cheng Lewin-Koh and Yasuo Amemiya. (2003). "Heteroscedastic factor analysis." *Biometrika*, 90, 85–97.

Tom Wansbeek and Erik Meijer (2000) *Measurement Error and Latent Variables in Econometrics*, Amsterdam: North-Holland.

#### See Also

rotations, GPForth, GPFoblq

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#### **Examples**

```
data("WansbeekMeijer", package="GPArotation")
fa.unrotated <- factanal(factors = 2, covmat=NetherlandsTV, rotation="none")
fa.eiv <- eiv(fa.unrotated$loadings)
fa.eiv2 <- factanal(factors = 2, covmat=NetherlandsTV, rotation="eiv")
cbind(loadings(fa.unrotated), loadings(fa.eiv), loadings(fa.eiv2))
fa.eiv3 <- eiv(fa.unrotated$loadings, identity=6:7)
cbind(loadings(fa.unrotated), loadings(fa.eiv), loadings(fa.eiv3))</pre>
```

print.GPArotation Print and Summary Methods for GPArotation

#### **Description**

Print an object or summary of an object returned by GPForth or GPFoblq.

# Usage

```
## S3 method for class 'GPArotation':
print(x, digits=3, Table=FALSE, ...)
## S3 method for class 'GPArotation':
summary(object, ...)
## S3 method for class 'summary.GPArotation':
print(x, digits=3, ...)
```

# **Arguments**

```
    a GPArotation object to summarize.
    a summary.GPArotation to print.
    digits precision of printed numbers.
    further arguments passed to other methods.
```

#### Value

The object printed or a summary object.

# See Also

```
GPForth, summary
```

rotations

Rotations

#### **Description**

Optimize factor loading rotation objective.

#### Usage

```
oblimin(L, Tmat=diag(ncol(L)), gam=0, normalize=FALSE, eps=1e-5, maxit=1000)
quartimin(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
targetT(L, Tmat=diag(ncol(L)), Target=NULL, normalize=FALSE, eps=1e-5, maxit
targetQ(L, Tmat=diag(ncol(L)), Target=NULL, normalize=FALSE, eps=1e-5, maxit
pstT(L, Tmat=diag(ncol(L)), W, Target=NULL, normalize=FALSE, eps=1e-5, maxit
pstQ(L, Tmat=diag(ncol(L)), W, Target=NULL, normalize=FALSE, eps=1e-5, maxit
oblimax(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
entropy(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
quartimax(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
Varimax(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
simplimax(L, Tmat=diag(ncol(L)), k=nrow(L), normalize=FALSE, eps=1e-5, maxit
bentlerT(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
bentlerQ(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
tandemI(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
tandemII(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
geominT(L, Tmat=diag(ncol(L)), delta=.01, normalize=FALSE, eps=1e-5, maxit=1
geominQ(L, Tmat=diag(ncol(L)), delta=.01, normalize=FALSE, eps=1e-5, maxit=1
cfT(L, Tmat=diag(ncol(L)), kappa=0, normalize=FALSE, eps=1e-5, maxit=1000)
cfQ(L, Tmat=diag(ncol(L)), kappa=0, normalize=FALSE, eps=1e-5, maxit=1000)
infomaxT(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
infomaxQ(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
mccammon(L, Tmat=diag(ncol(L)), normalize=FALSE, eps=1e-5, maxit=1000)
vqQ.oblimin(L, qam=0)
vgQ.quartimin(L)
vgQ.target(L, Target=NULL)
vgQ.pst(L, W, Target=NULL)
vgQ.oblimax(L)
vgQ.entropy(L)
vgQ.quartimax(L)
vqQ.varimax(L)
vgQ.simplimax(L, k=nrow(L))
vgQ.bentler(L)
vqQ.tandemI(L)
vqQ.tandemII(L)
vgQ.geomin(L, delta=.01)
vgQ.cf(L, kappa=0)
vgQ.infomax(L)
vgQ.mccammon(L)
```

#### **Arguments**

L a factor loading matrix

Tmat initial rotation matrix.

gam 0=Quartimin, .5=Biquartimin, 1=Covarimin.

Target rotation target for objective calculation.

W weighting of each element in target.

k number of close to zero loadings.

delta constant added to L2 in objective calculation.

kappa see details.

normalize parameter passed to optimization routine (GPForth or GPFoblq).

eps parameter passed to optimization routine (GPForth or GPFoblq).

maxit parameter passed to optimization routine (GPForth or GPFoblq).

#### **Details**

These functions optimize a rotation objective. They can be used directly or the function name can be passed to factor analysis functions like factanal. Several of the function names end in T or Q, which indicates if they are orthogonal or oblique rotations (using GPForth or GPFoblq respectively.

The vgQ.\* versions of the code are called by the optimization routine and would typically not be used directly, so these methods are not exported from the package namespace. (They simply return the function value and gradient for a given rotation matrix.) You can print these functions, but the package name needs to be specified since they are not exported. For example, use GPArotation::vgQ.oblimin to view the function vgQ.oblimin. The T or Q ending on function names should be omitted for the vgQ.\* versions of the code so, for example, use GPArotation::vgQ.target to view the target criterion calculation.

Rotations which are available are

oblimin quartimin	oblique oblique	oblimin family
targetT	orthogonal	target rotation
•	•	•
targetQ	oblique	target rotation
pstT	orthogonal	partially specified target rotation
pstQ	oblique	partially specified target rotation
oblimax	oblique	
entropy	orthogonal	minimum entropy
quartimax	orthogonal	
varimax	orthogonal	
simplimax	oblique	
bentlerT	orthogonal	Bentler's invariant pattern simplicity criterion
bentlerQ	oblique	Bentler's invariant pattern simplicity criterion
tandemI	orthogonal	Tandem Criterion
tandemII	orthogonal	Tandem Criterion
geominT	orthogonal	
geominQ	oblique	
cfT	orthogonal	Crawford-Ferguson family
cfQ	oblique	Crawford-Ferguson family
infomaxT	orthogonal	
infomaxQ	oblique	
mccammon	orthogonal	McCammon minimum entropy ratio

Note that Varimax defined here uses vgQ.varimax and is not varimax defined in the stats package. stats:::varimax does Kaiser normalization by default whereas Varimax defined here does not.

The argument kappa parameterizes the family for the Crawford-Ferguson method. If m is the number of factors and p is the number of indicators then kappa values having special names are 0=Quartimax, 1/p=Varimax, m/(2\*p)=Equamax, m-1/(p+m-2)=Parsimax, m-1/(p+m-2

New rotation methods can be programmed with a name "vgQ.newmethod". The inputs are the matrix L, and optionally any additional arguments. The output should be a list with elements

f the value of the criterion at L.

Gq the gradient at L.

Method a string indicating the criterion.

#### Value

A list (which includes elements used by factanal) with:

Lh from GPForth or GPFoblq.
Th Th from GPForth or GPFoblq.
Table Table from GPForth or GPFoblq.

method A string indicating the rotation objective function.

orthogonal A logical indicating if the rotation is orthogonal.

convergence Convergence indicator from GPForth or GPFoblq.

Phi t(Th) %\*% Th. The covariance matrix of the rotated factors. This will be the

identity matrix for orthogonal rotations so is omitted (NULL) for the result from

GPForth.

#### Author(s)

Coen A. Bernaards and Robert I. Jennrich with some R modifications by Paul Gilbert.

# References

Bernaards, C.A. and Jennrich, R.I. (2005) Gradient Projection Algorithms and Software for Arbitrary Rotation Criteria in Factor Analysis. *Educational and Psychological Measurement*, **65**, 676–696.

A discussion of rotation objectives can be found in many references, for example,

Tom Wansbeek and Erik Meijer (2000) Measurement Error and Latent Variables in Econometrics, Amsterdam: North-Holland.

#### See Also

```
GPForth, GPFoblq, WansbeekMeijer, eiv, factanal, varimax, promax
```

#### **Examples**

```
data(ability.cov)
factanal(factors = 2, covmat = ability.cov, rotation="oblimin")
data("Harman", package="GPArotation")
qHarman <- GPForth(Harman8, Tmat=diag(2), method="quartimax")</pre>
```

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