# 18-819F: Introduction to Quantum Computing 47-779/47-785: Quantum Integer Programming & Quantum Machine Learning

**Course Overview** 

Lecture 00

2022.08.29.







### **Agenda**

- Lecturers
- Objectives
- Expectations
- Pre-requisites
- Tentative Course Outline Mini I & II
  - Teasers of new content to be learned
- Grading Policy
  - Project choices and examples







### Lecturers

- Prof. Sridhar Tayur
  - Ford Distinguished Research Chair; University Professor of Operations Management; Tepper School of Business CMU
  - Academic Capitalist
- Prof. Elias Towe
  - Professor of Electrical and Computer Engineering
- Dr. Davide Venturelli
  - Associate Director for Quantum Computing of the Research Institute of Advanced Computer Science (RIACS) at the USRA.
  - Senior Scientist NASA Quantum AI Laboratory (QuAIL)
- Dr. David E. Bernal
  - Associate Scientist in Quantum Computing at USRA-RIACS and NASA QuAIL
  - 2019 awardee of USRA Feynman Quantum Academy Program at NASA Ames Research Center
- TA/Graders: Pruthviraj Gampalwar and Jiaqi Guo















### **Objectives**

This course covers recent developments in **Quantum Computing** for the solution of **combinatorial optimization problems** and **machine learning (ML)**. We will cover mathematical programming and machine learning, their non-quantum (classical) solution methods and concepts that **take advantage** of **near-term quantum** and **quantum-inspired computing**. The **annealing** and **circuit model of quantum computing** that are currently implemented in various hardware architectures will be discussed.

We will explore how these machines can potentially be used for **hardware-tailored ML** algorithms to **solve problems that classical computers struggle with**.

The course contains a series of lectures and practical exercises using quantum resources such as quantum annealing and gate-based computers to gain exposure to these novel computational models, all through the **cloud-based Quantum Computing** access platform Amazon Braket.

The course main deliverable is a **final group project** that allows the students to familiarize themselves with a problem of their interest and apply classical and unconventional computing tools towards addressing these applications.

**Universities Space Research Association** 

### **Expectations**

- This course is not going to focus on the following topics:
  - Computational complexity theory
    - 15-651 Algorithm Design and Analysis in CS
  - Quantum Information Theory
    - 33-658 Quantum computation and Info theory in Physics
  - Analysis of speedup using differential geometry, algebraic topology, etc.
    - 21-752 Algebraic Topology or 21-759 Differential Geometry in Mathematics







### **Pre-requisites**

- No explicit pre-requisites are listed but we recommend:
  - An undergraduate-level understanding of probability, calculus, statistics, graph theory, algorithms, and linear algebra is assumed.
  - Knowledge of linear and integer programming will be useful.
  - Programming skills are strongly recommended (Python preferred)
  - Basic concepts in physics are recommended but lack of prior knowledge is not an issue as pertinent ones will be covered in the lectures.
  - No particular knowledge in quantum mechanics or algebraic geometry is required.







### **Tentative Course Outline First Half / Mini 1**

- Introduction to Linear Algebra for Quantum Mechanics and Machine Learning:
  - Complex numbers, vectors and vector spaces, functions as vectors, inner product, norms, projections, Hilbert spaces, basis vectors, matrices, Hermitian operators, and special matrices
- Basic classical machine learning:
  - Support vector machine model; Deep learning neural networks; Running classical machine learning algorithms on computing systems with accelerators; Challenges of running machine learning algorithms on current state-of-the-art classical computing hardware
- Introduction to Mathematical Programming methods:
  - Linear Programming; Integer Programming; Nonlinear Programming; Mixed-Integer Nonlinear Programming; Introduction to computational complexity.
- Ising, Quadratic Unconstrained Binary Optimization (QUBO)
  - Ising model basics; Simulated Annealing, Markov-chain Monte Carlo methods, benchmarking classical methods, Formulating combinatorial problems as QUBOs.
- Introduction to Test Sets
  - Groebner basis; Graver basis; GAMA: Graver Augmented Multiseed algorithm; Applications: Portfolio Optimization, Cancer Genomics
- Quantum methods for solving Ising/QUBO in the NISQ Era
  - Adiabatic Quantum Computing, Quantum Annealing and D-Wave; QAOA: Quantum Alternating (Approximate) Optimization Ansatz (Algorithm); Exercises on Amazon Braket







### **Tentative Course Outline First Half / Mini 1**

- Axioms of Quantum Mechanics
  - Postulates of quantum mechanics, review of classical bits (cbits), the single quantum state and the quantum bit (qubit); Quantum measurement, quantum operations; Multiple quantum states, observables
- Qubit Gate model of quantum computing
  - Reversible operations on qubits, logic gates and quantum circuits; Qubits for information processing; general quantum computation process; Example of the power of quantum computing, Deutsch's problem
- Quantum methods for solving Ising/QUBO in the NISQ Era
  - Adiabatic Quantum Computing, Quantum Annealing and D-Wave; QAOA: Quantum Alternating (Approximate) Optimization Ansatz (Algorithm); Exercises on Amazon Braket







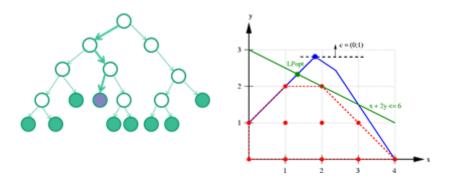
## Mathematical Programming – Discrete Optimization

Current status and perspectives

Classical methods

Methods based on divide-and-conquer

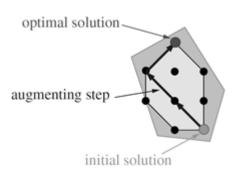
- Branch-and-Bound algorithms
- Harness advances in polyhedral theory
- With global optimality guarantees
- Very efficient codes available
- Exponential complexity



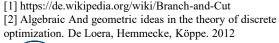
Not very popular classical methods

Methods based on test-sets

- Algorithms based on "augmentation"
- Use tools from algebraic geometry
- Global convergence guarantees
- Very few implementations out there
- Polynomial oracle complexity once we have test-set



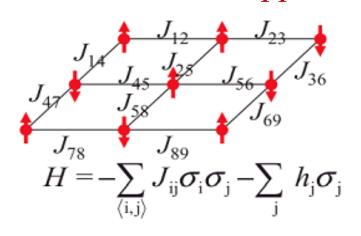


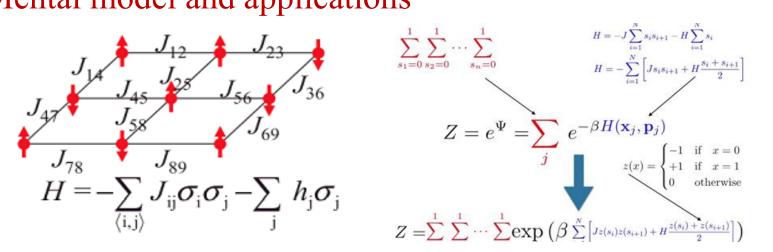


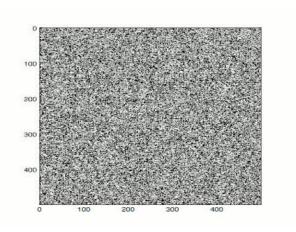


### Ising Model, QUBO

### Mental model and applications







$$\min c\mathbf{x}$$

$$A\mathbf{x} = b$$

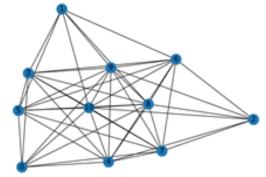
$$\mathbf{x} \in \{0,1\}^n$$



$$\min_{\mathbf{x}} c\mathbf{x} + \rho (A\mathbf{x} - b)^T (A\mathbf{x} - b) = \min_{\mathbf{x}} \mathbf{x}^T Q\mathbf{x} + c$$

$$\mathbf{x} \in \{0,1\}^n$$





[1] https://en.wikipedia.org/wiki/Ising model



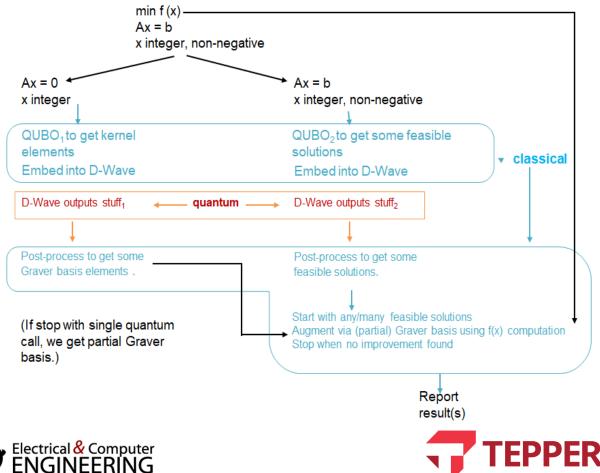




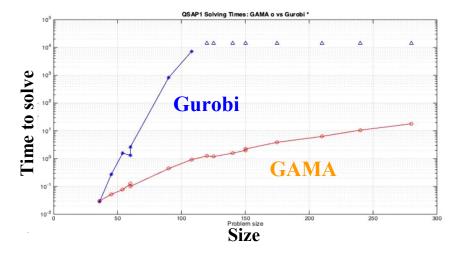
### Carnegie Mellon University

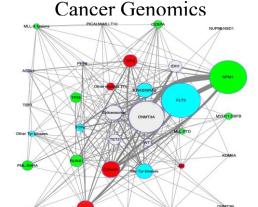
### **Graver Augmented, Multiseed Algorithm GAMA**

Mental model and applications



#### Cardinality Constrained Quadratic Optim





- [1] https://arxiv.org/pdf/1902.04215.pdf
- [2] https://arxiv.org/pdf/1907.10930.pdf
- [3]https://www.biorxiv.org/content/10.1101/845719v1.full.pdf





### **Unconventional Computing**

### Three Strategies, Multiple Technologies

#### FAULT-TOLERANT QUANTUM:

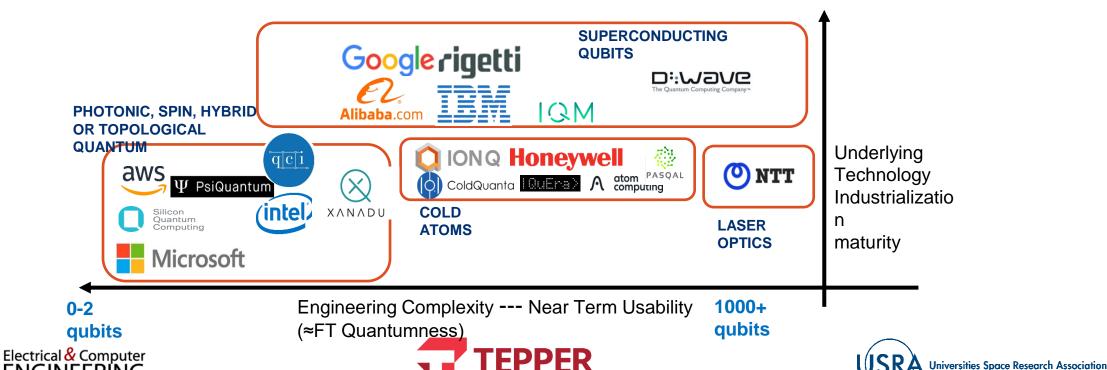
- Phase Estimation
- Amplitude Amplification/Estim.
- Sampling

#### GATE-MODEL NISQ:

- Quantum Approximate Optimization
- Quantum Alternate Operator Ansatz
- Variational Quantum Eigensover
- Quantum Neural Networks

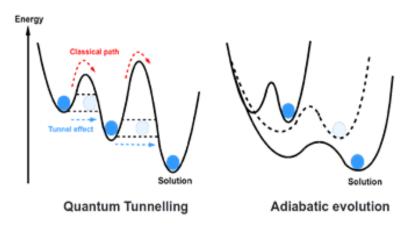
#### ANALOG:

- Quantum Annealing
- Coherent (Optical) Ising Machines
- Oscillator-based Computing
- Quantum-Inspired Digital Annealers



### Quantum methods for solving Ising/QUBO

### Adiabatic Quantum Computation



Gate-based computers and Quantum Annealers

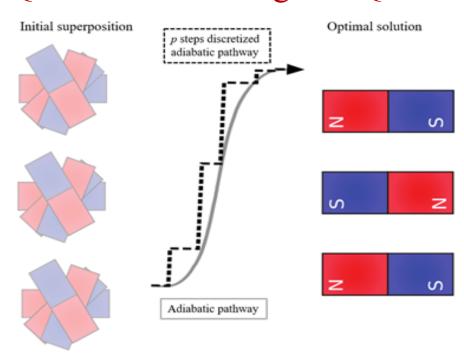








### Quantum Annealing and QAOA



- [1]https://miro.medium.com/max/2420/1\*n0wMIZVftp8cVLW8Mn6\_Ew.png
- [2]https://www.ibm.com/blogs/research/2017/11/the-future-is-quantum/
- [3]https://www.dwavesys.com/press-releases/d-wave-makes-new-lower-noise-quantum-processor-available-leap

### **Tentative Course Outline Second Half / Mini 2**

- Quantum Algorithms for future quantum processors
  - HHL Algorithms for solving a system of linear equations (Ax = b); Factorizing large numbers; period finding; quantum Fourier Transform; Quantum shell game; Grover's search algorithm
- Physics-Inspired Hardware for solving Ising/QUBO
  - Graphical Processing Units; Tensor Processing Units; Complementary metal-oxide-semiconductors (CMOS); Digital Annealers; Oscillator Based Computing; Coherent Ising Machines
- Benchmarking and assessing performance of these methods
  - Parameterized stochastic solvers, Assessing performance of physics-Inspired Hardware for solving Ising/QUBO; Adiabatic Quantum Computing, Quantum Annealing, and D-Wave; Digital Annealers; Oscillator Based Computing; Coherent Ising Machines

#### Guest lectures

- Noise in quantum computing and quantum error correction
  - Review of classical error correction methods; quantum error correction
- Neutral Atoms for implementation of physical qubits
- And more!







### **Recent Results: QA**

### Recent applied, advanced use (paused annealing, reverse annealing):

Ferromagnetically shifting the power of pausing

Zoe Gonzalez Izquierdo, 1, 2, 3 Shon Grabbe, 2 Stuart Hadfield, 2, 3 Jeffrey Marshall, 2, 3 Zhihui Wang, 2, 3 and Eleanor Rieffel

Department of Physics and Astronomy, and Center for Quantum Information Science & Technology, University of Southern California, Los Angeles, California 90089, USA

<sup>2</sup> QuAIL, NASA Ames Research Center, Moffett Field, California 94035, USA

<sup>3</sup> USRA Research Institute for Advanced Computer Science, Mountain View, California 94043, USA

(Dated: June 16, 2020)

#### Leveraging Quantum Annealing for Large MIMO Processing in Centralized Radio Access Networks

Minsung Kim Princeton University minsungk@cs.princeton.edu Davide Venturelli USRA Research Institute for Advanced Computer Science DVenturelli@usra.edu Kyle Jamieson Princeton Univeristy kylej@cs.princeton.edu

NOTE: ≈30 papers on applied use of quantum annealers in 2021 as of August (61 papers in 2020)

#### Quantumness:

#### REPOR

Phase transitions in a programmable quantum spin glass simulator

O R. Harris <sup>1,\*</sup>, Y. Sato <sup>1</sup>, O A. J. Berkley <sup>1</sup>, M. Reis <sup>1</sup>, F. Altomare <sup>1</sup>, M. H. Amin <sup>1,2</sup>, O K. Boothby <sup>1</sup>, P. Bunyk <sup>1</sup>, C. Deng <sup>1</sup>, O ...

+ See all authors and affiliations

Science 13 Jul 2018: Vol. 361, Issue 6398, pp. 162-165 DOI: 10.1126/science.aat2025

Letter | Published: 22 August 2018

### Observation of topological phenomena in a programmable lattice of 1,800 qubits

Andrew D. King <sup>™</sup>, Juan Carrasquilla, [...] Mohammad H. Amin

Nature **560**, 456–460(2018) | Cite this article

### Benchmarking:

#### REPORT

#### Defining and detecting quantum speedup

Troels F. Rønnow<sup>1</sup>, Zhihui Wang<sup>2,3</sup>, Joshua Job<sup>3,4</sup>, Sergio Boixo<sup>5,6</sup>, Sergei V. Isakov<sup>7</sup>, David Wecker<sup>8</sup>, John M. Martinis<sup>9</sup>, Dan...

+ See all authors and affiliations

Science 25 Jul 2014: Vol. 345, Issue 6195, pp. 420-424 DOI: 10.1126/science.1252319

#### What is the Computational Value of Finite-Range Tunneling?

Vasil S. Denchev, Sergio Boixo, Sergei V. Isakov, Nan Ding, Ryan Babbush, Vadim Smelyanskiy, John Martinis, and Hartmut Neven

Phys. Rev. X 6, 031015 – Published 1 August 2016







### Carnegie Mellon University

### **Recent Results: QAOA**

#### Optimizing Variational Quantum Algorithms Using Pontryagin's Minimum Principle

Zhi-Cheng Yang, Armin Rahmani, Alireza Shabani, Hartmut Neven, and Claudio Chamon

#### Low depth mechanisms for quantum optimization

Jarrod R. McClean, <sup>1</sup>, Matthew P. Harrigan, <sup>1</sup> Masoud Mohseni, <sup>1</sup> Nicholas C. Rubin, <sup>1</sup> Zhang Jiang, <sup>1</sup> Sergio Boixo, <sup>1</sup> Vadim N. Smelyanskiy, <sup>1</sup> Ryan Babbush, <sup>1</sup> and Hartmut Neven <sup>1</sup> Google Research, 340 Main Street, Venice, CA 90291, USA (Dated: August 21, 2020)

Behavior of Analog Quantum Algorithms

Lucas T. Brady, <sup>1, 2, \*</sup> Lucas Kocia, <sup>3</sup> Przemyslaw Bienias, <sup>1, 2</sup>
Aniruddha Bapat, <sup>1, 2</sup> Yaroslav Kharkov, <sup>1, 2</sup> and Alexey V. Gorshkov <sup>1, 2</sup>

<sup>1</sup> Joint Center for Quantum Information and Computer Science, NIST/University of Maryland, College Park, Maryland 20742, USA <sup>2</sup> Joint Quantum Institute, NIST/University of Maryland, College Park, Maryland 20742, USA <sup>3</sup> Sandia National Laboratories, Livermore, California 94550, USA (Dated: July 6, 2021)

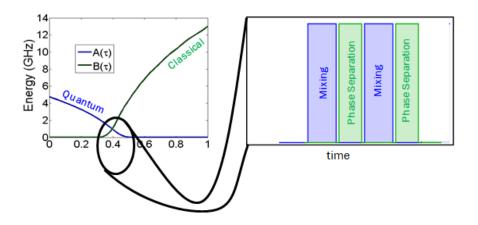
**NOTE:** ≈35 papers on quantum optimization algorithms in 2021 as of August (77 in 2020)

#### Quantum Approximate Optimization of Non-Planar Graph Problems on a Planar Superconducting Processor

Google AI Quantum and Collaborators\*
(Dated: April 10, 2020)

Reference	Date	Problem topology	$\Delta(G)$	n	p	Optimization
Otterbach et al. [22]	2017-12	Hardware	3	19	1	Yes
Qiang et al. [27]	2018-08	Hardware	1	2	1	No
Pagano et al. [26]	2019-06	Hardware <sup>1</sup> (system 1)	n	12, 20	1	Yes
	TOTAL CONTROL	Hardware <sup>1</sup> (system 2)	n	20-40	$1-2^{(2)}$	No
Willsch et al. [23]	2019-07	Hardware	3	8	1	No
Abrams et al. [24]	2019-12	Ring	2	4	1	No
		Fully-connected	n			No
Bengtsson et al. [25]	2019-12	Hardware	1	2	1, 2	Yes
This work		Hardware	4	2-23	1-5	Yes
		3-regular	3	4-22	1-3	Yes
		Fully-connected	n	3-17	1-3	Yes

### Relationship between QA and QAOA:



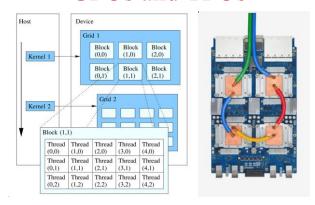






### Specialized hardware for solving Ising/QUBO

#### GPUs and TPUs

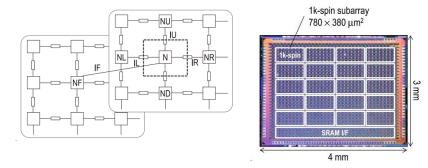


#### Digital annealers

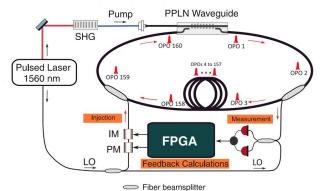




### Complementary metal-oxide semiconductors (CMOS)



#### Coherent Ising Machines (CIM)



[1]https://arxiv.org/pdf/1807.10750.pdf

[2]https://arxiv.org/pdf/1903.11714.pdf

[3]https://arxiv.org/pdf/1806.08815.pdf





### **Grading Policy**

- The final project accounts for 70% of the grade and weekly short quizzes account for 30% of the grade
- Bi-weekly homework or quizzes (30%)
  - Each week will have a short quiz to evaluate concepts covered in previous lectures
  - Worst quizzes won't be counted
- Final Project (70%)
  - Group project (2-4 people).
  - Formulate a relevant practical problem as an IP or ML in multiple ways (formulations)
  - Generate a family of instances of the problem to test solution methods
  - Review current state-of-the-art classical solution methods. Replicate it if possible.
  - Identify opportunities for unconventional computing solution methods
  - Map the problem into a formalism fit for physics-based or -inspired methods
  - Perform resource estimation and solve a proof-of-concept instance(s) on a real device or simulator
- Deliverables:
  - Ungraded project proposal at the 3<sup>rd</sup> week to evaluate validity of idea (or for us to provide a problem)
  - Provide a mid-term report with initial results and plan (15 points /70) with a short presentation (10/70)
  - Code to implement project
  - Write a report outlining strengths-limitations-functional requirements-opportunities of the different approaches used,
     highlighting the knowledge obtained while developing the project supported by computational results (25/70)
  - Make a presentation to the class reporting the findings of the project (20/70)

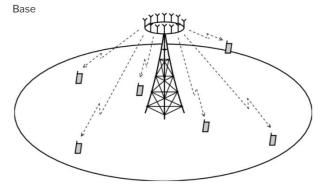






### **Project proposal ideas**

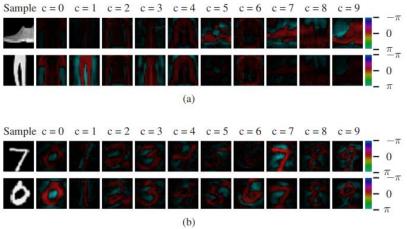
Multi-Input Multi-Output (MIMO) Maximum Likelihood Decoding problem



Many devices communicate with a base station. How to recover original message from noisy measurement?

https://arxiv.org/pdf/2001.04014.pdf

### Image processing and classification



Given an image and a group of categories. How to use quantum computing to help with image classification?

https://arxiv.org/pdf/2008.05859.pdf

#### • Other projects:

Bring your own application!

It must be a machine learning / combinatorial optimization problem of interest suited for quantum computing



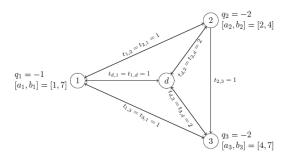




### **Project examples**

### Maritime Routing Problem

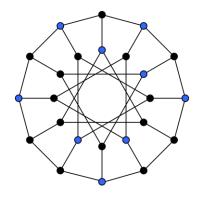




Real-life application problem

https://ieeexplore.ieee.org/iel7/8924785/9347847/09314905.pdf

### Max-k-coloring and stable-set of a graph



Graph theoretical

https://arxiv.org/pdf/2101.09462.pdf

• Other applications in Finance, Engineering, and Sciences





### 1QBit

### 1QBit

### QUBO Techniques for Feature Selection in Credit Scoring

- Credit scoring and classification, feature selection to reduce the number of variables input to a classifier.
- One can use a QUBO model to select features.
- Compare to previous results using the German Credit Data
- Compare with recursive feature elimination (RFE)

## Portfolio Optimization using Gate Model VQE / QAOA

- Mean-variance analysis is used to weigh risk against expected return.
- Implement a basic Strategic Asset Allocation Mean-Variance portfolio by solving a QUBO defined by the returns of each asset and the covariance matrix defined by the assets.
- This can be extended to more realistic problems as risk parity analysis and more sophisticated financial inputs.

Extra full-semester (longer) projects as graduation projects







### **2020 Tayur Prize Winners**

- First: <u>Time-Multiplexed CIM</u>: Gautham, Parth, Gautam. They focused on <u>Max-Cut</u> problem.
- Second: <u>Spatial-Photonic IM</u>: Vikram, Vignesh. They tackled the *Number Partitioning* problem.
- Paper published in Philosophical Transactions of the Royal Society A:
- https://www.cmu.edu/tepper/faculty-andresearch/assets/docs/ising\_machines\_royal\_ society\_proceedings\_a-revision.pdf

### PROCEEDINGS OF THE ROYAL SOCIETY A

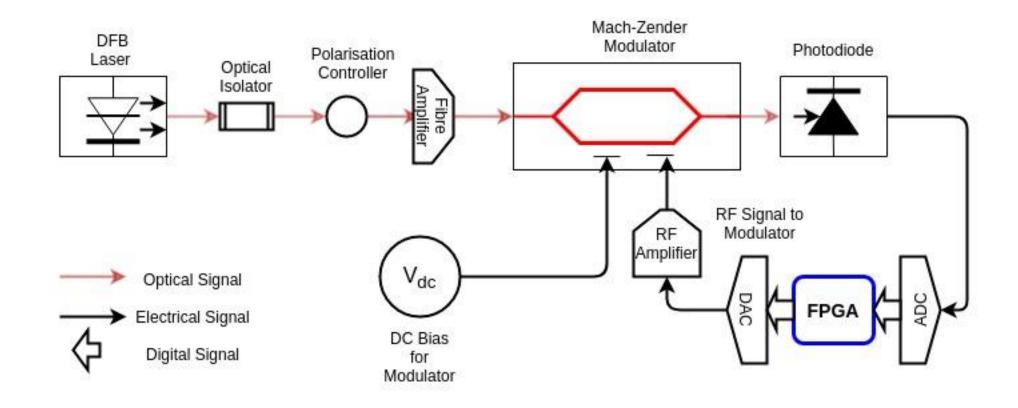
MATHEMATICAL, PHYSICAL AND ENGINEERING SCIENCES







### Motivated by "Poor Man's Ising Machine"









### **Optical-Electronic-Optical Model**

$$x_{n}[k+1] = \cos^{2}(f_{n}[k] - \pi/4 + \zeta_{n}[k]) - \frac{1}{2}.$$

$$f_{n}[k] = \alpha x_{n}[k] + \beta \sum_{m} J_{mn} x_{m}[k].$$

$$\sigma_{n} = sig_{n}(x_{n}[k])$$

$$H_{\text{Ising}} = -\frac{1}{2} \sum_{mn}^{N} J_{mn} \sigma_m \sigma_n.$$

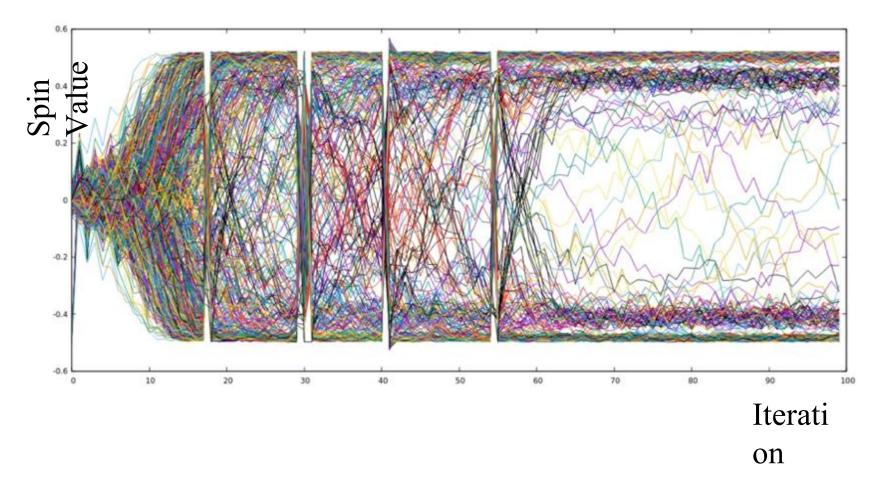
- $\circ$  Self bias term  $\alpha$
- Coupling coefficient β
- Weights between spins J
- O What does the optics do?
  - Nonlinear function cos<sup>2</sup>







### 24 x 24 spin lattice









### **2021 Tayur Prize**

- Supply Chain Management (Bin Packing, Job Shop Scheduling, Process Reliability, Drone+ Truck)
- Computational Biology (Cyclic Peptides, Cancer Genomics)
- Hedge Fund Portfolio with Kurtosis and Skewness
- Track Reconstruction (HL-LHC, LIGO)
- Message Decoding
- VLSI Design
- Quantum State Tomography
- O Image Recognition (COVID19? Pneumonia?)











### Other applications

### Applied:

- Air Traffic Management
- Portfolio Optimization
- Airport Gate Scheduling
- Autoencoders
- Anomaly detection in networks
- Vehicle Routing
- Robot Operations Planning

### Paradigmatic:

- SAT
- Traveling Salesman Problem
- Job Shop Scheduling
- Spin Glasses







### **Course Policy**

- Auditing students are encouraged to participate actively in the lectures
  - Consider doing the project, one learns by doing
- Regular attendance is essential and expected
- CMU students: use canvas
  - The quizzes are being posted there
  - Questions should be asked there to make it available to everyone

• Academic honesty is expected. Refer to the CMU's policies on academic integrity when in doubt.







### Videos and extra resources

- This year's website
  - https://bernalde.github.io/QuIPML22/
- Teaser video
  - https://www.linkedin.com/posts/carnegie-mellon-tepper-school-of-business\_quantum-computing-activity-6698655542186913792-001\_
- CMU Quantum Computing Group Website
  - https://lnkd.in/d6m5ECV
- Pittsburgh Quantum Institute
  - https://www.pqi.org/
- Prof. Tayur's seminar at Cornell on GAMA
  - https://cornell.hosted.panopto.com/Panopto/Pages/Viewer.aspx?id=3d46643f-03ea-4e3f-ad7a-ab9901290472







### **USRA** collaboration and NASA/USRA resources

- USRA Research Institute for Advanced Computer Science (RIACS) Quantum Group Website
  - https://riacs.usra.edu/quantum (includes a full login-protected QC course and last year's QIP Lectures)
- NASA Quantum and Artificial Intelligence Laboratory (QuAIL)
  - https://quantum.nasa.gov
- Students of this course are encouraged to apply to the Feynman Academy Internship program <a href="https://riacs.usra.edu/quantum/qacademy">https://riacs.usra.edu/quantum/qacademy</a> that sponsors research projects at NASA Ames Research Center.









### **Why Universities Exist**

"The justification for a university is that it preserves the connection between knowledge and zest of life, by uniting the young and old in the imaginative consideration of learning...The task of the university is to weld together imagination and experience.....The task of the university is the creation of the future...."





