

# Prerequisites from Linear Algebra and Matrix Theory

Finite-Dimensional Complex Linear Spaces and Matrices.

Complex Linear  $n$ -space.

We define an  $n$ -vector  $x$  to be an ordered  $n$ -tuple of complex numbers  $\xi_1, \xi_2, \dots, \xi_n$  which we write as a column:

$$x = \begin{bmatrix} \xi_1 \\ \dots \\ \xi_n \end{bmatrix}$$

The set of all such vectors is denoted by  $\mathbb{C}^n$ . We denote complex conjugation by a bar: ( $\bar{z} = a - ib, z = a + ib$ )

$$\bar{x} = \begin{bmatrix} \bar{\xi}_1 \\ \dots \\ \bar{\xi}_n \end{bmatrix}$$

# Prerequisites from Linear Algebra and Matrix Theory

The vector with zero components will be denoted by  $0$ . The transpose of an  $n$ -vector  $x$  is an ordered  $n$ -tuple of complex numbers written as a row:

$$x^t = (\xi_1, \xi_2, \dots, \xi_n)$$

The Hermitian conjugate of  $x$  is defined by

$$x^* = \overline{x^t} = (\bar{\xi}_1, \bar{\xi}_2, \dots, \bar{\xi}_n)$$

The vectors  $x + y$  and  $\lambda x$ , where  $\lambda$  is a complex number are defined by

$$\begin{bmatrix} \xi_1 + \eta_1 \\ \vdots \\ \xi_n + \eta_n \end{bmatrix} \quad \text{and} \quad \begin{bmatrix} \lambda \xi_1 \\ \vdots \\ \lambda \xi_n \end{bmatrix}$$