# **ASSIGNMENT TWO**

## **Semester 2 - 2021**

**PAPER NAME: Data Mining and Machine Learning** 

PAPER CODE: COMP809

DUE DATE: Sunday 24 Oct 2021 at midnight

**TOTAL MARKS: 100** 

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Note: This assignment must be complemented individually

**Submission:** A soft copy needs to be submitted through Turnitin (a link for this purpose will be set up in Blackboard) Include your actual code (no screenshot) in Appendix with appropriate comments for each task.

## **INSTRUCTIONS:**

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## Part A

The pre-processing performed was to bring all of the data in to Pandas dataframes, then apply categorisation to all the data so that it is all numeric and then go through the feature selection process. Following feature selection for each dataset, the selected features were nomalised prior to going through the algorithm.

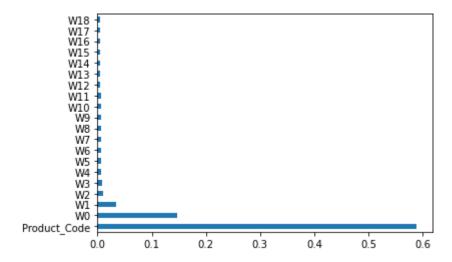
For consistency, the PCA algorithm was used for feature selection for each of the datasets.

## Datasets and feature selection

## Sales Transaction Data

The Sales Transaction dataset contains weekly volumes of 800 products sold over a period of 52 week. Weeks are represented as columns and products are represented as rows. The dataset resembled a matrix, with a product column on the left. A normalised figure is provided for each record, however I have elected to normalise the entire dataset anyway.

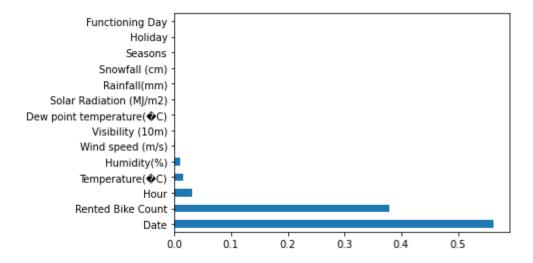
The top three parameters were selected for this data as together they explained most of the variance.



## Seoul Bike Data

The Seoul Bike Sharing Demand dataset runs for between start of December 2017 and end of November 2019. There are over 8000 records, which describe the atmospheric conditions on the day and hour of the hirage, how many bikes were rented and whether the day was a holiday.

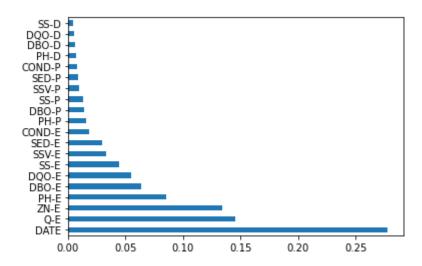
The top two parameters were selected for this data as together they explained most of the variance.



## Water Treatment Data

The Water Treatment dataset contains over 500 records and covers a range of parameters that describe the chemical composition of water treatment samples between March 1990 and August 1991 – 18 months worth of data.

The top five parameters were selected for this data as together they explained most of the variance.



Task 1
K means algorithm

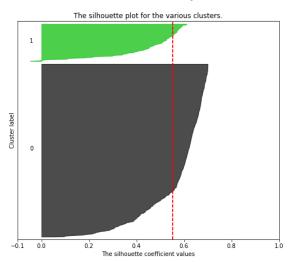
Table A: K means algorithm

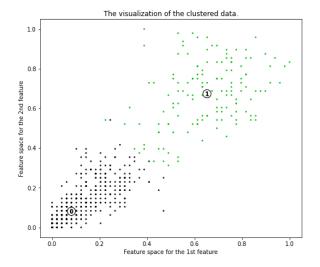
	Time taken (seconds)	CSM / SSE	K parameter
Sales Transactions	0.39674830436706543	0.5529922804905653	2
Data		/	
		14.437368116537462	
Water Treatment	0.42758846282958984	0.1979742286699438	6
Data		/	
		14.219162585579324	

Seoul Bike Data	5.6746766567230225	0.2736422972611256	2
		/	
		297.7696053888172	

## **Sales Transactions Data CSM chart for KMeans**

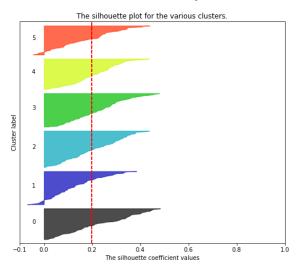
#### Silhouette analysis for KMeans clustering on sample data with $n_c$ lusters = 2

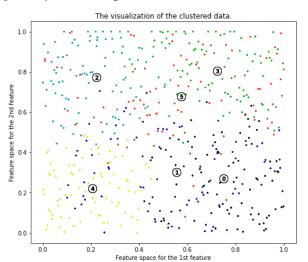




## **Water Treatment Data CSM chart for KMeans**

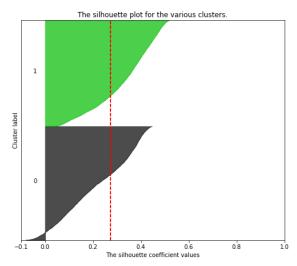
#### Silhouette analysis for KMeans clustering on sample data with n\_clusters = 6

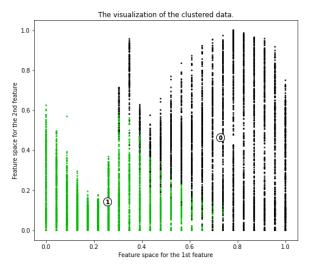




Seoul Bike Data CSM chart for KMeans

Silhouette analysis for KMeans clustering on sample data with n\_clusters = 2





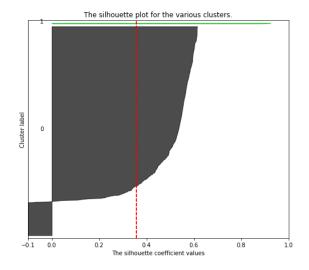
DBSCAN algorithm

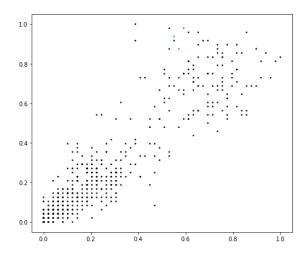
Table B: DBSCAN algorithm

For the DBSCAN algorithm I needed to adjust the EPS value also, but unfortunately I was unable to get a correct value of the EPS so that the algorithm would complete correctly for the Water Treatment Data and Seoul Bikes Data.

	Time taken (seconds)	CSM / SSE	EPS parameter
Sales Transactions Data	0.346055269241333	0.3571425685830280 6 / 27.772162712889 894	0.2
Water Treatment Data	[Incomplete]	0.0181424937055316 6 / [Incomplete]	0.3
Seoul Bike Data	[Incomplete]	-0.489653439764812 96/[Incomplete]	0.1

## Sales Transactions Data CSM chart for DBSCAN



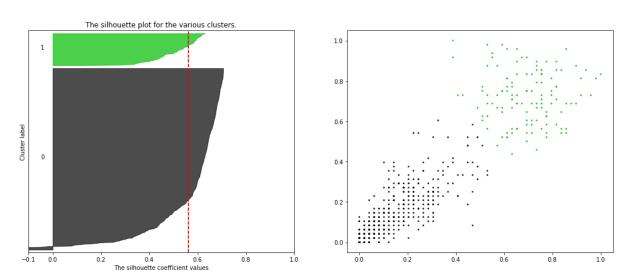


# Agglomerative algorithm

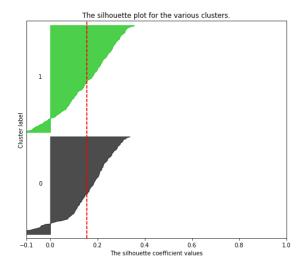
**Table C: Agglomerative algorithm** 

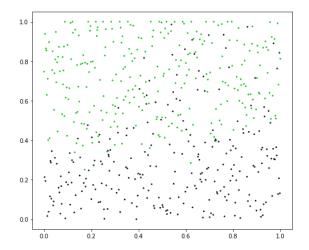
	Time taken (seconds)	CSM / SSE	Clusters parameter
Sales Transactions Data	0.2312090396881103 5	0.5630813204653953 / 14.907766709758 254	2
Water Treatment Data	0.1230895519256591 8	0.1552454137520582 8 / 24.894066528279 865	2
Seoul Bike Data	8.33217167854309	0.2468869043596790 5 / 308.64342487739 03	2

# **Sales Transactions Data CSM chart for Agglomerative**

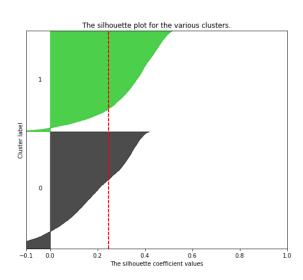


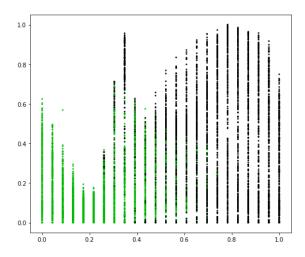
Water Treatment Data CSM chart for Agglomerative





## Seoul Bike Data CSM chart for Agglomerative





Task 2
Answer A: which clustering algorithm performed best

The KMeans algorithm appears to perform slower than the aglomorative algorithm in general, although not in all cases. Unfortunately I struggled with the DBSCAN algorithm so have incomplete data for this experiment. For that reason I am only comparing the Aglomorative algorithm and K Means algorithms.

For the Sales Transactions Data the Aglomorative algorithm performed best, with CSM of 0.56 and time taken of 0.23 seconds, for 2 clusters.

For the Water Treatment Data the K Means algorithm performed best, with CSM of 0.197 and time taken of 0.43 seconds, for 2 clusters.

For the Seoul Bike Data the K Means algorithm performed best, with CSM of  $\bf 0$  .27 and time taken of  $\bf 5.6$  seconds, for  $\bf 2$  clusters.

I am using a combination of time taken and CSM score to rank the algorithms. The higher the CSM score, the better the algorithm. If the CSM score is high and the time taken is low, then that algorithm is considered the better one.

## Answer B: why did it produced the best value for the CSM measure

Looking at the shape of the data, DBSCAN might have been good to apply to the Seoul Bike dataset as it appears to have some overlap in it's structure. Unfortunately I have have not been able to test this on the dataset. The best performance for the Seoul Bike dataset was K Means.

The result I had for the Water Treatment data was the K Means was the better algorithm. This was somewhat surprising as looking at the dataset, it seems relatively even distributed with no noticeable clustering. I would have thought that the Aglomorative algorithm would have performed better for this dataset.

The result I had for the Sales Transaction data indicated that the Agglomorative algorithm slightly outperformed the K Means algorithm. This dataset is quite neatly dividied in to two clusters, which probably makes it equally good for a hierarchical, a divisive or a partitional algorithm.

## Answer C: which clustering algorithm is the overall winner

Of the three algorithms, K Means seemed easiest to work with and to understand. K Means also generally performed the quickest of the three algorithms although I did not get to test DBSCAN to a significant extent.

## Part B

#### Pre-processing

I have used the file Penrose\_Hourly\_AggregateData\_Jan2016Dec2020.csv that was provided for the assignment.

To be able to include the hourly segmentation, I needed to do feature engineering to produce four new columns from the Timestamp column. This was done y concerting the Timestamp type to a datetime and then getting the hour, day, month and year values form the datetime and creating new columns.

I also followed the guidance in the assignment and removed values of greater than 100 from the relatively humidity (%) and temperatures of above 40 degrees Celsius from the Air Temp column.

Finally, all columns were converted to categorical. Initially I wasn't going to do this, but the MLP compained that the target categories were floats. I ended up "binning" these values anyway to reduce the number of possible categories, so this step may not have been necessary.

## Feature selection (top 5)

The following sections provide details of the five features that were selected for the predictor variables for the experiment due to their being the variables that had the highest correlation in comparison to the target variable when assessed indicidually against the target (PM2.5 (�g/m�)) using linear regression. A corellation plot for the linear regression model for each predictor is provided.

The statistics for each predictor are provided, including the Pearson Correlation which describes each individual attribute's influence on the target variable.

The reason I used this approach is because it seemed like the most intuitive and simplistic way to get a very clear view of what each predictor variable looked like when it was plotted against the target. An alternative approach would have been to plot all of the predictor variables against the target in a single table.

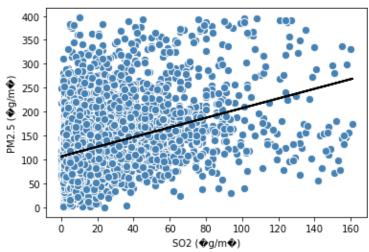
## SO2 ( **\***g/m **\***)

Slope: 1.011 Intercept: 106.215

explained\_variance: 0.1236

r2: 0.1236 MAE: 36.4505 MSE: 2458.9511 RMSE: 49.5878

Pearsons correlation: 0.3515

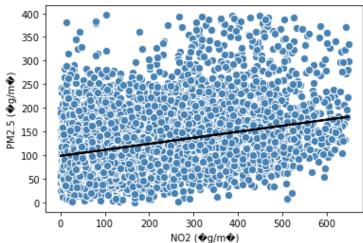


## NO2 ( **\***g/m **\***)

Slope: 0.128 Intercept: 98.190

explained\_variance: 0.1137

r2: 0.1137 MAE: 36.438 MSE: 2486.5994 RMSE: 49.8658



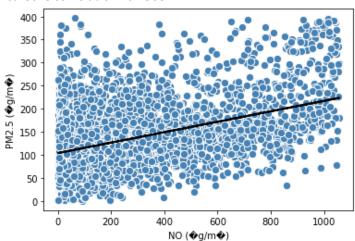
# NO (**\***g/m**\***)

Slope: 0.113 Intercept: 103.757

explained\_variance: 0.1904

r2: 0.1904 MAE: 35.2568 MSE: 2271.5162 RMSE: 47.6604

Pearsons correlation: 0.4363



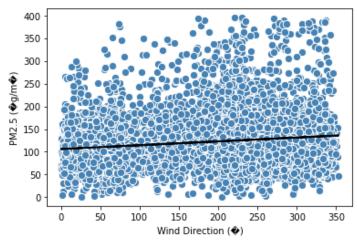
## Wind Direction (�)

Intercept: 106.028

explained\_variance: 0.0211

r2: 0.0211 MAE: 38.016 MSE: 2746.4533 RMSE: 52.4066

Pearsons correlation: 0.1452

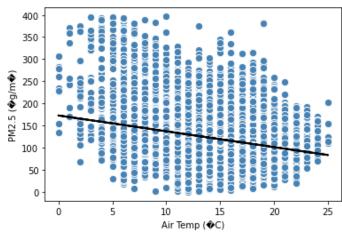


## Air Temp ( C)

Slope: -3.581 Intercept: 172.655

explained\_variance: 0.0722

r2: 0.0722 MAE: 37.9256 MSE: 2603.0704 RMSE: 51.0203 Pearsons correlation: -0.2687



## Summary statistics for PM2.5 (�g/m�)

The following summary statistics were attained for the target variable by using the .describe() function against the variable, as is provided by the Pandas package.

 count
 10313.000000

 mean
 121.846310

 std
 52.970365

 min
 0.000000

 25%
 88.000000

 50%
 113.000000

 75%
 145.000000

 max
 397.000000

Name: PM2.5 (�g/m�), dtype: float64

## Table of summary stats for predictors

The formula for Pearson Corrleation is as follows:

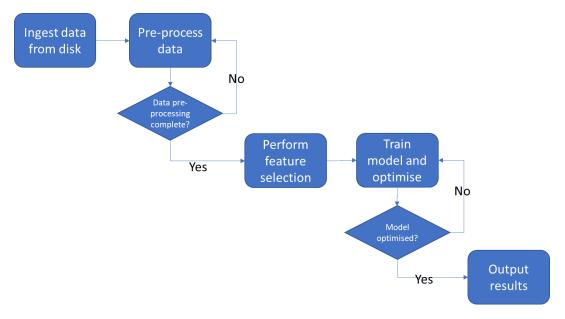
$$r = rac{\sum \left(x_i - ar{x}
ight)\left(y_i - ar{y}
ight)}{\sqrt{\sum \left(x_i - ar{x}
ight)^2 \sum \left(y_i - ar{y}
ight)^2}}$$

The five best matched variables based on Pearson Correlation are covered in the following table. The Pearson Correlation value provided is the result of a linear regression for each variable against the target. Higher values are better and generally values that are higher in each direction than 0.5 or -0.5 are considered highly correlated. Unfortunately I didn't get any results that were highly correlated.

Predictor variable	Pearson Correlation value
S02 (�g/m�)	0.3515
NO2 (�g/m�)	0.3372
NO ( <b>Q</b> g/m <b>Q</b> )	0.4363
Wind Direction (�)	0.1452
Air Temp (�C)	-0.2687

## Experimental methods

The following diagram issulstrates the process used to generated the model that is created for the MLPClassifier and the LTSM model. This is a high-level overview of the process, and detailed steps such as the train/test-split are incorporated into the bigger parts of the process.

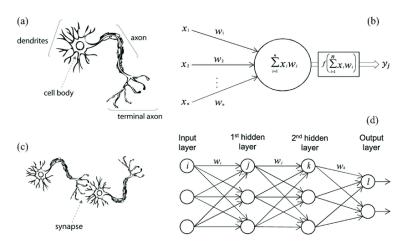


## Multilayer Perceptron (MLP)

## Answer 1: describe multilayer perceptron

The Multilayer Perceptron is a machine learning approach that tries to mimic the process biological process that is used by brain to achieve predictive capability based on incoming information.

The perceptron element of the model mimics the behaviour of a biological neuron in a brain, and synapses, which link neorons together.



This image is taken from Meng Z., et.al. [1] provides an overview for the model of the synapse and the neuron that the Multi Layer Perceptron borrows from.

The neuron is modelled by the "perceptron" by emulating input signals, applying a weight to each signal, summing the values of the output of the signals multiplied by the respective weights and then deciding of it will in turn output a signal based on whether the sum of the values input and calculated cross a threshold, defined by another function such as the Sigmod function. The neuron in

the brain performs this work using input chemical signal, whereas the perceptron performs work work using digital signals. Perceptrons are combined in layers to mimic the function of synapses, which link neurons in the brain.

Artificial neural networks have been around as a concept for a relatively long time, but have become increasingly popular and viable in recent years with the availability of highly parallel computing models such as GPU processors and cloud computing. Because an artificial neural networks mimic the biological brain which is a massively parallel computing process, the ANN also requires platforms that support highly parallel worksloads.

A limitation of the ANN is that it is not inherently explainable in that the process that the training algoritm applies to produce the optimised model is very difficult to interpret in terms of understanding which aspect of the model is responsible for a particular outcome.

## Answer 2: single hidden layer MLP with k= 25 neurons

The single layer network with 25 nerons in the single layer took several minutes to run and yielded a model with accuracy of approximately 0.45 across 7 target categories. The target categories were reached by "binning" the target variable, which was distributed across many values between 0 and 397, resulting initially in a very low accuracy model. I therefore decided to apply binning and split the variable in to 7 evenly split categories with range of 50 values, between 0 and 400. This was achieve as follows:

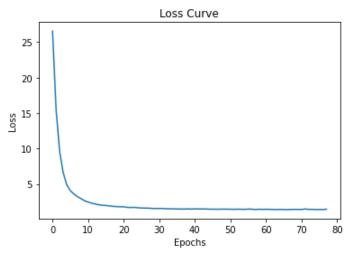
$$y = np.digitize(y, bins=[50, 100, 150, 200, 250, 300, 350])$$

Without bining, the accuracy of the model dropped to 0.01, with binning across 4 categories, the accuracy of the model increases to about 0.6. & seemed like an acceptable compromise.

Details of the model are provided below, along with charts and metrics.



Loss 1.4461270468227754 iterations 78 Assigned classes [0 1 2 3 4 5 6 7]



Accuracy score: 0.44

Answer 3: two hidden layer MLP with with k= 24 neurons (max)

The following table provides a summary of the result of running the algorithm across 25 iterations of the process of incrementing the first layer of a 2 layer MLP by one and decrementing the second layer by one, with a starting value of 1 for the first layer and 24 for the second layer, until the values are swapped.

Combination of neurons	Accuracy
17,8	0.450226
6,19	0.446025
16,9	0.445055
11,14	0.443439
19,6	0.441823
9,16	0.4415
10,15	0.441176
1,24	0.43956
7,18	0.43956
14,11	0.43245
13,12	0.430834
8,17	0.425339
22,3	0.423077
18,7	0.420491
21,4	0.419522
23,2	0.419198
24,1	0.419198
3,22	0.418875
20,5	0.417582
12,13	0.413704
15,10	0.411441
4,21	0.410472
2,23	0.389787
5,20	0.378474

## Answer 4: variation in the obtained performance metrics

As can be seen from the table provided in the (3) part of this section, although there is variation in the results, no obvious pattern has emerged – i.e. there is no marked difference based on the number of perceptrons in the hidden layers being about the same or being very different, the result seems quite random. The two lowest results where where the first hidden layer had low number of perceptrons, but also one of the highest results was where the first layer has 1 perceptron (and the second layer had 24).

It is difficult to say which architecture gives the better performance, or to explain the results, as no pattern has emerged from this experiment and therefore I am unable to make any assumptions about what might (or might not) be happening. What I can say though is that since the pattern is randm, perhaps for this dataset a deeper network is onconsequential.

# Long Short-Term Memory (LSTM) asdf (1) DNC (2) DNC (3) DNC (4) DNC Model Comparison DNC (1) DNC

## References

(2) DNC

[1] Meng Z, Hu Y, Ancey C. "Using a Data Driven Approach to Predict Waves Generated by Gravity Driven Mass Flows." *Water.* 2020; 12(2):600. <a href="https://doi.org/10.3390/w12020600">https://doi.org/10.3390/w12020600</a>

## **Appendix**

## Four appendixes are provided

19075153\_O'Leary\_PartA1\_AM: extract from Jupyter-Labs for answers to Part A (Agglomerative) 19075153\_O'Leary\_PartA1\_DB: extract from Jupyter-Labs for answers to Part A (DBSCAN) 19075153\_O'Leary\_PartA1\_KM: extract from Jupyter-Labs for answers to Part A (Kmeans) 19075153\_O'Leary\_PartB: extract from Jupyter-Labs for answers to Part B

# 19075153 O'Leary PartB

October 24, 2021

```
[1]: import pandas as pd
     import numpy as np
     from sklearn.model_selection import train_test_split
     import matplotlib.pyplot as plt
     import warnings
     from pandas.plotting import scatter_matrix
     import seaborn as sns
     from sklearn.model_selection import cross_val_score
     from sklearn.tree import DecisionTreeClassifier
     from sklearn.metrics import classification report, confusion matrix
     from sklearn import tree
     from sklearn.feature_selection import SelectKBest
     from sklearn.feature_selection import chi2
     from numpy import set_printoptions
     from sklearn.decomposition import PCA
     from sklearn import preprocessing
     from sklearn.linear_model import LinearRegression
     from sklearn.linear_model import RANSACRegressor
     from sklearn.model selection import train test split
     from sklearn.metrics import mean_squared_error
     from scipy.stats import pearsonr
     import sklearn.metrics as metrics
     warnings.filterwarnings('ignore')
```

# 1 Data load and pre-processing

```
# Rearrange Timestamp column
# Remove incorrect values or outliers
rawdata = rawdata[rawdata['Relative Humidity (%)'] <= 100]</pre>
rawdata = rawdata[rawdata['Air Temp (C)'] <= 40]</pre>
rawdata = rawdata.dropna(how='any',axis=0)
rawdata['Timestamp (UTC+12:00)'] = pd.to_datetime(rawdata['Timestamp (UTC+12:
ر[ا (00↔
rawdata = rawdata.set index('Timestamp (UTC+12:00)')
rawdata['Hour'] = rawdata.index.hour
rawdata['Day'] = rawdata.index.day
rawdata['Month'] = rawdata.index.month
rawdata['Year'] = rawdata.index.year
# categorise everything and create array
list of columns = rawdata.columns
rawdata[list_of_columns] = rawdata[list_of_columns].apply(lambda col:pd.

→Categorical(col).codes)
```

## 2 Inspecting outliers

```
[3]: # A function that will plot a scatterplot of the training samples and add the
     \rightarrowregression line
    def lin_reg_plot(x_name):
        # Create the model
        slr = LinearRegression()
        slr.fit(X, y)
        # Regression metrics
        explained variance=metrics explained variance_score(y, slr.predict(X))
        mean_absolute_error=metrics.mean_absolute_error(y, slr.predict(X))
        mse=metrics.mean_squared_error(y, slr.predict(X))
        median_absolute_error=metrics.median_absolute_error(y, slr.predict(X))
        r2=metrics.r2_score(y, slr.predict(X))
        corr, _ = pearsonr(rawdata[x_name], y)
        # Print stats
        print('====== ' + x name + ',
      →========')
        print('Slope: %.3f' % slr.coef_[0])
        print('Intercept: %.3f' % slr.intercept_)
        print('explained_variance: ', round(explained_variance,4))
        print('r2: ', round(r2,4))
        print('MAE: ', round(mean_absolute_error,4))
        print('MSE: ', round(mse,4))
        print('RMSE: ', round(np.sqrt(mse),4))
```

```
print('Pearsons correlation: ', round(corr,4)) # Over 0.5 or less than -0.5
 \rightarrow signifies strongest correlation
    # Chart
    plt.scatter(X, y, c='steelblue', edgecolor='white', s=70)
    plt.plot(X, slr.predict(X), color='black', lw=2)
    plt.xlabel(x name)
    plt.ylabel('PM2.5 (g/m)')
    plt.show()
# Starting point X and y
X = rawdata[['Hour','Air Temp (C)','Relative Humidity (%)','Solar Radiation (W/
\rightarrowm)','Wind Direction ()','Wind Speed (m/s)','NO (g/m)','NO2 (g/m)','SO2 (g/m)'
→m )']].values
y = rawdata['PM2.5 (g/m)'].values
# Display data in 2D
x_n = 'S02 (g/m)'
X = rawdata[[x_name]].values
lin_reg_plot(x_name)
x_name = 'NO2 (g/m)'
X = rawdata[[x_name]].values
lin_reg_plot(x_name)
x_name = 'NO (g/m)'
X = rawdata[[x_name]].values
lin_reg_plot(x_name)
x name = 'Wind Speed (m/s)'
X = rawdata[[x name]].values
lin_reg_plot(x_name)
x_name = 'Wind Direction ()'
X = rawdata[[x_name]].values
lin_reg_plot(x_name)
x_name = 'Solar Radiation (W/m)'
X = rawdata[[x_name]].values
lin_reg_plot(x_name)
x name = 'Relative Humidity (%)'
X = rawdata[[x_name]].values
lin_reg_plot(x_name)
x_name = 'Air Temp (C)'
X = rawdata[[x_name]].values
lin_reg_plot(x_name)
x_name = 'Hour'
X = rawdata[[x_name]].values
lin_reg_plot(x_name)
```

======= S02 (g/m)

\_\_\_\_\_

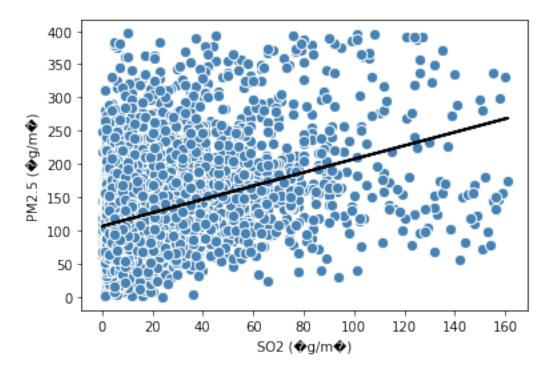
Slope: 1.011

Intercept: 106.215

explained\_variance: 0.1236

r2: 0.1236 MAE: 36.4505 MSE: 2458.9511 RMSE: 49.5878

Pearsons correlation: 0.3515



======== NO2 ( g/m )

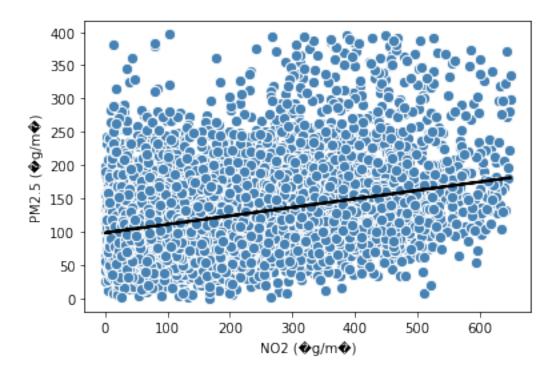
\_\_\_\_\_\_

Slope: 0.128

Intercept: 98.190

explained\_variance: 0.1137

r2: 0.1137 MAE: 36.438 MSE: 2486.5994 RMSE: 49.8658



======= NO (g/m)

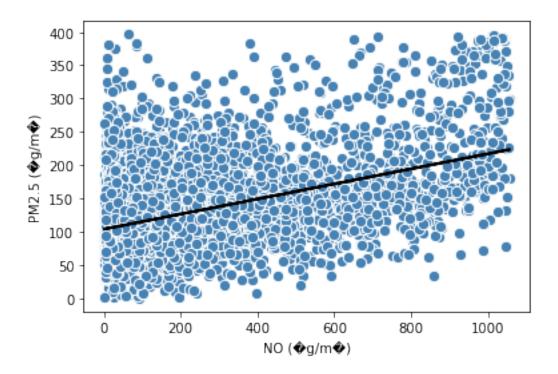
\_\_\_\_\_

Slope: 0.113

Intercept: 103.757

explained\_variance: 0.1904

r2: 0.1904 MAE: 35.2568 MSE: 2271.5162 RMSE: 47.6604



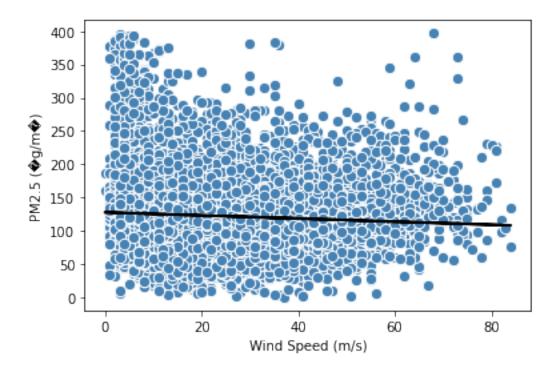
======= Wind Speed (m/s)

\_\_\_\_\_

Slope: -0.233 Intercept: 127.722

explained\_variance: 0.0045

r2: 0.0045 MAE: 38.6166 MSE: 2792.8766 RMSE: 52.8477



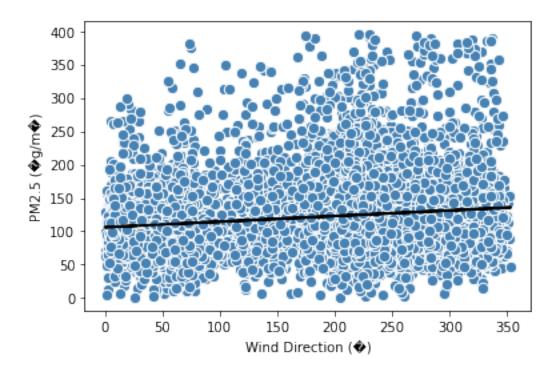
======= Wind Direction ()

Slope: 0.085

Intercept: 106.028

explained\_variance: 0.0211

r2: 0.0211 MAE: 38.016 MSE: 2746.4533 RMSE: 52.4066



======= Solar Radiation (W/m)

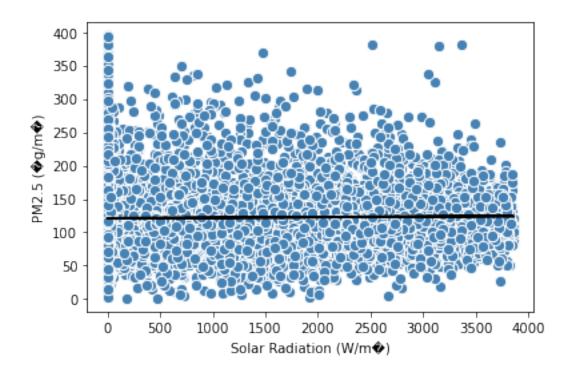
-----

Slope: 0.001

Intercept: 121.037

explained\_variance: 0.0004

r2: 0.0004 MAE: 38.47 MSE: 2804.466 RMSE: 52.9572

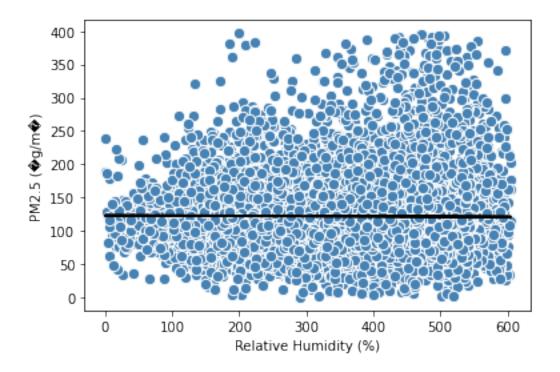


======== Relative Humidity (%)

Slope: -0.003 Intercept: 123.050

explained\_variance: 0.0001

r2: 0.0001 MAE: 38.4961 MSE: 2805.3804 RMSE: 52.9658



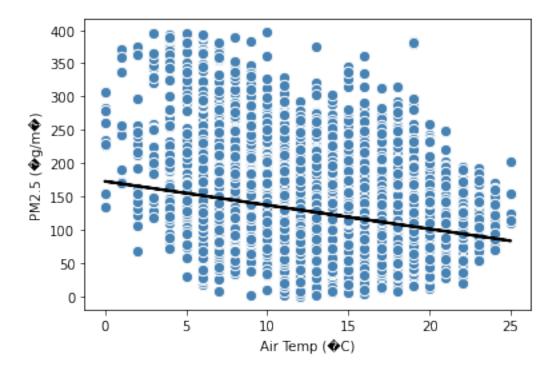
----- Air Temp (C)

\_\_\_\_\_

Slope: -3.581 Intercept: 172.655

explained\_variance: 0.0722

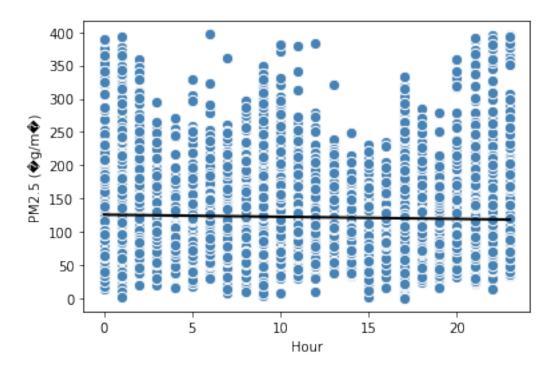
r2: 0.0722 MAE: 37.9256 MSE: 2603.0704 RMSE: 51.0203



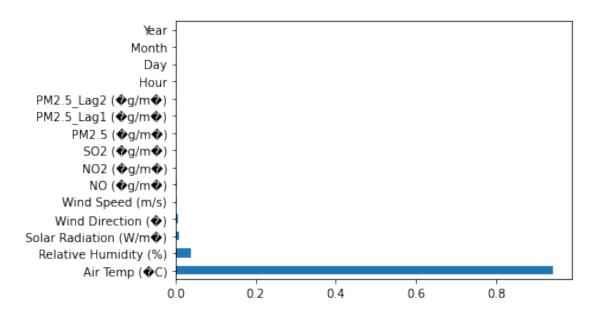
Slope: -0.318 Intercept: 125.667

explained\_variance: 0.0017

r2: 0.0017 MAE: 38.4984 MSE: 2800.7835 RMSE: 52.9224



# 3 Feature importance



# 4 Summary stats for PM2.5 ( g/m )

```
[5]: rawdata['PM2.5 (g/m)'].describe()
[5]: count
              10313.000000
                121.846310
     mean
     std
                 52.970365
                  0.000000
    min
     25%
                 88.000000
     50%
                113.000000
     75%
                145.000000
                397.000000
     Name: PM2.5 (g/m), dtype: float64
```

# 5 Do the train/test split

```
[9]: # Get final X and y - we want to keep the top five attributes based on Pearsons

correlation

# Five topmost correlated variables are 'Air Temp (C)', 'Wind Direction

()','NO (g/m)','NO2 (g/m)','SO2 (g/m)'

X = rawdata[['Air Temp (C)','Wind Direction ()','NO (g/m)','NO2 (g/m)','SO2

(g/m)']].values

y = rawdata['PM2.5 (g/m)'].values
```

```
# We need to reduce the number of categories for y - max is 397, we can

→ probably start with 7 categories

# In this case we get about 0.45 accuracy score

# If we reduce the categories to 4, we get about 0.6 accuracy score

y = np.digitize(y,bins=[50,100,150,200,250,300,350])

# Do the train/test split

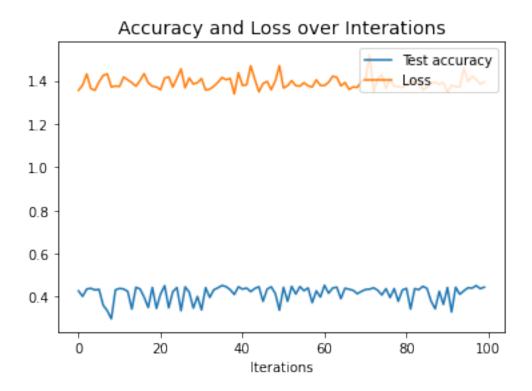
pred_train, pred_test, tar_train, tar_test = train_test_split(X, y, test_size=.

→3, random_state=4)
```

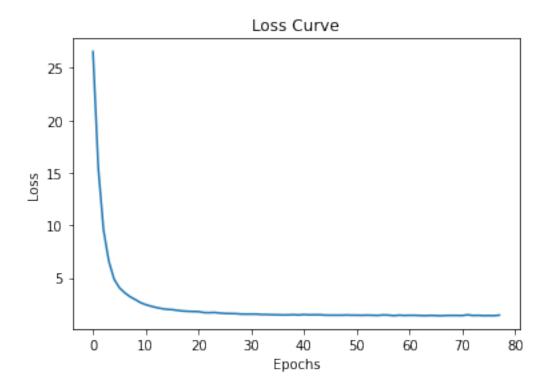
## 6 MLP classifier

```
[10]: import pandas
      import numpy as np
      from sklearn.model_selection import train_test_split
      from sklearn.metrics import accuracy_score
      from sklearn.neural_network import MLPClassifier
      import matplotlib.pyplot as plt
      #A function to see some of the attributes of NN
      def NN properties(model):
          loss_values = model.loss_
          print("Loss", loss_values)
          iterations = model.n_iter_
          print("iterations",iterations)
          classes_assigned= model.classes_
          print("Assigned classes", classes_assigned)
      #Displaying loss curve using loss_curve method. Note that this only works with_
       → the MLP default solver "adam"
      def make plots default(model):
          plt.plot(model.loss_curve_)
          plt.title('Loss Curve')
          plt.xlabel('Epochs')
          plt.ylabel('Loss')
          plt.show()
      #A generic function to display training loss and testing accuracy of [1]
       \hookrightarrow MLPClassifier
      def make_plots_all(mlp, target_train, target_test,_
       →predictors_test,predictors_train):
          max iter = 100
          accuracy = []
          losses = []
          for i in range(max_iter):
              mlp.fit(predictors_train, target_train)
```

```
iter_acc = mlp.score(predictors_test, target_test)
        accuracy.append(iter_acc)
        losses.append(mlp.loss_)
   plt.plot(accuracy, label='Test accuracy')
   plt.plot(losses, label='Loss')
   plt.title("Accuracy and Loss over Interations", fontsize=14)
   plt.xlabel('Iterations')
   plt.legend(loc='upper right')
   plt.show()
#A function for model building and calculating accuracy
def get_accuracy(target_train, target_test, predictors_test, predictors_train):
    # Two hidden layers with 10 and 5 neurons - NN
   clf = MLPClassifier(hidden_layer_sizes=(25), max_iter=100)
    #Calling the make_plots_allfunction with unfitted model
   make_plots_all(clf, target_train, target_test, predictors_test,_
 →predictors_train)
    clf.fit(predictors_train, np.ravel(target_train, order='C'))
   predictions = clf.predict(predictors test)
   NN_properties(clf) ##Calling NN_properties to see the model attributes
   make plots default(clf) ##Calling make plots function to see the error plots
   return accuracy_score(target_test, predictions)
#train-test split
pred_train, pred_test, tar_train, tar_test = train_test_split(X, y, test_size=.
→3, random_state=4)
#Calling get_accuracy function which also invoke other functions NN_properties,
→ make_plots, make_plots_all
print("Accuracy score: %.2f" % get_accuracy(tar_train, tar_test, pred_test, u
 →pred_train))
```



Loss 1.4461270468227754 iterations 78 Assigned classes [0 1 2 3 4 5 6 7]



Accuracy score: 0.44

# 7 2-Layer MLP

```
[11]: #train-test split
      pred_train, pred_test, tar_train, tar_test = train_test_split(X, y, test_size=.
       \rightarrow3, random_state=4)
      def two_layer_mlp(num_l1):
          tlmlp = MLPClassifier(hidden_layer_sizes=(num_l1, 25-num_l1,), max_iter=84)
          fit_tlmlp = tlmlp.fit(pred_train, np.ravel(tar_train, order='C'))
          pred_tlmlp = tlmlp.predict(pred_test)
          prob_tlmlp = tlmlp.predict_proba(pred_test)
          accuracy_tlmlp = accuracy_score(tar_test, pred_tlmlp)
          return accuracy_tlmlp
      results = pd.DataFrame(columns=["Combination of neurons", "Accuracy"])
      for i in range(1,25):
          new_row = {"Combination of neurons": str(i)+","+str(25-i), "Accuracy": __

→str(two_layer_mlp(i))}
          results = results.append(new_row, ignore_index=True)
      # Drop results out to a table
```

## results

[11]:	Combination of neurons	Accuracy
0	1,24	0.43956043956043955
1	2,23	0.38978668390433097
2	3,22	0.4188752424046542
3	4,21	0.41047188106011634
4	5,20	0.3784744667097608
5	6,19	0.4460245636716225
6	7,18	0.43956043956043955
7	8,17	0.4253393665158371
8	9,16	0.4414996767937944
9	10,15	0.4411764705882353
10	11,14	0.4434389140271493
11	12,13	0.4137039431157078
12	2 13,12	0.4308338720103426
13	3 14,11	0.43244990303813835
14	15,10	0.4114414996767938
15	16,9	0.44505494505494503
16	17,8	0.4502262443438914
17	18,7	0.4204912734324499
18	19,6	0.44182288299935357
19	20,5	0.4175824175824176
20	21,4	0.41952165481577247
21	22,3	0.4230769230769231
22	23,2	0.4191984486102133
23	3 24,1	0.4191984486102133
[]:		

# 19075153 O'Leary PartA1 KM

October 16, 2021

```
[1]: import pandas
     from sklearn.model_selection import train_test_split
     import matplotlib.pyplot as plt
     import warnings
     from pandas.plotting import scatter_matrix
     import seaborn as sns
     from sklearn.model_selection import cross_val_score
     from sklearn.tree import DecisionTreeClassifier
     from sklearn.metrics import classification_report, confusion_matrix
     from sklearn import tree
     from sklearn.feature_selection import SelectKBest
     from sklearn.feature_selection import chi2
     from numpy import set_printoptions
     from sklearn.decomposition import PCA
     from sklearn import preprocessing
     warnings.filterwarnings('ignore')
```

# 1 Data load and pre-processing

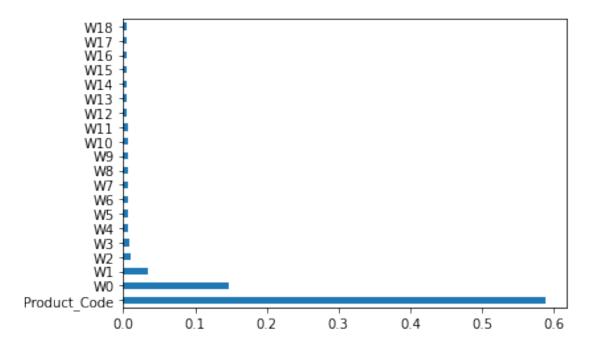
```
print(rawdata_sales.shape)
print(rawdata_sales.head())
#################
# load data seoul
################
path_seoul = "/mnt/c/Users/T828808/Study/AUT/COMP809/Ass2/SeoulBikeData.csv"
rawdata_seoul = pandas.read_csv(path_seoul)
# categorise everything and create array
list_of_columns_seoul = rawdata_seoul.columns
rawdata_seoul[list_of_columns_seoul] = rawdata_seoul[list_of_columns_seoul].
 →apply(lambda col:pandas.Categorical(col).codes)
# Create array
array_seoul = rawdata_seoul.values
predictors_seoul = array_seoul[:, 0:14]
# Print some stats
print(rawdata_seoul.shape)
print(rawdata_seoul.head())
##################
# load data water
##################
path_water = "/mnt/c/Users/T828808/Study/AUT/COMP809/Ass2/water-treatment.data"
rawdata_water = pandas.read_csv(path_water)
rawdata_water.columns =__
 # categorise everything and create array
list of columns water = rawdata water.columns
rawdata_water[list_of_columns_water] = rawdata_water[list_of_columns_water].
 →apply(lambda col:pandas.Categorical(col).codes)
# Create array
array_water = rawdata_water.values
predictors_water = array_water[:, 0:39]
# Print some stats
print(rawdata_water.shape)
print(rawdata_water.head())
(811, 107)
  Product_Code W0 W1 W2 W3 W4 W5 W6 W7
                                             W8 ... Normalized 42 \
0
            0
              11 12 10
                           8 13 12 14 21
                                                               3
                                              6
                7 6
                           2
                              7
                                                              17
1
           111
                      3
                                  1
                                      6
                                         3
                                              3 ...
2
           222
               7 11
                      8 9 10
                                   8 7 13 12 ...
                                                              24
3
           331 12
                    8 13
                          5
                               9
                                      9 13 13
                                                              37
                    5 13 11
                               6
                                   7
                                      9 14
           442
               8
                                              9
                                                              24
  Normalized 43 Normalized 44 Normalized 45 Normalized 46 Normalized 47 \
             20
                          26
                                        35
                                                      46
```

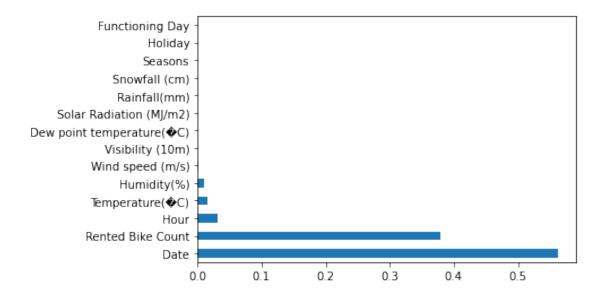
```
38
                                47
                                                 7
                                                                                  35
1
                                                                  6
2
               83
                                16
                                                 15
                                                                 32
                                                                                  40
3
               45
                                 4
                                                                 20
                                                                                  30
                                                 9
4
               51
                                25
                                                 56
                                                                 16
                                                                                  15
   Normalized 48
                   Normalized 49
                                    Normalized 50
                                                     Normalized 51
                                13
                                                 7
                                                                 35
0
               16
                                 7
               44
                                                 55
                                                                  0
1
2
               82
                                41
                                                 41
                                                                 32
3
               65
                                31
                                                 25
                                                                 31
4
                8
                                49
                                                 29
                                                                 36
[5 rows x 107 columns]
(8760, 14)
   Date Rented Bike Count
                              Hour
                                     Temperature(C) Humidity(%) \
                         253
                                  0
0
                                                   111
                                                                  28
1
     11
                         203
                                  1
                                                   108
                                                                  29
2
     11
                         172
                                  2
                                                   103
                                                                  30
3
     11
                         106
                                  3
                                                   101
                                                                  31
4
                          77
                                  4
                                                   103
                                                                  27
     11
   Wind speed (m/s) Visibility (10m)
                                           Dew point temperature(C) \
0
                   22
                                    1788
                                                                   114
                   8
                                    1788
                                                                   114
1
2
                   10
                                    1788
                                                                   113
3
                   9
                                    1788
                                                                   114
4
                   23
                                    1788
                                                                   104
   Solar Radiation (MJ/m2)
                              Rainfall(mm)
                                                                         Holiday \
                                              Snowfall (cm)
                                                               Seasons
0
                           0
                                           0
                                                                      3
                                                                               1
                                                            0
                                                                      3
                           0
                                           0
1
                                                                               1
                                                                      3
2
                           0
                                           0
                                                            0
                                                                               1
3
                           0
                                                            0
                                                                      3
                                                                               1
                                           0
4
                           0
                                           0
                                                            0
                                                                      3
                                                                                1
   Functioning Day
0
1
                   1
2
                   1
3
                   1
                   1
4
(526, 39)
   DATE Q-E
               ZN-E
                      PH-E
                            DBO-E
                                    DQO-E
                                            SS-E
                                                   SSV-E
                                                          SED-E
                                                                  COND-E
    197
                         6
                               204
                                       169
                                              57
                                                              50
         330
                116
                                                     201
                                                                      409
0
1
    427
           99
                143
                         5
                               204
                                      231
                                              42
                                                     208
                                                              28
                                                                      303
2
    443
                126
                         8
                                93
                                      256
         219
                                              45
                                                     171
                                                              36
                                                                      402
3
    461
         282
                 66
                         9
                               126
                                      211
                                              37
                                                     164
                                                              33
                                                                      381
    479
         319
                116
                         7
                                90
                                      117
                                              42
                                                     197
                                                              36
                                                                      295
```

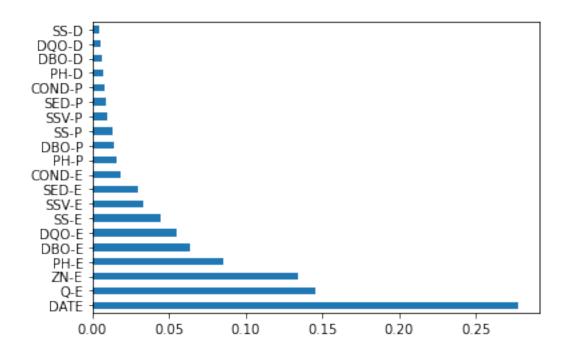
```
COND-S RD-DBO-P RD-SS-P
                               RD-SED-P
                                          RD-DBO-S
                                                    RD-DQO-S
                                                               RD-DBO-G \
0
      372
                 314
                          165
                                     104
                                               184
                                                          233
                                                                     155
1
      334
                 314
                          143
                                     111
                                               184
                                                           37
                                                                     155
2
                 100
                                     108
                                                          165
                                                                      95
      322
                          196
                                               131
                 314
3
      349
                          183
                                     111
                                               184
                                                          153
                                                                     114
4
      301
                 314
                          157
                                     118
                                               125
                                                          216
                                                                      94
   RD-DQO-G RD-SS-G
                      RD-SED-G
0
        134
                  126
                              0
                             26
1
        101
                  92
2
        158
                  101
                              0
3
                   82
        121
                             37
4
         78
                   61
                              0
```

[5 rows x 39 columns]

# 2 Feature importance







# 3 Clustering

```
[6]: from sklearn.datasets import make_blobs
     from sklearn.cluster import KMeans
     from sklearn.metrics import silhouette_samples, silhouette_score
     import matplotlib.pyplot as plt
     import matplotlib.cm as cm
     import numpy as np
     from sklearn.cluster import AgglomerativeClustering
     from sklearn.cluster import DBSCAN
     import time
     def do_sse(X, cluster_labels, n_clusters, model):
         cluster_centers = [X[cluster_labels == i].mean(axis=0) for i in_
     →range(n_clusters)]
         clusterwise_sse = [0, 0, 0, 0, 0, 0]
         for point, label in zip(X, cluster_labels):
             clusterwise_sse[label] += np.square(point - cluster_centers[label]).
      ⇒sum()
         clusterwise_sse_avg = np.mean(clusterwise_sse)
         return clusterwise_sse_avg
     def do_cluster_analysis(name):
```

```
# To find out the optimal number of clusters we can search through range of \Box
\rightarrow clusters.
  range_n_clusters = [2, 3, 4, 5, 6]
  for n_clusters in range_n_clusters:
→print('=====
     print('n_clusters = ', n_clusters)
start_time = time.time()
     # Create a subplot with 1 row and 2 columns
     fig, (ax1, ax2) = plt.subplots(1, 2)
     fig.set_size_inches(18, 7)
     # The 1st subplot is the silhouette plot
     # The silhouette coefficient can range from -1, 1
     # but in this example code all lie within [-0.1, 1]
     ax1.set_xlim([-0.1, 1])
     # # The (n_clusters+1)*10 is for inserting blank space between
     # silhouette plots of individual clusters, to demarcate them
     # clearly.
     ax1.set_ylim([0, len(X) + (n_clusters + 1) * 10])
     #Apply k-means
     clusterer = KMeans(n_clusters, random_state=0)
     cluster_labels = clusterer.fit_predict(X)
     # The silhouette_score gives the average value for all the
     # samples. This gives a perspective into the density and
     # separation of the formed clusters
     silhouette_avg = silhouette_score(X, cluster_labels)
# Print the values
     #
print("For n_clusters =", n_clusters, "The average silhouette_score is :

→", silhouette_avg)
```

```
print("For n_clusters =", n_clusters, "The average SSE is :", do_sse(X,__
→clusterer.labels_, n_clusters, clusterer))
      # Compute the silhouette scores for each sample
      sample_silhouette_values = silhouette_samples(X, cluster_labels)
      y lower = 10
      for i in range(n_clusters):
          # Aggregate the silhouette scores for samples belonging to
          # cluster i, and sort them
# Create the plot
# Aggregate the silhouette scores for samples belonging to
          # cluster i, and sort them
          ith_cluster_silhouette_values = __
→sample_silhouette_values[cluster_labels == i]
         ith_cluster_silhouette_values.sort()
         size_cluster_i = ith_cluster_silhouette_values.shape[0]
         y_upper = y_lower + size_cluster_i
         color = cm.nipy_spectral(float(i) / n_clusters)
         ax1.fill_betweenx(np.arange(y_lower, y_upper),
                          0, ith_cluster_silhouette_values,
                          facecolor=color, edgecolor=color,
                          alpha=0.7)
          # Label the silhouette plots with their cluster numbers at the
          # mi.d.d.l.e.
         ax1.text(-0.05, y_lower + 0.5 * size_cluster_i, str(i))
          # Compute the new y_lower for next plot
         y_lower = y_upper + 10 # 10 for the 0 samples
         ax1.set_title("The silhouette plot for the various clusters.")
         ax1.set_xlabel("The silhouette coefficient values")
         ax1.set_ylabel("Cluster label")
          # The vertical line for average silhouette score of all the
          # values
```

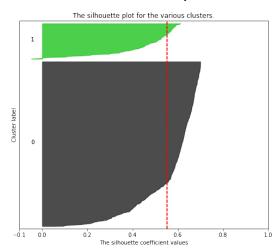
```
ax1.axvline(x=silhouette_avg, color="red", linestyle="--")
            ax1.set_yticks([]) # Clear the yaxis labels / ticks
            ax1.set_xticks([-0.1, 0, 0.2, 0.4, 0.6, 0.8, 1])
            # 2nd Plot showing the actual clusters formed
            colors = cm.nipy_spectral(cluster_labels.astype(float) / n_clusters)
            ax2.scatter(X[:, 0],
                        X[:, 1],
                        marker='.',
                        s = 30,
                        lw=0,
                        alpha=0.7,
                        c=colors,
                        edgecolor='k')
            # Labeling the clusters by centers
            centers = clusterer.cluster_centers_
            # Draw white circles at cluster centers
            ax2.scatter(centers[:, 0],
                        centers[:, 1],
                        marker='o',
                        c="white",
                        alpha=1,
                        s = 200,
                        edgecolor='k')
            for i, c in enumerate(centers):
                ax2.scatter(c[0],
                            c[1],
                            marker='$%d$' % i,
                            alpha=1,
                            s = 50,
                             edgecolor='k')
            ax2.set_title("The visualization of the clustered data.")
            ax2.set_xlabel("Feature space for the 1st feature")
            ax2.set_ylabel("Feature space for the 2nd feature")
            plt.suptitle(("Silhouette analysis for KMeans clustering on sample⊔
\rightarrowdata with n_clusters = %d" % n_clusters),
                         fontsize=14,
                         fontweight='bold')
        # Time to run
        print("--- %s seconds ---" % (time.time() - start_time))
#################
```

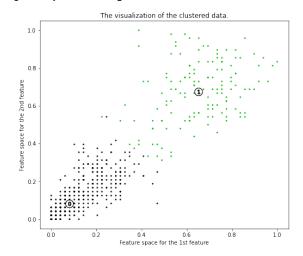
```
# Sales
################
print('sales')
X = pca_data_sales
min max scaler = preprocessing.MinMaxScaler()
x scaled = min max scaler.fit transform(X)
X = x \text{ scaled}
do_cluster_analysis('sales')
##################
# Water
#################
print('water')
X = pca data water
min_max_scaler = preprocessing.MinMaxScaler()
x scaled = min max scaler.fit transform(X)
X = x \text{ scaled}
do cluster analysis('water')
#################
# Seoul
#################
print('seoul')
X = pca_data_seoul
min_max_scaler = preprocessing.MinMaxScaler()
x_scaled = min_max_scaler.fit_transform(X)
X = x \text{ scaled}
do_cluster_analysis('seoul')
1111
sales
```

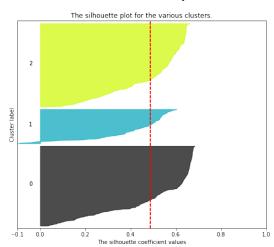
```
IIIII
n clusters = 2
______
For n_clusters = 2 The average silhouette_score is: 0.5529922804905653
For n_{clusters} = 2 The average SSE is : 14.437368116537462
--- 0.39674830436706543 seconds ---
_____
n_{clusters} = 3
______
For n_clusters = 3 The average silhouette_score is: 0.488051563750343
For n_{clusters} = 3 The average SSE is : 8.004891084595682
--- 0.3482513427734375 seconds ---
______
n clusters = 4
______
For n_clusters = 4 The average silhouette_score is: 0.4956690385768799
For n_clusters = 4 The average SSE is : 6.000403406587895
--- 0.36387038230895996 seconds ---
______
n clusters = 5
______
For n_clusters = 5 The average silhouette_score is: 0.48706090844597216
For n_{clusters} = 5 The average SSE is : 4.577621604668537
--- 0.3974940776824951 seconds ---
_____
n clusters = 6
______
For n_clusters = 6 The average silhouette_score is : 0.4905602367765982
For n_{clusters} = 6 The average SSE is : 3.540858712458992
--- 0.4951903820037842 seconds ---
IIII
water
```

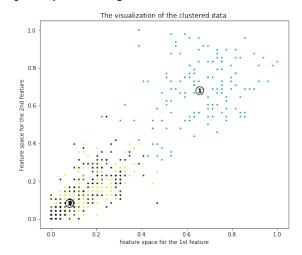
```
n clusters = 2
______
For n_clusters = 2 The average silhouette_score is: 0.19182821192769825
For n_{clusters} = 2 The average SSE is : 23.774174486620684
--- 0.2271566390991211 seconds ---
_____
n_{clusters} = 3
______
For n_clusters = 3 The average silhouette_score is: 0.18095097792392195
For n_{clusters} = 3 The average SSE is : 20.271440855256856
--- 0.2882091999053955 seconds ---
_____
n clusters = 4
For n_clusters = 4 The average silhouette_score is: 0.1962198321867441
For n_{clusters} = 4 The average SSE is : 17.68019667536556
--- 0.3564331531524658 seconds ---
_____
n_{clusters} = 5
_____
For n_clusters = 5 The average silhouette_score is: 0.19376529853466307
For n clusters = 5 The average SSE is : 15.661026408267285
--- 0.5259983539581299 seconds ---
______
n_{clusters} = 6
For n_clusters = 6 The average silhouette_score is: 0.1979742286699438
For n_{clusters} = 6 The average SSE is : 14.219162585579324
--- 0.42758846282958984 seconds ---
\Pi\Pi\Pi
```

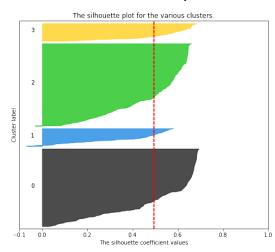
```
seoul
n_{clusters} = 2
For n_clusters = 2 The average silhouette_score is: 0.2736422972611256
For n_{clusters} = 2 The average SSE is : 297.7696053888172
--- 5.6746766567230225 seconds ---
______
n clusters = 3
For n_clusters = 3 The average silhouette_score is: 0.260409768356324
For n clusters = 3 The average SSE is : 237.01495785978295
--- 5.756635904312134 seconds ---
n_{clusters} = 4
______
For n_clusters = 4 The average silhouette_score is: 0.2749784228827367
For n_{clusters} = 4 The average SSE is : 191.5564379329348
--- 7.438884973526001 seconds ---
______
n_{clusters} = 5
______
For n clusters = 5 The average silhouette score is: 0.2715519364075326
For n_{clusters} = 5 The average SSE is : 163.49507869017359
--- 6.142277956008911 seconds ---
_______
n_{clusters} = 6
______
For n_clusters = 6 The average silhouette_score is: 0.263011224680275
For n_{clusters} = 6 The average SSE is : 145.85463685892572
--- 6.458942413330078 seconds ---
```

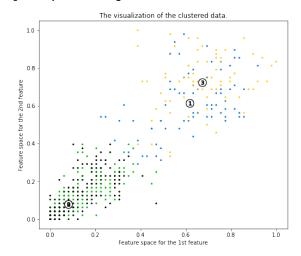


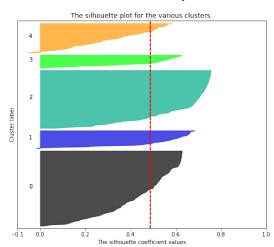


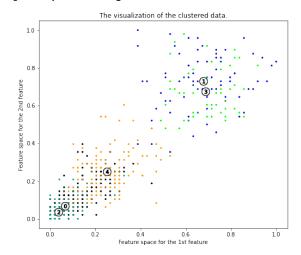


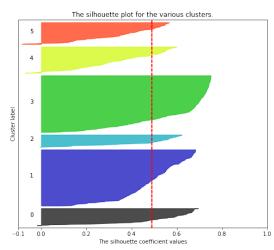


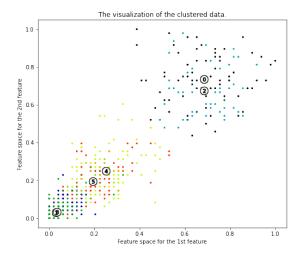


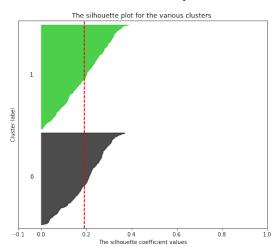


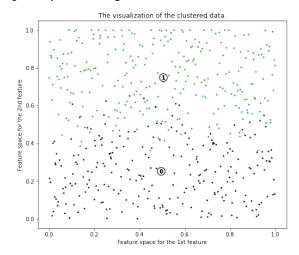




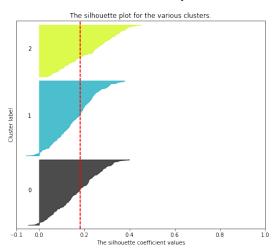


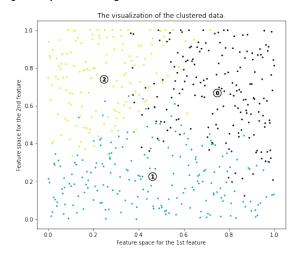


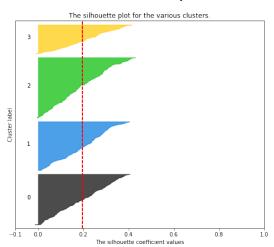


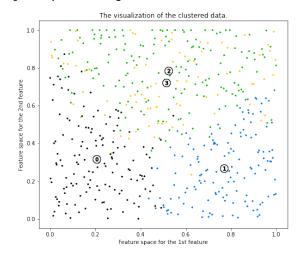


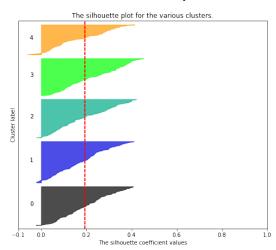
Silhouette analysis for KMeans clustering on sample data with  $n_c$ clusters = 3

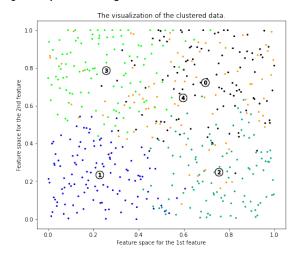


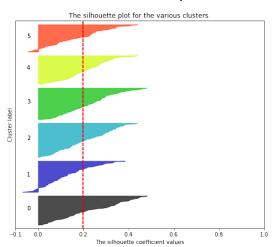


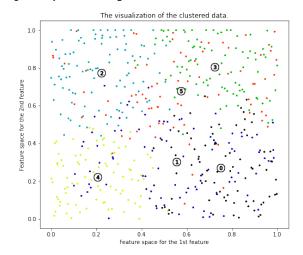




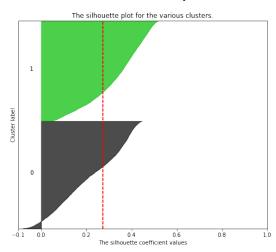


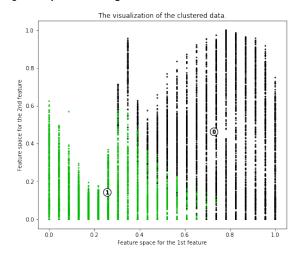


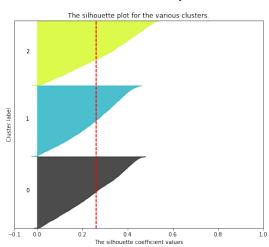


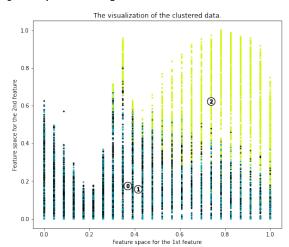


Silhouette analysis for KMeans clustering on sample data with n\_clusters = 2

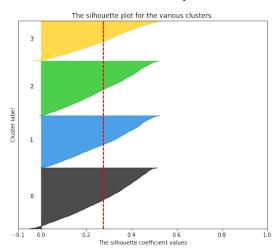


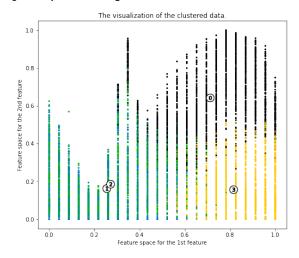




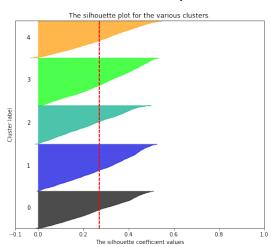


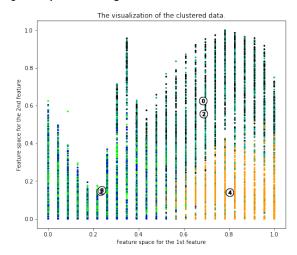
Silhouette analysis for KMeans clustering on sample data with n\_clusters = 4



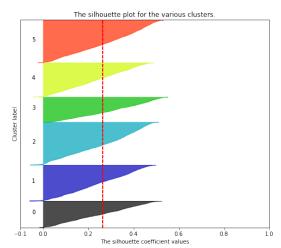


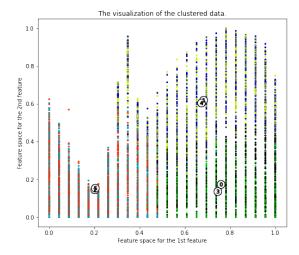
Silhouette analysis for KMeans clustering on sample data with  $n_c$ lusters = 5





Silhouette analysis for KMeans clustering on sample data with n\_clusters = 6





[]:

# 19075153 O'Leary PartA1 DB

October 16, 2021

```
[1]: import pandas
     from sklearn.model_selection import train_test_split
     import matplotlib.pyplot as plt
     import warnings
     from pandas.plotting import scatter_matrix
     import seaborn as sns
     from sklearn.model_selection import cross_val_score
     from sklearn.tree import DecisionTreeClassifier
     from sklearn.metrics import classification_report, confusion_matrix
     from sklearn import tree
     from sklearn.feature_selection import SelectKBest
     from sklearn.feature_selection import chi2
     from numpy import set_printoptions
     from sklearn.decomposition import PCA
     from sklearn import preprocessing
     warnings.filterwarnings('ignore')
```

## 1 Data load and pre-processing

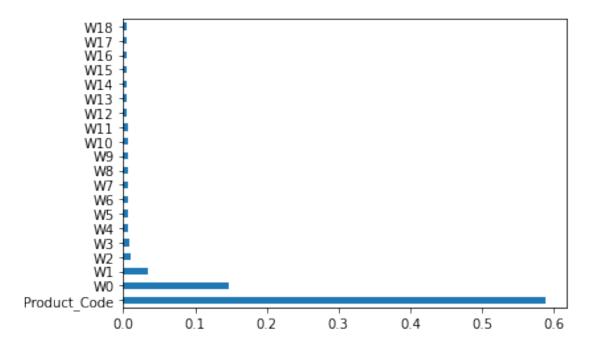
```
print(rawdata_sales.shape)
print(rawdata_sales.head())
#################
# load data seoul
#################
path_seoul = "/mnt/c/Users/T828808/Study/AUT/COMP809/Ass2/SeoulBikeData.csv"
rawdata_seoul = pandas.read_csv(path_seoul)
# categorise everything and create array
list_of_columns_seoul = rawdata_seoul.columns
rawdata_seoul[list_of_columns_seoul] = rawdata_seoul[list_of_columns_seoul].
 →apply(lambda col:pandas.Categorical(col).codes)
# Create array
array_seoul = rawdata_seoul.values
predictors_seoul = array_seoul[:, 0:14]
# Print some stats
print(rawdata_seoul.shape)
print(rawdata_seoul.head())
##################
# load data water
##################
path_water = "/mnt/c/Users/T828808/Study/AUT/COMP809/Ass2/water-treatment.data"
rawdata_water = pandas.read_csv(path_water)
rawdata_water.columns =__
 # categorise everything and create array
list of columns water = rawdata water.columns
rawdata_water[list_of_columns_water] = rawdata_water[list_of_columns_water].
 →apply(lambda col:pandas.Categorical(col).codes)
# Create array
array_water = rawdata_water.values
predictors_water = array_water[:, 0:39]
# Print some stats
print(rawdata_water.shape)
print(rawdata_water.head())
(811, 107)
  Product_Code W0 W1 W2 W3 W4 W5 W6 W7
                                             W8 ... Normalized 42 \
0
            0
              11 12 10
                           8 13 12 14 21
                                                               3
                                              6
                7 6
                           2
                              7
                                                              17
1
           111
                      3
                                  1
                                      6
                                         3
                                              3 ...
2
           222
               7 11
                      8 9 10
                                   8 7 13 12 ...
                                                              24
3
           331 12
                    8 13
                          5
                               9
                                      9 13 13
                                                              37
                    5 13 11
                               6
                                   7
                                      9 14
           442
               8
                                              9
                                                              24
  Normalized 43 Normalized 44 Normalized 45 Normalized 46 Normalized 47 \
             20
                          26
                                        35
                                                      46
```

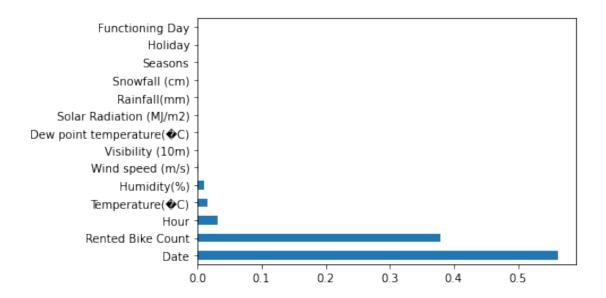
```
38
                                47
                                                 7
                                                                                  35
1
                                                                  6
2
               83
                                16
                                                 15
                                                                 32
                                                                                  40
3
               45
                                 4
                                                                 20
                                                                                  30
                                                 9
4
               51
                                25
                                                 56
                                                                 16
                                                                                  15
   Normalized 48
                   Normalized 49
                                    Normalized 50
                                                     Normalized 51
                                13
                                                 7
                                                                 35
0
               16
                                 7
               44
                                                 55
                                                                  0
1
2
               82
                                41
                                                 41
                                                                 32
3
               65
                                31
                                                 25
                                                                 31
4
                8
                                49
                                                 29
                                                                 36
[5 rows x 107 columns]
(8760, 14)
   Date Rented Bike Count
                              Hour
                                     Temperature(C) Humidity(%) \
                         253
                                  0
0
                                                   111
                                                                  28
1
     11
                         203
                                  1
                                                   108
                                                                  29
2
     11
                         172
                                  2
                                                   103
                                                                  30
3
     11
                         106
                                  3
                                                   101
                                                                  31
4
                          77
                                  4
                                                   103
                                                                  27
     11
   Wind speed (m/s) Visibility (10m)
                                           Dew point temperature(C) \
0
                   22
                                    1788
                                                                   114
                   8
                                    1788
                                                                   114
1
2
                   10
                                    1788
                                                                   113
3
                   9
                                    1788
                                                                   114
4
                   23
                                    1788
                                                                   104
   Solar Radiation (MJ/m2)
                              Rainfall(mm)
                                                                         Holiday \
                                              Snowfall (cm)
                                                               Seasons
0
                           0
                                           0
                                                                      3
                                                                               1
                                                            0
                                                                      3
                           0
                                           0
1
                                                                               1
                                                                      3
2
                           0
                                           0
                                                            0
                                                                               1
3
                           0
                                                            0
                                                                      3
                                                                               1
                                           0
4
                           0
                                           0
                                                            0
                                                                      3
                                                                                1
   Functioning Day
0
1
                   1
2
                   1
3
                   1
                   1
4
(526, 39)
   DATE Q-E
               ZN-E
                      PH-E
                            DBO-E
                                    DQO-E
                                            SS-E
                                                   SSV-E
                                                          SED-E
                                                                  COND-E
    197
                         6
                               204
                                       169
                                              57
                                                              50
         330
                116
                                                     201
                                                                      409
0
1
    427
           99
                143
                         5
                               204
                                      231
                                              42
                                                     208
                                                              28
                                                                      303
2
    443
                126
                         8
                                93
                                      256
         219
                                              45
                                                     171
                                                              36
                                                                      402
3
    461
         282
                 66
                         9
                               126
                                      211
                                              37
                                                     164
                                                              33
                                                                      381
    479
         319
                116
                         7
                                90
                                      117
                                              42
                                                     197
                                                              36
                                                                      295
```

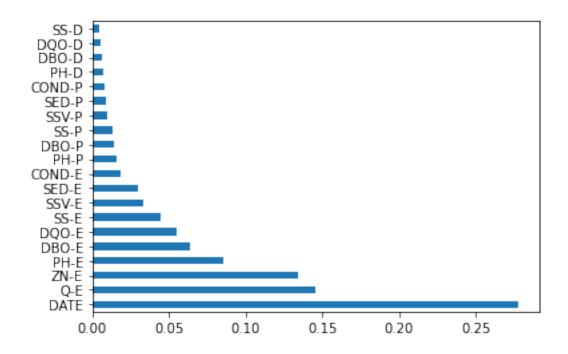
```
COND-S RD-DBO-P RD-SS-P
                               RD-SED-P
                                          RD-DBO-S
                                                    RD-DQO-S
                                                               RD-DBO-G \
0
      372
                 314
                          165
                                     104
                                               184
                                                          233
                                                                     155
1
      334
                 314
                          143
                                     111
                                               184
                                                           37
                                                                     155
2
                 100
                                     108
                                                          165
                                                                      95
      322
                          196
                                               131
                 314
3
      349
                          183
                                     111
                                               184
                                                          153
                                                                     114
4
      301
                 314
                          157
                                     118
                                               125
                                                          216
                                                                      94
   RD-DQO-G RD-SS-G
                      RD-SED-G
0
        134
                  126
                              0
                             26
1
        101
                  92
2
        158
                  101
                              0
3
                   82
        121
                             37
4
         78
                   61
                              0
```

[5 rows x 39 columns]

# 2 Feature importance







## 3 Clustering

```
[12]: from sklearn.datasets import make_blobs
      from sklearn.cluster import KMeans
      from sklearn.metrics import silhouette_samples, silhouette_score
      import matplotlib.pyplot as plt
      import matplotlib.cm as cm
      import numpy as np
      from sklearn.cluster import AgglomerativeClustering
      from sklearn.cluster import DBSCAN
      import time
      def do_sse(X, cluster_labels, n_clusters, model):
          cluster_centers = [X[cluster_labels == i].mean(axis=0) for i in_
       →range(n_clusters)]
          clusterwise_sse = [0, 0, 0, 0, 0, 0]
          for point, label in zip(X, cluster_labels):
              clusterwise_sse[label] += np.square(point - cluster_centers[label]).
       ⇒sum()
          clusterwise_sse_avg = np.mean(clusterwise_sse)
          return clusterwise_sse_avg
      def do_cluster_analysis(name):
```

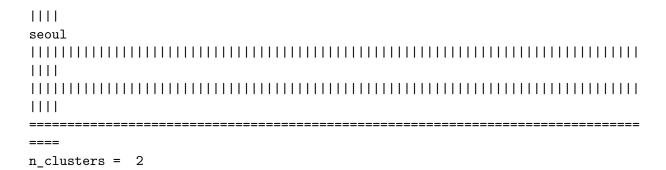
```
# To find out the optimal number of clusters we can search through range of \Box
\rightarrow clusters.
  range_n_clusters = [2, 3, 4, 5, 6]
  for n_clusters in range_n_clusters:
→print('======
      print('n_clusters = ', n_clusters)
start_time = time.time()
      # Create a subplot with 1 row and 2 columns
      fig, (ax1, ax2) = plt.subplots(1, 2)
      fig.set_size_inches(18, 7)
      # The 1st subplot is the silhouette plot
      # The silhouette coefficient can range from -1, 1
      # but in this example code all lie within [-0.1, 1]
      ax1.set_xlim([-0.1, 1])
      # # The (n_clusters+1)*10 is for inserting blank space between
      # silhouette plots of individual clusters, to demarcate them
      # clearly.
      ax1.set_ylim([0, len(X) + (n_clusters + 1) * 10])
      #Apply DBSCAN and set the EPS
      eps = 0
      if name == 'sales':
          eps = 0.2
      elif name == 'water':
          eps = 0.3
      elif name == 'seoul':
          eps = 0.1
      clusterer = DBSCAN(eps, min_samples=n_clusters, metric='euclidean')
      cluster_labels = clusterer.fit_predict(X)
      # The silhouette_score gives the average value for all the
      # samples. This gives a perspective into the density and
      # separation of the formed clusters
      try:
          silhouette_avg = silhouette_score(X, cluster_labels)
```

```
# Print the values
print("For n_clusters =", n_clusters, "The average silhouette_score⊔
→is :", silhouette_avg)
        print("For n_clusters =", n_clusters, "The average SSE is :", _
→do_sse(X, clusterer.labels_, n_clusters, clusterer))
     except:
        print('DBSCAN EXCEPTION')
        break
     # Compute the silhouette scores for each sample
     sample_silhouette_values = silhouette_samples(X, cluster_labels)
     v lower = 10
     for i in range(n clusters):
        # Aggregate the silhouette scores for samples belonging to
        # cluster i, and sort them
        #
# Create the plot
# Aggregate the silhouette scores for samples belonging to
        # cluster i, and sort them
        ith cluster silhouette values = ____
→sample_silhouette_values[cluster_labels == i]
        ith_cluster_silhouette_values.sort()
        size cluster i = ith cluster silhouette values.shape[0]
        y_upper = y_lower + size_cluster_i
        color = cm.nipy spectral(float(i) / n clusters)
        ax1.fill_betweenx(np.arange(y_lower, y_upper),
                      0, ith cluster silhouette values,
                      facecolor=color, edgecolor=color,
                      alpha=0.7)
        # Label the silhouette plots with their cluster numbers at the
        # middle
        ax1.text(-0.05, y_lower + 0.5 * size_cluster_i, str(i))
```

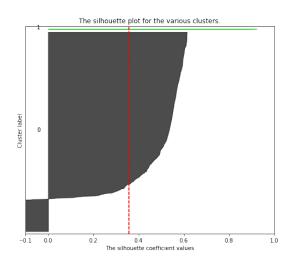
```
# Compute the new y_lower for next plot
        y_lower = y_upper + 10 # 10 for the 0 samples
        ax1.set_title("The silhouette plot for the various clusters.")
        ax1.set_xlabel("The silhouette coefficient values")
        ax1.set_ylabel("Cluster label")
         # The vertical line for average silhouette score of all the
         # values
        ax1.axvline(x=silhouette_avg, color="red", linestyle="--")
        ax1.set yticks([]) # Clear the yaxis labels / ticks
        ax1.set_xticks([-0.1, 0, 0.2, 0.4, 0.6, 0.8, 1])
         # 2nd Plot showing the actual clusters formed
         colors = cm.nipy_spectral(cluster_labels.astype(float) / n_clusters)
         ax2.scatter(X[:, 0],
                 X[:, 1],
                 marker='.',
                 s = 30,
                 lw=0,
                 alpha=0.7,
                 c=colors,
                 edgecolor='k')
         # Labeling the clusters by centers
        centers = clusterer.labels
      # Time to run
     print("--- %s seconds ---" % (time.time() - start_time))
##################
# Sales
##################
print('sales')
X = pca data sales
min_max_scaler = preprocessing.MinMaxScaler()
x_scaled = min_max_scaler.fit_transform(X)
X = x_scaled
do_cluster_analysis('sales')
################
```

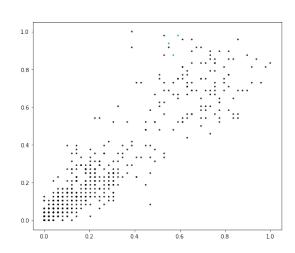
```
# Water
################
print('water')
X = pca_data_water
min max scaler = preprocessing.MinMaxScaler()
x scaled = min max scaler.fit transform(X)
X = x \text{ scaled}
do cluster analysis('water')
##################
# Seoul
##################
print('seoul')
X = pca data seoul
min_max_scaler = preprocessing.MinMaxScaler()
x scaled = min max scaler.fit transform(X)
X = x \text{ scaled}
do cluster analysis('seoul')
\Pi\Pi\Pi
sales
n clusters = 2
For n_clusters = 2 The average silhouette_score is : 0.35714256858302806
For n clusters = 2 The average SSE is : 27.772162712889894
--- 0.346055269241333 seconds ---
n clusters = 3
```

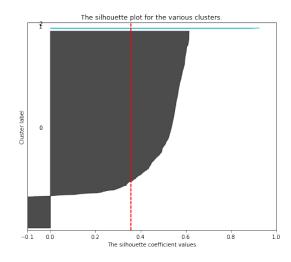
```
For n_clusters = 3 The average silhouette_score is: 0.35714256858302806
For n_{clusters} = 3 The average SSE is : 27.772162712889894
--- 0.23154139518737793 seconds ---
_____
n_{clusters} = 4
For n_clusters = 4 The average silhouette_score is: 0.35714256858302806
For n_clusters = 4 The average SSE is : nan
--- 0.17214298248291016 seconds ---
______
n clusters = 5
For n_clusters = 5 The average silhouette_score is : 0.35714256858302806
For n clusters = 5 The average SSE is : nan
--- 0.14641571044921875 seconds ---
n_{clusters} = 6
For n_clusters = 6 The average silhouette_score is: 0.35714256858302806
For n_clusters = 6 The average SSE is : nan
--- 0.1602458953857422 seconds ---
\Pi\Pi\Pi
n_{clusters} = 2
______
For n_clusters = 2 The average silhouette_score is: 0.01814249370553166
DBSCAN EXCEPTION
```

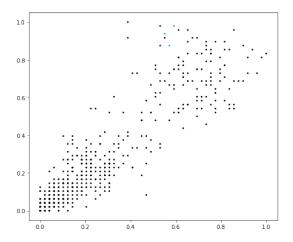


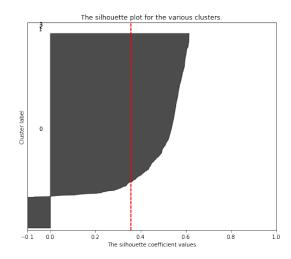
For n\_clusters = 2 The average silhouette\_score is : -0.48965343976481296 DBSCAN EXCEPTION

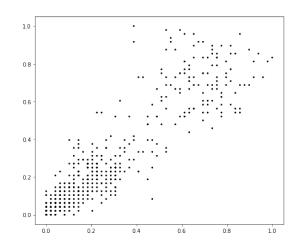


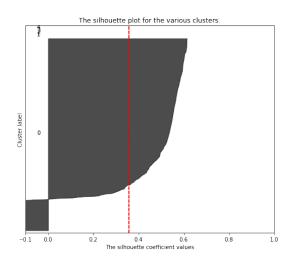


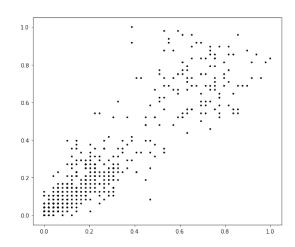


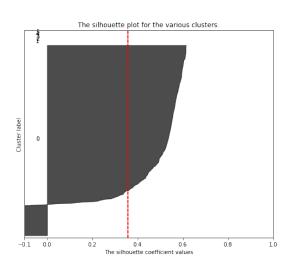


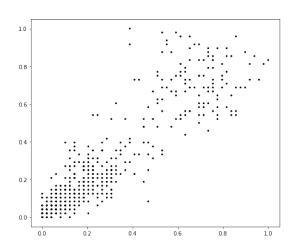


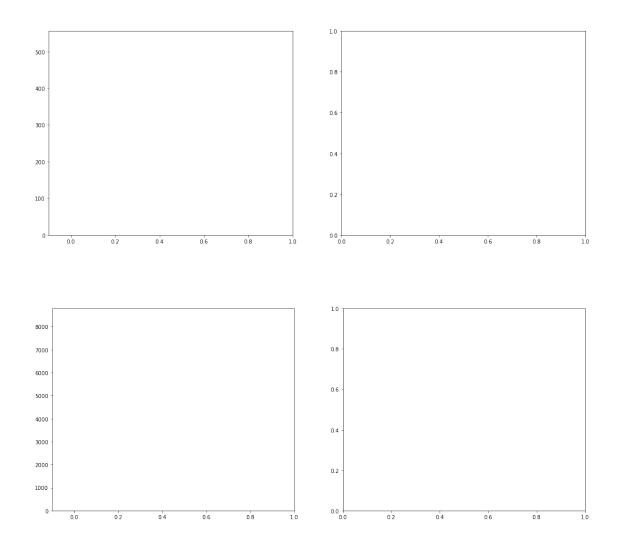












[]:

# 19075153 O'Leary PartA1 AM

October 16, 2021

```
[1]: import pandas
     from sklearn.model_selection import train_test_split
     import matplotlib.pyplot as plt
     import warnings
     from pandas.plotting import scatter_matrix
     import seaborn as sns
     from sklearn.model_selection import cross_val_score
     from sklearn.tree import DecisionTreeClassifier
     from sklearn.metrics import classification_report, confusion_matrix
     from sklearn import tree
     from sklearn.feature_selection import SelectKBest
     from sklearn.feature_selection import chi2
     from numpy import set_printoptions
     from sklearn.decomposition import PCA
     from sklearn import preprocessing
     warnings.filterwarnings('ignore')
```

## 1 Data load and pre-processing

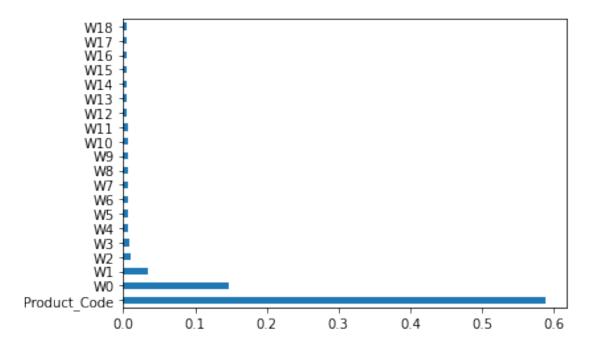
```
print(rawdata_sales.shape)
print(rawdata_sales.head())
#################
# load data seoul
#################
path_seoul = "/mnt/c/Users/T828808/Study/AUT/COMP809/Ass2/SeoulBikeData.csv"
rawdata_seoul = pandas.read_csv(path_seoul)
# categorise everything and create array
list_of_columns_seoul = rawdata_seoul.columns
rawdata_seoul[list_of_columns_seoul] = rawdata_seoul[list_of_columns_seoul].
 →apply(lambda col:pandas.Categorical(col).codes)
# Create array
array_seoul = rawdata_seoul.values
predictors_seoul = array_seoul[:, 0:14]
# Print some stats
print(rawdata_seoul.shape)
print(rawdata_seoul.head())
##################
# load data water
##################
path_water = "/mnt/c/Users/T828808/Study/AUT/COMP809/Ass2/water-treatment.data"
rawdata_water = pandas.read_csv(path_water)
rawdata_water.columns =__
 # categorise everything and create array
list of columns water = rawdata water.columns
rawdata_water[list_of_columns_water] = rawdata_water[list_of_columns_water].
 →apply(lambda col:pandas.Categorical(col).codes)
# Create array
array_water = rawdata_water.values
predictors_water = array_water[:, 0:39]
# Print some stats
print(rawdata_water.shape)
print(rawdata_water.head())
(811, 107)
  Product_Code W0 W1 W2 W3 W4 W5 W6 W7
                                             W8 ... Normalized 42 \
0
            0
              11 12 10
                           8 13 12 14 21
                                                               3
                                              6
                7 6
                           2
                              7
                                                              17
1
           111
                      3
                                  1
                                      6
                                         3
                                              3 ...
2
           222
               7 11
                      8 9 10
                                   8 7 13 12 ...
                                                              24
3
           331 12
                    8 13
                          5
                               9
                                      9 13 13
                                                              37
                    5 13 11
                               6
                                   7
                                      9 14
           442
               8
                                              9
                                                              24
  Normalized 43 Normalized 44 Normalized 45 Normalized 46 Normalized 47 \
             20
                          26
                                        35
                                                      46
```

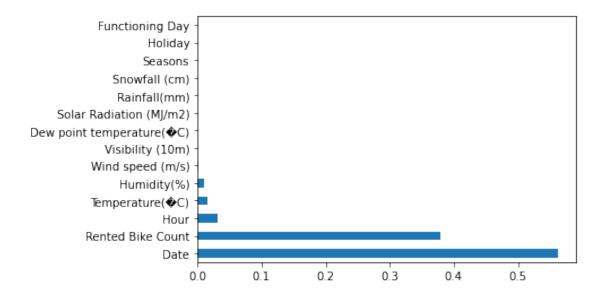
```
38
                                47
                                                 7
                                                                                  35
1
                                                                  6
2
               83
                                16
                                                 15
                                                                 32
                                                                                  40
3
               45
                                 4
                                                                 20
                                                                                  30
                                                 9
4
               51
                                25
                                                 56
                                                                 16
                                                                                  15
   Normalized 48
                   Normalized 49
                                    Normalized 50
                                                     Normalized 51
                                13
                                                 7
                                                                 35
0
               16
                                 7
               44
                                                 55
                                                                  0
1
2
               82
                                41
                                                 41
                                                                 32
3
               65
                                31
                                                 25
                                                                 31
4
                8
                                49
                                                 29
                                                                 36
[5 rows x 107 columns]
(8760, 14)
   Date Rented Bike Count
                              Hour
                                     Temperature(C) Humidity(%) \
                         253
                                  0
0
                                                   111
                                                                  28
1
     11
                         203
                                  1
                                                   108
                                                                  29
2
     11
                         172
                                  2
                                                   103
                                                                  30
3
     11
                         106
                                  3
                                                   101
                                                                  31
4
                          77
                                  4
                                                   103
                                                                  27
     11
   Wind speed (m/s) Visibility (10m)
                                           Dew point temperature(C) \
0
                   22
                                    1788
                                                                   114
                   8
                                    1788
                                                                   114
1
2
                   10
                                    1788
                                                                   113
3
                   9
                                    1788
                                                                   114
4
                   23
                                    1788
                                                                   104
   Solar Radiation (MJ/m2)
                              Rainfall(mm)
                                                                         Holiday \
                                              Snowfall (cm)
                                                               Seasons
0
                           0
                                           0
                                                                      3
                                                                               1
                                                            0
                                                                      3
                           0
                                           0
1
                                                                               1
                                                                      3
2
                           0
                                           0
                                                            0
                                                                               1
3
                           0
                                                            0
                                                                      3
                                                                               1
                                           0
4
                           0
                                           0
                                                            0
                                                                      3
                                                                                1
   Functioning Day
0
1
                   1
2
                   1
3
                   1
                   1
4
(526, 39)
   DATE Q-E
               ZN-E
                      PH-E
                            DBO-E
                                    DQO-E
                                            SS-E
                                                   SSV-E
                                                          SED-E
                                                                  COND-E
    197
                         6
                               204
                                       169
                                              57
                                                              50
         330
                116
                                                     201
                                                                      409
0
1
    427
           99
                143
                         5
                               204
                                      231
                                              42
                                                     208
                                                              28
                                                                      303
2
    443
                126
                         8
                                93
                                      256
         219
                                              45
                                                     171
                                                              36
                                                                      402
3
    461
         282
                 66
                         9
                               126
                                      211
                                              37
                                                     164
                                                              33
                                                                      381
    479
         319
                116
                         7
                                90
                                      117
                                              42
                                                     197
                                                              36
                                                                      295
```

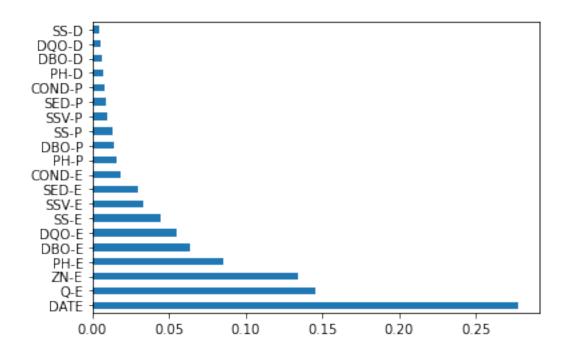
```
COND-S RD-DBO-P RD-SS-P
                               RD-SED-P
                                          RD-DBO-S
                                                    RD-DQO-S
                                                               RD-DBO-G \
0
      372
                 314
                          165
                                     104
                                               184
                                                          233
                                                                     155
1
      334
                 314
                          143
                                     111
                                               184
                                                           37
                                                                     155
2
                 100
                                     108
                                                          165
                                                                      95
      322
                          196
                                               131
                 314
3
      349
                          183
                                     111
                                               184
                                                          153
                                                                     114
4
      301
                 314
                          157
                                     118
                                               125
                                                          216
                                                                      94
   RD-DQO-G RD-SS-G
                      RD-SED-G
0
        134
                  126
                              0
                             26
1
        101
                  92
2
        158
                  101
                              0
3
                   82
        121
                             37
4
         78
                   61
                              0
```

[5 rows x 39 columns]

# 2 Feature importance







## 3 Clustering

```
[9]: from sklearn.datasets import make_blobs
     from sklearn.cluster import KMeans
     from sklearn.metrics import silhouette_samples, silhouette_score
     import matplotlib.pyplot as plt
     import matplotlib.cm as cm
     import numpy as np
     from sklearn.cluster import AgglomerativeClustering
     from sklearn.cluster import DBSCAN
     import time
     def do_sse(X, cluster_labels, n_clusters, model):
         cluster_centers = [X[cluster_labels == i].mean(axis=0) for i in_
     →range(n_clusters)]
         clusterwise_sse = [0, 0, 0, 0, 0, 0]
         for point, label in zip(X, cluster_labels):
             clusterwise_sse[label] += np.square(point - cluster_centers[label]).
      ⇒sum()
         clusterwise_sse_avg = np.mean(clusterwise_sse)
         return clusterwise_sse_avg
     def do_cluster_analysis(name):
```

```
# To find out the optimal number of clusters we can search through range of \Box
\rightarrow clusters.
  range n clusters = [2, 3, 4, 5, 6]
  for n_clusters in range_n_clusters:
→print('=====
     print('n_clusters = ', n_clusters)
start_time = time.time()
     # Create a subplot with 1 row and 2 columns
     fig, (ax1, ax2) = plt.subplots(1, 2)
     fig.set_size_inches(18, 7)
     # The 1st subplot is the silhouette plot
     # The silhouette coefficient can range from -1, 1
     # but in this example code all lie within [-0.1, 1]
     ax1.set_xlim([-0.1, 1])
     # # The (n_clusters+1)*10 is for inserting blank space between
     # silhouette plots of individual clusters, to demarcate them
     # clearly.
     ax1.set_ylim([0, len(X) + (n_clusters + 1) * 10])
     #Apply AgglomerativeClustering
     clusterer = AgglomerativeClustering(n_clusters, affinity='euclidean', __
→linkage='complete')
     cluster_labels = clusterer.fit_predict(X)
     # The silhouette score gives the average value for all the
     # samples. This gives a perspective into the density and
     # separation of the formed clusters
     silhouette_avg = silhouette_score(X, cluster_labels)
     #__
# Print the values
     #
print("For n_clusters =", n_clusters, "The average silhouette_score is :
→", silhouette_avg)
```

```
print("For n_clusters =", n_clusters, "The average SSE is :", do_sse(X,__
→clusterer.labels_, n_clusters, clusterer))
      # Compute the silhouette scores for each sample
      sample_silhouette_values = silhouette_samples(X, cluster_labels)
      y lower = 10
      for i in range(n_clusters):
          # Aggregate the silhouette scores for samples belonging to
          # cluster i, and sort them
# Create the plot
# Aggregate the silhouette scores for samples belonging to
          # cluster i, and sort them
          ith_cluster_silhouette_values = __
→sample_silhouette_values[cluster_labels == i]
         ith_cluster_silhouette_values.sort()
         size_cluster_i = ith_cluster_silhouette_values.shape[0]
         y_upper = y_lower + size_cluster_i
         color = cm.nipy_spectral(float(i) / n_clusters)
         ax1.fill_betweenx(np.arange(y_lower, y_upper),
                          0, ith_cluster_silhouette_values,
                          facecolor=color, edgecolor=color,
                          alpha=0.7)
          # Label the silhouette plots with their cluster numbers at the
          # mi.d.d.l.e.
         ax1.text(-0.05, y_lower + 0.5 * size_cluster_i, str(i))
          # Compute the new y_lower for next plot
         y_lower = y_upper + 10 # 10 for the 0 samples
         ax1.set_title("The silhouette plot for the various clusters.")
         ax1.set_xlabel("The silhouette coefficient values")
         ax1.set_ylabel("Cluster label")
          # The vertical line for average silhouette score of all the
          # values
```

```
ax1.axvline(x=silhouette_avg, color="red", linestyle="--")
      ax1.set_yticks([]) # Clear the yaxis labels / ticks
      ax1.set_xticks([-0.1, 0, 0.2, 0.4, 0.6, 0.8, 1])
      # 2nd Plot showing the actual clusters formed
      colors = cm.nipy_spectral(cluster_labels.astype(float) / n_clusters)
      ax2.scatter(X[:, 0],
             X[:, 1],
             marker='.',
             s = 30,
             lw=0.
             alpha=0.7,
             c=colors.
             edgecolor='k')
      # Labeling the clusters by centers
      centers = clusterer.labels_
    # Time to run
    print("--- %s seconds ---" % (time.time() - start_time))
#################
# Sales
##################
print('sales')
X = pca_data_sales
min_max_scaler = preprocessing.MinMaxScaler()
x_scaled = min_max_scaler.fit_transform(X)
X = x \text{ scaled}
do cluster_analysis('sales')
##################
# Water
#################
print('water')
X = pca_data_water
min_max_scaler = preprocessing.MinMaxScaler()
x_scaled = min_max_scaler.fit_transform(X)
X = x_scaled
```

```
do_cluster_analysis('water')
##################
# Seoul
#################
print('seoul')
X = pca data seoul
min_max_scaler = preprocessing.MinMaxScaler()
x scaled = min max scaler.fit transform(X)
X = x_scaled
do_cluster_analysis('seoul')
1111
sales
n clusters = 2
For n_clusters = 2 The average silhouette_score is: 0.5630813204653953
For n clusters = 2 The average SSE is : 14.907766709758254
--- 0.23120903968811035 seconds ---
_____
n_{clusters} = 3
______
For n_clusters = 3 The average silhouette_score is: 0.4517887084052137
For n_{clusters} = 3 The average SSE is : 8.755768394980814
--- 0.15660643577575684 seconds ---
n clusters = 4
______
For n_clusters = 4 The average silhouette_score is: 0.4537820793098297
```

```
For n_{clusters} = 4 The average SSE is : 6.962470134634124
--- 0.22800803184509277 seconds ---
______
n clusters = 5
For n_clusters = 5 The average silhouette_score is : 0.45281621283033274
For n clusters = 5 The average SSE is : 5.376949572658198
--- 0.23021531105041504 seconds ---
_____
n_{clusters} = 6
______
For n_clusters = 6 The average silhouette_score is: 0.427459801328905
For n_{clusters} = 6 The average SSE is : 5.164992693901558
--- 0.5414533615112305 seconds ---
1111
______
n clusters = 2
_______
For n_clusters = 2 The average silhouette_score is: 0.15524541375205828
For n_{clusters} = 2 The average SSE is : 24.894066528279865
--- 0.12308955192565918 seconds ---
n clusters = 3
For n_clusters = 3 The average silhouette_score is: 0.1227273605961021
For n_{clusters} = 3 The average SSE is : 22.316291857947885
--- 0.12271738052368164 seconds ---
______
n clusters = 4
______
```

```
For n_clusters = 4 The average silhouette_score is: 0.13617035449634593
For n_{clusters} = 4 The average SSE is : 20.056887615553745
--- 0.12484121322631836 seconds ---
n clusters = 5
______
For n_clusters = 5 The average silhouette_score is: 0.12186405302481013
For n_{clusters} = 5 The average SSE is : 18.775880768282853
--- 0.12403750419616699 seconds ---
_____
n clusters = 6
______
For n_clusters = 6 The average silhouette_score is: 0.1411477652760043
For n_{clusters} = 6 The average SSE is : 16.26094953544457
--- 0.13375568389892578 seconds ---
IIIII
seoul
_____
n_{clusters} = 2
_____
For n_clusters = 2 The average silhouette_score is: 0.24688690435967905
For n clusters = 2 The average SSE is : 308.6434248773903
--- 8.33217167854309 seconds ---
______
n_{clusters} = 3
For n_clusters = 3 The average silhouette_score is: 0.23314084347983294
For n_{clusters} = 3 The average SSE is : 253.88981532100146
--- 7.827468156814575 seconds ---
______
n_{clusters} = 4
______
```

#### ====

For n\_clusters = 4 The average silhouette\_score is : 0.2239192996437419

For  $n_{clusters} = 4$  The average SSE is : 223.3114014879127

--- 7.871132850646973 seconds ---

\_\_\_\_\_\_

#### ====

n clusters = 5

\_\_\_\_\_\_

#### \_\_\_\_

For n\_clusters = 5 The average silhouette\_score is : 0.2127806695469617

For n\_clusters = 5 The average SSE is : 186.38571116085453

--- 8.309257984161377 seconds ---

\_\_\_\_\_

#### ====

### $n_{clusters} = 6$

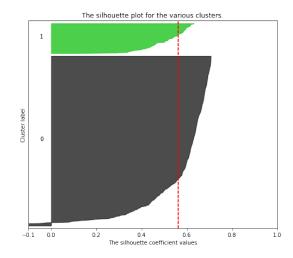
\_\_\_\_\_\_

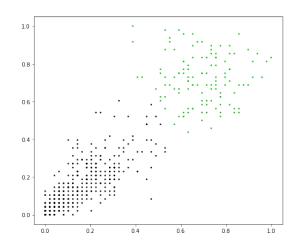
#### ====

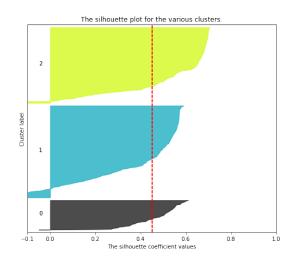
For n\_clusters = 6 The average silhouette\_score is : 0.20436498901055802

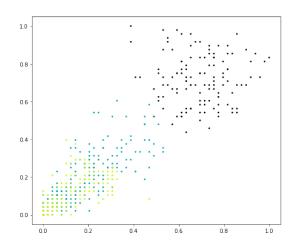
For  $n_{clusters} = 6$  The average SSE is : 168.10840550212362

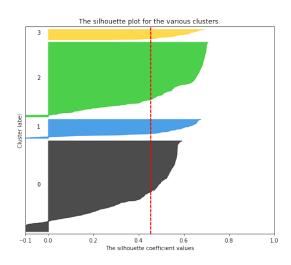
--- 9.070887804031372 seconds ---

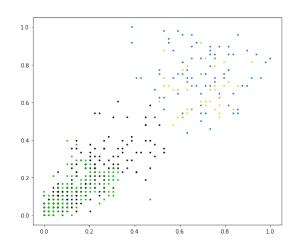


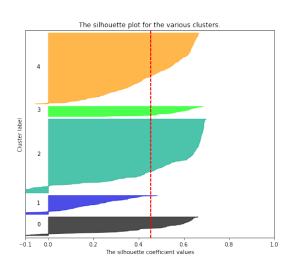


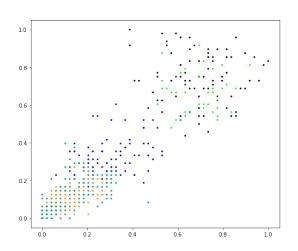


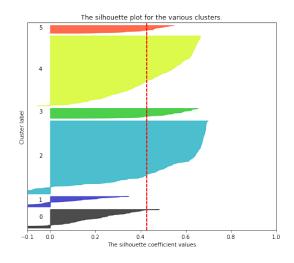


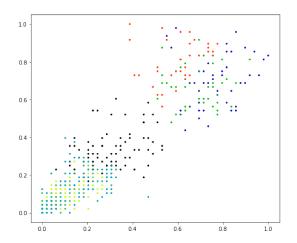


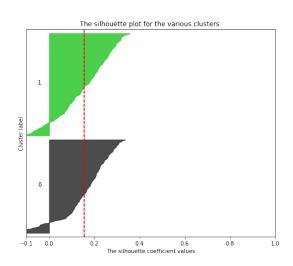


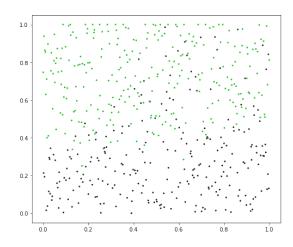


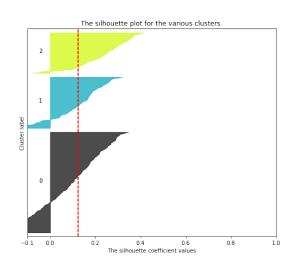


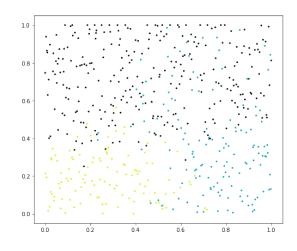


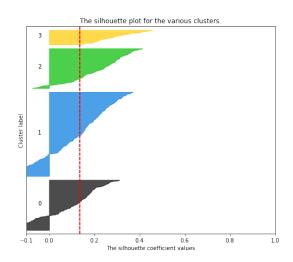


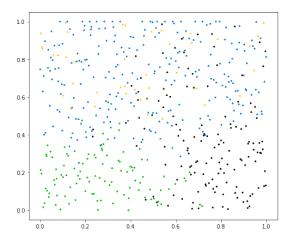


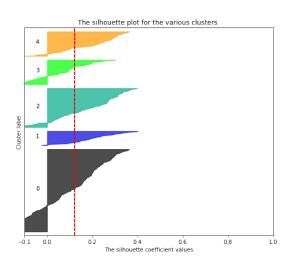


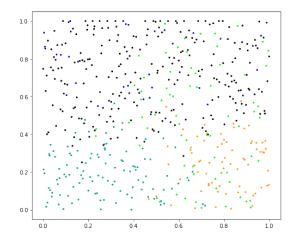


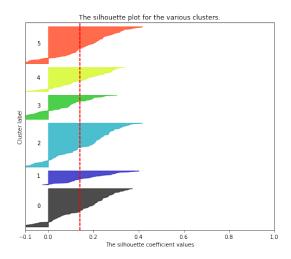


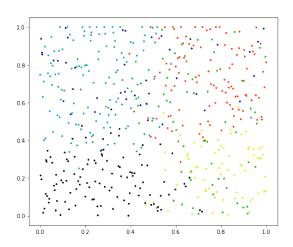


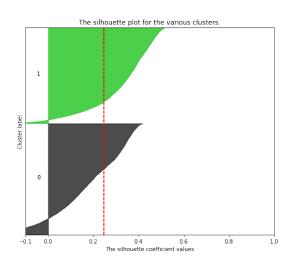


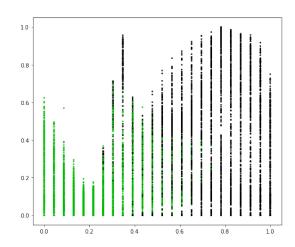


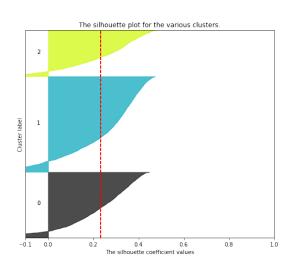


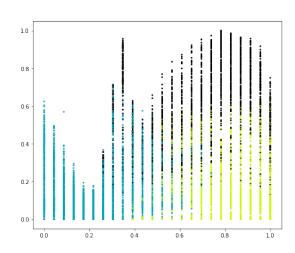


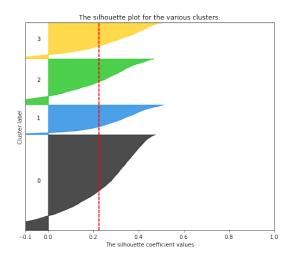


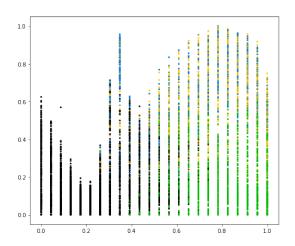


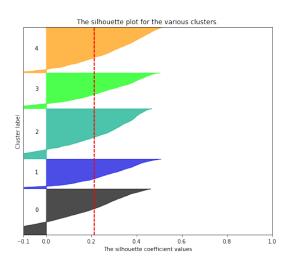


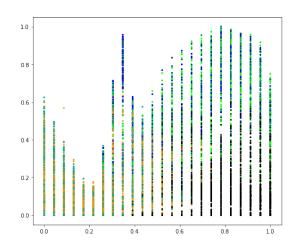


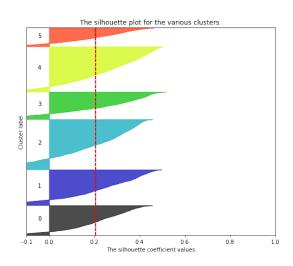


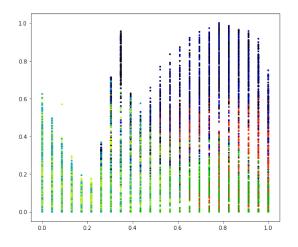












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