

# 1 Some Code

## 1.1 Outline of the algorithm

```
1  /*!
2  * @brief Build the DIIS error matrix.
3  *
4  * The formula for the error matrix at the \textit{i}th iteration is:
5  *  $e_i = F_i D_i S - S D_i F_i$ 
6  */
7  arma::mat build_error_matrix(const arma::mat &F,
8                               const arma::mat &D,
9                               const arma::mat &S) {
10     return (F*D*S) - (S*D*F);
11 }

1  /*!
2  * @brief Build the DIIS B matrix, or ‘‘A’’ in  $Ax = b$ .
3  */
4  arma::mat build_B_matrix(const deque< arma::mat > &e) {
5     int NErr = e.size();
6     arma::mat B(NErr + 1, NErr + 1);
7     B(NErr, NErr) = 0.0;
8     for (int a = 0; a < NErr; a++) {
9         B(a, NErr) = B(NErr, a) = -1.0;
10        for (int b = 0; b < a + 1; b++)
11            B(a, b) = B(b, a) = arma::dot(e[a].t(), e[b]);
12    }
13    return B;
14 }

1  /*!
2  * @brief Build the extrapolated Fock matrix from the Fock vector.
3  *
4  * The formula for the extrapolated Fock matrix is:
5  *  $F' = \sum_k^m c_k F_k$ 
6  * where there are m elements in the Fock and error vectors.
7  */
8  void build_extrap_fock(arma::mat &F_extrap,
9                          const arma::vec &diis_coeffs,
10                          const deque< arma::mat > &diis_fock_vec) {
11     const int len = diis_coeffs.n_elem - 1;
12     F_extrap.zeros();
13     for (int i = 0; i < len; i++)
14         F_extrap += (diis_coeffs(i) * diis_fock_vec[i]);
15 }
```

```

1  /*!
2   * @brief Build the DIIS "zero" vector, or "b" in  $Ax = b$ .
3   */
4  arma::vec build_diis_zero_vec(const int len) {
5      arma::vec diis_zero_vec(len, arma::fill::zeros);
6      diis_zero_vec(len - 1) = -1.0;
7      return diis_zero_vec;
8  }

1 /*!
2  * Prepare structures necessary for DIIS extrapolation.
3  */
4 int NErr;
5 deque< arma::mat > diis_error_vec;
6 deque< arma::mat > diis_fock_vec;
7 int max_diis_length = 6;
8 arma::mat diis_error_mat;
9 arma::vec diis_zero_vec;
10 arma::mat B;
11 arma::vec diis_coeff_vec;

1 // Start collecting elements for DIIS once we're past the first iteration.
2 if (iter > 0) {
3     diis_error_mat = build_error_matrix(F, D, S);
4     NErr = diis_error_vec.size();
5     if (NErr >= max_diis_length) {
6         diis_error_vec.pop_back();
7         diis_fock_vec.pop_back();
8     }
9     diis_error_vec.push_front(diis_error_mat);
10    diis_fock_vec.push_front(F);
11    NErr = diis_error_vec.size();
12    // Perform DIIS extrapolation only if we have 2 or more points.
13    if (NErr >= 2) {
14        diis_zero_vec = build_diis_zero_vec(NErr + 1);
15        B = build_B_matrix(diis_error_vec);
16        diis_coeff_vec = arma::solve(B, diis_zero_vec);
17        build_extrap_fock(F, diis_coeff_vec, diis_fock_vec);
18    }
19 }

```