

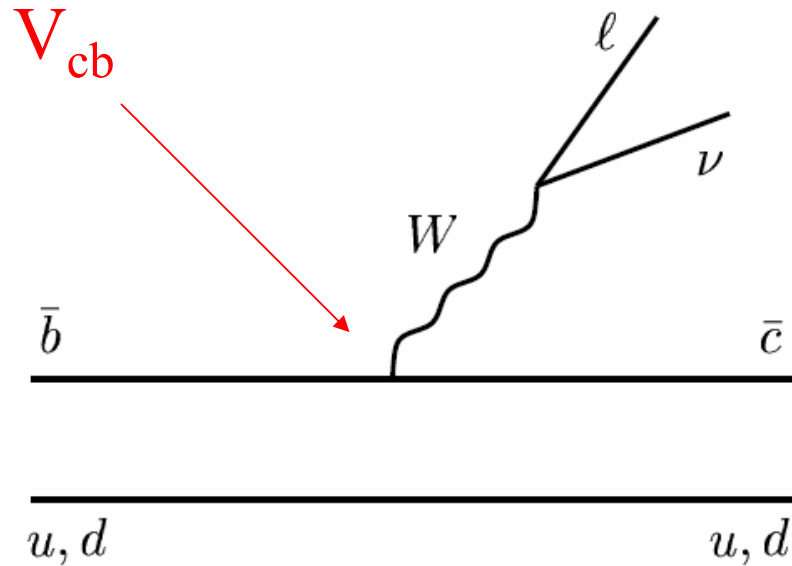
**Studies of semileptonic B decays  
with the BaBar experiment:  
Measurement of  $|V_{cb}|$  and Heavy Quark  
Parameters**

**hep-ex/0403030, 0403031, 0404017**

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**APS Meeting  
Denver, Colorado  
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# Why study semileptonic B decays?



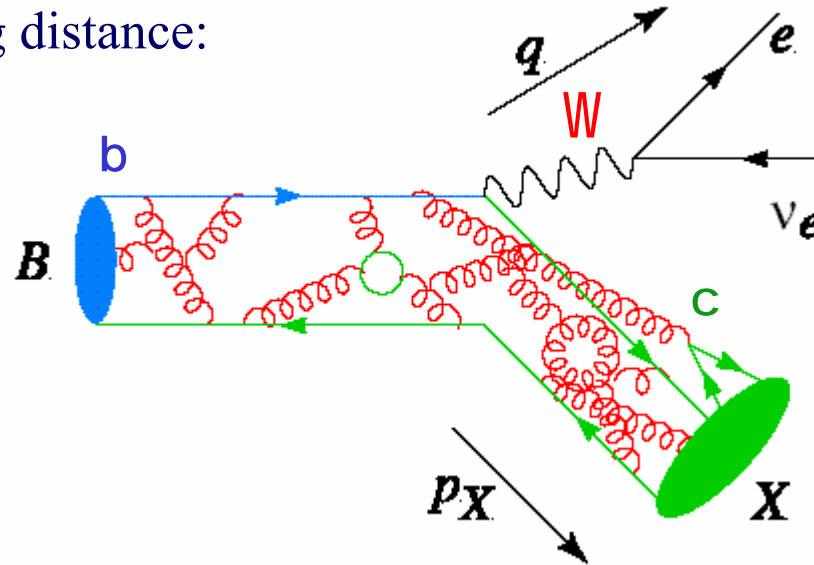
Tree level, short distance:

## Precision electroweak physics

- Decay properties depend directly on fundamental Standard Model parameters:  
 $|V_{cb}|$ ,  $m_b$ ,  $m_c$
- $|V_{cb}|$ : essential ingredient in tests of CKM unitarity
- $m_b$ ,  $m_c$ : important in predictions of B decay rates,  
precision electroweak observables

# Why study semileptonic B decays?

+ higher order & long distance:



## QCD phenomenology of heavy quarks

- Higher order QCD ( $\alpha_s^n$ ) corrections to short-distance interaction
- Non-perturbative, long-distance interactions of b quark with light quark
- Need theoretical technology to factorize these two effects and produce observables with precise relation to short distance parameters

# The Heavy Quark Expansion (HQE)

An operator product expansion in the heavy quark limit

- Short-distance, perturbative physics in the coefficients of operator products (to some order in  $\alpha_s$ ). **Calculable!**
- Long-distance, non-perturbative physics in exp. values of products of quark operators (to some order in  $1/m_b$ ). **NOT calculable. Measure them!**

$$\Gamma_{cl\nu} = \frac{G_F^2 m_b^5}{192\pi^3} |V_{cb}|^2 (1 + A_{ew}) A_{pert}(r, \mu) \times$$

$$\left[ z_0(r) \left( 1 - \frac{\mu_\pi^2 - \mu_G^2 + \frac{\rho_D^3 + \rho_{LS}^3}{m_b}}{2m_b^2} \right) \right.$$

$$\left. - 2(1-r)^4 \frac{\mu_G^2 + \frac{\rho_D^3 + \rho_{LS}^3}{m_b}}{m_b^2} + d(r) \frac{\rho_D^3}{m_b^3} + \mathcal{O}(1/m_b^4) \right].$$

$$r = m_c^2 / m_b^2$$

**N.B. Several HQE schemes exist; op's and coeff's are scheme dependent**

# HQE and spectral moments

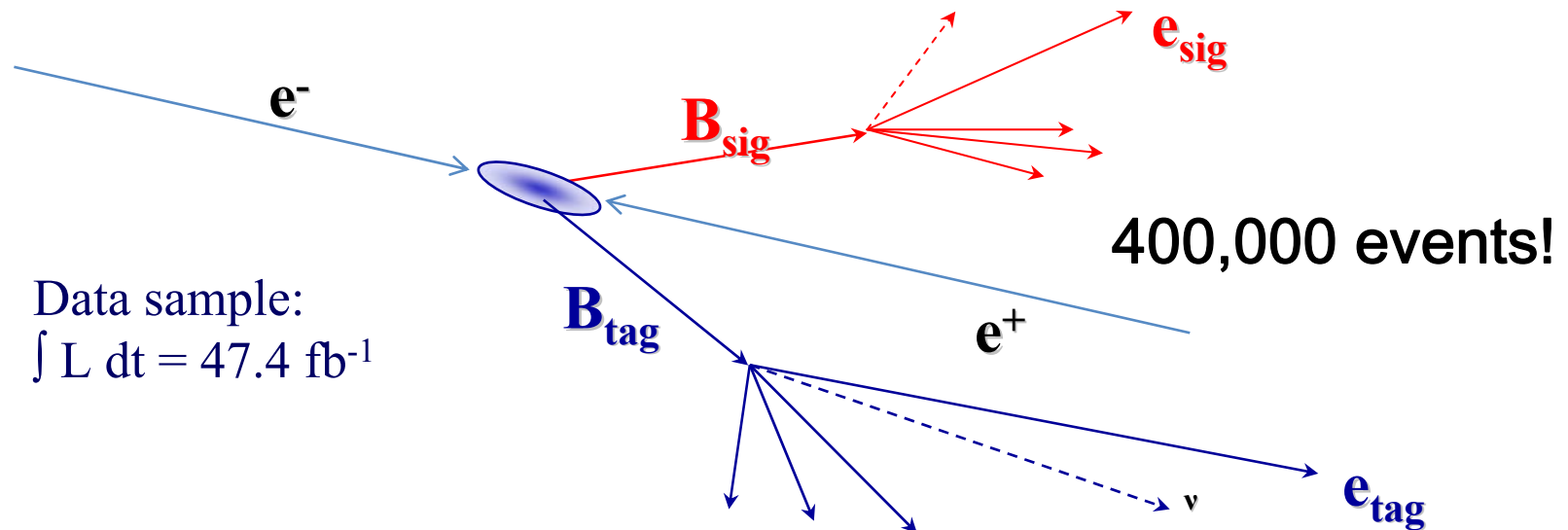
- Multiple  $b \rightarrow c l \nu$  observables needed for simultaneous extraction of all HQE parameters
- HQE calculations now exist for several **inclusive spectral moments** of the semileptonic decay products, as a function of the minimum (B rest frame) lepton energy,  $E_{cut}$ , required:

$$\langle X^n \rangle (E_{cut}) = \frac{\int (X - X^0)^n \frac{d\Gamma}{dX} dX}{\int \frac{d\Gamma}{dX} dX} \Bigg|_{E_l > E_{cut}}$$

- **Partial branching fraction**  $n = 0$  moment
- **Lepton-energy spectrum**  $\langle E_l^n \rangle$   $n = 1$ ,  $\langle E_l^n - \langle E_l \rangle^n \rangle$ ,  $n = 2, 3$
- **Hadronic-mass distribution**  $\langle M_X^n \rangle$   $n = 1, 2, 3, 4$
- photon energy spectrum in  $b \rightarrow s \gamma$  decays  $\langle E_\gamma^n \rangle$  (not discussed here)

# Lepton Energy Spectrum: Selection

- **Tag**  $Y(4S)$  events with high energy electron ( $p^* > 1.4$  GeV in  $Y(4S)$  frame) “ $e_{\text{tag}}$ ”
- **Measure** spectrum of any second electron in the event ( $p^* > 0.5$  GeV in  $Y(4S)$  frame) “ $e_{\text{sig}}$ ”
- Split into **same sign** (mostly from  $D$  to  $X l \nu$ ) and **opposite sign** (mostly signal) samples



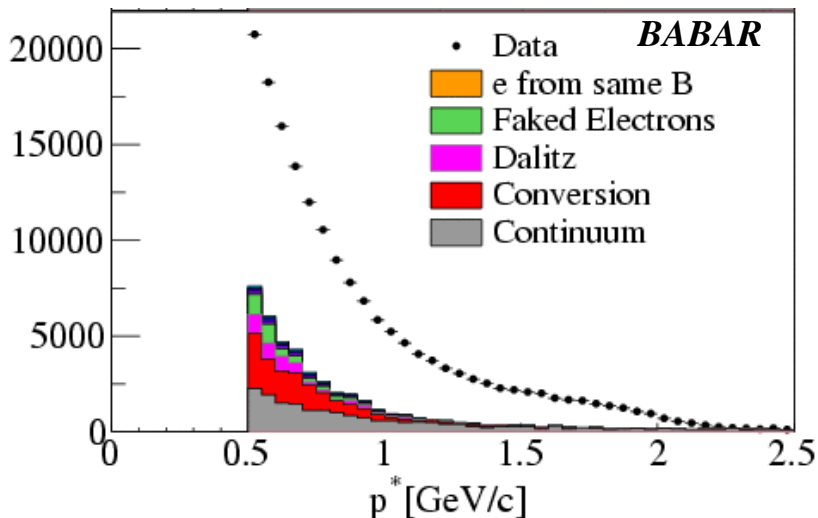
# Lepton Energy Spectrum: Background

- Suppress charm decay electrons in opp. sign sample with opening angle cut and J/psi veto

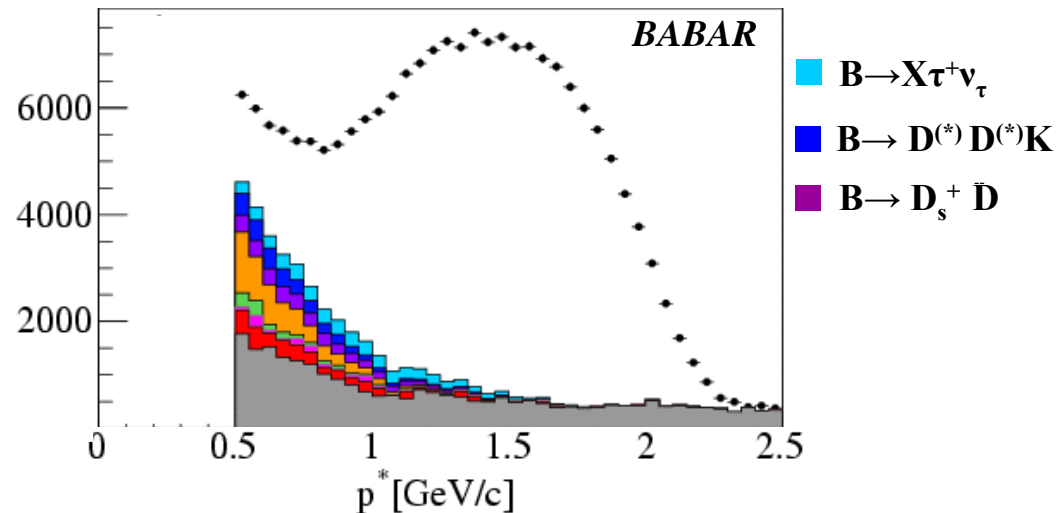
## Subtract remaining background:

- continuum with off-resonance data
- charm decays with same sign dielectron data (corrected for mixing)
- fake/conversion/Dalitz electrons estimated from data
- b to ccs and b to  $c\tau\nu$  decays from MC

Same sign (mostly from D decays)

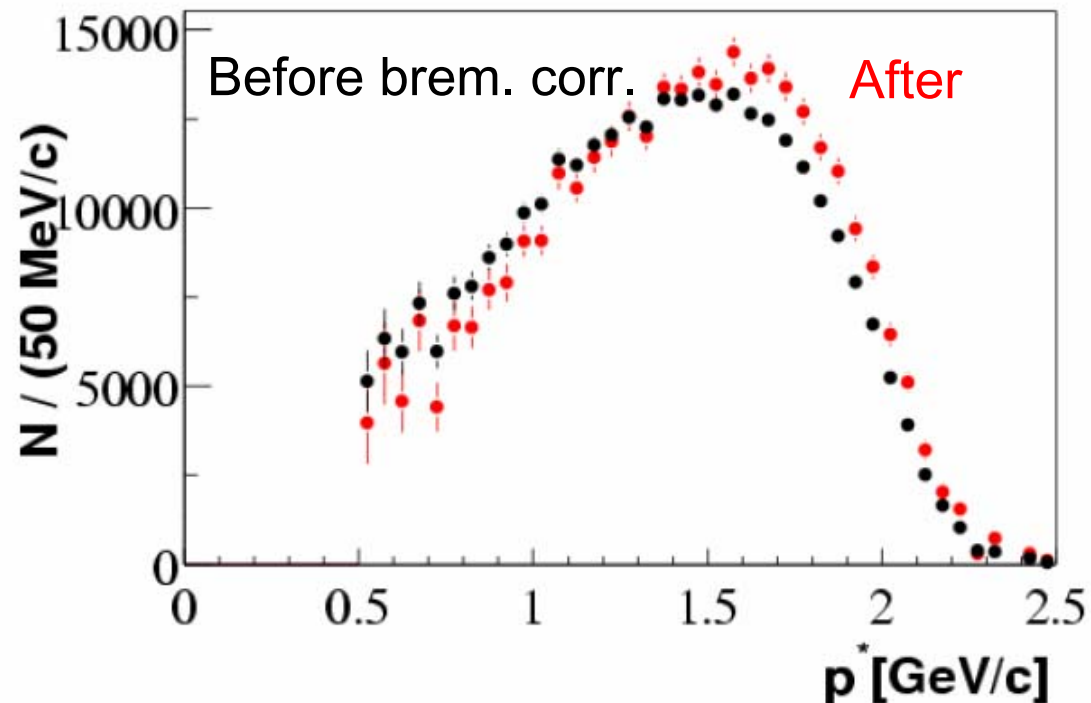


Opp. sign (mostly from B decays)



# Lepton Energy Spectrum: Corrections

- **Electron ID efficiency** precisely measured in radiative Bhabhas vs.  $(p, \cos \theta, +/-)$
- **Detector Bremsstrahlung** corrected via inversion of smearing matrix (detector material model  $X_0$  agrees with data to 0.14%!)
- **B momentum** correction from B spectrum in data
- **$B \rightarrow X_u l \nu$**  background estimated from measured BF, MC spectral shape



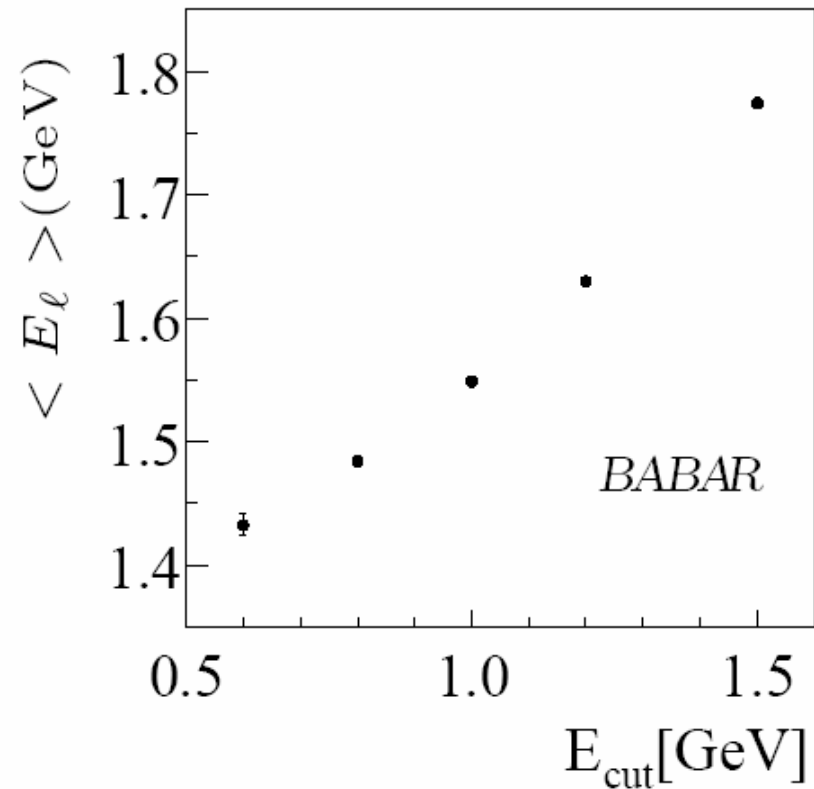
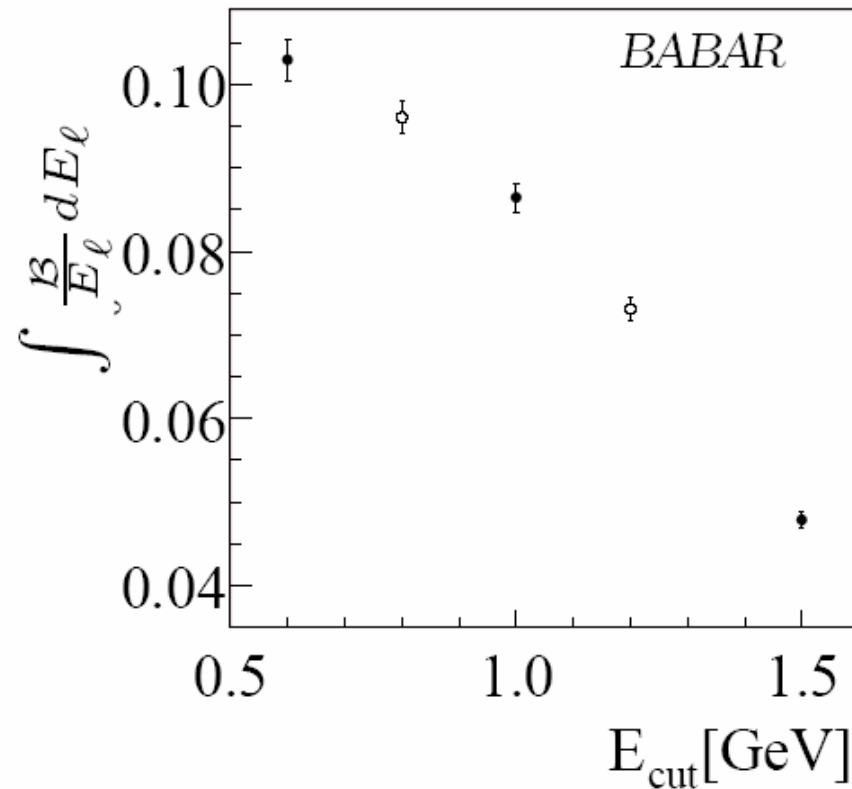


# Lepton Energy Spectrum: Moments

Individual measurements are highly correlated!

submitted to Phys. Rev. D: hep-ex/0403030

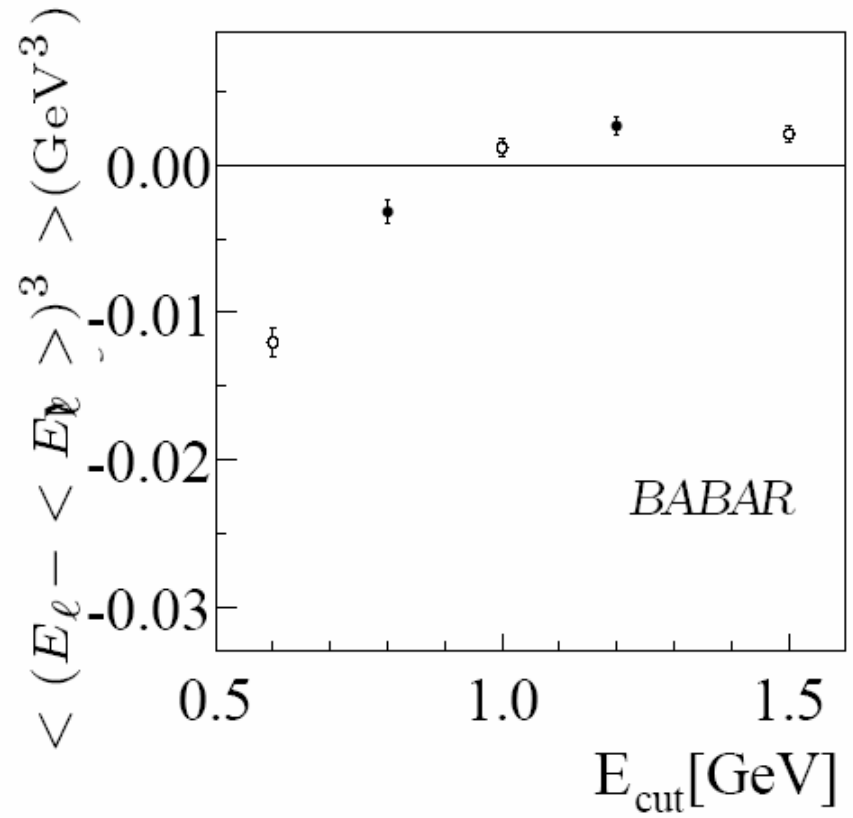
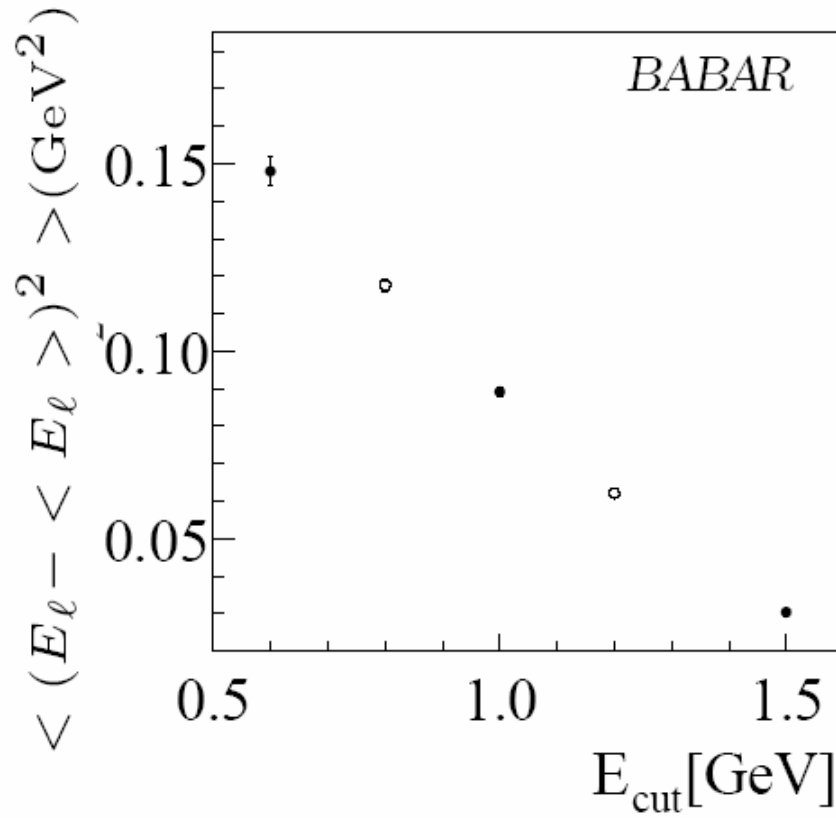
$B$  rest frame



# Lepton Energy Spectrum: Moments

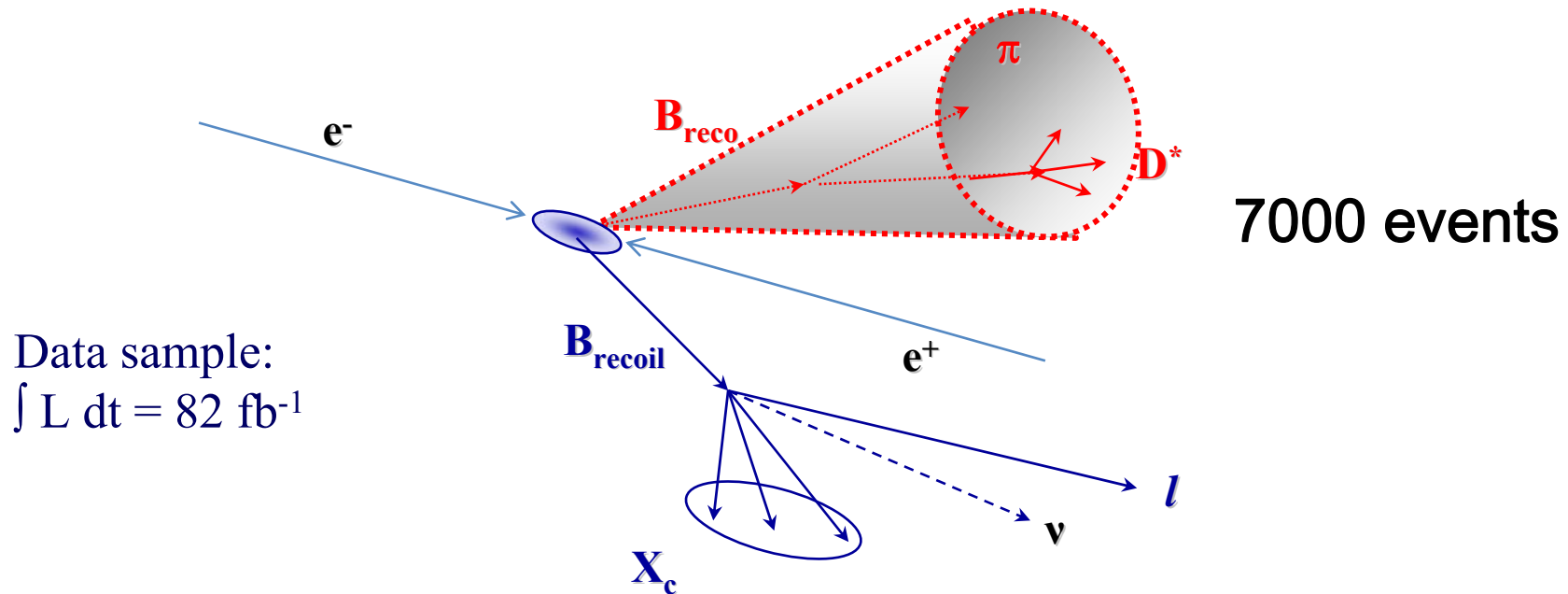
Individual measurements are highly correlated!

submitted to Phys. Rev. D: hep-ex/0403030



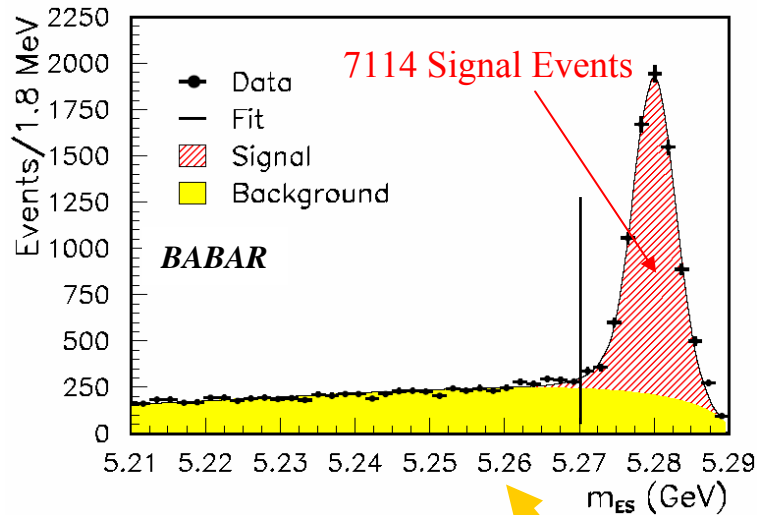
# Hadronic-Mass Spectrum: Selection

- Tag Y(4S) decays with **fully reconstructed hadronic B decays “ $B_{\text{reco}}$ ”**
- **Measure  $X_c$  mass** in “ $B_{\text{recoil}}$ ” side of the event:
  - exactly one “right sign” lepton ( $e$  or  $\mu$ )
  - lepton  $p^*$  in B rest frame  $> 0.9$  GeV
  - $|\text{net charge}| \leq 1$
  - $E_{\text{miss}}$  and  $P_{\text{miss}}$  consistent with neutrino



# Hadronic-Mass Spectrum: Background

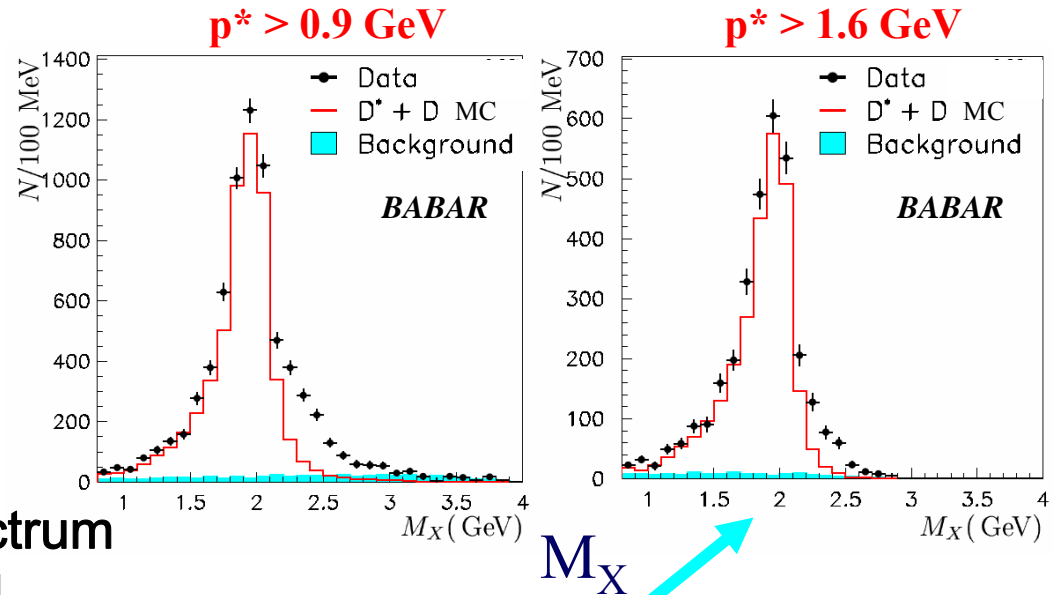
$B_{\text{reco}}$  mass peak in selected events



Combinatoric background  $M_X$  spectrum estimated from  $B_{\text{reco}}$   $m_{\text{ES}}$  sideband

$M_X$  extracted from kinematic fit to the entire event

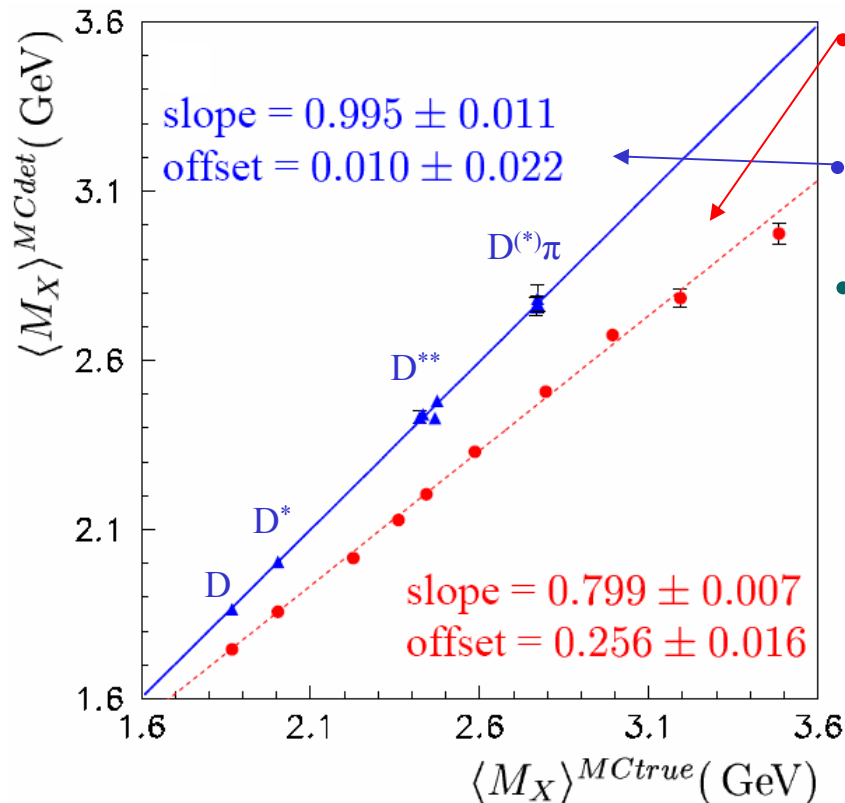
$$\sigma(M_X) \approx 350 \text{ MeV}$$



Small remaining background spectrum estimated from MC

# Hadronic-Mass Moments: Corrections

- Exploit observed linear relations between measured and generated masses
- Calibrate on an event-by-event basis, separately for each moment
- 9 MC calib. curves for each moment: 3X3 bins of (multiplicity,  $E_{\text{miss}} - P_{\text{miss}}$ )



• Calibration curve from inclusive  $X_c l \nu$  MC

• Validated in MC on exclusive final states

• Validated on partially reconstructed  
 $B \rightarrow D^{*\pm} l \nu$  ( $D^{*\pm} \rightarrow D^0 \pi^\pm$ ) DATA

Main uncertainties:

Detector Response

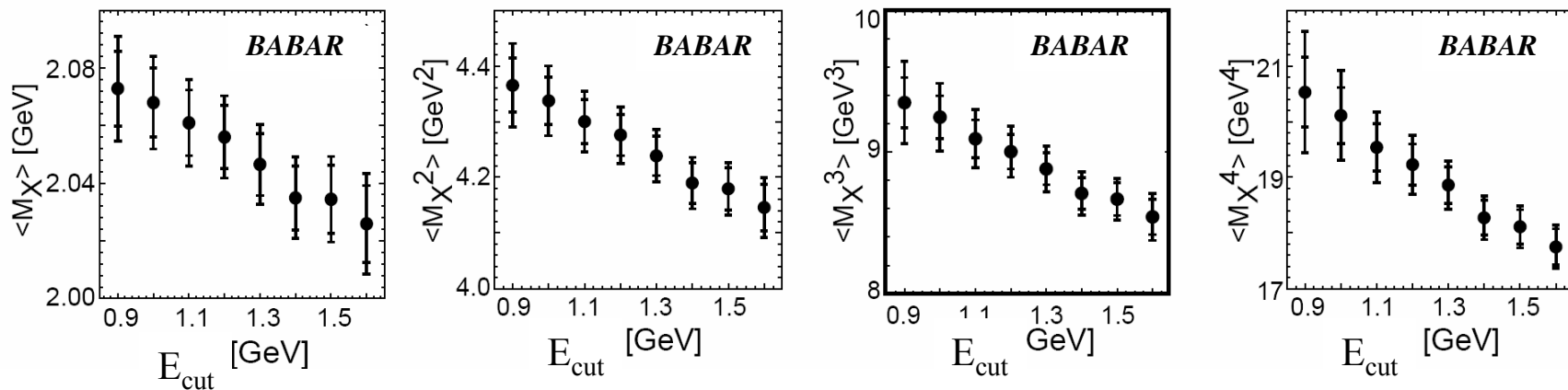
Background Subtraction

Little model dependence!!

# Hadronic-Mass Moments

Moments  $\langle M_X^n \rangle$  ( $n=1, \dots, 4$ ) of the hadronic mass spectrum  
in  $B \rightarrow X_c \ell \nu$  decays for  $0.9 \text{ GeV} < E_{\text{cut}} < 1.6 \text{ GeV}$

- Clear dependence on  $E_{\text{cut}}$  of lepton.
- Comparable statistical and systematic errors.
- Individual measurements are highly correlated!



submitted to Phys. Rev. D: hep-ex/0403031

# Fit of HQE Parameters to Moments

We use calculations in [kinetic mass scheme](#) by Gambino and Uraltsev  
(HQE to order  $1/m_b^3, \alpha_s^2$ )

hep-ph/0401063

hep-ph/0403166

## 8 Fit Parameters:

•  $BF(B \rightarrow X_c \ell \nu)$ ,  $|V_{cb}|$ ,  $m_b$ ,  $m_c$  and **4 HQE parameters**:

- $\mu_\pi^2$  - exp. value of kinetic energy of b quark inside B meson
- $\mu_G^2$  - exp. value of chromomagnetic moment operator

$\mathcal{O}(1/m_b^2)\{$

- $\rho_D^3$  - exp. value of Darwin operator
- $\rho_{LS}^3$  - exp. value of Spin-Orbit operator

$\mathcal{O}(1/m_b^3)\{$

27 lepton-energy and hadronic-mass moment measurements

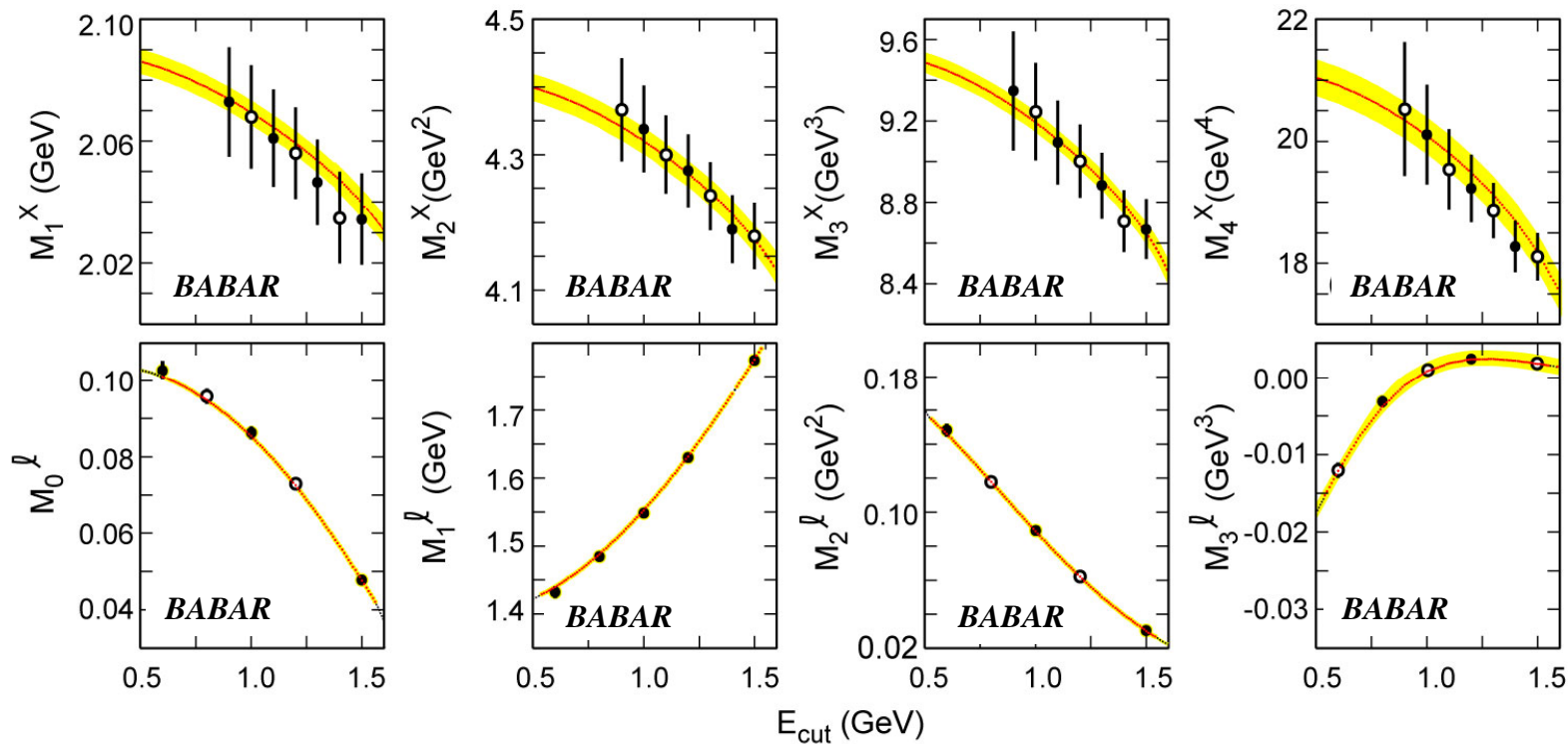
27 separate HQE prediction functions in the 8 fit parameters

(higher order moments sensitive to higher order HQE parameters)

# HQE Fit Results

- All parameters unconstrained.
- Only solid points are used in the fit.
- Correlations taken into account.

- Error bars show experimental errors  
(stat. & syst.)
- Bands correspond to theoretical uncertainties.



$$\chi^2 = 15$$

$$N_{\text{dof}} = 20$$



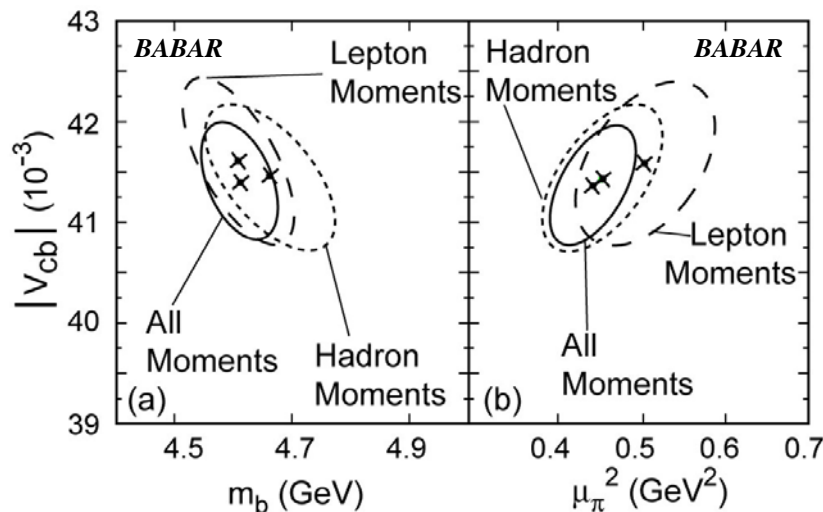
# Fit Results

kinetic mass scheme

$$\begin{aligned}
 |V_{cb}| &= (41.4 \pm 0.4_{\text{exp}} \pm 0.4_{\text{HQE}} \pm 0.2_{\alpha_s} \pm 0.6_{\Gamma_{\text{SL}}}) \times 10^{-3} \\
 Br(B \rightarrow X_c e \nu) &= (10.61 \pm 0.16_{\text{exp}} \pm 0.06_{\text{HQE}}) \% \\
 m_b(1 \text{ GeV}) &= (4.61 \pm 0.05_{\text{exp}} \pm 0.04_{\text{HQE}} \pm 0.02_{\alpha_s}) \text{ GeV} \\
 m_c(1 \text{ GeV}) &= (1.18 \pm 0.07_{\text{exp}} \pm 0.06_{\text{HQE}} \pm 0.02_{\alpha_s}) \text{ GeV}
 \end{aligned}$$

$$\begin{aligned}
 \mu_\pi^2 &= (0.45 \pm 0.04_{\text{exp}} \pm 0.04_{\text{HQE}} \pm 0.01_{\alpha_s}) \text{ GeV}^2 \\
 \mu_G^2 &= (0.27 \pm 0.06_{\text{exp}} \pm 0.03_{\text{HQE}} \pm 0.02_{\alpha_s}) \text{ GeV}^2 \\
 \rho_D^3 &= (0.20 \pm 0.02_{\text{exp}} \pm 0.02_{\text{HQE}} \pm 0.00_{\alpha_s}) \text{ GeV}^3 \\
 \rho_{LS}^3 &= (-0.09 \pm 0.04_{\text{exp}} \pm 0.07_{\text{HQE}} \pm 0.01_{\alpha_s}) \text{ GeV}^3
 \end{aligned}$$

submitted to  
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hep-ex/0404017

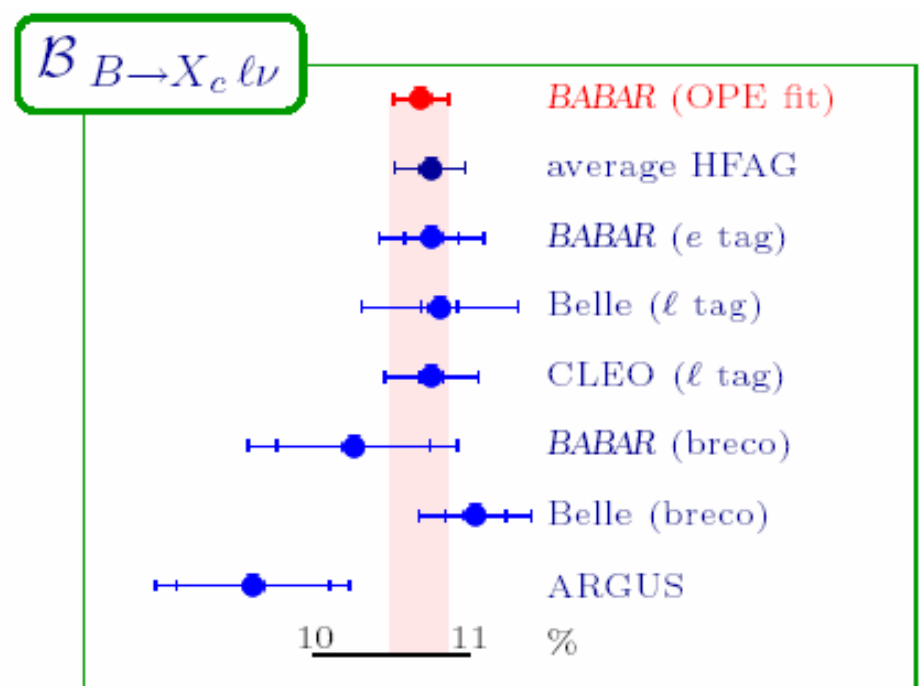
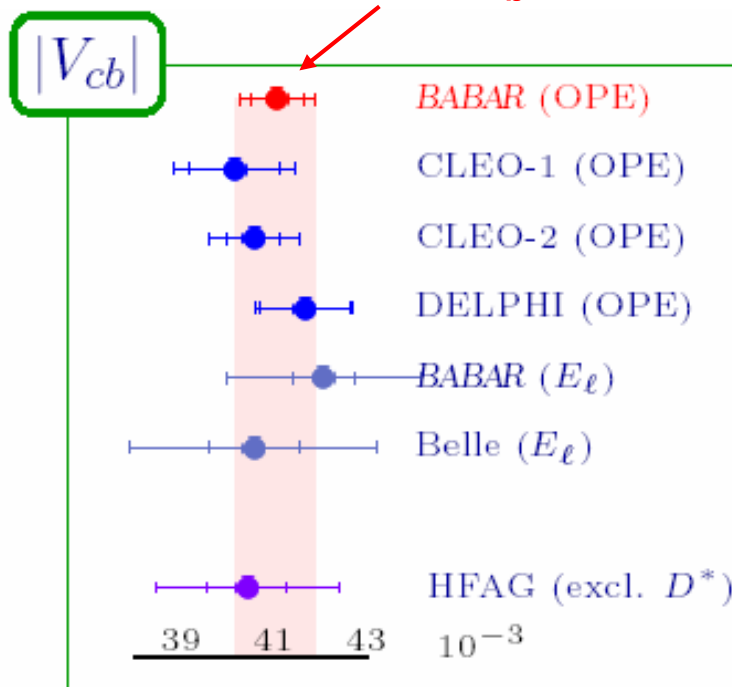


2D projections  
of the fit result:

$\Delta\chi^2=1$  ellipses  
of separate fits  
to lepton or  
hadron moments  
are consistent

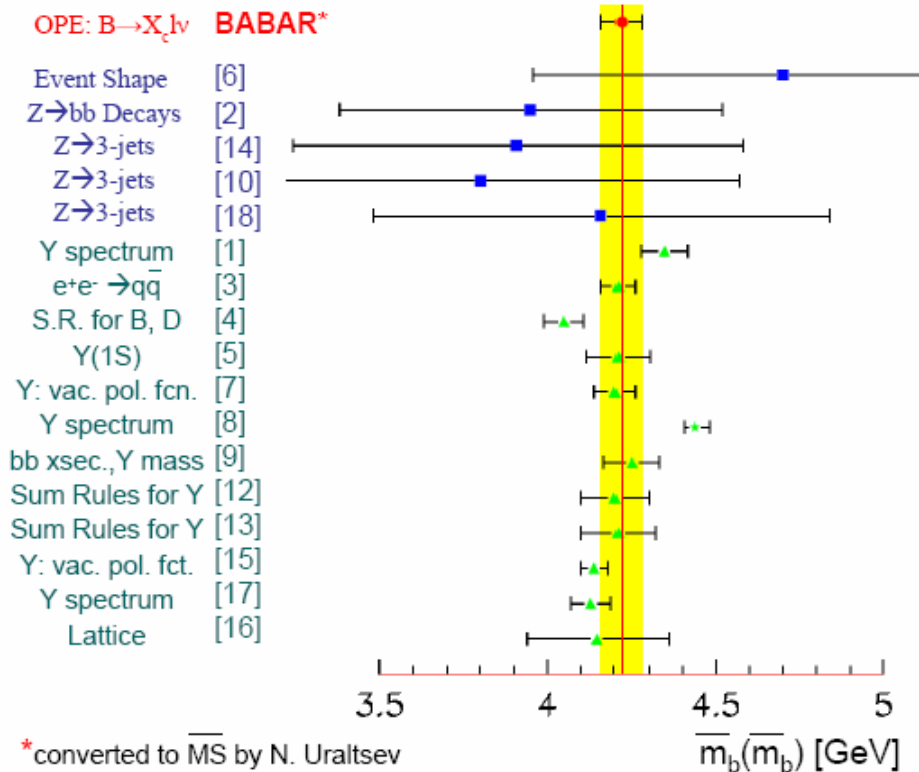
# Comparison with previous Determinations

First measurement with all parameters floating to order  $1/m_b^3$

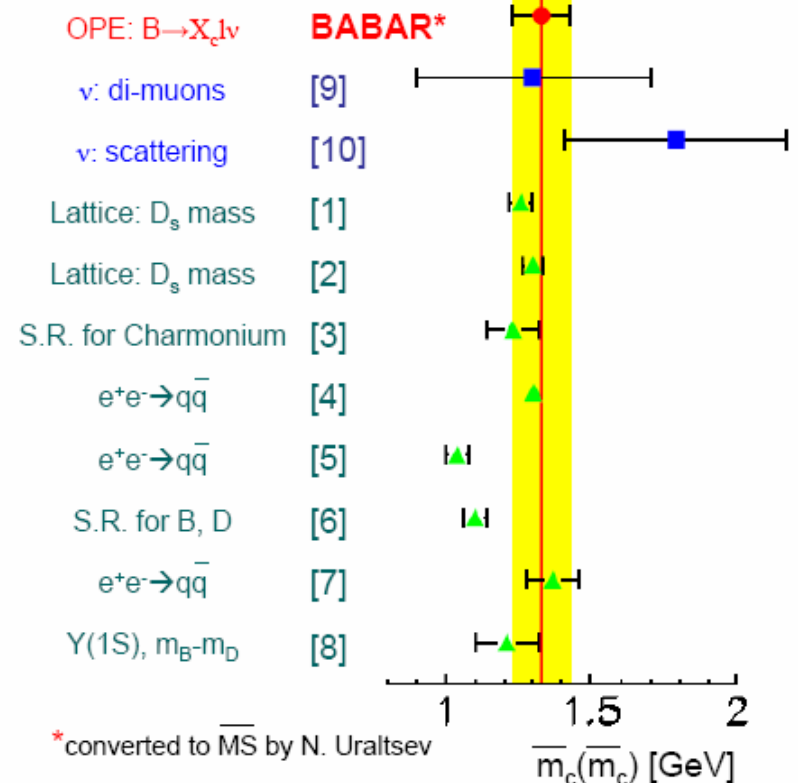


# Comparison with other Determinations

## Measurements and Predictions of the b-Quark Mass ( $\overline{\text{MS}}$ scheme) PDG2003



## Measurements and Predictions of the c-Quark Mass ( $\overline{\text{MS}}$ scheme) PDG2003



$$\overline{m}_b(\overline{m}_b) = 4.22 \pm 0.06 \text{ GeV} \quad \text{BABAR}$$

$$\overline{m}_c(\overline{m}_c) = 1.33 \pm 0.10 \text{ GeV}$$

Conversion from kinetic mass scheme  
 to  $\overline{\text{MS}}$  scheme with hep-ph/9708372, hep-ph/0302262  
 See also report from CKM WS hep-ph/0304132

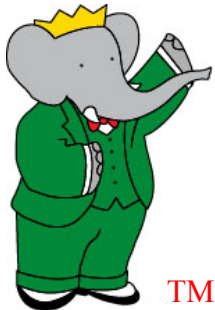
# Summary

## New Measurements of

- Hadronic Mass Moments up to 4<sup>th</sup> order for  $0.9 \text{ GeV} < E_{\text{cut}} < 1.6 \text{ GeV}$  [hep-ex/0403031](#)
- Lepton Energy Moments up to 3<sup>rd</sup> order for  $0.6 \text{ GeV} < E_{\text{cut}} < 1.5 \text{ GeV}$  [hep-ex/0403030](#)

Serve as input to **OPE fit** with no external constraints:

$$\begin{aligned} |V_{cb}| &= (41.4 \pm 0.4_{\text{exp}} \pm 0.4_{\text{HQE}} \pm 0.2_{\alpha_s} \pm 0.6_{\Gamma_{SL}}) \times 10^{-3} \\ Br(B \rightarrow X_c e \nu) &= (10.61 \pm 0.16_{\text{exp}} \pm 0.06_{\text{HQE}}) \% \\ m_b(1 \text{ GeV}) &= (4.61 \pm 0.05_{\text{exp}} \pm 0.04_{\text{HQE}} \pm 0.02_{\alpha_s}) \text{ GeV} \\ m_c(1 \text{ GeV}) &= (1.18 \pm 0.07_{\text{exp}} \pm 0.06_{\text{HQE}} \pm 0.02_{\alpha_s}) \text{ GeV} \\ m_b(1 \text{ GeV}) - m_c(1 \text{ GeV}) &= (3.44 \pm 0.03_{\text{exp}} \pm 0.02_{\text{HQE}} \pm 0.01_{\alpha_s}) \text{ GeV} \end{aligned}$$



2% error on  $|V_{cb}|$  from BaBar

submitted to Phys. Rev. Lett.  
[hep-ex/0404017](#)