# Fundamentals of Machine Learning

## NETWORK ARCHITECTURES, ATTENTION

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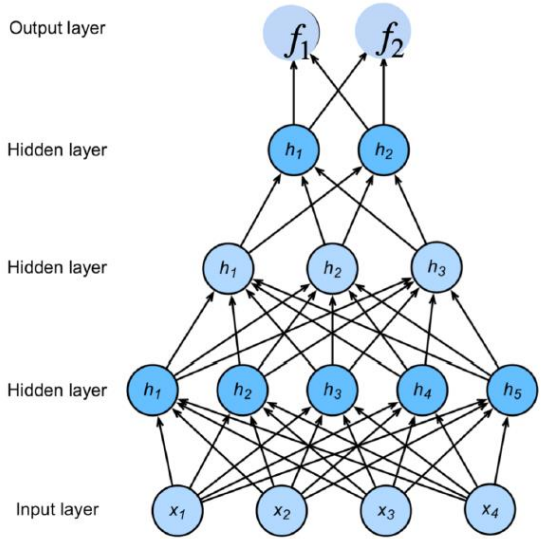
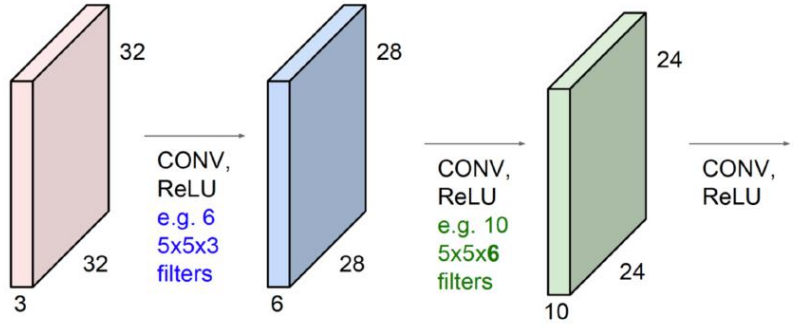
https://developer.ibm.com/articles/cc-machine-learning-deep-learning-architectures/

# Feedforward Networks

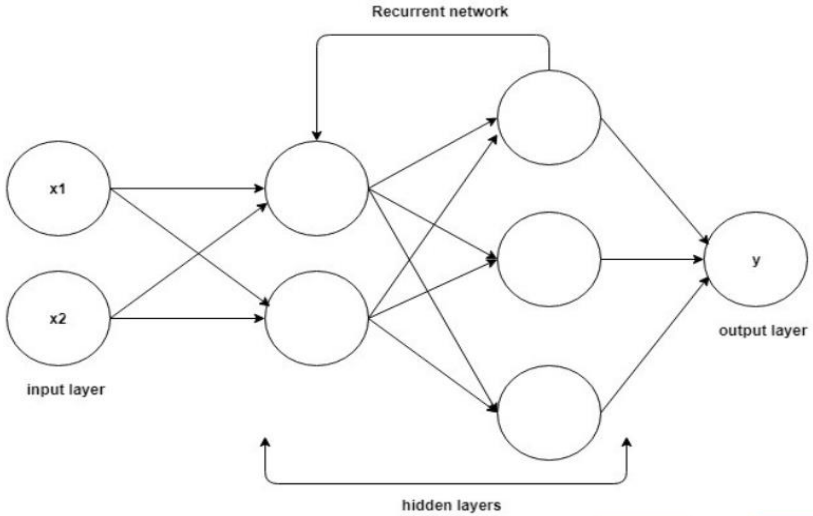


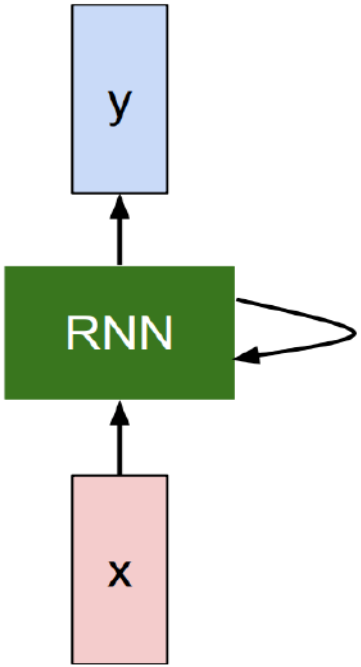

MLP




CNN

# Recurrent Neural Networks

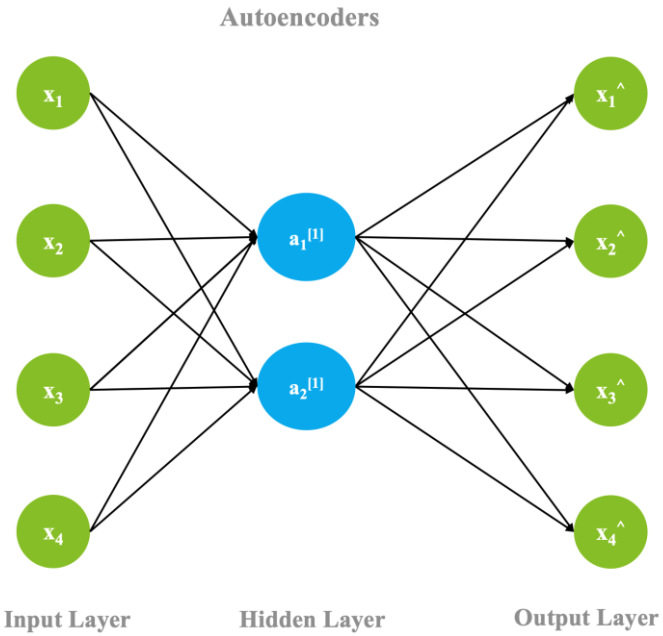


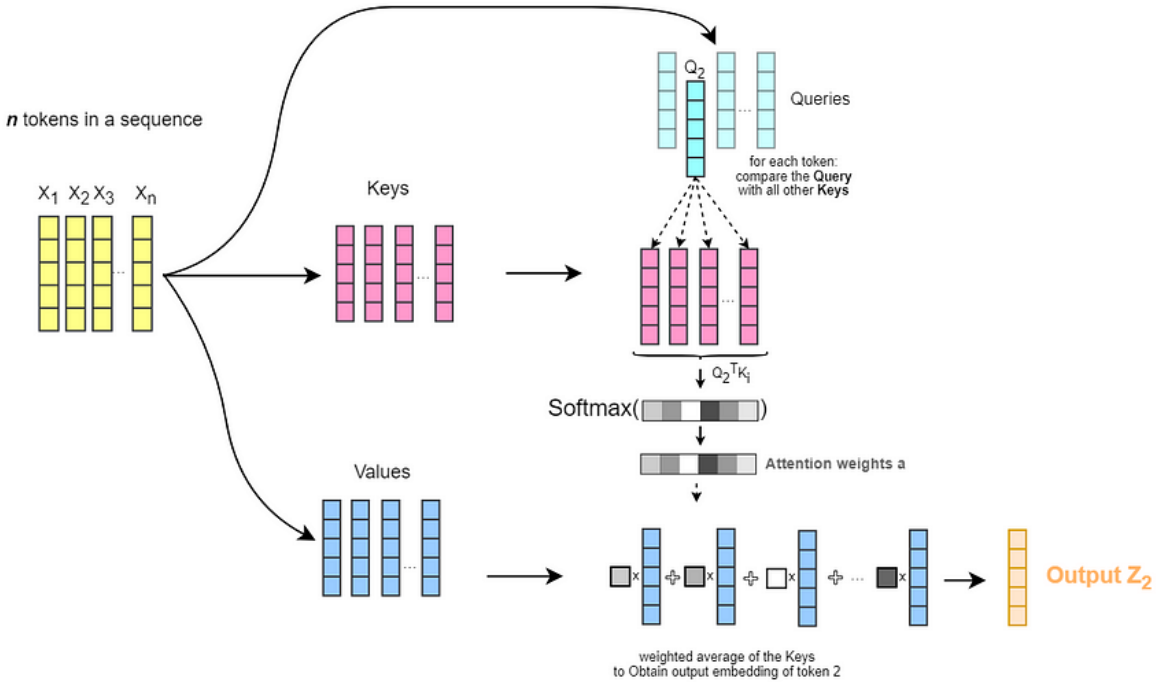

$$h_t = f_W(h_{t-1}, x_t)$$

new state — old state — input at some time step

# Autoencoders



# Transformers




https://towardsdatascience.com/what-are-query-key-and-value-in-the-transformer-architecture-and-why-are-they-used-acbe73f731f2

# Key, Query, Value

Value: $\mathbf{V} \in \mathbb{R}^{m \times v}$ set of $m$ feature vectors

Query: $q \in \mathbb{R}^{q}$

Keys: $\mathbf{K} \in \mathbb{R}^{m \times k}$ set of $m$ **keys**

Find the query that is most similar to a key and use the corresponding value.

$$\text{Attn}(\boldsymbol{q}, (\boldsymbol{k}_1, \boldsymbol{v}_1), \ldots, (\boldsymbol{k}_m, \boldsymbol{v}_m)) = \text{Attn}(\boldsymbol{q}, (\boldsymbol{k}_{1:m}, \boldsymbol{v}_{1:m})) = \sum_{i=1}^{m} \alpha_i(\boldsymbol{q}, \boldsymbol{k}_{1:m}) \boldsymbol{v}_i$$

$$0 \leq \alpha_i(\boldsymbol{q}, \boldsymbol{k}_{1:m}) \leq 1 \qquad \sum_i \alpha_i(\boldsymbol{q}, \boldsymbol{k}_{1:m}) = 1$$

# Computing Attention Weights

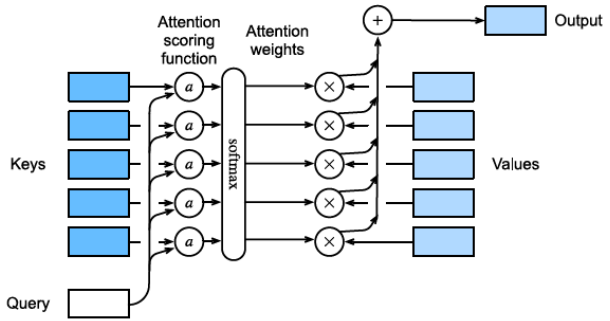
Find the query that is most similar to a key and use the corresponding value.

$$\text{Attn}(\boldsymbol{q}, (\boldsymbol{k}_1, \boldsymbol{v}_1), \ldots, (\boldsymbol{k}_m, \boldsymbol{v}_m)) = \text{Attn}(\boldsymbol{q}, (\boldsymbol{k}_{1:m}, \boldsymbol{v}_{1:m})) = \sum_{i=1}^{m} \alpha_i(\boldsymbol{q}, \boldsymbol{k}_{1:m}) \boldsymbol{v}_i$$

$$0 \leq \alpha_i(\boldsymbol{q}, \boldsymbol{k}_{1:m}) \leq 1 \qquad \sum_i \alpha_i(\boldsymbol{q}, \boldsymbol{k}_{1:m}) = 1$$

Attention similarity/score: $a(\boldsymbol{q}, \boldsymbol{k}_i) \in \mathbb{R}$

$$\alpha_i(\boldsymbol{q}, \boldsymbol{k}_{1:m}) = \text{softmax}_i([a(\boldsymbol{q}, \boldsymbol{k}_1), \ldots, a(\boldsymbol{q}, \boldsymbol{k}_m)]) = \frac{\exp(a(\boldsymbol{q}, \boldsymbol{k}_i))}{\sum_{j=1}^{m} \exp(a(\boldsymbol{q}, \boldsymbol{k}_j))}$$

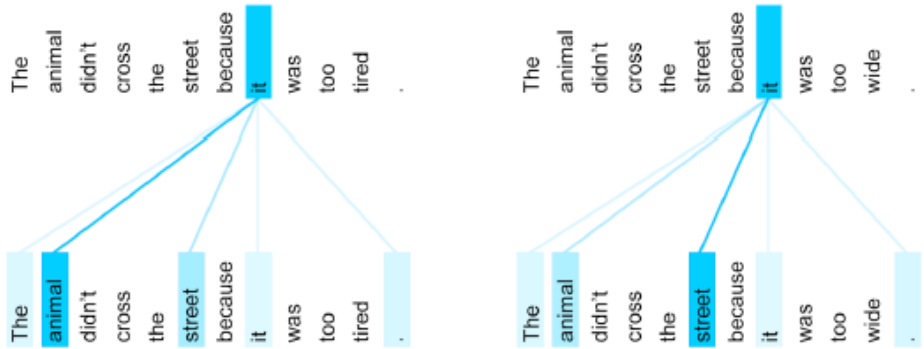


# Self Attention

$$y_i = \text{Attn}(x_i, (x_1, x_1), \ldots, (x_n, x_n))$$

input tokens $x_1, \ldots, x_n$, where $x_i \in \mathbb{R}^d$

query is $x_i$, and the keys and values are all the (valid) inputs $x_1, \ldots, x_n$



# Multimodal Models